Anomalous quantum critical spin dynamics in $YFe₂Al₁₀$

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We report results of a muon spin relaxation (μ SR) study of YFe₂Al₁₀, a quasi-two-dimensional (2D) nearly ferromagnetic metal in which unconventional quantum critical behavior is observed. No static Fe^{2+} magnetism, with or without long-range order, is found down to 19 mK. The dynamic muon spin relaxation rate *λ* exhibits power-law divergences in temperature and magnetic field, the latter for fields that are too weak to affect the electronic spin dynamics directly. We attribute this to the proportionality of $\lambda(\omega_\mu,T)$ to the dynamic structure factor $S(\omega_{\mu},T)$, where $\omega_{\mu} \approx 10^5 - 10^7$ s⁻¹ is the muon Zeeman frequency. These results suggest critical divergences of $S(\omega_\mu, T)$ in both temperature and frequency. Power-law scaling and a 2D dissipative quantum XY model both yield forms for $S(\omega, T)$ that agree with neutron scattering data ($\omega \approx 10^{12} \text{ s}^{-1}$). Extrapolation to μ SR frequencies agrees semiquantitatively with the observed temperature dependence of $\lambda(\omega_\mu,T)$, but predicts frequency independence for $\omega_{\mu} \ll T$, in extreme disagreement with experiment. We conclude that the quantum critical spin dynamics of $YFe₂Al₁₀$ is not well understood at low frequencies.

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I. INTRODUCTION

Quantum phase transitions (QPTs) occur at absolute zero temperature, and are fundamentally different phenomena than thermally driven transitions. Ferromagnetic QPTs in metals, in particular, exhibit a broad spectrum of properties [1]. Theoretical work suggests that clean quantum critical ferromagnets should exhibit a discontinuous first-order phase transition, but it has been argued that inclusion of disorder [\[2,3\]](#page-4-0) or strong quantum fluctuations in low-dimensional systems [\[2\]](#page-4-0) can destroy the first-order character [\[4\]](#page-4-0), resulting in a quantum critical point. Thus investigating ferromagnetic quantum critical points (QCPs) in clean systems is crucial but difficult, as genuine reduced dimensionality and elimination of disorder are both hard to achieve. Furthermore, many measurement techniques (e.g., conventional magnetization, NMR) require applied magnetic fields that can tune the system away from criticality.

First reported in 1998 [\[5\]](#page-4-0), the layered compound $YFe₂Al₁₀$ is a rare example of a quasi-two-dimensional (2D) material that is on the threshold of ferromagnetism. Magnetic susceptibility and specific heat measurements reveal unusual divergences at

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low temperatures [\[4,6–9\]](#page-4-0), differing significantly from conventional Fermi-liquid metals. The divergences are quenched by a magnetic field [\[8\]](#page-4-0), which is characteristic of a ferromagnet. Such divergent or non-Fermi-liquid behavior is thought to be due to quantum fluctuations associated with a QCP [\[10\]](#page-4-0). $YFe₂Al₁₀$ is a clean [\[8\]](#page-4-0) stoichiometric compound, and is close to quantum criticality without tuning by chemical substitution, pressure, or magnetic field [\[4,8\]](#page-4-0).

Recent neutron scattering experiments [\[11\]](#page-4-0) revealed no long-range order in $YFe₂Al₁₀$ (i.e., no divergence of the spatial correlation length), but indicated a divergence of the fluctuation time scale. This contrasts strongly with the usual paradigm for critical phenomena, in which both spatial and temporal correlation scales diverge at the transition. It agrees, however, with the separability of these correlations found in the 2D dissipative quantum XY (2D-DQXY) model proposed by Varma and collaborators [\[12–](#page-4-0)[14\]](#page-5-0). The momentum-integrated magnetic dynamic structure factor $S(\omega, T)$ was observed to be essentially temperature independent, and over the range of energies in the experiment (0.35–0.7 meV, $\omega \approx 5{\text -}10 \times$ 10¹¹ s[−]1) its frequency dependence could be fit equally well by either by power-law scaling suggested by earlier work [\[4\]](#page-4-0) or the 2D-DQXY functional form [\[15\]](#page-5-0). The absolute value of $S(\omega, T)$ was determined in this study.

Magnetic resonance techniques such as NMR and muon spin rotation/relaxation (μSR) [\[16–19\]](#page-5-0) are local probes of magnetic behavior, and are therefore complementary to bulk measurements and reciprocal-space (scattering) probes. In

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magnetic resonance the dynamic or "spin-lattice" relaxation rate $\lambda(\omega, T)$ of the spin probe (nucleus or muon) also measures *S*(ω ,*T*) [\[20,21\]](#page-5-0), but at much lower frequencies (10⁵ − 10⁷ s⁻¹) than neutron scattering. Absolute values of $S(\omega, T)$ can thus be determined at both neutron and *μ*SR frequencies. An advantage of μ SR compared to NMR is that no external magnetic field is needed, since the muons in the incident beam are 100% spin polarized [\[16–19\]](#page-5-0). A field of any magnitude can be applied if desired.

This paper reports μ SR measurements of $\lambda(\omega, T)$ in single crystals of $YFe₂Al₁₀$. No evidence of magnetic order was found down to 19 mK. In contrast to a previous study [\[22\]](#page-5-0), significantly enhanced dynamic muon relaxation was observed at low temperatures and magnetic fields. This strongly suggests the presence of quantum critical spin fluctuations. The temperature dependence of $\lambda(\omega,T)$ agrees with that from extrapolation to low frequencies of $S(\omega, T)$ from either a power-law scaling description or the 2D-DQXY model, although the divergence of λ in temperature is cut off below ∼0.1 K; YFe₂Al₁₀ is close to but perhaps not exactly at quantum criticality. However, both of these approaches predict the frequency independence of *S*($ω$,*T*) at low frequencies, whereas a strong divergence ($λ$ $α$ 1*/H* at 25 mK) is observed. This rather extreme disagreement leads us to conclude that the low-frequency quantum critical dynamics in this compound is not well understood, and that more work is required.

II. EXPERIMENT

Single crystals of $YFe₂Al₁₀$ were grown in an aluminum flux as described previously [\[8\]](#page-4-0). Separate samples were prepared with *b* and *c* axes normal to the large faces. Oriented single crystals were mounted on silver sample holders using dilute GE varnish. Zero-field and longitudinal-field (applied field H_L parallel to the initial muon spin polarization P_μ) μ SR experiments (ZF- μ SR and LF- μ SR, respectively) were carried out at the M15 and M20 beam lines at TRIUMF, Vancouver, Canada, and at the LTF beam line at the Paul Scherrer Institute, Villigen, Switzerland. The time-differential μ SR technique [\[18,19\]](#page-5-0) was used, in which the evolution of the ensemble muon spin polarization is monitored via measurements of the decay positron count-rate asymmetry *A*(*t*) versus time *t* after muon implantation.

A. Zero-field *μ***SR**

ZF-*μ*SR experiments were performed over the temperature range 19 mK–10 K. ZF-*μ*SR asymmetry spectra are roughly temperature independent for $T \sim 1-10$ K, but exhibit a strong temperature dependence at lower temperatures. Representative spectra are shown in Fig. 1 for P_μ parallel to the *b* and *c* crystal axes [Figs. $1(a)$ and $1(b)$, respectively]. A constant background signal from muons that stop in the silver sample holder has been subtracted.

The ZF spectra are well described by the functional form

$$
A(t) = A_0 \exp(-\lambda_{ZF} t) G_{ZF}^{\text{KT}}(\Delta, t), \tag{1}
$$

where A_0 is the initial count-rate asymmetry, and

$$
G_{\text{ZF}}^{\text{KT}}(\Delta, t) = \frac{1}{3} + \frac{2}{3}(1 - \Delta^2 t^2) \exp\left(-\frac{1}{2}\Delta^2 t^2\right) \tag{2}
$$

FIG. 1. Zero-field (ZF) *μ*SR asymmetry spectra (time evolution of decay positron count-rate asymmetry) from single crystals of $YFe₂Al₁₀$. A constant background signal from muons that stop in the silver sample holder has been subtracted. (a) Initial muon spin polarization P_μ parallel to the *b* crystal axis, data taken at TRIUMF. (b) $P_\mu \parallel c$, data taken at PSI. Curves: Fits of exponentially damped ZF static Gaussian Kubo-Toyabe functions to the data (see text). No asymmetry loss or oscillations are observed, evidence that there is no static Fe²⁺ magnetism down to 19 mK.

is the ZF Kubo-Toyabe (KT) form expected [\[23\]](#page-5-0) from an isotropic Gaussian distribution of randomly oriented static or quasistatic local fields at muon sites. In Eqs. (1) and (2), Δ/γ_{μ} is the rms width of this distribution ($\gamma_{\mu} = 2\pi \times$ 135.53 MHz/T is the muon gyromagnetic ratio), and λ_{ZF} in Eq. (1) is the rate of exponential damping due to dynamic fluctuations of the local muon fields.

At 1.2 K the $ZF-\mu SR$ spectra (Fig. 1) are nearly of the KT form; the exponential damping is weak. This indicates that the relaxation is dominated by muon precession in quasistatic nuclear dipolar fields. Fits of Eq. (1) to the 1.2-K data yield $\Delta = 0.32(1)$ and $0.27(2)$ μ s⁻¹ for $P_\mu \parallel$ **b** and **c**, respectively. These values are typical of static nuclear dipolar field distributions, indicating the absence of motional narrowing; implanted muons are immobile. At low temperatures, the relaxation is considerably faster and more nearly exponential than at 1.2 K (Fig. 1); λ_{ZF} increases with decreasing temperature, whereas Δ is essentially unchanged (data not shown).

Figure [2](#page-2-0) gives the temperature dependence of λ_{ZF} . From values ∼0.05−0.1 μ s⁻¹ above 1 K, λ _{ZF} increases by an order of magnitude with decreasing temperature and then saturates below ∼0*.*1 K. Below ∼0*.*5 K the relaxation is isotropic. At higher temperatures, where the spin dynamics is presumably dominated by a mechanism or mechanisms other than quantum criticality, the relaxation becomes anisotropic.

The temperature dependence of the bulk magnetic susceptibility with field in the *ac* plane exhibits a $T^{-1.4}$ power-law divergence [\[4\]](#page-4-0). The dotted line in Fig. [2](#page-2-0) is a power-law fit to the data for $P_\mu \parallel b$, 0.1 K < T \leq 1 K; this yields an

FIG. 2. Temperature dependence of zero-field muon spin relaxation rate λ_{ZF} . Circles: $P_\mu \parallel \mathbf{b}$, data taken at TRIUMF. Triangles: \mathbf{P}_{μ} | c, data taken at PSI. Dotted line: Power-law fit to the data for $\mathbf{P}_{\mu} \parallel \mathbf{b}$, 0.1 K < T ≤ 1 K. Dashed line: $T^{-1.4}$ power law. Solid curve: 2D-DQXY functional form [\[15\]](#page-5-0). The latter two curves are normalized to neutron scattering data (see text). Inset: Temperature dependence of total zero-field initial asymmetry A_{tot} (sample+silver background).

exponent −1*.*2(1), not far from the susceptibility value. The dashed line in Fig. 2 is from a $T^{-1.4}$ power-law scaling scenario [\[11\]](#page-4-0), and the solid curve is from from the 2D-DQXY model [\[15\]](#page-5-0). The magnitudes of both predictions are normalized using neutron scattering data, as discussed in detail in Sec. III. In this temperature range the predictions are nearly the same, and quite comparable to the observed data, particularly for $P_\mu \parallel b$ (although the absolute magnitudes are a factor 3–4 too small).

In a number of quantum ferromagnetic materials the temperature dependence of the muon spin relaxation rate also obeys a power law (above the Curie temperature if there is ferromagnetic ordering). Experimental values of the exponent are −0.8 in CePd_{0.15}Rh_{0.85} [\[24\]](#page-5-0), −0.33 in YbCu_{4.4}Au_{0.6} [\[25\]](#page-5-0), −0*.*4 to −0*.*5 in YNi4P2 [\[26\]](#page-5-0), and −0*.*01 to −0*.*13 in YbNi₄($P_{1x}As_x$)₂ [\[27\]](#page-5-0). In YFe₂Al₁₀ the exponent magnitude is considerably larger than in these materials.

The inset in Fig. 2 shows the temperature dependence of the total initial asymmetry A_{tot} (sample+silver background). Its temperature independence and the absence of oscillations in the spectra due to precession in an internal field (Fig. [1\)](#page-1-0) are evidence against static Fe^{2+} magnetism, ordered or disordered, down to 19 mK.

B. Longitudinal-field *μ***SR**

LF- μ SR relaxation rates were measured in YFe₂Al₁₀ for applied magnetic fields up to 200 Oe at a number of temperatures. Figures $3(a)$ and $3(b)$ show LF- μ SR asymmetry spectra at base temperatures for $H_L \parallel b$ and $H_L \parallel c$, respectively. The LF-*μ*SR spectra are well described by an exponentially damped static relaxation function similar to that of Eq. [\(1\)](#page-1-0), except that the static Gaussian KT function $G_{LF}^{KT}(\Delta, t)$ for a longitudinal magnetic field [\[23\]](#page-5-0) is used. The majority of the field dependence seen in Fig. 3 is due to "decoupling" of the static relaxation by the field [\[23\]](#page-5-0), but the dynamic relaxation also slows with increasing field.

FIG. 3. Dependence of muon asymmetry relaxation function *A*(*t*) on longitudinal field H_L in oriented single crystals of $YFe₂Al₁₀$. (a) $H_L \parallel b$, data taken at TRIUMF. (b) $H_L \parallel c$, data taken at PSI. Curves: Fits of exponentially damped Gaussian static Kubo-Toyabe functions to the data (see text). Decoupling of static relaxation and slowing of dynamic relaxation both contribute to the field dependence.

Figure [4](#page-3-0) shows the field dependence of λ_{LF} from LF- μ SR data for longitudinal field **H***^L* oriented along the *b* and *c* crystal axes. The lines are power-law fits to all $(\mathbf{H}_L \parallel \mathbf{b})$ or part $(\mathbf{H}_L \parallel \mathbf{c})$ of the data. There is a general tendency for the power-law exponent to decrease with increasing temperature. For $H_L \parallel c$ the data deviate from power laws at low fields, and the change of *λ*LF is small enough to cast doubt on the uniqueness of the power-law fits. The behavior of λ_{LF} is clearly anisotropic. This is not well understood, but may be due to the anisotropy in the $Fe²⁺$ dipolar fields at muon sites [\[28\]](#page-5-0).

The field dependence of λ_{LF} might suggest that it originates from a Lorentzian contribution to the static field distribution and is thus decoupled by the field, as in $PrP_{4}Ge_{12}$ [\[29\]](#page-5-0). In this scenario the nearly exponential relaxation at low temperatures (Fig. [1\)](#page-1-0) indicates dominance of the (static) Lorentzian contribution, such that decoupling would be complete for $H_L \gtrsim 5\lambda_{\text{ZF}}/\gamma_\mu \approx 20$ Oe [\[23,30\]](#page-5-0). This scenario seems unlikely, however. Particularly for $H_L \parallel b$, the field dependence of λ is accurately represented by a power law for fields above and below 20 Oe [Fig. $4(a)$].

III. DISCUSSION

As a consequence of the fluctuation-dissipation theorem, the muon spin relaxation rate is approximately [\[19,20,31\]](#page-5-0) related to the imaginary component $\chi''(\mathbf{q}, \omega_{\mu}, T)$ of the dynamic

FIG. 4. Field dependence of the LF dynamic relaxation rate $\lambda_{LF}(H)$ at low temperatures. Lines are power-law fits to the data. (a) Longitudinal field H_L parallel to crystal axis **b**. Solid line: $T =$ 25 mK, slope $= -1.00(5)$, data taken at TRIUMF. Dashed line: $T =$ 200 mK, slope = $-0.78(4)$. (b) $H_L \parallel c$, data taken at PSI. Lines are fit to data above 10 Oe. Solid line: $T = 19$ mK, slope = $-0.39(11)$. Dashed line: $T = 100$ mK, slope $= -0.47(7)$. Dashed-dotted line: $T = 400$ mK, slope = $-0.35(8)$.

susceptibility,

$$
\lambda(\omega_{\mu},T) = \frac{2\hbar\gamma_{\mu}^{2}}{g^{2}\mu_{B}^{2}} \left(\frac{k_{B}T}{\hbar\omega_{\mu}}\right) \sum_{\mathbf{q}} A_{\mathbf{q}} A_{-\mathbf{q}} \chi''(\mathbf{q},\omega_{\mu},T), \quad (3)
$$

where $\omega_{\mu} = \gamma_{\mu} H_L$ is the muon Zeeman frequency and A_q is the spatial Fourier transform of the coupling magnetic field between electronic fluctuations and probe spins. Furthermore, the dynamic structure factor $S(\omega, T)$ is given by [\[11\]](#page-4-0)

$$
S(\mathbf{q}, \omega, T) = \frac{2(n+1)}{\pi g^2 \mu_B^2} \chi''(\mathbf{q}, \omega, T), \tag{4}
$$

where $n + 1 = [1 - \exp(-\hbar \omega / k_B T)]^{-1}$ is the Bose or detailed balance factor. In the limit $\omega \ll T$, $n + 1 \rightarrow k_B T / \hbar \omega$, which is the factor in parentheses in Eq. (3). Thus *S* and λ are closely related.

If the electronic spin fluctuations are not spatially corre-lated, as is the case in YFe₂Al₁₀ [\[11\]](#page-4-0), then $\chi''(\mathbf{q}, \omega_{\mu}, T)$ is independent of **q**, and from Eq. (3),

$$
\lambda(\omega_{\mu},T) = \frac{2\hbar\gamma_{\mu}^2|A|^2}{g^2\mu_B^2} \left(\frac{k_B T}{\hbar\omega_{\mu}}\right) \chi''(\omega_{\mu},T),\tag{5}
$$

where $|A^2| = \sum_{\mathbf{q}} A_{\mathbf{q}} A_{-\mathbf{q}}$. Then,

$$
S(\omega_{\mu}, T) = \lambda(\omega_{\mu}, T) / \pi \hbar \gamma_{\mu}^{2} |A|^{2},
$$
 (6)

and the field dependence of $\lambda(H_L, T)$ directly probes the frequency dependence of $S(\omega, T)$ at the low muon frequencies. In effect, we are sweeping the muon Zeeman frequency through the noise power spectrum of the fluctuations [\[32,33\]](#page-5-0).

For this analysis to be valid, the applied field must be low enough that the fluctuating spin dynamics is not affected. This appears to be the case in $YFe₂Al₁₀ [4,11]$ $YFe₂Al₁₀ [4,11]$, and we attribute the field dependence of λ_{LF} to the frequency dependence of the dynamic structure factor.

Thus we can make a quantitative comparison between neutron and *μ*SR results, notwithstanding the large difference in frequencies probed in the two experiments. In neutron scattering $\hbar \omega / k_B$ is typically of the order of degrees Kelvin or greater, whereas $\hbar \gamma_\mu / k_B \sim 10^{-6}$ K/Oe.

We consider two models for $\chi''(\omega,T)$. Motivated by magnetic susceptibility results and scaling arguments from earlier studies [\[4\]](#page-4-0), Gannon *et al.* [\[11\]](#page-4-0) have shown that their data can be fit by either a temperature-independent *ω*[−]1*.*⁴ power law or the ω/T scaling form (in units where $\hbar/k_B = 1$)

$$
\chi''(\omega, T) \propto [\omega^2 + (\pi T)^2]^{-1.4/2} \tanh(\omega/T). \tag{7}
$$

Alternatively, a treatment of critical spin dynamics within the 2D-DQXY model [\[15\]](#page-5-0) suggests the form

$$
\chi''(\omega,T) \propto \frac{\log^2\{[\omega^2 + (\pi T)^2]^{1/2}/\omega_c\}}{[\omega^2 + (\pi T)^2]^{1/2}} \tanh(\omega/T), \quad (8)
$$

where ω_c is a high-frequency cutoff. The combination of temperature and frequency avoids a divergence in the Kramers-Kronig relation between χ'' and χ' that would occur without the temperature cutoff in the frequency dependence [\[11](#page-4-0)[,15\]](#page-5-0). Over the temperature range of the experiments, the frequency and temperature dependencies of Eqs. (7) and (8) are essentially indistinguishable at μ SR frequencies, as is also the case at meV neutron scattering energies as noted above.

To obtain quantitative values of *S* from relaxation rates and Eq. (6), we must determine $|A|^2$. We have calculated dipolar fields due to Fe moments [\[34\]](#page-5-0) in the *ac* plane at two candidate muon spin sites [\[35\]](#page-5-0) from lattice sums in the orthorhombic YbFe2Al10 structure (space group *Cmcm*, No. 63). The rms dipolar coupling field $A_{\text{rms}} = |A^2|^{1/2}$ varies between 400 and 800 G/ μ_B , depending on the site and the muon spin direction. Then, $\gamma_{\mu}A_{\text{rms}} \approx 5 \times 10^7 \text{ s}^{-1}/\mu_B$ to within a factor of 2. As an example, the measured value of λ_{ZF} at 25 mK is about 4×10^5 s⁻¹. With $\hbar = 6.582 \times 10^{-13}$ meV s, the effective structure factor from Eq. (6) is

$$
S \approx \frac{4 \times 10^5}{\pi \hbar (5 \times 10^7)^2} \approx 80 \mu_B^2/\text{meV} \,\text{Fe},\tag{9}
$$

to within a factor of 4.

We next compare these model results with our data.

A. Zero-field *μ***SR.**

As noted in Sec. [II A,](#page-1-0) the observed temperature dependence of $\lambda_{\text{ZF}}(T)$ is compatible with either of the above scenarios. The absolute value of $\lambda_Z F$ is underestimated by a factor of 3–4 (Fig. [2\)](#page-2-0), but this may be considered as a semiquantitative agreement, considering the accumulated uncertainty involved in determining the normalization factor and the effect of noncritical relaxation mechanisms.

B. Longitudinal-field *μ***SR.**

An order-of-magnitude suppression of *λ*LF is observed in fields as low as 50 Oe (Fig. 4). A possible scenario for this might involve the preasymptotic/asymptotic crossover predicted for

FIG. 5. Frequency dependence of the dynamic structure factor *S*(ω ,*T*). Circles: *S*(ω) from neutron scattering [11]. Triangles: *S*(ω) from μ SR relaxation rates for $H_L \parallel b$ and $T = 25$ mK [Fig. [4\(a\)](#page-3-0) and Eq. [\(6\)](#page-3-0)]. Solid curves: $S(\omega, T)$ from 2D-DQXY model [\[15\]](#page-5-0) [Eq. [\(8\)](#page-3-0), $\omega_c = 161$ K [11]]. Dashed curves: Scaling power law [Eq. [\(7\)](#page-3-0)]. Both sets of curves are normalized to the neutron scattering data.

disordered quantum ferromagnets [1[,36\]](#page-5-0). But Park *et al.* [8] have argued that $YFe₂Al₁₀$ is a clean system, for which the theory of Ref. [\[36\]](#page-5-0) would not be appropriate. Furthermore, the field dependence of the Fe^{2+} spin fluctuation spectrum seems unlikely, since both the uniform [4] and dynamic [11] spin susceptibilities are unaffected by fields of this magnitude. Instead, as discussed above, we attribute the field dependence of λ_{LF} to the frequency dependence of χ'' and hence of *S*.

Figure 5 gives the calculated frequency dependence of $S(\omega, T)$ from the scaling scenarios at various temperatures, together with results from neutron scattering [11] and from LF- μ SR relaxation data and Eq. [\(6\)](#page-3-0) (the error bars are due to the uncertainty in the estimate of the rms coupling field noted above, which is much greater than the statistical error in λ_{LF}). The curves are from Eqs. [\(7\)](#page-3-0) and [\(8\)](#page-3-0) ($\omega_c = 161$ K [\[15\]](#page-5-0)), normalized to the neutron scattering data and evaluated at various temperatures. For $\omega \ll T$ the scaling scenarios predict no frequency dependence of *S* and hence no field dependence of *λ*LF for low fields, contrary to the considerable observed power-law field dependence.

This discrepancy is not understood at present. We note that the data seem to suggest a product form $S(\omega, T) \propto \omega^{-\Gamma} T^{-\Delta}$ at ultralow frequencies, rather than the $\omega^2 + (\pi T)^2$ dependence of the power-law and 2D-DQXY model results. Such a product

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preserves ω/T scaling, but the resultant divergence in $\chi''(\omega)$ leads to the problem with the Kramers-Kronig relation discussed above.

It should perhaps also be noted that the suppression of λ_{LF} with field at low temperatures cannot be due to mechanisms other than that which increases λ_{ZF} at low temperatures. Such mechanisms would increase the rate rather than decreasing it.

IV. SUMMARY

Dynamic muon spin relaxation has been studied in the quasi-2D nearly ferromagnetic compound $YFe₂Al₁₀$. The relaxation behavior indicates that there is no static electronic magnetism, ordered or disordered, down to 19 mK. In zero applied field the dynamic muon spin relaxation rate $λ_{ZF}$ is strongly enhanced below 1 K, saturating at $\sim 0.4 \ \mu s^{-1}$ below 0.1 K. In the temperature range 0.1–1.0 K, a power law $\lambda_{\text{ZF}}(T) \propto T^{-1.2(1)}$ was observed. This power and the magnitude of λ_{ZF} are in semiquantitative agreement with extrapolations of power-law scaling or the 2D-DQXY model for 2D ferromagnetic quantum critical fluctuations. At 25 mK, $\lambda_{LF}(\mathbf{H}_{L} \parallel \mathbf{b})$ exhibits a power-law dependence on field, with exponent $-1.00(5)$. This is in extreme disagreement with the frequency independence expected from power-law scaling or the 2D-DQXY model. We conclude that neither of these fully captures the low-frequency spin dynamics associated with the QCP in $YFe₂Al₁₀$, and that more work is necessary to understand this elusive system.

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