Electronic states and possible origin of the orbital-glass state in a nearly metallic spinel cobalt vanadate: An x-ray magnetic circular dichroism study

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We have investigated the orbital states of the orbital-glassy (short-range orbital ordered) spinel vanadate $Co_{1,21}V_{1,79}O_4$ using x-ray absorption spectroscopy (XAS), x-ray magnetic circular dichroism (XMCD), and subsequent configuration-interaction cluster-model calculation. From the sign of the XMCD spectra, it was found that the spin magnetic moment of the Co ion is aligned parallel to the applied magnetic field and that of the V ion antiparallel to it, consistent with neutron scattering studies. It was revealed that the excess Co ions at the octahedral site take the trivalent low-spin state and induce a random potential to the V sublattice. The orbital magnetic moment of the V ion is small, suggesting that the ordered orbitals mainly consist of real-number orbitals.

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I. INTRODUCTION

Spinel-type transition-metal oxides AB_2O_4 [Fig. [1\(a\)\]](#page-1-0) are one of the most attractive playgrounds for the studies of emergent physical properties arising from multiple degrees of freedom in strongly correlated electron systems. This structure consists of the diamond sublattice of the *A* site and the pyrochlore sublattice of the *B* site [Fig. $1(b)$]. Particularly in the pyrochlore sublattice, there is strong geometrical spin frustration. In the spinel-type vanadates $AV₂O₄$, in addition to the spin frustration, the orbital degree of freedom also exists in the triply degenerate V t_{2g} orbitals, as shown in Fig. [1\(c\).](#page-1-0) Therefore, a number of experimental and theoretical studies have been performed on the spinel-type vanadates, particularly on the orbital ordering in AV_2O_4 , where $A = Mg$ [\[1\]](#page-5-0), Mn [\[2–8\]](#page-5-0), Fe [\[5,6,9,10\]](#page-5-0), Zn [\[11,12\]](#page-5-0), and Cd [\[13,14\]](#page-5-0). All of them exhibit structural phase transitions from the cubic to a low-symmetry phase with decreasing temperature, and the orbital ordering is usually associated with the structural phase transition.

To understand the orbital ordering in these systems, theoretical models based on the pyrochlore network of V ions have been studied [\[15–18\]](#page-5-0). Through a strong coupling approach using the Kugel-Khomskii-type Hamiltonian [\[19\]](#page-5-0), Tsunetsugu and Motome proposed an antiferro-orbital ordering model for ZnV_2O_4 [\[15,16\]](#page-5-0), which consists of the alternating d_{zx} and d_{yz} orbitals. Khomskii and Mizokawa proposed an orbital-Peierls model [\[17\]](#page-5-0), which is induced by the dimerization of orbitals in 1D chains consisting of the σ bonds of the d_{zx} and d_{yz} orbitals. In contrast to these real orbital models, Tchernyshyov proposed

In addition to the above orbital ordering mechanisms, a spontaneous lattice-distortion mechanism without orbital ordering was also proposed by Pardo *et al.* [\[20\]](#page-5-0) for nearly metallic spinel-type vanadate, where partially delocalized V 3*d* electrons drive a homopolar bond formation and V-V dimerization in a system where the *U/W* (the ratio of the on-site Coulomb energy to the bandwidth) is not sufficiently larger than one.

Among the spinel-type vanadates, $CoV₂O₄$ has attracted particular attention because of the close proximity to the Mott-type metal-insulator-transition from the insulator side due to the short V-V bond length [\[21,22\]](#page-5-0). This compound shows ferrimagnetism below $T_N = 160$ K, but neither a structural phase transition nor a signature of orbital ordering had been seen down to 10 K by x-ray diffraction [\[21\]](#page-5-0). The absence of orbital ordering is consistent with the itinerant character of V 3*d* electrons in $CoV₂O₄$. The absence of orbital ordering was also proposed by extrapolating results of a neutron scattering study on $Mn_{1-y}Co_yV_2O_4$ ($y \le 0.8$) single crystals to $y = 1.0$ [\[23\]](#page-5-0). However, recently a very small structural phase transition $(\Delta a/a \sim 10^{-4})$ at 90 K was reported by a neutron scattering study of stoichiometric $CoV₂O₄$ powders [\[24\]](#page-5-0). A small distortion was also reported for single crystals of $\text{Co}_{1+x}\text{V}_{2-x}\text{O}_4$ (0.16 $\leq x \leq 0.3$) by strain gauge measurements, and an orbital-glass (short-range orbital ordering) state was proposed from its gradual lattice distortion and the slow dynamics of the dielectric constant [\[25\]](#page-5-0). Very recently, two structural phase transitions, one at 95 K [cubic to tetragonal $(I4_1/amd)$] and the other at 59 K [tetragonal

a ferro-orbital model, where the d_{xy} and one of the complex $d_{zx} \pm i d_{yz}$ orbitals are occupied by two electrons [\[18\]](#page-5-0). This complex-number orbital has a large orbital magnetic moment $(\pm 1 \mu_B \text{ at most}).$

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FIG. 1. Illustrations of the crystal structure and the electronic configurations of the 3*d* orbitals of spinel-type oxides. (a) Cubic unit cell of *AB*2O4. The red (blue) polyhedra denote the *A*O4 tetrahedra $(BO₆ octahedra)$. (b) Pyrochlore and diamond structures consisting of the *B* and *A* site network, respectively. (c) Electronic configuration of the Co^{2+} ion at the tetrahedral (*A*) site and those of the V^{3+} and $Co³⁺$ ions at the octahedral (*B*) site.

 $(I4₁/and)$ to tetragonal $(I4₁/a)$], were reported by neutron powder diffraction and single-crystal synchrotron-radiation x-ray diffraction measurements on stoichiometric $CoV₂O₄$ [\[26\]](#page-5-0). It was also proposed that a long-range antiferro-orbital ordering exists below the 59-K structural phase transition, where an anomaly in the specific heat was reported [\[27](#page-5-0)[,28\]](#page-6-0). Since the anomaly persists up to $x \sim 0.15$ [\[28\]](#page-6-0), the long-range orbital ordering should also persist up to $x \sim 0.15$. On the other hand, because of the close proximity of $CoV₂O₄$ to the Mott-type metal-insulator transition, the homopolar bond formation mechanism [\[20\]](#page-5-0) might be the origin of the lattice distortion.

In the present study, in order to obtain more direct information about the V 3*d* electrons, we have measured *L*-edge x-ray absorption spectra (XAS) and x-ray magnetic circular dichroism (XMCD) of $CoV₂O₄$. Because *L*-edge XAS is a well established probe of the 3*d* electronic structure, and *L*-edge XMCD gives us the quantitative information about the orbital magnetic moments which is the key information about the orbital states. It should be noted that high-quality single crystals of $CoV₂O₄$ can be grown only for compositions with excess Co. Therefore, the composition of the crystals studied in this paper was $Co_{1,21}V_{1,79}O_4$ [\[25\]](#page-5-0). The excess Co ions enter the octahedral site and significantly affect the physical properties of Co1+*^x*V2−*^x*O4. Upon increasing excess Co, the activation energy for the transport becomes higher $[29,30]$, T_N becomes higher, and the onset temperature of the orbital-glass state becomes lower [\[25\]](#page-5-0). Therefore, it is necessary to elucidate the electronic state of excess Co ions, and*L*-edge XAS and XMCD are ideal tools for that purpose, too. Using the configurationinteraction (CI) cluster-model analysis of the XAS and XMCD data, one can discuss the electronic states of the Co ions at the tetrahedral site and the excess Co ions at the octahedral site separately.

FIG. 2. Schematic pictures of the experimental geometry (a), the magnetization of $Co_{1,21}V_{1,79}O_4$ as a function of magnetic field along the [001] and [111] directions (b), and the sign of XMCD signals (c). The upper and lower panels of (c) show typical XMCD spectra where the projection of the spin magnetic moment onto the x-ray incident vector $m_{\text{spin}}^{\text{proj}}$ is negative and positive, respectively.

II. METHODS OF EXPERIMENT AND CALCULATION

Bulk single crystals of $Co_{1.21}V_{1.79}O₄$ were grown by the floating zone method. In order to avoid the formation of the V_2O_3 impurity phase, the compositions of the feed rod was not stoichiometric (Co : $V = 1 : 2$) but containing 50% excess Co $(Co: V = 1.5: 2)$ relative to the stoichiometric one. The Co: V ratio of the synthesized single crystals was determined to be 1*.*21 : 1*.*79 by induction-coupled plasma (ICP) analysis [\[25\]](#page-5-0).

Magnetic field angle-dependent XAS and XMCD were measured at the undulator beamline BL-16A of Photon Factory. The energy resolution in the Co $L_{2,3}$ - and V $L_{2,3}$ - edge region was about 0.2 and 0.1 eV, respectively. The spectra were taken in the total electron-yield (TEY) mode at 30, 70, and 110 K. The sample angle was fixed so that the incident x rays form an angle of 45◦ from the [001] direction and within the [001]–[111] plane in the cubic notation. (Hereafter, we use the cubic notation.) A magnetic field of 0.5 T was applied along the [001] and [111] directions using a 'vector magnet' XMCD apparatus [\[31\]](#page-6-0). A schematic picture of the experimental geometry is shown in Fig. $2(a)$. The magnetic field of 0.5 T was enough to saturate magnetization in the [001] direction but not enough in the [111] direction [Fig. 2(b)]. In order to obtain clean surfaces, the samples were cleaved in vacuum (base pressure *<*⁸ [×] ¹⁰−¹⁰ Torr). The XMCD intensities have been corrected for the degree of circular polarization of BL-16A.

To examine the detailed electronic structure, we have fitted the CI cluster-model calculation to the experimental XAS and XMCD spectra [\[32\]](#page-6-0). In the calculation, we adopted the empirical ratio between the on-site Coulomb energy U_{dd} and the 3*d*-2*p* hole Coulomb energy U_{dc} , $U_{dc}/U_{dd} \sim 1.3$ [\[33,34\]](#page-6-0), and that between Slater-Koster parameters (*pdσ*) and (*pdπ*),

FIG. 3. XAS and XMCD spectra of $Co_{1,21}V_{1,79}O_4$. (a),(b) XAS and XMCD at the Co $L_{2,3}$ edge. (c),(d) XAS and XMCD at the V $L_{2,3}$ edge. The dotted curves in (a) and (c) are two-step background functions representing the edge jump. The dotted curves in (d) are a magnified XMCD spectrum around 531 eV.

 $(pd\sigma)/(pd\pi) \sim -2.17$ [\[35\]](#page-6-0). Hybridization strength between the O 2p orbitals T_{pp} was fixed at 0.7 eV (for the O_h site) and 0 eV (for the T_d site) [\[32,36\]](#page-6-0). The ionic Hartree-Fock (HF) values were used for the spin-orbit interaction constants of Co 3*d*, Co 2*p*, and V 2*p* states, and 80% of the ionic HF values were used for the Slater integrals [\[32\]](#page-6-0). Thus, the crystal-field splitting $10Dq$, U_{dd} , the charge-transfer energy Δ , and $(pd\sigma)$ were treated as fitting parameters. For each absorption edge, further assumptions (as described) were adopted to reduce the number of adjustable parameters. We note that calculations for the tetrahedral site have been performed by negative values of 10*Dq* with *Oh* symmetry.

III. RESULTS AND DISCUSSION

Figure 3 shows the XAS ($\mu^+ + \mu^-$) and XMCD ($\mu^+ - \mu^-$) spectra of the $Co_{1.21}V_{1.79}O₄$ single crystal at the V and Co $L_{2,3}$ edges under the magnetic field of 0.5 T and at the temperature of 30 K. Here, μ^+ (μ^-) denote the absorption coefficients for the photon helicities parallel (antiparallel) to the majority spin direction. The energy-integrated XMCD spectra are also shown in Figs. $3(b)$ and $3(d)$ by red solid curves. The sign of XMCD provides us with the information about the spin magnetic moment. As shown in Fig. $2(c)$, the sign of XMCD at the *L*² and *L*³ edges indicates whether the projection of the spin magnetic moment onto the x-ray incident vector $m_{\text{spin}}^{\text{proj}}$ is positive or negative. According to the ionic picture shown in Fig. $1(c)$, since the total spin magnetic moment of the two V^{3+} ($2\mu_B \times 2$ ions = $4\mu_B$) ions in the unit formula is larger than that of the Co²⁺ (3 μ _B) ion, the spin magnetic moment of the V^{3+} ion is expected to be parallel to the applied magnetic field and that of the $Co³⁺$ ion antiparallel to it. However, the sign of the XMCD signals in Figs. $3(b)$ and $3(d)$ shows that the magnetic moment of the Co ion and of the V ion are, respectively, parallel and antiparallel to the magnetic field. This spin orientation and the reduction of the spin magnetic moment of V from the ionic value is consistent with previous neutron studies on Mn_{1−}*y*Co_{*y*}V₂O₄ and $Co_{1+x}V_{2-x}O_4$ [\[23–25\]](#page-5-0), reflecting the strong geometrical frustration of the pyrochlore-type V sublattice. The XAS and

XMCD spectra at both edges show clear multiplet structures, reflecting that the V and Co electrons of this system are still localized even though the itineracy is indeed increased due to the short V-V bond length [\[21,22\]](#page-5-0). The spectral line shapes at the V edge is very similar to those of other ferrimagnetic insulating AV_2O_4 ($A = Fe$, Mn) [\[7–9\]](#page-5-0). This similarity also indicates that the V 3*d* electrons of $Co_{1.21}V_{1.79}O₄$ are almost localized similarly to the insulating AV_2O_4 ($A = Fe$, Mn). Therefore the homopolar bond formation mechanism [\[20\]](#page-5-0) which cannot take place for well localized V 3*d* electrons, where the U/W ratio should be large, may be ruled out as the origin of the lattice distortion in this material. It should be noted that the other ferrimagnetic insulating AV_2O_4 ($A = Fe$, Mn) show clearer structural phase transitions and are more distorted than $Co_{1+x}V_{2-x}O_4$. In particular, for MnV_2O_4 , $(c/a) - 1$ in the low-temperature tetragonal phase is 50 times larger than those of $Co_{1+x}V_{2-x}O_4$ [\[25\]](#page-5-0), indicating that the tetragonal distortions (elongation or contraction along the $\langle 001 \rangle$ directions), which accompany the orbital ordering, do not have a significant effect on the spectral line shapes of XAS and XMCD. A weak but clear XMCD signal was observed around the small O *K*-edge XAS pre-peak around 531 eV [Fig. $3(d)$] similarly to the reports on manganese oxides [\[37,38\]](#page-6-0). This XAS pre-peak is considered to arise from the 3*d*-2*p* hybridization. The observed XMCD signal should originate from the O 2*p*-hole orbital polarization induced by the overlap of the 3*d* and 2*p* orbital wave functions. According to the XMCD orbital sum rule [\[39\]](#page-6-0), the integral of the XMCD spectrum is proportional to the orbital magnetic moment. Therefore, the XMCD data show that the orbital magnetic moment of O is parallel to the spin and orbital magnetic moments of Co and parallel to the orbital magnetic moment of V. (Note that the spin and orbital magnetic moments of V are antiparallel to each other).

Figure [4](#page-3-0) shows XAS and XMCD spectra of the $Co_{1.21}V_{1.79}O₄$ single crystal under a magnetic field of 0.5 T along the [001] and [111] directions at various temperatures. Here, the XMCD spectra have been divided by $\cos \theta_H$ for comparison because the XMCD intensity is proportional to the projection of the magnetization onto the x-ray incident direction. The spectral line shapes of the XAS and XMCD

FIG. 4. Experimental spectra of $Co_{1,21}V_{1,79}O₄$ under the magnetic field of 0.5 T along the [001] and [111] directions at various temperatures. (a),(b) XAS and XMCD spectra at the Co $L_{2,3}$ edge. (c),(d) XAS and XMCD spectra at the V $L_{2,3}$ edge.

do not show any notable dependence on the magnetic field direction and temperature except for the intensities of XMCD. As shown in Figs. $4(b)$ and $4(d)$, the anisotropy of the XMCD intensity decreases with increasing temperature. This behavior is consistent with bulk magnetization measurements [\[25](#page-5-0)[,28\]](#page-6-0).

In order to clarify the electronic state of the excess Co ion and its role in the orbital-glass state, we have analyzed the obtained Co XAS and XMCD spectra using CI cluster-model calculation [\[32\]](#page-6-0). Since the Co : V ratio of this sample was estimated to be $1.21 : 1.79$, some of the V^{3+} ions at the octahedral site should be replaced by the excess Co^{3+} ions. In order to take the excess $Co³⁺$ ions into account, we calculated the spectra of Co both at the tetrahedral site (major component) and the octahedral site (minor component) and the weighted sum of the calculated spectra for the two sites were used for fitting. The ratio of the Co²⁺ ions at the tetrahedral site and the Co³⁺ ions at the octahedral site were fixed at $\text{Co}^{2+}(T_d): \text{Co}^{3+}(O_h) = 1$: 0*.*21. As for the tetrahedral site, the crystal-field splitting 10*Dq* and the $d-d$ Coulomb interaction energy U_{dd} were assumed to be −0*.*5 eV and 5.0 eV, respectively. The charge-transfer energy Δ and the Slater-Koster parameter ($pd\sigma$) were treated as adjustable parameters. As for the octahedral site, 10*Dq* was set to 1.1 eV and 0.7 eV in order to simulate the $Co³⁺$ low-spin (LS) $[(t_{2g})^6(e_g)^0]$ and high-spin (HS) $[(t_{2g})^4(e_g)^2]$ states, respectively. Other parameters were adopted from the previous report which reproduced the spectra of Co^{3+} in O_h site of $EuCoO₃$ [\[40\]](#page-6-0).

Figure 5 shows a comparison between the experimental and calculated Co $L_{2,3}$ XAS and XMCD spectra of Co_{1.21}V_{1.79}O₄. Two calculations were carried out by assuming two different scenarios: One is that the excess $Co³⁺$ ions take the LS state (red curves), and the other is that they take the HS state (blue

FIG. 5. Comparison between calculated (solid curves) and experimental (dots connected by lines) XAS (a) and XMCD spectra (b) at the Co $L_{2,3}$ edge of Co_{1.21}V_{1.79}O₄. The excess Co ions are assumed to be in the HS (blue curves) and LS (red curves) states. The inset of panel (b) shows a magnified view of the spectra around 776 eV. Discrepancies between the HS calculation and the experiment are marked by black arrows. Magnified views of XAS and XMCD spectra at the L_3 edge are also shown in (c) and (d), respectively.

curves). The adjusted parameters for these calculations are listed in Table I. (The parameters used for the calculation of $Co³⁺$ ions at the octahedral site are described in the previous text).

Although both the LS and HS $Co³⁺$ scenarios generally reproduce experimental spectra, the HS $Co³⁺$ scenario shows some structures (indicated by black arrows) which do not exist in the experimental spectra. Particularly in the pre-peak region of the Co-*L*³ XMCD spectrum [inset of Fig. 5(b).], the HS $Co³⁺$ scenario must show a clear peak which does not exist in the experimental spectra. Thus, the excess Co ions are more likely to take the magnetically and orbitally inactive LS state and, therefore, they can be dealt as a simple random potential similar to the substituted Al atoms of $Mn(V_{1-x}Al_x)O_4$ [\[41,42\]](#page-6-0). Taking into account the long-range orbital ordering in the low*x* region ($0 \le x < 0.15$) of Co_{1+*x*}V_{2−*x*}O₄ [\[26,](#page-5-0)[28\]](#page-6-0), the origin

TABLE I. Adjusted parameters in units of eV for the CI clustermodel calculation.

Element		$pd\sigma$	10Dq	U_{dd}
$Co(T_d)$	6.0	1.8		
V	5.0	2.3	0.8	5.0

FIG. 6. Comparison of the calculated and experimental XAS (a) and XMCD (b) spectra at the V $L_{2,3}$ edge of $Co_{1.21}V_{1.79}O₄$. The trigonal distortion of the $VO₆$ octahedron is taken into account as the splitting of the t_{2g} level. The calculated XAS and XMCD spectra have been normalized to the peak height at 518.0 eV and 517.8 eV, respectively.

of the orbital-glass state in this material may be the induced random potential due to the excess LS $Co³⁺$ ions.

We have also performed CI cluster-model calculations for the V $L_{2,3}$ edge. The parameters used for these calculations are also listed in Table [I.](#page-3-0) Because the important role of strong local trigonal distortion of the VO_6 octahedra, which intrinsically exists in the spinel-type structure, has recently been pointed out from first-principles calculations [\[4\]](#page-5-0), we included the trigonal distortion in the cluster-model calculation as a splitting of the t_{2g} level $[\epsilon(e'_g) - \epsilon(a_{1g}) = 100 \text{ meV}]$. As performed in previous reports $\left[\dot{7}, 9\right]$, we also calculated the spectra for the cases of reduced and full 3*d* spin-orbit interaction (0–30% and 100% of the ionic HF values, respectively). Figure 6 shows comparison between the experimental and calculated spectra. The calculation with weak 3*d* spin-orbit interaction reproduced the experiment well even though the trigonal distortion was taken into account.

Based on the above results, we have deduced the spin and orbital magnetic moments of Co and V using the XMCD sum rules [\[39,43\]](#page-6-0) and the results of the calculations. As for the Co edge, since the excess Co ions take the nonmagnetic LS state at the octahedral site, one can adapt the XMCD sum rules by subtracting the contributions of excess Co from the experimental XAS spectrum. The relative contributions of the $Co²⁺$ ions at the tetrahedral site (three holes in the 3*d* orbitals) and the $Co³⁺$ ions at the octahedral site (four holes) have been set as 1 : 0*.*28. Here, the latter contribution is assumed to be $\frac{4}{2}$ times as large as the excess Co concentration estimated from the ICP analysis because the absorption coefficient of an ion is proportional to the number of 3*d* holes. The magnetic

TABLE II. Spin and orbital magnetic moments in units of μ_B /atom and the total magnetic moments in units of μ_B /f.u. deduced from the XAS and XMCD spectra ($T = 30$ K, $H \parallel [001]$) using the XMCD sum rules and comparison with the calculation. Errors are evaluated from the reproducibility of multiple measurements.

Element	spin	orbital	$spin + orbital$
$Co(T_d)$	2.46 ± 0.03 $-0.91 \pm 0.05^{\circ}$	0.53 ± 0.03 0.07 ± 0.07	2.99 ± 0.06 -0.84 ± 0.12
total			1.48 ± 0.27

^a Evaluated by comparison with the calculation (see the main text).

dipole term of the XMCD spin sum rule has been neglected. As for the V edge, since the spin sum rule is not applicable due to the small energy separation between the V $2p_{3/2}$ and $2p_{1/2}$ levels [\[44\]](#page-6-0), the spin magnetic moment was evaluated by comparing the experimental XMCD/XAS intensity ratio with the calculated one. Here, the calculation with a small V 3*d* spin-orbit interaction parameter (10% of the Hartree-Fock value) was employed for the comparison. The effect of varying spin-orbit interaction to the calculated spin magnetic moment is included in the error shown in Table II. The orbital magnetic moment was deduced using the orbital sum rule, where the ionic 3*d*-hole number of 8 ($V^{3+}[3d^2]$) was assumed. The deduced spin and orbital magnetic moments are listed in Table II. Note that the total magnetic moment is $M_{Co,Td}$ + $1.79M_{V,Oh}$ because 10.5% of the octahedral site is occupied by the nonmagnetic Co^{3+} ions. We also note that the deduced total magnetic moment $1.48 \pm 0.27 \mu_B$ /f.u. is close to the results of bulk SQUID measurements $(1.54 \mu_B/f.u.)$. The deduced orbital magnetic moment of V (0.07 \pm 0.07 μ _B/atom) is small $(\ll 1 \mu_B)$. Since the ferro-orbital model [\[18\]](#page-5-0) should have a large orbital magnetic moment, the experimentally observed small one indicates that the ordered orbitals consist of predominantly real-number orbitals such as the antiferro-orbital [\[15,16\]](#page-5-0) or orbital-Peierls [\[17\]](#page-5-0) model.

IV. CONCLUSION

The electronic and magnetic properties of $Co_{1.21}V_{1.79}O₄$, where the V ions are in the orbital-glass state at low temperatures [\[24,25\]](#page-5-0), have been investigated by XAS and XMCD measurements and subsequent cluster-model analysis. From the line shapes of the XMCD spectra, it was found that the spin magnetic moments of Co are aligned parallel to the applied magnetic field and that those of the V ions are antiparallel to it. This spin orientation, which is opposite to the expectation from the simple ionic model, is consistent with previous neutron scattering studies. We have performed CI clustermodel calculation for both the Co and V $L_{2,3}$ edge spectra. As for the Co edge, the calculation assuming the LS state of the excess $Co³⁺$ ions at the octahedral site well reproduced the experimental spectra. This result indicates that the excess Co ions at the octahedral site are in the orbitally and magnetically inactive LS $Co³⁺$ state and induce a random potential to the crystal, which is a possible origin of the orbital-glass state in this material. The results of the XMCD sum rules are consistent with bulk magnetization measurements. The orbital magnetic moment of V was found to be small although finite

FIG. 7. Spin magnetic moment, orbital magnetic moment, and their ratio of Co as functions of temperature deduced by XMCD sum rule. (a) Spin and orbital magnetic moment. (b) Ratio of the orbital magnetic moment to the spin magnetic moment deduced only from the XMCD spectra.

 $(0.1 \mu_B/\text{atom})$. The results suggest that the ordered orbitals consist of predominantly real-number orbitals.

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APPENDIX: RESULTS OF THE XMCD SUM RULE AT THE CO *L***²***,***³ EDGE**

In this Appendix, we show all the results of XMCD sum rule for the Co $L_{2,3}$ edge. Figure 7 shows the temperature dependence of the spin magnetic moment, orbital magnetic moment, and their ratio of Co deduced by XMCD sum rule.

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