

Evidence for magnetic-field-induced decoupling of superconducting bilayers in $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ Ruidan Zhong,^{1,2,*} J. A. Schneeloch,^{1,†} Hang Chi,¹ Qiang Li,¹ Genda Gu,¹ and J. M. Tranquada^{1,‡}¹*Condensed Matter Physics and Materials Science Division, Brookhaven National Laboratory, Upton, New York 11973, USA*²*Materials Science and Engineering Department, Stony Brook University, Stony Brook, New York 11794, USA*

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We report a study of magnetic susceptibility and electrical resistivity as a function of temperature and magnetic field in superconducting crystals of $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ with $x = 0.10$ and 0.15 and transition temperature $T_c^m = 54$ K (determined from the susceptibility). When an external magnetic field is applied perpendicular to the CuO_2 bilayers, the resistive superconducting transition measured with currents flowing perpendicular to the bilayers is substantially lower than that found with currents flowing parallel to the bilayers. Intriguingly, this anisotropic behavior is quite similar to that observed for the magnetic irreversibility points with the field applied either perpendicular or parallel to the bilayers. We discuss the results in the context of other studies that have found evidence for the decoupling of superconducting layers induced by a perpendicular magnetic field.

DOI: [10.1103/PhysRevB.97.134520](https://doi.org/10.1103/PhysRevB.97.134520)**I. INTRODUCTION**

An unusual state of matter has been observed in the underdoped regime of at least one cuprate superconductor family, in which application of a c -axis magnetic field (perpendicular to the CuO_2 planes) destroys the phase coherence between the planes but appears to leave the superconducting response within the layers unaffected. This effect was first detected by Schafgans *et al.* [1] in c -axis optical reflectivity measurements of the Josephson plasma resonance in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, with related behavior observed in a careful study of anisotropic susceptibility [2]. It was confirmed in $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ (LBCO) with $x = 0.095$ through measurements of in-plane and c -axis resistivity [3], with the decoupling still prominent in fields up to at least 35 T [4]. In these systems, the decoupling is correlated with the occurrence of charge-stripe order [5–7] and presumably reflects a field-induced frustration of interlayer Josephson coupling by pair-density-wave superconductivity [8–11] as proposed for the case of LBCO with $x = 0.125$ [12,13].

It is of interest to test whether such phenomena may occur in other cuprates. A field-induced charge-density-wave transition has been observed in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ [14–16]. It appears to be associated with the loss of superconducting order [17]; however, torque magnetometry [18] and specific heat [19] studies suggest that significant superconducting correlations survive to higher fields. The relationship to the decoupling behavior described above remains to be resolved.

In this paper, we investigate another cuprate system. We have recently succeeded in preparing superconducting crystals of $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ (La-Ca-2126) of sufficient size

for inelastic neutron scattering experiments [20]. Here we present a study of the anisotropic transport and magnetic susceptibility for two of these samples. This system is different from $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ in that it contains CuO_2 bilayers, as in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$, though the bilayers are stacked in a centered fashion, similar to $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$, as shown in Fig. 1(a). Interpretation of the results requires some care, as the high-pressure oxygen annealing essential to achieving superconductivity also results in the presence of minority phases of $\text{La}_{2-x}\text{Ca}_x\text{CuO}_4$ (La-214) and $\text{La}_8\text{Cu}_8\text{O}_{20}$. The latter compound is an antiferromagnetic insulator, while the former occurs as very thin intergrowths; all phases are crystallographically aligned along the c axis [20,21]. We believe that the segregation of these phases enhances the Ca concentration of the main La-Ca-2126 phase, thus providing sufficient hole doping to yield superconductivity.

Despite the complications, we find that application of a c -axis magnetic field results in distinct temperatures at which the in-plane and c -axis resistivities reach the normal state. The anisotropy in these transitions is quite similar to that in the irreversibility field for magnetic susceptibility measured with the field applied perpendicular or parallel to the c axis. We interpret the resistivity results as evidence of decoupling of the superconducting bilayers, indicating that such behavior is not unique to single-layer cuprates.

II. EXPERIMENTAL METHODS

Crystals of La-Ca-2126 with $x = 0.10$ and 0.15 were grown by the traveling-solvent floating zone method [23]. The as-grown crystals were not superconducting, but they were converted to bulk superconductors by high-pressure annealing in a gas of 20% O_2 /80% Ar [20]. Transmission electron microscopy (TEM) on an early version of such an annealed crystal demonstrated the presence of thin intergrowths of La-214 [21]. Layers of La-214 were observed with thicknesses of 1.5 or 3 unit cells along the c axis, which are commensurate with 1 or 2 unit cells, respectively, of the La-Ca-2126 phase.

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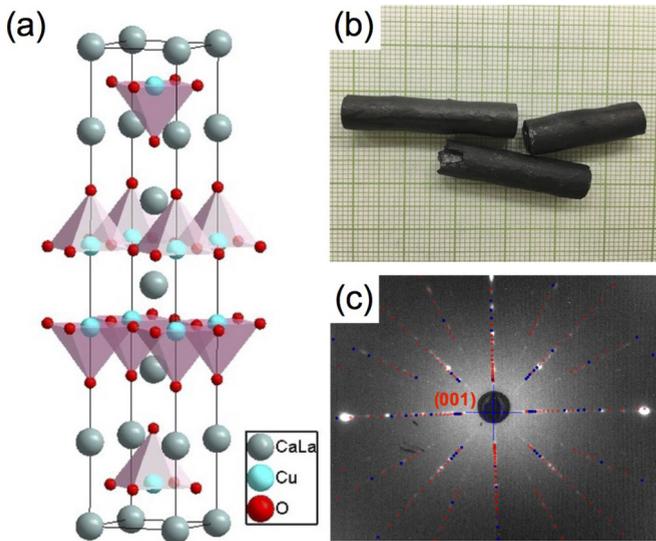


FIG. 1. (a) Crystal structure of the $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$. (b) As-grown $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ single-crystal rods grown by the traveling-solvent floating-zone method. (c) Laue back-diffraction image of $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ single crystal with (001) direction (c axis) pointing along the x-ray beam. Color points in (c) correspond to the calculated diffraction pattern, generated by software QLaue [22].

Neutron diffraction confirmed the presence of the thin La-214 layers, but, in combination with muon spin rotation, provided evidence for thicker layers of antiferromagnetic $\text{La}_8\text{Cu}_8\text{O}_{20}$ [20]. The volume fraction associated with the superconducting La-Ca-2126 was estimated to be $\sim 70\%$.

The annealed single crystals were aligned to the desired orientations via x-ray Laue back-diffraction; the ab -plane diffraction pattern with the c axis pointing along the incident x-ray beam is shown in Fig. 1(c). Then the crystals were cut and polished into a nearly rectangular parallelepiped shape, with dimensions along $a \times b \times c$ of either (a) $4 \times 1 \times 1 \text{ mm}^3$ or (b) $1 \times 1 \times 3 \text{ mm}^3$. For magnetization measurements, the field was applied along the long axis. For resistivity measurements, the current was applied along the long axis, with the field always along the c axis. For each composition, at least two crystals were prepared of type (a), and they yielded similar results. Because of difficulties preparing crystals without cracks, only one each of type (b) was studied.

To study the magnetization and transport anisotropy, we performed measurements on samples with both orientations. The dc magnetic susceptibility measurements were performed using a Magnetic Property Measurement System from Quantum Design, with a superconducting quantum interference device (SQUID) magnetometer. Electrical resistivity was measured using the in-line four-point configuration, with an excitation current of 1 mA, in a Quantum Design Physical Properties Measurement System (PPMS).

III. SUSCEPTIBILITY MEASUREMENTS

Magnetic susceptibility measurements performed with a field of 10 Oe for both samples are displayed in Fig. 2. Measurements with the field perpendicular [parallel] to the CuO_2 planes are shown in Figs. 2(a) and 2(d) [Figs. 2(b)

and 2(e)]. Evidence for the compositional uniformity of the superconducting phase in the annealed samples is given by the sharp superconducting transitions (width ~ 5 K). A linear extrapolation of the transition region yields a magnetically determined superconducting transition temperature $T_c^m = 54$ K for both compositions, slightly higher¹ than previously reported single-crystal results [21,24–26]. For the zero-field-cooling (ZFC) curves, 100% volume shielding would correspond to $\chi = 0.0126 \text{ emu g}^{-1} \text{ Oe}^{-1}$; the observed response is of this magnitude despite the fact that the volume fraction of the La-Ca-2126 phase is just 70% [20]. The Meissner fraction, determined by the field-cooled (FC) measurements, is considerably smaller; such behavior in cuprates is common and is typically attributed to flux pinning [25].

For comparison, magnetization measurements on a La-Ca-2126 crystal with $x = 0.1$ previously grown and annealed by our group had a similar T_c^m of 53.5 K, but also showed a small enhancement of the diamagnetic response below 13 K [21,26]. That contribution might be due to La-214 layers, which are also present in the current samples; however, no low-temperature jumps in the diamagnetism are apparent in Fig. 2.

We have also measured the temperature dependence of $\chi = M/H$ for a range of magnetic fields up to 7 T. A comparison of FC and ZFC results obtained for both field orientations on the $x = 0.1$ sample is presented in Fig. 3; the results for the $x = 0.15$ sample (not shown) are quite similar. Hysteresis in the magnetic response provides evidence of pinning of magnetic vortices in the mixed phase [27–29]. The irreversibility field, H_{irr} , which is defined as the field that separates reversible and irreversible regions, provides a lower limit on the loss of static vortex matter. It is observed to be sensitive both to temperature and to the orientation of the field with respect to the CuO_2 planes. The temperature dependence of H_{irr} for both field orientations is summarized in Fig. 3(c); note that the results for both samples are included and are nearly identical. As shown in the figure, the irreversibility field at any given temperature is much higher when the field is applied parallel to the planes. In other words, it is easier to pin vortices aligned parallel with, and centered between, the superconducting bilayers than it is to pin vortices that pierce the bilayers.²

It is important to avoid confusing H_{irr} with the loss of superconducting correlations. As shown in a study of the reversible magnetization on a similar sample of La-Ca-2126 with $x = 0.1$ [26], the temperature of the onset of diamagnetism shows very little change with fields up to 5 T, which is relatively close to what we observe for H_{irr} when the field is parallel to the bilayers. To gain further insight into the behavior when the field is perpendicular, we turn to the measurements of transport anisotropy.

¹The results are consistent with those previously presented for the same samples in Ref. [20] and characterized as $T_c = 55$ K. We have used a slightly different determination of T_c here.

²The layers of impurity phases may provide some local enhancement of pinning for $H \parallel ab$; however, it is not clear that this would significantly impact the irreversibility field for pinning within superconducting domains. In any case, the anisotropy we find in H_{irr} is consistent with previous observations in cuprates free of impurity phases [28,47,48].

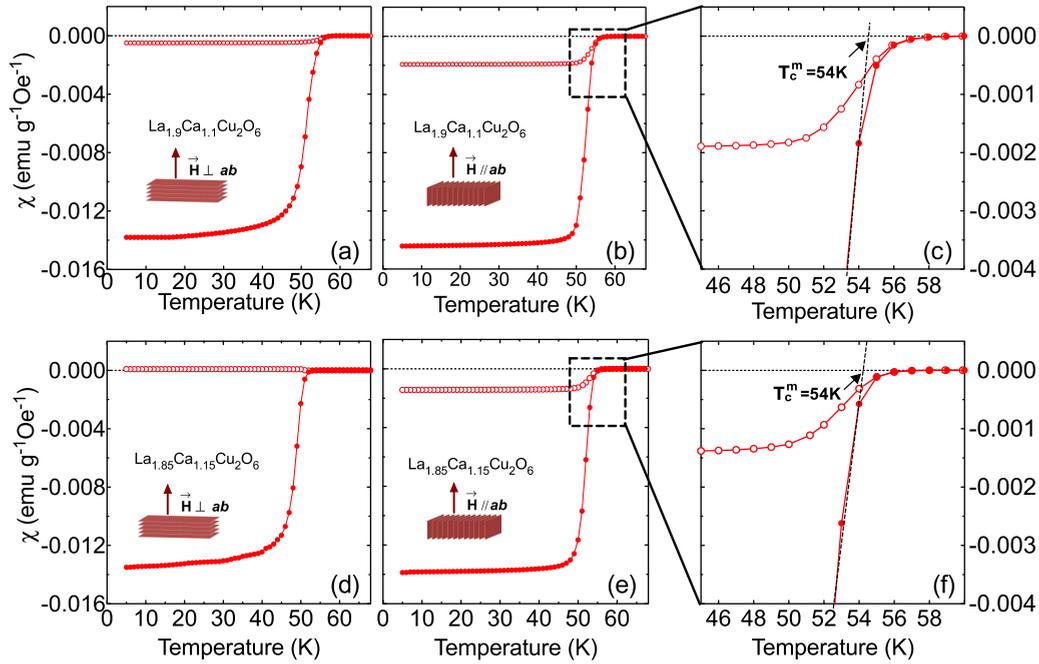


FIG. 2. Mass magnetic susceptibility ($\chi = M/H$) of $\text{La}_{1.9}\text{Ca}_{1.1}\text{Cu}_2\text{O}_6$ (top row) and $\text{La}_{1.85}\text{Ca}_{1.15}\text{Cu}_2\text{O}_6$ (bottom row), measured with a magnetic field of 10 Oe applied (a), (d): perpendicular to the CuO_2 planes or (b), (c), (e)–(f): parallel to the planes. Measurements were performed both in zero-field cooling (ZFC, filled circles) and field-cooling (FC, open circles) modes. The insets illustrate the relative directions of CuO_2 planes and the magnetic field H . The criteria to determine T_c^m is shown in (c) and (f).

IV. TRANSPORT MEASUREMENTS

A. Zero-field results

The resistivities measured with currents flowing in-plane, ρ_{ab} , and along the c axis, ρ_c , are shown in Fig. 4(a) for both samples. We observed a metallic temperature dependence of the resistivity in both directions. The magnitudes of ρ_{ab} and ρ_c are comparable to those reported for a superconducting crystal ($T_c \approx 46$ K) of La-Ca-2126 with $x = 0.1$ by Okuya *et al.* [25] (though they are each about an order of magnitude larger than the results obtained on a flux-grown crystal with $x = 0.13$ and $T_c \approx 40$ K from an earlier study by Ishii *et al.* [24]). Comparing with other cuprates, the magnitude of ρ_c is comparable to that of optimally doped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ [30], while lower than that of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ [31] and higher than that of $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ [32]; however, ρ_{ab} is about an order of magnitude larger than that for most cuprates [30–34].

The anomalously large magnitude of ρ_{ab} requires further discussion. We expect that the intrinsic ρ_{ab} for our La-Ca-2126 samples should be similar to that of other cuprates near optimal doping. The measured quantity, however, is impacted by the presence of other phases, especially the $\text{La}_8\text{Cu}_8\text{O}_{20}$ phase, which we expect to be insulating [20]. While the extra phases are coherently oriented with the main phase, the TEM study showed that interfaces between phases can occur along in-plane directions as well as along the c axis. As a consequence, the current path in a resistivity measurement may involve detours that mix contributions from in-plane and out-of-plane directions. Because ρ_{ab} is much smaller than ρ_c , any current path that includes flow along the c axis causes a substantial increase in the measured result for ρ_{ab} .

These effects are also apparent when we look at an expanded view of the superconducting transition region, shown in Fig. 4(b). In particular, ρ_{ab} has turned down by T_c^m , but it only reaches zero at 52 K. (In a single-phase sample, the situation is usually reversed, with the diamagnetism only starting to grow when the resistivity reaches zero.)

In contrast to ρ_{ab} , the magnitude of ρ_c is found to be comparable to that of other cuprates. We believe this is also compatible with an indirect current path. If the current flowing along the c axis of the La-Ca-2126 phase hits a layer of impurity phase, the path of least resistance may involve a detour parallel to the CuO_2 bilayers, before arriving at a domain where it can once again run along the c -axis of the main phase. Any excursions within the planes are effectively like electrical shorts, and will not impact the measurement of ρ_c .

It is evident from Fig. 4(c) that the measurements of ρ_c cannot entirely avoid the insulating $\text{La}_8\text{Cu}_8\text{O}_{20}$ phase, as there is residual resistivity below T_c . For the $x = 0.15$ sample, ρ_c just below T_c is only $\sim 1\%$ of that in the normal state; considering that the resistivity of the insulating phase is much greater than that of La-Ca-2126 in the normal state, the relative path length through the insulator must be far less than 1%. For the $x = 0.10$ sample, ρ_c drops to a much smaller but finite value at 52 K.

B. Dependence on a c -axis field

Next, we consider the impact of a c -axis magnetic field on the temperature dependence of ρ_{ab} and ρ_c . Measurements in fields up to 7 T are presented in Fig. 5. As one can see, the field has only a small impact on the resistive transition as measured with currents parallel to the planes, whereas it causes

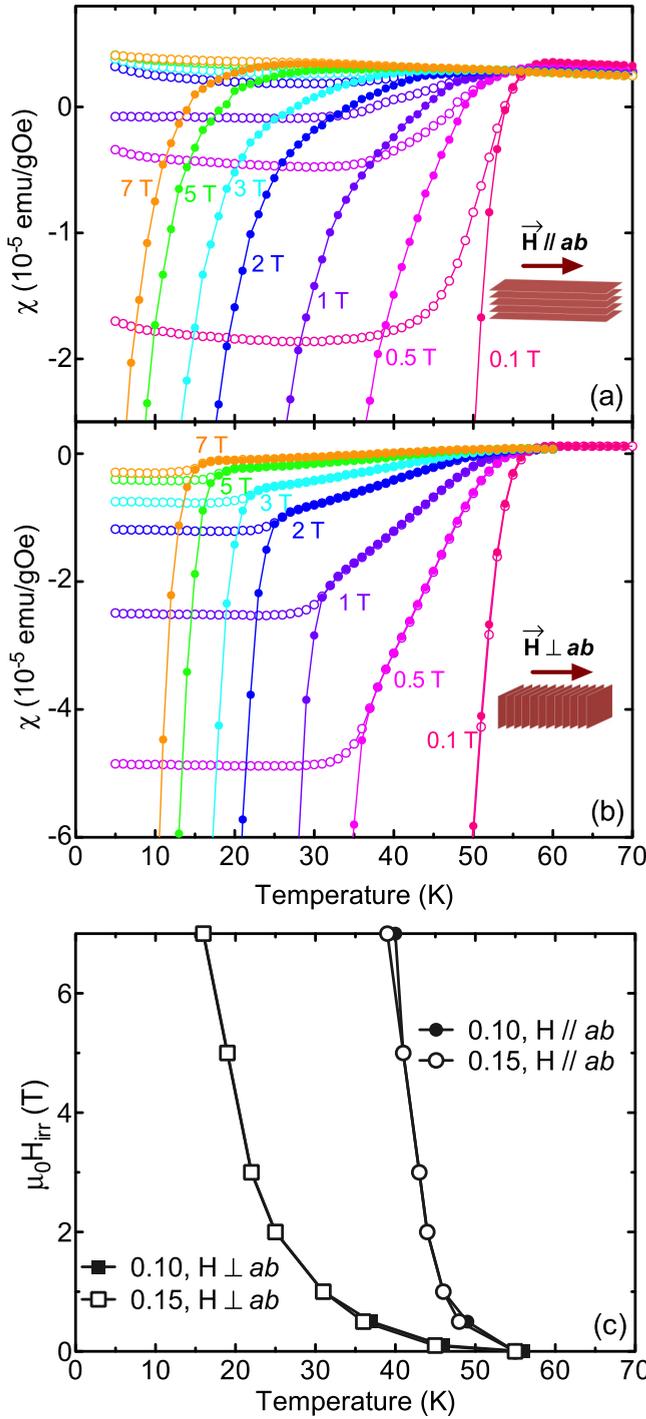


FIG. 3. (a) The hysteretic curves of magnetic susceptibility versus temperature in sample $\text{La}_{1.9}\text{Ca}_{1.1}\text{Cu}_2\text{O}_6$ under an in-plane field ($H \parallel ab$) up to 7 T. (b) Similar hysteretic curves obtained under a perpendicular field ($H \perp ab$). (c) The T dependences of irreversibility field $H_{irr}(T)$ in both directions relative to the CuO_2 planes for the $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ ($x = 0.10$ and 0.15) single crystals.

a substantial reduction in the transition temperature when the measuring current is along the c axis.

To quantify the anisotropic transition temperatures, we have to take account of the extrinsic resistivity observed in ρ_c when ρ_{ab} goes to zero. To do this, we identify the

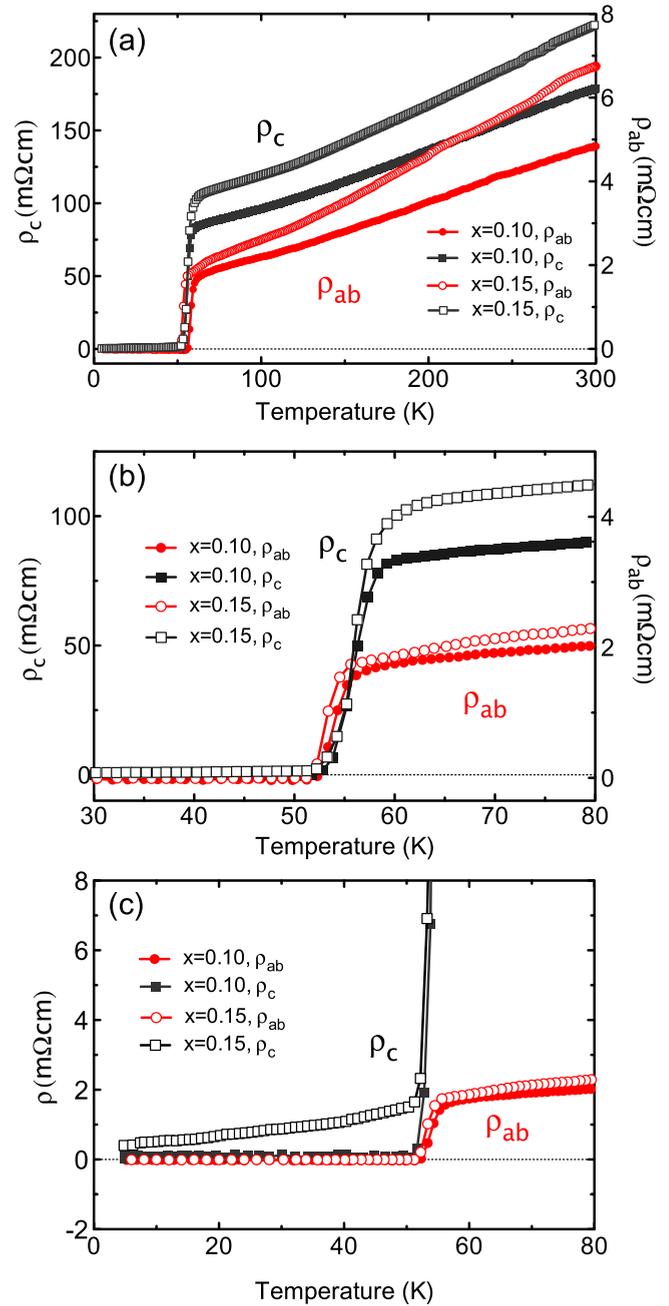


FIG. 4. (a) The in-plane resistivity $\rho_{ab}(T)$ and interlayer resistivity $\rho_c(T)$ of the superconducting $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ single crystals. Different y-axis values are used to illustrate the normal-state resistivity in both directions. (b) A zoomed-in figure showing the superconducting transition near 54 K. (c) A zoomed-in figure showing the finite resistivity in ρ_c at low temperature.

transition in $\rho_c(T, H)$ as occurring when it reaches the value of $\rho_c(T = 52\text{K}, H = 0)$. With this choice, we obtain the effective transition temperatures plotted in Fig. 5(c).

We note that there is a substantial range of temperature and field in which the bilayers appear to be superconducting while there is no coherent superconducting transport between bilayers. Analysis of the magnetization in the reversible range near the onset of diamagnetism found evidence of 2D scaling behavior [26]. Our results indicate that this is not just a matter

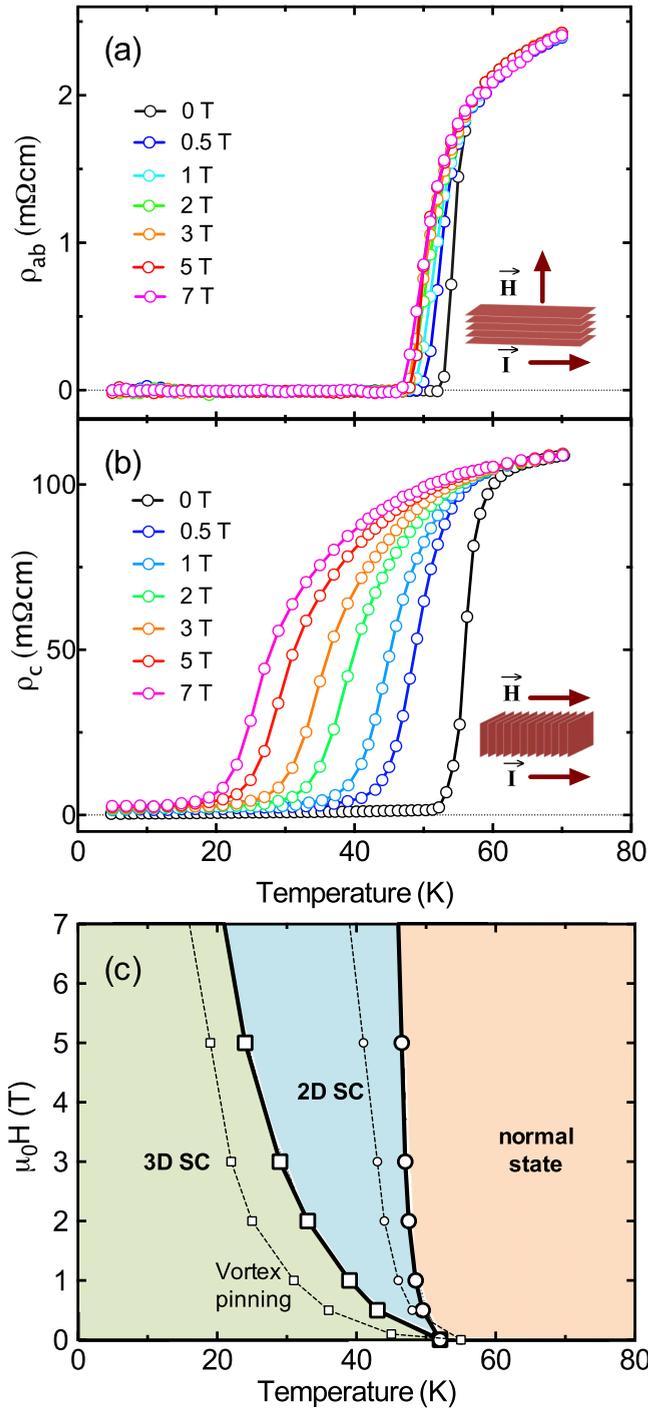


FIG. 5. Electrical resistivity of (a) ρ_{ab} and (b) ρ_c as a function of temperature, obtained under a perpendicular field up to 7 T. (c) Phase diagram indicating the boundaries between the normal state, 2D and 3D superconductivity of $\text{La}_{1.85}\text{Ca}_{1.15}\text{Cu}_2\text{O}_6$. Large squares (circles) represent the superconducting transition determined from ρ_c (ρ_{ab}) with $\mathbf{H} \parallel \mathbf{c}$. Small squares (circles) represent H_{irr} determined from χ with $\mathbf{H} \parallel \mathbf{c}$ ($\mathbf{H} \perp \mathbf{c}$).

of strong anisotropy in a 3D system, but that superconductivity actually develops within bilayers before Josephson coupling can provide 3D coherence.

V. DISCUSSION

The observed field-induced decoupling of superconducting layers is similar to the field-induced behavior found previously in LBCO with $x = 0.095$ [3,4]. Of course, the latter was similar to the zero-field observation of decoupled superconducting planes in LBCO with $x = 0.125$ [12,13]. In LBCO, the superconductivity coexists with spin and charge stripe order [5], and it has been proposed that a suppression of Josephson coupling between layers is the consequence of pair-density-wave (PDW) superconducting order [9,35].

Could the presence of intergrowths of impurity phases qualitatively impact our results? When the magnetic field is applied parallel to the planes, insulating layers would allow the field to locally penetrate the sample; however, unless there are special pinning effects near a surface, this should not impact the response of thick domains of the La-Ca-2126 phase. In any case, it would only impact H_{irr} measured with $\mathbf{H} \perp \mathbf{c}$. The decoupling effect observed in the resistivity occurs for $\mathbf{H} \parallel \mathbf{c}$, where there is no obvious way for the intergrowths to impact the anisotropic superconducting transition temperatures.

Inelastic neutron scattering measurements have been performed on a large crystal of the La-Ca-2126 $x = 0.15$ sample [36]. Although no static spin order was observed in association with the La-Ca-2126 phase, the bilayer magnetic excitations were found to be gapless, the latter being similar to the case of LBCO with $x = 0.095$ [37] and $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ with $x = 0.07$ [38], and suggestive of intertwined order [11]. It would be interesting to test whether a c -axis magnetic field can induce spin order.

It is notable that the region of decoupled layers in Fig. 5(c) shows a significant correlation with the region between the irreversibility lines determined from the magnetic susceptibility measurements with the field parallel to c or to the planes. The irreversibility line in near-optimal $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ for a c -axis field is also shifted far below the onset of diamagnetism, and there is evidence from in-plane and out-of-plane resistivity measurements for decoupling of the superconducting bilayers [39,40]. In that case, there is a substantial gap in the spin fluctuations below T_c [41,42]; however, charge modulations are prevalent and enhanced by a magnetic field [43–46]. The role of intertwined orders could provide a common connection [11].

VI. SUMMARY

In summary, we have presented experimental results of magnetic susceptibility and electrical resistivity measurements for superconducting single crystals La-Ca-2126 with $x = 0.1$ and 0.15. The magnetic susceptibility measurements confirm the bulk superconductivity in the samples, showing a narrow superconducting transition as well as $T_c^m = 54$ K. From the variation of the magnetization with magnetic field, we find that there is a large difference in the irreversibility line depending on whether the field is applied along the c axis or in plane. From the transport measurements, we find that the observed ρ_{ab} is larger than expected, reflecting the impact of two non-superconducting minority phases that develop during the high-pressure annealing [20]. Nevertheless, we are able to identify the resistive superconducting transition and its dependence

on the direction of current flow as a magnetic field is applied along the c axis. We find that there is relatively little shift in the transition temperature for currents flowing parallel to the planes, but a substantial change when the current flows between planes. Hence, there appears to be a significant region in the phase space of temperature and magnetic field where we have superconducting bilayers that are decoupled from one another, and the boundaries are close to the anisotropic irreversibility lines. These results demonstrate that the phenomenon of field-induced decoupling of superconducting layers is not limited to single-layer cuprates such as LBCO [3,4] and

they raise the question of the potential role of intertwined orders [11].

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- [1] A. A. Schafgans, A. D. LaForge, S. V. Dordevic, M. M. Qazilbash, W. J. Padilla, K. S. Burch, Z. Q. Li, Seiki Komiyama, Yoichi Ando, and D. N. Basov, Towards a Two-Dimensional Superconducting State of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ in a Moderate External Magnetic Field, *Phys. Rev. Lett.* **104**, 157002 (2010).
- [2] Gil Drachuck, Meni Shay, Galina Bazalitsky, Jorge Berger, and Amit Keren, Parallel and perpendicular susceptibility above T_c in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ single crystals, *Phys. Rev. B* **85**, 184518 (2012).
- [3] Jinsheng Wen, Qing Jie, Qiang Li, M. Hücker, M. v. Zimmermann, Su Jung Han, Zhijun Xu, D. K. Singh, R. M. Konik, Liyuan Zhang, Genda Gu, and J. M. Tranquada, Uniaxial linear resistivity of superconducting $\text{La}_{1.905}\text{Ba}_{0.095}\text{CuO}_4$ induced by an external magnetic field, *Phys. Rev. B* **85**, 134513 (2012).
- [4] Z. Stegen, Su Jung Han, Jie Wu, A. K. Pramanik, M. Hücker, Genda Gu, Qiang Li, J. H. Park, G. S. Boebinger, and J. M. Tranquada, Evolution of superconducting correlations within magnetic-field-decoupled $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ ($x = 0.095$), *Phys. Rev. B* **87**, 064509 (2013).
- [5] M. Hücker, M. v. Zimmermann, G. D. Gu, Z. J. Xu, J. S. Wen, Guangyong Xu, H. J. Kang, A. Zheludev, and J. M. Tranquada, Stripe order in superconducting $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ ($0.095 \leq x \leq 0.155$), *Phys. Rev. B* **83**, 104506 (2011).
- [6] T. P. Croft, C. Lester, M. S. Senn, A. Bombardi, and S. M. Hayden, Charge density wave fluctuations in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ and their competition with superconductivity, *Phys. Rev. B* **89**, 224513 (2014).
- [7] V. Thampy, M. P. M. Dean, N. B. Christensen, L. Steinke, Z. Islam, M. Oda, M. Ido, N. Momono, S. B. Wilkins, and J. P. Hill, Rotated stripe order and its competition with superconductivity in $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$, *Phys. Rev. B* **90**, 100510 (2014).
- [8] A. Himeda, T. Kato, and M. Ogata, Stripe States with Spatially Oscillating d -Wave Superconductivity in the Two-Dimensional $t - t' - J$ Model, *Phys. Rev. Lett.* **88**, 117001 (2002).
- [9] E. Berg, E. Fradkin, E.-A. Kim, S. A. Kivelson, V. Oganesyan, J. M. Tranquada, and S. C. Zhang, Dynamical Layer Decoupling in a Stripe-Ordered High- T_c Superconductor, *Phys. Rev. Lett.* **99**, 127003 (2007).
- [10] Patrick A. Lee, Amperian Pairing and the Pseudogap Phase of Cuprate Superconductors, *Phys. Rev. X* **4**, 031017 (2014).
- [11] Eduardo Fradkin, Steven A. Kivelson, and John M. Tranquada, Colloquium: Theory of intertwined orders in high temperature superconductors, *Rev. Mod. Phys.* **87**, 457 (2015).
- [12] Q. Li, M. Hücker, G. D. Gu, A. M. Tsvelik, and J. M. Tranquada, Two-Dimensional Superconducting Fluctuations in Stripe-Ordered $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$, *Phys. Rev. Lett.* **99**, 067001 (2007).
- [13] J. M. Tranquada, G. D. Gu, M. Hücker, Q. Jie, H.-J. Kang, R. Klingeler, Q. Li, N. Tristan, J. S. Wen, G. Y. Xu, Z. J. Xu, J. Zhou, and M. v. Zimmermann, Evidence for unusual superconducting correlations coexisting with stripe order in $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$, *Phys. Rev. B* **78**, 174529 (2008).
- [14] Tao Wu, Hadrien Mayaffre, Steffen Kramer, Mladen Horvatic, Claude Berthier, W. N. Hardy, Ruixing Liang, D. A. Bonn, and Marc-Henri Julien, Magnetic-field-induced charge-stripe order in the high-temperature superconductor $\text{YBa}_2\text{Cu}_3\text{O}_y$, *Nature* **477**, 191 (2011).
- [15] S. Gerber, H. Jang, H. Nojiri, S. Matsuzawa, H. Yasumura, D. A. Bonn, R. Liang, W. N. Hardy, Z. Islam, A. Mehta, S. Song, M. Sikorski, D. Stefanescu, Y. Feng, S. A. Kivelson, T. P. Devereaux, Z.-X. Shen, C.-C. Kao, W.-S. Lee, D. Zhu, and J.-S. Lee, Three-dimensional charge density wave order in $\text{YBa}_2\text{Cu}_3\text{O}_{6.67}$ at high magnetic fields, *Science* **350**, 949 (2015).
- [16] J. Chang, E. Blackburn, O. Ivashko, A. T. Holmes, N. B. Christensen, M. Hücker, Ruixing Liang, D. A. Bonn, W. N. Hardy, U. Rütt, M. v. Zimmermann, E. M. Forgan, and S. M. Hayden, Magnetic field controlled charge density wave coupling in underdoped $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$, *Nat. Commun.* **7**, 11494 (2016).
- [17] B. Vignolle, B. J. Ramshaw, James Day, David LeBoeuf, Stéphane Lepault, Ruixing Liang, W. N. Hardy, D. A. Bonn, Louis Taillefer, and Cyril Proust, Coherent c -axis transport in the underdoped cuprate superconductor $\text{YBa}_2\text{Cu}_3\text{O}_y$, *Phys. Rev. B* **85**, 224524 (2012).
- [18] Fan Yu, Max Hirschberger, Toshinao Loew, Gang Li, Benjamin J. Lawson, Tomoya Asaba, J. B. Kemper, Tian Liang, Juan Porras, Gregory S. Boebinger, John Singleton, Bernhard Keimer, Lu Li, and N. Phuan Ong, Magnetic phase diagram of underdoped $\text{YBa}_2\text{Cu}_3\text{O}_y$ inferred from torque magnetization and thermal conductivity, *Proc. Natl. Acad. Sci. USA* **113**, 12667 (2016).
- [19] Scott C. Riggs, O. Vafek, J. B. Kemper, J. B. Betts, A. Migliori, F. F. Balakirev, W. N. Hardy, Ruixing Liang, D. A. Bonn, and G. S. Boebinger, Heat capacity through the magnetic-field-induced resistive transition in an underdoped high-temperature superconductor, *Nat. Phys.* **7**, 332 (2011).
- [20] J. A. Schneeloch, Z. Guguchia, M. B. Stone, Wei Tian, Ruidan Zhong, K. M. Mohanty, Guangyong Xu, G. D. Gu, and J. M. Tranquada, Growth and structural characterization of large superconducting crystals of $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$, *Phys. Rev. Materials* **1**, 074801 (2017).
- [21] Hefei Hu, Yimei Zhu, Xiaoya Shi, Qiang Li, Ruidan Zhong, John A. Schneeloch, Genda Gu, John M. Tranquada, and Simon J. L.

- Billinge, Nanoscale coherent intergrowthlike defects in a crystal of $\text{La}_{1.9}\text{Ca}_{1.1}\text{Cu}_2\text{O}_{6+\delta}$ made superconducting by high-pressure oxygen annealing, *Phys. Rev. B* **90**, 134518 (2014).
- [22] Stuart B. Wilkins, QLaue, Version 0.2 (2010), <https://github.com/stuwilkins/QLaue>.
- [23] G. D. Gu, M. Hücker, Y.-J. Kim, J. M. Tranquada, H. Dabkowska, G. M. Luke, T. Timusk, B. D. Gaulin, Q. Li, and A. R. Moodenbaugh, Crystal growth and superconductivity of $(\text{La}_{1-x}\text{Ca}_x)_2\text{CaCu}_2\text{O}_{6+\delta}$, *J. Phys. Chem. Solids* **67**, 431 (2006).
- [24] Takao Ishii, Takao Watanabe, Kyoichi Kinoshita, and Azusa Matsuda, Single crystal growth and superconductivity in $\text{La}_{1.87}\text{Ca}_{1.13}\text{Cu}_2\text{O}_6$, *Physica C: Superconductivity* **179**, 39 (1991).
- [25] M. Okuya, T. Kimura, R. Kobayashi, J. Shimoyama, K. Kitazawa, K. Yamafuji, K. Kishio, K. Kinoshita, and T. Yamada, Single-crystal growth and anisotropic electrical properties of $(\text{La}_{1-x}\text{Ca}_x)_2\text{CaCu}_2\text{O}_6$, *J. Supercond.* **7**, 313 (1994).
- [26] Xiaoya Shi, I. K. Dimitrov, Toshinori Ozaki, Genda Gu, and Qiang Li, Quasi-two-dimensional fluctuations in the magnetization of $\text{La}_{1.9}\text{Ca}_{1.1}\text{Cu}_2\text{O}_{6+\delta}$ superconductors, *Phys. Rev. B* **96**, 184519 (2017).
- [27] T. Sasagawa, K. Kishio, Y. Togawa, J. Shimoyama, and K. Kitazawa, First-Order Vortex-Lattice Phase Transition in $(\text{La}_{1-x}\text{Sr}_x)_2\text{CuO}_4$ Single Crystals: Universal Scaling of the Transition Lines in High-Temperature Superconductors, *Phys. Rev. Lett.* **80**, 4297 (1998).
- [28] T. Sasagawa, Y. Togawa, J. Shimoyama, A. Kapitulnik, K. Kitazawa, and K. Kishio, Magnetization and resistivity measurements of the first-order vortex phase transition in $(\text{La}_{1-x}\text{Sr}_x)_2\text{CuO}_4$, *Phys. Rev. B* **61**, 1610 (2000).
- [29] Lu Li, J. G. Checkelsky, Seiki Komiyama, Yoichi Ando, and N. P. Ong, Low-temperature vortex liquid in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, *Nat. Phys.* **3**, 311 (2007).
- [30] K. Nakajima, K. Yamada, S. Hosoya, T. Omata, and Y. Endoh, *J. Phys. Soc. Jpn.* **62**, 4438 (1993).
- [31] T. Watanabe, T. Fujii, and A. Matsuda, Anisotropic Resistivities of Precisely Oxygen Controlled Single-Crystal $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$: Systematic Study on “Spin Gap” Effect, *Phys. Rev. Lett.* **79**, 2113 (1997).
- [32] D. Babić, J. R. Cooper, J. W. Hodby, and Chen Changkang, Changes in irreversibility line, anisotropy, and condensation energy by oxygen depletion of $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$, *Phys. Rev. B* **60**, 698 (1999).
- [33] T. Ito, K. Takenaka, and S. Uchida, Systematic Deviation from T -Linear Behavior in the in-Plane Resistivity of $\text{YBa}_2\text{Cu}_3\text{O}_{7-y}$: Evidence for Dominant Spin Scattering *Phys. Rev. Lett.* **70**, 3995 (1993).
- [34] Yoichi Ando, Y. Kurita, Seiki Komiyama, S. Ono, and Kouji Segawa, Evolution of the Hall Coefficient and the Peculiar Electronic Structure of the Cuprate Superconductors, *Phys. Rev. Lett.* **92**, 197001 (2004).
- [35] E. Berg, E. Fradkin, S. A. Kivelson, and J. M. Tranquada, Striped superconductors: how spin, charge and superconducting orders intertwine in the cuprates, *New J. Phys.* **11**, 115004 (2009).
- [36] J. A. Schneeloch, R. D. Zhong, M. B. Stone, G. D. Gu, G. Y. Xu, and J. M. Tranquada, Magnetic excitations in superconducting $\text{La}_{2-x}\text{Ca}_{1+x}\text{Cu}_2\text{O}_6$ (unpublished).
- [37] Zhijun Xu, C. Stock, Songxue Chi, A. I. Kolesnikov, Guangyong Xu, Genda Gu, and J. M. Tranquada, Neutron-Scattering Evidence for a Periodically Modulated Superconducting Phase in the Underdoped Cuprate $\text{La}_{1.905}\text{Ba}_{0.095}\text{CuO}_4$, *Phys. Rev. Lett.* **113**, 177002 (2014).
- [38] H. Jacobsen, I. A. Zaliznyak, A. T. Savici, B. L. Winn, S. Chang, M. Hücker, G. D. Gu, and J. M. Tranquada, Neutron scattering study of spin ordering and stripe pinning in superconducting $\text{La}_{1.93}\text{Sr}_{0.07}\text{CuO}_4$, *Phys. Rev. B* **92**, 174525 (2015).
- [39] J. H. Cho, M. P. Maley, S. Fleshler, A. Lacerda, and L. N. Bulaevskii, High-magnetic-field transport properties of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$ single crystals, *Phys. Rev. B* **50**, 6493 (1994).
- [40] N. Morozov, L. Krusin-Elbaum, T. Shibauchi, L. N. Bulaevskii, M. P. Maley, Yu. I. Latyshev, and T. Yamashita, High-Field Quasiparticle Tunneling in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$: Negative Magnetoresistance in the Superconducting State, *Phys. Rev. Lett.* **84**, 1784 (2000).
- [41] H. F. Fong, P. Bourges, Y. Sidis, L. P. Regnault, A. Ivanov, G. D. Gu, N. Koshizuka, and B. Keimer, Neutron scattering from magnetic excitations in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$, *Nature* **398**, 588 (1999).
- [42] Guangyong Xu, G. D. Gu, M. Hücker, B. Fauque, T. G. Perring, L. P. Regnault, and J. M. Tranquada, Testing the itinerancy of spin dynamics in superconducting $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$, *Nat. Phys.* **5**, 642 (2009).
- [43] Colin V. Parker, Pegor Aynajian, Eduardo H. da Silva Neto, Aakash Pushp, Shimpei Ono, Jinsheng Wen, Zhijun Xu, Genda Gu, and Ali Yazdani, Fluctuating stripes at the onset of the pseudogap in the high- T_c superconductor $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$, *Nature* **468**, 677 (2010).
- [44] Eduardo H. da Silva Neto, Pegor Aynajian, Alex Frano, Riccardo Comin, Enrico Schierle, Eugen Weschke, Andrés Gyenis, Jinsheng Wen, John Schneeloch, Zhijun Xu, Shimpei Ono, Genda Gu, Mathieu Le Tacon, and Ali Yazdani, Ubiquitous interplay between charge ordering and high-temperature superconductivity in cuprates, *Science* **343**, 393 (2014).
- [45] K. Fujita, Chung Koo Kim, Inhee Lee, Jinho Lee, M. H. Hamidian, I. A. Firmo, S. Mukhopadhyay, H. Eisaki, S. Uchida, M. J. Lawler, E.-A. Kim, and J. C. Davis, Simultaneous transitions in cuprate momentum-space topology and electronic symmetry breaking, *Science* **344**, 612 (2014).
- [46] J. E. Hoffman, E. W. Hudson, K. M. Lang, V. Madhavan, H. Eisaki, S. Uchida, and J. C. Davis, A four unit cell periodic pattern of quasi-particle states surrounding vortex cores in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$, *Science* **295**, 466 (2002).
- [47] Y. Radzyner, A. Shaulov, Y. Yeshurun, I. Felner, K. Kishio, and J. Shimoyama, Anisotropic order-disorder vortex transition in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$, *Phys. Rev. B* **65**, 214525 (2002).
- [48] B. Lundqvist, Ö. Rapp, M. Andersson, and Yu. Eltsev, Nearly field-independent in-plane vortex solid-to-liquid transition in the c -axis resistivity of oxygen deficient single crystals of $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$, *Phys. Rev. B* **64**, 060503 (2001).