## Contributions of oxygen vacancies and titanium interstitials to band-gap states of reduced titania

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(Received 2 July 2017; published 9 January 2018)

The spectroscopic fingerprints of the point defects of titanium dioxide remain highly controversial. Seemingly indisputable experiments lead to conflicting conclusions in which oxygen vacancies and titanium interstitials are alternately referred to as the primary origin of the Ti 3*d* band-gap states. We report on experiments performed by electron energy loss spectroscopy whose key is the direct annealing of only the very surface of rutile TiO<sub>2</sub>(110) crystals and the simultaneous measurement of its temperature via the Bose-Einstein loss/gain ratio. By surface preparations involving reactions with oxygen and water vapor, in particular, under electron irradiation, vacancy-and interstitial-related band-gap states are singled out. Off-specular measurements reveal that both types of defects contribute to a unique charge distribution that peaks in subsurface layers with a common dispersive behavior.

## DOI: 10.1103/PhysRevB.97.041403

Already used in self-cleaning coatings and dye-sensitized solar cells, titanium dioxide TiO<sub>2</sub> offers promising solutions to water/air purification and water splitting [1,2]. Its rich physics and chemistry is mostly tied to the reduced  $TiO_{2-x}$  form in which dominant point defects, bridging oxygen vacancies  $(O_b$ -vac) and titanium interstitials  $(Ti_{int})$  widely explored on rutile (110) [2–6] (Fig. 1), play a pivotal role. At the origin of the *n*-type electron conductivity, excess electrons generated by defects populate Ti 3d related band-gap states (BGS). They have long been associated with  $O_b$ -vac (herein labeled V-BGS) because O<sub>2</sub> dissociation both eliminates O<sub>b</sub>-vac and heals them by a charge transfer toward  $O_b$  and O adatoms ( $O_{ad}$ ) adsorbed on five-coordinated  $Ti_{5c}$  [7]. The model became hotly debated when vacancy-free  $TiO_2(110)$  obtained by reacting off H from hydroxylated  $TiO_{2-x}$  was shown to retain most of the BGS that were consequently related to Ti<sub>int</sub> (I-BGS) [4]. Their healing by O<sub>2</sub> was explained by a charge donation from Ti<sub>int</sub> that promotes a non-vacancy-related  $O_2$  dissociation [4]. Consistently, the  $TiO_x$  islands formed upon annealing O-covered rutile [4,8–12] were attributed to the reaction of Oad with Tiint which, as the reoxidation of  $TiO_{2-x}$  [13], relies on the diffusion of Ti<sub>int</sub> in rutile above 400 K. Finally, extra O<sub>ad</sub> atoms (relative to dissociation on  $O_b$ -vac), obtained by reacting  $O_2$  with  $TiO_{2-x}$ , were associated with charge transfer from  $Ti_{int}$  [4,14]. Additional support given to the O-vacancy model [7] fed the controversy. The oxidative chemistry of  $TiO_{2-x}$  was suggested to be controlled by a donor species ( $O_b$ -vac and OH) rather than Ti<sub>int</sub> [15] and, based on a relationship of proportionality between O<sub>b</sub>-vac counting by microscopy and photoemission signals, BGS appeared to mostly stem from  $O_b$ -vac [16].

The crux of the debate is that the signatures of V-BGS and I-BGS look identical. The case is tackled herein by the rarely used high-resolution electron energy loss spectroscopy (HREELS). The key experiment to single out BGS contributions is the quick annealing (up to 1000 K within a few seconds) of the surface only via a hot filament facing the crystal within the spectrometer, while probing *T* (temperature) via the Bose-Einstein statistics (Fig. S1 in Supplemental Material [18]) of the loss/gain phonon ratio. Annealed samples are labeled SA-*T*-TiO<sub>2</sub> hereafter. Controversial or unexplained data involving annealing treatments, electron bombardment, and exposures to O<sub>2</sub> and H<sub>2</sub>O, have been revisited to feature I-BGS and V-BGS. Finally, BGS in-depth profiles [19–23] were probed by off-specular EELS.

 $TiO_2(110)$  single crystals were mounted in an ultrahigh vacuum (UHV) setup [24] equipped with an EELS spectrometer (Sec. S1 in Supplemental Material [18]). Sputtering and annealing  $TiO_2(110)$  resulted in reduced dark blue color samples R-TiO<sub>2</sub> whose surfaces could be reoxidized (O-TiO<sub>2</sub>) by 30 min annealing (1100 K) [9] and cooling in  $O_2$  (5 ×  $10^{-6}$  mbar) at a rate of ~30 K min<sup>-1</sup> (Sec. S1 in Supplemental Material [18]). EEL spectra were collected between 100 and 300 K. Unless stated, they were recorded in specular geometry (incident angle  $\Theta_I = 60^\circ$ , incident plane along the [110] direction) at an energy of  $E_I = 38$  eV. Typical EELS spectra (Fig. S3 in Supplemental Material [18]) show broad BGS features at  $\sim 0.8$  eV before the onset of band-to-band excitations at 3.2 eV. Bulk sensitivity at the phonon energies provides a reliable intensity normalization (Sec. S3 in Supplemental Material [18]). Exposures are expressed in Langmuir (1 L = $1.33 \times 10^{-6}$  mbar s<sup>-1</sup>). EELS spectra recorded on R-TiO<sub>2</sub> at 100 K [Fig. S3(a) in Supplemental Material [18]] and 300 K [Fig. S3(b) in Supplemental Material [18]] under  $O_2$  show progressive BGS healing, although the kinetics are different. The fast and slow decreases in BGS intensity that are observed at 100 and 300 K, respectively, rely on mechanisms that are under debate [10,13,25]. Importantly, the similarity between the final BGS intensities [Fig. S3(a) inset in Supplemental Material [18]] indicates two equivalent healing processes.

The preparation of SA-TiO<sub>2</sub> surfaces is central in pinpointing the categories of point defects. Indisputable proof of the existence of I-BGS is provided by the defect peak growing on

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FIG. 1. Ball model of defective  $TiO_2(110)$  (Ti, O, H,  $Ti_{int}$ , and  $O_{ad}$  are blue, red, white, cyan, and pink spheres, respectively); bridging oxygen rows involve  $O_b$ -vac and  $O_bH$ ;  $O_{ad}$  lie on  $Ti_{5c}$ ;  $Ti_{int}$  occupy octahedral sites [17]; the localization of excess electrons (question mark) associated with defects is under debate.

SA-420 K-TiO<sub>2</sub> [Fig. 2(a)]. The formation of O<sub>b</sub>-vac at 420 K being excluded, this peak is assigned to I-BGS formed via an outward Ti<sub>int</sub> diffusion [4,26–28] as supported by the square root of the time dependence of the BGS intensity [Fig. 2(a) inset].

In contrast to the slow kinetics of BGS formation on SA-420 K-TiO<sub>2</sub> [Fig. 2(a)], SA-TiO<sub>2</sub> surfaces prepared by annealing of 10 s above 800 K [Fig. 2(b)] show strong BGS whose intensity rises with T. Indeed,  $O_b$ -vac are expected to form [3], but it is unclear whether defect states are I-BGS or V-BGS. More is learned of I-BGS by preparing SA-TiO<sub>2</sub> at increasing temperature followed by 20 L of O<sub>2</sub> at 300 K [Fig. 2(c), steps 1– 4; inset: BGS intensities]. First, healing I-BGS from SA-420 K- $TiO_2$  by  $O_2$  (step 1) validates the non-vacancy-related  $O_2$  dissociation associated with charge transfer from Ti<sub>int</sub> [4,14]. Then, increasing BGS are observed on SA-970 K-TiO2 and SA-1140 K-TiO<sub>2</sub> although, surprisingly, the residual BGS observed after  $O_2$  exposure continuously decreases through steps 1, 2, and 4 [Fig. 2(c)]. Extra healing of  $O_b$ -vac is excluded since there is no reason why reacting O<sub>b</sub>-vac with 20 L of O<sub>2</sub> should leave fewer  $O_b$ -vac sites intact while their initial concentration is higher. Therefore, Fig. 2(c) shows that the commonly observed residual BGS (Fig. S4 in Supplemental Material [18] and Refs. [4,16,25]) mostly involve I-BGS. Annealing O-covered surfaces at increasing temperature triggers outward Ti<sub>int</sub> dif-



FIG. 2. Singling out BGS from  $Ti_{int}$  by surface annealing of O-TiO<sub>2</sub>. EELS measurements at 300 K: (a) BGS recorded on SA-420 K-TiO<sub>2</sub> vs time. Inset: Time evolution of the BGS area (500–2500 meV) fitted by a square-root function. (b) BGS from SA-TiO<sub>2</sub> prepared at different temperatures during 10 s. (c) BGS recorded upon successive treatments (steps 1–4): Surface annealing (10 s) at given temperatures (strong color) and then 20 L of O<sub>2</sub> (light color) at 300 K (from bottom to top). Inset: BGS intensities step by step. The black dotted lines show the order of treatments, and the orange and blue arrows to guide the eye evidence an increase in BGS intensity upon an increase in annealing temperature and a corresponding decrease in residual intensity after 20 L O<sub>2</sub>.



FIG. 3. Distinguishing V-BGS from I-BGS by exposure to  $H_2O$  and  $O_2$ : (a) BGS of an E-TiO<sub>2</sub> surface are totally healed by 1 L of  $O_2$  at 100 K. (b) BGS of SA-970 K-TiO<sub>2</sub> surface (10 s annealing) are healed at 300 K by  $H_2O$  under an electron beam at 38 eV. (c) Same experiment as in (b), but at 22 eV. (d) BGS of SA-470 K-TiO<sub>2</sub> (2100 s annealing) at 300 K are not affected by  $H_2O$  under electrons at 38 eV but, in contrast, are healed by  $O_2$ . (e) BGS from R-TiO<sub>2</sub> are partially healed at 300 K by  $H_2O$  under electrons at 38 eV and even more canceled by further  $O_2$  exposure.

fusion [10,29] from increasingly deeper layers. Assuming that  $Ti_{int}$  segregate on step 2 (SA-970 K-TiO<sub>2</sub>) over deeper layers than those reached by SA-420 K-TiO<sub>2</sub> (step 3) explains the marginal BGS change on step 3, in an apparent contrast with step 1. The depletion in subsurface  $Ti_{int}$  which progressively extends inward [steps 1–4, Fig. 2(c)] suggests that annealing/oxidation cycles can lead to a BGS-free surface region.

The existence of V-BGS has not been singled out yet. Often accepted [16], the attribution to V-BGS of  $O_b$ -vac created by electron stimulated desorption (ESD) via the Knotek-Feibelmann process [30,31] is nevertheless strongly discussed [32,33]. Electron bombarded surfaces (E-TiO<sub>2</sub>) were prepared by illuminating O-TiO<sub>2</sub> by a 75 eV electron beam (current density ~1  $\mu$ A cm<sup>-2</sup>) [30,31]. Totally healed at 100 K by only 1 L O<sub>2</sub> [Fig. 3(a)], the resulting BGS thus stem from very surface defects but, still, there is no indisputable evidence that they are V-BGS. A clue came from the observation that ESD-induced BGS level off at a rather low intensity after 5 min, to remain stable for hours (not shown). Comparisons with other groups show that rather weak BGS were obtained with electron fluxes of  $1.25 \times 10^{12} e \text{ cm}^{-2} \text{ s}^{-1}$  [34] and  $6.25 \times 10^{12} e \text{ cm}^{-2} \text{ s}^{-1}$  [16]

and  $3 \times 10^{15} e \text{ cm}^{-2} \text{ s}^{-1}$  [15] led to strong BGS, although the fluences were similar  $[3 \times 10^{15} \text{ e cm}^{-2} \text{ [34]}; 2 \times 10^{15}$  $e \text{ cm}^{-2}$  (this work);  $6-25 \times 10^{15} e \text{ cm}^{-2}$  [16]]. Clearly, the electron-induced BGS intensity depends on the flux rather than on the fluence, which suggests a continuous healing of related  $O_b$ -vac. We may wonder what is the combined effect of residual water and ESD removal of H adatoms (threshold at 21-22 eV [30,31]). Although reacting O<sub>b</sub>-vac by H<sub>2</sub>O does not heal BGS [4,35-37], H<sub>2</sub>O under 38 eV electrons does heal BGS of SA-970 K-TiO<sub>2</sub> [Fig. 3(b)]. Consistently, 22 eV electrons (threshold for H ESD) have no effect [Fig. 3(c)]. In contrast, I-BGS from SA-420 K-TiO<sub>2</sub> are not healed at 38 eV when exposed to H<sub>2</sub>O [Fig. 3(d)], although, as in Fig. 2(d) (step 1), they are healed by  $O_2$ . Beyond the demonstration of the existence of V-BGS and I-BGS, the healing of V-BGS via H<sub>2</sub>O adsorption provides a means of distinguishing the two states, as in Fig. 3(e), where R-TiO<sub>2</sub> is exposed to H<sub>2</sub>O, under a 38 eV electron beam (healing V-BGS) and then exposed to O2 (healing I-BGS). Notably, the plateau reached by the intensity of the ESD-induced BGS supports their V-BGS nature because, if I-BGS were created, the inability of H2O to heal them would result in a continuous increase in their intensity.



FIG. 4. Concentration profile and dispersion of BGS at 300 K: (a) BGS of R-TiO<sub>2</sub> at different collection angles relative to the specular direction  $\Delta\Theta_S = \Theta_S - \Theta_I$  at fixed incidence  $\Theta_I = 60^\circ$ , as prepared (strong color) and after exposure to 20 L of O<sub>2</sub> (light color). Inset: Calculated off-specular probing depth (see text) averaged over a detector aperture of  $\sim 1^\circ$  vs energy loss and angular position  $\Delta\Theta_S$  at fixed incident angle at an energy of 38 eV. The gray dotted lines correspond to specular geometry and to BGS energy loss. (b) BGS area normalized to that recorded in specular geometry (maximum probing depth) vs probing depth (bottom scale) and  $\Delta\Theta_S$  (top): R-TiO<sub>2</sub> and SA-970 K-TiO<sub>2</sub>, as prepared and after 20 L of O<sub>2</sub> at 300 K, are compared. Inset: Schematic concentration profile of excess electrons in the subsurface region. (c) Dispersion of the position of the BGS with the wave-vector transfer  $k_{\parallel}$ .  $k_{\parallel}$  error stems from a detector aperture of  $\sim 1^\circ$ . Gray lines in (b) and (c) are given in (c).

Finally, the concentration profiles of the excess electrons and the dispersion of the associated BGS were explored by off-specular EELS (Fig. 4), where the cross section gets more surface sensitive by switching from the dipolar to impact regime [38]. The inverse of the modulus of the wave-vector transfer parallel to the surface gives an estimate of the probing depth [38],

$$k_{\parallel} = \frac{\sqrt{2mE_I}}{\hbar} \sin \Theta_I - \frac{\sqrt{2m(E_I - \hbar\omega)}}{\hbar} \sin \Theta_S, \quad (1)$$

where  $E_I$  is the incident electron energy,  $\hbar\omega$  the energy loss,  $2\pi\hbar$  the Planck constant, and  $\Theta_I$  and  $\Theta_S$  the incident and scattering angles, respectively (Sec. S3 in Supplemental Material [18]). BGS were recorded off-specular at 300 K, before and after 20 L O<sub>2</sub> exposure, on R-TiO<sub>2</sub> [Fig. 4(a)] and SA-TiO<sub>2</sub> (Fig. S5 in Supplemental Material [18]). Data were normalized to interband transitions whose probing depth does not change significantly with  $\Theta_S$  [Fig. 4(a) inset and Fig. S2(c) in Supplemental Material [18]]. The dramatic decrease in BGS intensity with  $\Theta_S$  shows that excess charges are not located at the extreme surface, as confirmed by the poor effect of  $O_2$  at the highest  $\Theta_S$ . Normalized BGS area versus probing depth from R-TiO<sub>2</sub> and SA-TiO<sub>2</sub> [Fig. 4(b)] and BGS positions versus  $k_{\parallel}$ (Fig. 4(c) show that the four series of data are strikingly similar [Figs. 4(b) and 4(c)]. This shows that the electron localization and state dispersion are independent of whether they are related to  $O_b$ -vac (R-TiO<sub>2</sub> and SA-TiO<sub>2</sub>) or to Ti<sub>int</sub> (after O<sub>2</sub> exposure). Generalizing previous theory [39] and experiment [20], the observation directly proves that the surface/subsurface electrostatic potentials dictate the location of the excess charges. A unique representation of the charge distribution can be drawn for all surfaces, either reduced or oxidized [Fig. 4(b) inset]. Going inward, after an almost charge-free atomic layer, excess charges pass through a maximum, consistently with photoelectron diffraction [19,20] and calculations [21–23,37,40]. Going deeper, the defect density lowers to reach the bulk value. The dispersive trend up to a cutoff of  $k_{\parallel} \sim 0.1$  Å<sup>-1</sup> [Fig. 4(c)] demonstrates the transport behavior of excess electrons down to a distance (~10 Å) that can be interpreted as the polaron radius at 300 K [22,23,35,37,40,41].

To summarize, vacancy- and interstitial-related BGS have been singled out by EELS experiments based on annealing of the very surface. The associated excess electrons contribute to a unique subsurface distribution whose profile and dispersive behavior are robust with respect to the nature of the defects. In contrast, their role in surface chemistry relies on the specificity of the defects. The dual origin of BGS allows for the understanding of seemingly contradictory observations and opens up different ways of interpreting experiments carried out on TiO<sub>2</sub> surfaces.

J.L. acknowledges support from the China Scholarship Council for his Ph.D. Grant. J.L. did the experimental measurements under the supervision of R.L., with S.C. contributing all the required technical assistance. J.L., R.L., and J.J contributed to interpretations and wrote the manuscript. R.L. and J.J. designed the research strategy.

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