Superconductor-insulator transition in fcc GeSb$_2$Te$_4$ at elevated pressures

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We show that polycrystalline GeSb$_2$Te$_4$ in the fcc phase (f-GST), which is an insulator at low temperature at ambient pressure, becomes a superconductor at elevated pressures. Our study of the superconductor-insulator transition versus pressure at low temperatures reveals a second-order quantum phase transition with linear dependence of the transition temperature on the pressure above the critical zero-temperature pressure. In addition, we demonstrate that at higher pressures the f-GST goes through a structural phase transition via amorphization to bcc GST (b-GST), which also becomes superconducting. We also find that in the pressure regime where an inhomogeneous mixture of amorphous and b-GST exists, there is an anomalous peak in magnetoresistance, and we suggest an explanation for this anomaly.

I. INTRODUCTION

GeSb$_2$Te$_4$ (GST) is a phase-change material which can be rapidly and reversibly switched between the amorphous and crystalline states. This phase transformation is accompanied by a significant change of electronic transport and optical properties [1–4] enabling these materials to be exploited for various industrial application like nonvolatile electronic memories and fast electrical switching [5–7].

Over the past decade, there have been intense efforts to link these unique features to the atomic structures, and by now many ingredients are well understood. For instance, crystalline GST (c-GST), one of the functional phases in memory devices, forms a rocksaltlike structure upon fast crystallization, with Te occupying one face-centered-cubic (fcc) sublattice and random arrangement of Ge/Sb/vacancies occupying the other [8,9]. This random arrangement on the cation sublattice creates pronounced disorder-induced Anderson localization effects [1,2,10]. Long-range order of the crystalline state enables resonance bonding which is responsible for the physical properties of this phase. On the other hand, amorphous GST (a-GST) is more controversial, and is likely to be of a mixed nature. Evidence for tetrahedral configuration around Ge, indicating sp^3 bonding, has been found [11]. However, recent simulations [12–14] suggest that the majority of the atoms have octahedral arrangement and squarelike connections with predominantly p bonding of the atoms with a 90° bond angle and a large amount of vacant areas (or voids) that permeate the whole lattice.

One of the interesting propertiesof GST is the emergence of superconductivity under elevated pressures [15]. In our previous high-pressure study of GST [15], superconductivity was observed in amorphous GST (a-GST), orthorhombic GST (o-GST), and in bcc GST (b-GST). In addition we

have demonstrated [15] that hexagonal GST remained in the normal state for the entire range of available temperatures and pressures. However, the transport properties of fcc GST (f-GST) at elevated pressure and at low temperatures remained unexplored.

This paper is devoted to the study of the properties of GST material in the fcc phase at high pressure and low temperatures. We demonstrate that f-GST undergoes a superconductor to insulator transition (SIT) at low temperatures when the pressure is applied as an external control parameter. We find that the superconducting transition temperature vanishes linearly with pressure, while the GST remains in the f-GST phase, strongly suggesting a second-order quantum phase transition (QPT) with a critical exponent close to unity.

The observed appearance of superconductivity is preceded by a significant change in the normal state resistance of the samples by a few orders of magnitude. Furthermore, we demonstrate that superconductivity with somewhat higher T_c appears at higher pressures, when b-GST starts to form. In the region where these two phases coexist, an anomalous behavior of the magnetoresistance is observed, whereby a sharp resistance peak appears in the vicinity of the upper critical field. We suggest an explanation for this behavior.

II. EXPERIMENT

In our transport and XRD experiments, we have used the following procedure for the preparation of f-GST samples. Initially, few micron-thick GST films were sputtered from a commercial target of h-GST (hexagonal GeSb$_2$Te$_4$). As we reported earlier [15], the films sputtered onto a room-temperature substrate are amorphous (a-GST). An atomic composition and morphology of the as-prepared a-GST film was checked by scanning electron microscopy (SEM), energy dispersive x-ray spectroscopy (EDS), and x-ray photoelectron spectroscopy (XPS) analysis [15]. The annealing of the sputtered films
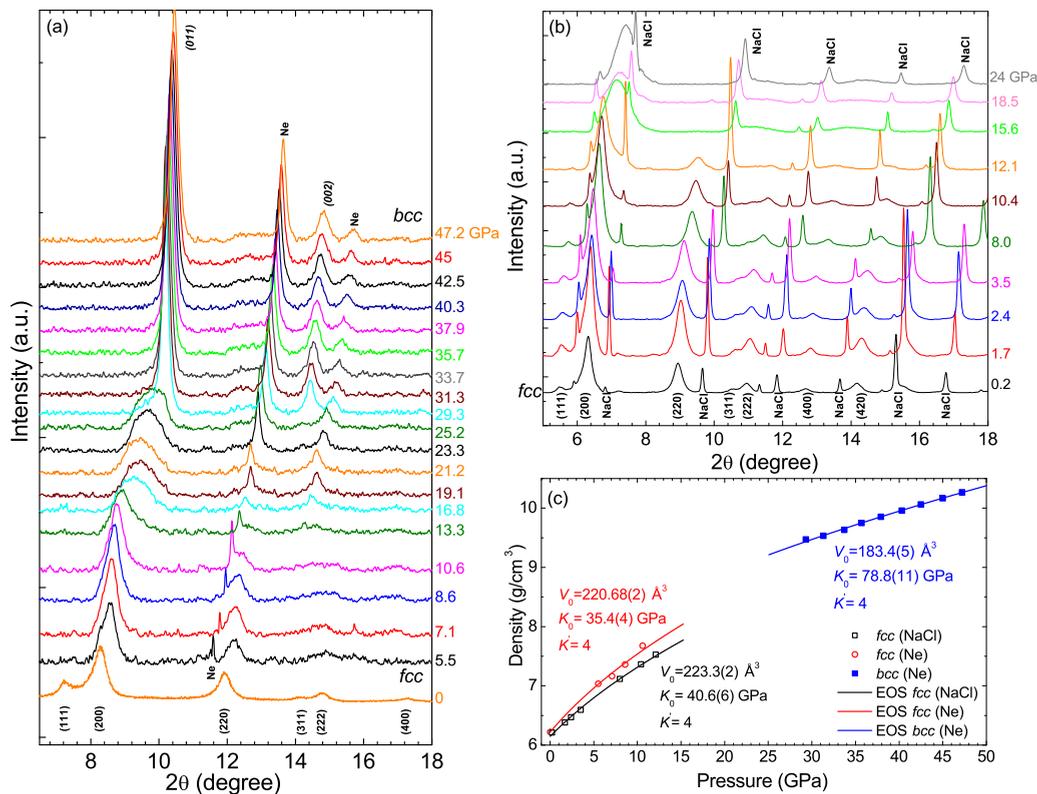
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FIG. 1. X-ray diffraction upon compression as a function of pressure at $T = 298$ K for two slots of measurements at two different beam lines and the density of the observed phases. Miller indices indicate the observed reflections of the fcc and bcc phases. (a) At the range of pressures from 5.5 to 47.2 GPa with Ne as pressure medium and $\lambda = 0.434$ Å (0 GPa data were taken from the annealed film on the substrate). (b) At the range of pressures from 0.2 to 24 GPa with NaCl as pressure medium and $\lambda = 0.3344$ Å. (c) Pressure dependence of the density of the fcc and bcc phases of GST along with the fitted curves extracted from the corresponding BM2 EOS [21]. EOSs were calculated using the data for unit-cell volumes as functions of the pressure; K_0 and V_0 are, respectively, the bulk modulus and the volume per formula unit at 1 bar and 300 K. K' is the pressure derivative of the bulk modulus. The vertical error bars do not exceed the size of the symbols.

at 146 °C causes the transformation of the a-GST into an fcc polycrystalline phase. X-ray diffraction (XRD) analysis confirming the formation of the fcc phase of the annealed films is shown in Fig. 1(a) at 0 GPa. Finally, a powder of f-GST was prepared by the mechanical removal of the f-GST film from the substrate.

Pressure was exerted using miniature diamond anvil cells (DACs) [16] with diamond anvil culets of 250 μm. A preindented stainless-steel or rhenium gasket was drilled and then filled and covered with a powder layer of 75% Al₂O₃ and 25% NaCl for electrical insulation. The powder of f-GST was placed onto the culets. A Pt foil with a thickness of 5–7 μm was cut into triangular probes connecting the sample and the copper leads, allowing electrical transport measurements at elevated pressures. Six probes were placed in each DAC. Figure 2(a) depicts a setup of six Pt foils (bright areas) between the diamond and the sample (dark areas) in a four-probe configuration. A few ruby fragments for pressure determination were located in the region between the Pt electrode tips overlapping the sample. No liquid pressure-transmitting medium was used, but pressure is effectively transmitted to the sample upon compression by way of the surrounding Al₂O₃ + NaCl insulation. Figure 2(b) shows a typical fluorescence spectra of two ruby fragments positioned ∼20 μm apart. The spectra suggest a ∼5% pressure inhomogeneity over this distance.

Electrical transport measurements were performed using a ⁴He cryostat. The sample was compressed up to 44 GPa in increments of 2 GPa on average, and cooled down from
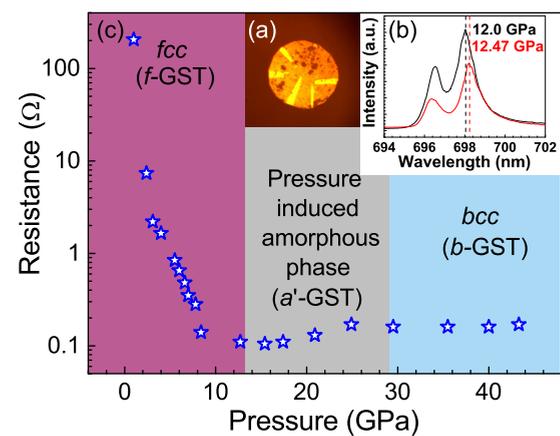

FIG. 2. Room-temperature resistance versus pressure. (a) Contact configuration. (b) Spectra taken from two Ruby fragments indicating a ∼5% pressure inhomogeneity. (c) Resistance as a function of pressure. The colored regions are marked according to our XRD data from Fig. 1.

ambient temperature down to 1.4 K. After each pressure increment a temperature cycle was performed.

Synchrotron XRD measurements of f-GST powder were performed at room temperature up to 47 GPa at the beamlines 13ID-D and 13-BM-C of APS (Argonne, IL), with wavelengths of $\lambda = 0.3344$ and 0.434 Å, respectively, in angle-dispersive mode with patterns collected using a MAR CCD detector. NaCl and Ne were used as the pressure-transmitting medium in these two measurements, respectively. They also served as pressure markers. Ruby was used as a pressure gauge as well. The image data were integrated using DIOPTAS [17] and the resulting diffraction patterns were analyzed with the GSAS + EXPGUI [18,19] program. XRD data at ambient temperature and pressure have been collected in symmetric Bragg-Brentano geometry with Cu Kα radiation ($\lambda = 1.5406$ Å) on a Bruker D8 Discover Θ:Θ x-ray diffractometer equipped with a one-dimensional LynxEye XE detector.

III. EXPERIMENTAL RESULTS OF XRD AND TRANSPORT STUDIES

We start the description of our experimental results with XRD and transport studies at room temperature.

As depicted in Figs. 1(a) and 1(b), the diffraction patterns obtained from both slots of measurements show the existence of the fcc phase up to about 14 GPa. The broadening and shifting of the (200) and (400) peaks along with the disappearance of the other fcc peaks of GST is clearly observed for pressures above 14 GPa, indicating the amorphization of the fcc phase. Upon further increase in pressure the emergence of the bcc phase of GST becomes evident at pressures exceeding 29 GPa [Fig. 1(a)]. The observed amorphization as well as the formation of the bcc phase are consistent with previously reported results [20]. We would like to note that the appearance of the intermediate orthorhombic phase reported in [20] was not detected in our data. Based on the values of the unit-cell volumes, obtained from refinement of the XRD patterns, we calculated the density values of the fcc and bcc phases at various pressures. The calculated density as a function of pressure along with the fitted curves, calculated based on the corresponding second-order Birch-Murnaghan (BM2) equation of state (EOS) [21], are depicted in Fig. 1(c). The extracted parameters of each EOS are indicated in the figure labels in the respective colors.

As depicted in Fig. 2(c), the room-temperature resistance of f-GST drops very sharply (by more than two orders of magnitude) as a result of the application of just a few GPa. This sharp decrease is followed by a more moderate drop of one order of magnitude as a result of compression of the sample to about 8 GPa. For pressures above 8 GPa, the resistance remains roughly constant. We would like to emphasize that the resistance drop is not accompanied by any crystallographic change as already mentioned above (Fig. 1). The observed slight increase in resistance (by a factor of 2) corresponds to the pressure range where the amorphization is observed, namely, coinciding with the region between f-GST and b-GST. For pressures above 25 GPa the value of the resistance remains roughly constant.
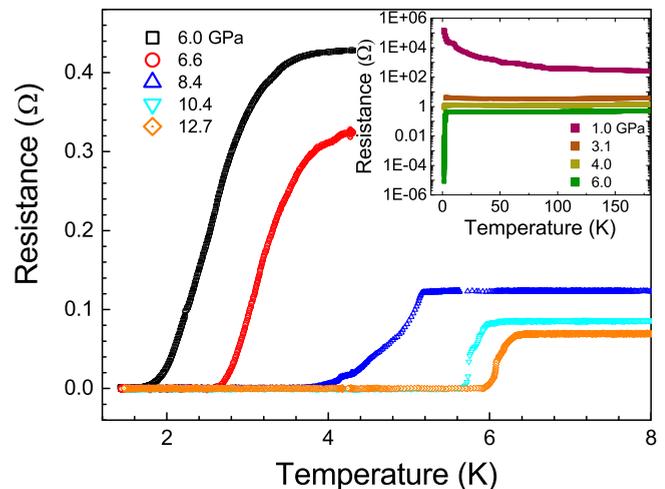

FIG. 3. Temperature dependence of the resistance in f-GST. The graph shows complete superconductivity transitions (resistance drops to zero). The pressure points demonstrating the SIT in f-GST can be seen in the inset.

We now present the results of our transport measurements at low temperatures in Figs. 3 and 4. The resistance versus temperature at pressures between 1 and 6 GPa reveals a clear SIT type behavior in f-GST, as depicted in the inset of Fig. 3. One can clearly see the large resistance change during the transition from an insulating state at 1.0 GPa to the full superconducting state at 6.0 GPa. It is also evident that the onset of superconductivity appears at 4.0 GPa. Figure 3 focuses on the superconductivity transitions in the pressure range where the samples remain in the fcc phase [pressures up to 12.7 GPa; cf. Fig. 2(c), purple]. Throughout the paper, the definition for critical temperature is that of the temperature at which the resistance equals half of the normal state resistance immediately above the transition. As can be seen from Fig. 3, the superconducting transition temperature increases with pressure for pressures between 6 and 12.7 GPa.

Upon further increase of the pressure, in the range between 12.7 and 27 GPa, the superconducting transition temperature shows saturation, as can be inferred from Fig. 4(a). In this pressure range, the pressure-induced amorphous phase forms [Fig. 2(c), gray] and one may expect the coexistence of f-GST and the amorphous phase, as discussed below. The fact that there is only a single transition in the curves for this pressure range, along with the moderate increase in T_c up to 27.0 GPa, suggest that the pressure-induced amorphous phase is similar to f-GST, at least in its superconductivity properties. This assumption is in good agreement with recent theoretical simulations [22], which show a formation of an amorphous structure of cubic framework for GST at pressures above 18 GPa (hereafter referred to as a'-GST), characterized by the collapse of long-range order, formation of homopolar bonds, and slight increase of coordination numbers. Furthermore, according to [14], at ~27GPa strong distortions in the crystal structure are observed, resulting in the formation of a bcc phase. These results correspond well with our experimental observations. For pressures exceeding 27.0 GPa, two distinct transitions appear in the resistance versus T curves, as shown in
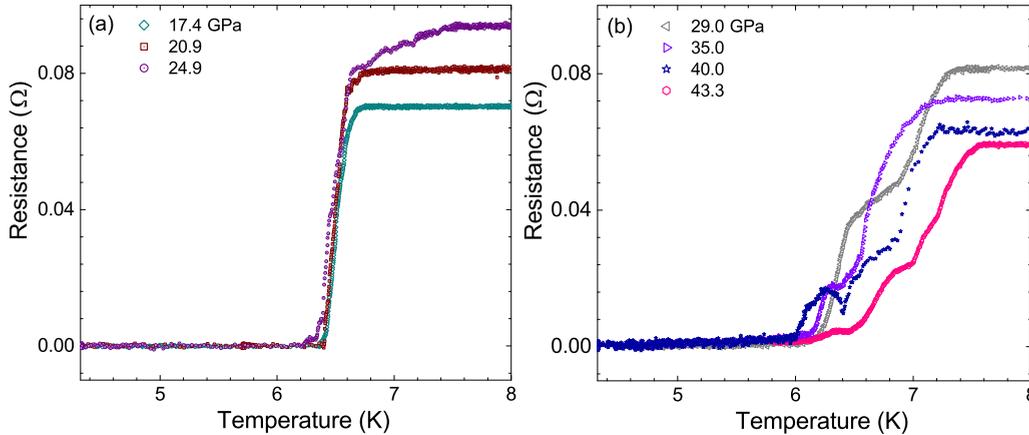
FIG. 4. Superconductivity transitions of (a) a′-GST and (b) a′-GST and b-GST mixture. The double transitions observed in (b) are interpreted as a mixture of a′-GST and b-GST.

Fig. 4(b). This signifies the appearance of the b-GST phase, in accordance with the XRD data [Fig. 2(c), blue]. These double transitions can be interpreted as coexistence of a′-GST with b-GST, both becoming superconductors at different temperatures. The observed coexistence of both phases throughout a wide range of pressures indicates a slow kinetics of the structural transformation of the sample, which is additionally aggravated by inhomogeneous pressure distribution inside the cell (Al$_2$O$_3$ + NaCl is considered a poor pressure medium relative to Ne which is used in the XRD measurements). The double transition will be observed in this case provided that the scale of inhomogeneity exceeds the superconducting coherence length. Moreover, lack of hydrostaticity could be an additional source of the double transition, provided that the grain size in b-GST is larger than the coherence length. We associate the higher T_c value with b-GST, since it is apparent that the critical temperature of a′-GST has already been saturated at about 6.6 K and the higher value for b-GST is consistent with our previously reported results for this phase [15].

A summary of the critical temperature dependence on pressure results in the *T-P* phase diagram shown in Fig. 5. The two distinct critical temperatures are deduced from the analysis of Fig. 4(b), where the T_c for each phase is defined by the midvalue of the corresponding resistance drop. The superconducting critical temperature T_c increases roughly linearly from 1.8 K at 4.0 GPa to 5.8 K at 10.4 GPa [23]. The linear dependence is emphasized by the straight dashed trend line in Fig. 5, which extrapolates to zero temperature at $P_{c,0} = 3.1$ GPa. As will be discussed below, this linear dependence is expected from a Ginzburg-Landau type mean-field theory. Note that other definitions of T_c, such as the onset of zero resistance, do not change the linear dependence of T_c on pressure. They do, however, change the extrapolated value of P_c where $T_c = 0$. In order to verify that this dependence remains linear down to $T_c = 0$ more data are required at lower temperatures.

The appearance of the double transition is accompanied by the observation of anomalous magnetoresistance at $T = 4.2$ K at different pressures, as shown in Fig. 6. Figure 6(a) reveals that for pressures below 29.0 GPa the magnetoresistance behaves as expected—a distinct normal transition from the superconducting state to the normal state for all pressures for which $T_c > 4.2$ K, with a well-defined upper critical field H_{c2}.

However, at higher pressures where a considerable fraction of the sample transforms into b-GST, we observe an anomalous behavior, where the resistance sharply increases above the normal state resistance, followed by a drop to its normal value [Fig. 6(b)]. This peak starts appearing at 35.0 GPa, becomes most pronounced at 36.0 GPa (where the peak reaches 1.5 times the value of the normal state resistance), and then gradually decreases, practically disappearing at 43.3 GPa, where the entire sample is probably in a single b-GST phase.

IV. DISCUSSION AND ANALYSIS OF THE RESULTS

We now turn to the analysis of our experimental findings. Let us start with the linear increase of T_c for pressures immediately above the zero-temperature critical pressure, $P_{c,0} = 3.1$ GPa (Fig. 5). In Ginzburg-Landau theory [24], in the absence of a magnetic field, the superconducting part of the free-energy density can be expanded near the transition to fourth order in the order parameter ψ,

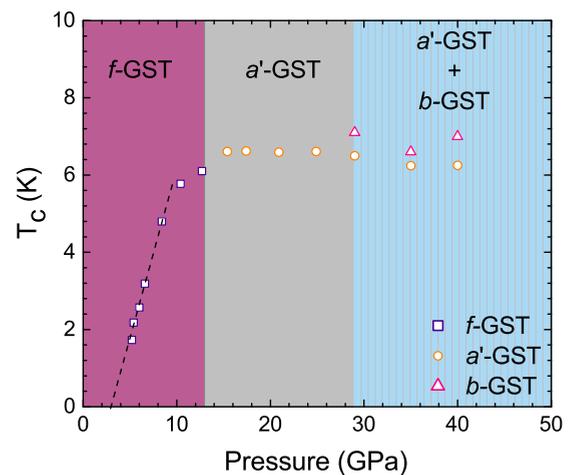$$f_{SC} = \alpha(T,P)|\psi|^2 + \beta(T,P)|\psi|^4,$$

FIG. 5. Superconducting phase diagram. The colored regions are marked according to our XRD data [Figs. 1 and 2(b)] and our superconductivity results (Figs. 3 and 4). The vertical error bars do not exceed the size of the symbols.
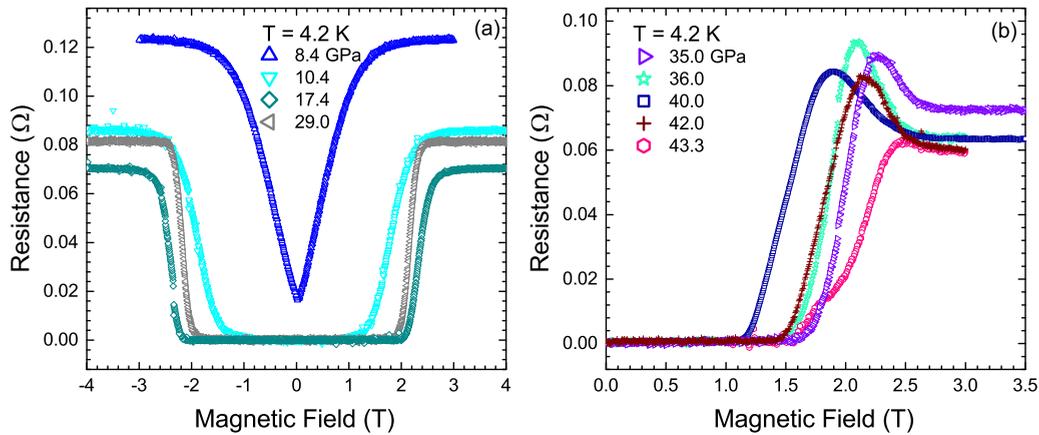
FIG. 6. Magnetoresistance at 4.2 K for (a) pressures up to 29.0 GPa and (b) pressures above 29.0 GPa. In (a) normal transitions are observed, whereas the curves in (b) exhibit an anomalous behavior, with the resistance sharply increasing above its normal state value.

where the coefficients α and β are now not only functions of the temperature T, but also of the pressure P. As usual, $\beta > 0$ to ensure the finiteness of $|\psi|$ at the minimum; hence its exact T and P dependence is irrelevant near the transition. As for α, it is positive in the normal phase and negative in the superconducting phase. Since it vanishes at the transition, in its vicinity it can be expanded to linear order in temperature and pressure,

$$\alpha(T,P) \sim AT + BP + C = A[T - T_C(P)],$$

where $A > 0$ (as usual), and furthermore, $T_c(P) = -(B/A)(P - P_{c,0})$ with $P_{c,0} = -C/B$ (and hence $B\langle 0, C\rangle 0$). Thus, in Ginzburg-Landau theory T_c should indeed be a linear function of P close to the zero-temperature critical pressure $P_{c,0}$. While this is a mean-field prediction, Ginzburg-Landau theory is known to give a good quantitative description of the superconducting transition in three dimensions (3D), due to the typical extreme smallness of the Ginzburg number. Moreover, in the vicinity of the quantum critical point at $T = 0$, $P = P_{c,0}$, the system is effectively four dimensional (counting also the time axis), and mean-field theory becomes an even better approximation [25].

At present, we do not know the exact microscopic mechanism by which the insulator becomes a superconductor, and further experimental and theoretical work is needed in order to determine it. In clean (nondisordered) systems the insulator to superconductor transition is usually explained by changes in the electronic structure due to the so-called Mott transition (Mott-Hubbard model) [26,27]. In disordered systems the situation is more complicated and the transition takes place due to electron localization as described by the Anderson model [10,28]. The system can first undergo a transition from insulator to metal and can only become superconductor at higher pressures. In such a situation it is believed that the pressure introduces superconductivity by modifying the electron density of states at the Fermi energy, $N(E_F)$, the characteristic phonon frequency, and the electron-phonon coupling constant [29].

Let us now turn to the anomalous peak in the magnetoresistance [Fig. 6(b)]. It occurs at the pressure range where b-GST starts to form. In this range, as we already mentioned, we observe a double transition as a function of temperature

at zero field, indicating the coexistence of the a′-GST and b-GST phases. It is reasonable to associate the appearance of the anomalous magnetoresistance with the formation of an inhomogeneous mixture of these two phases. One possible scenario for such an anomalous peak in the magnetoresistance has been discussed in theoretical papers [30–32] trying to explain the huge magnetoresistance peak observed in superconductor thin films of InO [33,34] and TiN [35,36]. In these models, the experimental system is viewed as a two-dimensional (2D) array of Josephson-coupled superconducting islands at zero magnetic field. It is argued that such a system possesses a highly resistive state when the magnetic field is large enough to suppress the coherence between the islands, while not being large enough to destroy the superconductivity in each island. Although it is possible that the anomalous magnetoresistance (MR) observed in our 3D system has a similar origin, there is an alternative explanation which might be more relevant to our system.

In a system where two structural phases coexist, there should exist a range of magnetic fields where one phase is superconducting while the other is normal. The finite superconducting gap suppresses the transmission of quasi-particles between the superconducting and normal regions at low temperatures. On the other hand, Andreev reflections are still allowed. In this process Cooper pairs are transmitted into the superconductor while the electrons are reflected as holes into the normal phase. However, when the transparency of the interface between the phases is low, the tunneling probability of pairs is strongly suppressed [37]. This implies that the resistance of a percolating phase in the normal with nonpercolating islands of a different phase might be larger when these islands are superconducting (intermediate magnetic fields) than when the islands are normal (high magnetic fields).

Now, in our samples we observe two superconducting transitions as a function of temperature at zero field and in the pressure range of 29–40 GPa [Fig. 4(b)]. It is reasonable to assume that the b-GST, which has a higher transition temperature, and thus presumably also a higher critical field, is not percolating between the contacts, since otherwise there would be only one transition, when b-GST becomes superconducting. Therefore, the anomalous MR observed in our samples for some pressure values in the above-mentioned range can be

explained as follows. For low magnetic fields, both percolating a′-GST regions of the sample and isolated islands of b-GST are in the superconducting state, resulting in zero resistance of the sample. When the upper critical field of a′-GST is approached, the resistance starts to rise and reaches the values above the normal state resistance, since the b-GST remains in the superconducting state. The sample resistance starts to decrease towards the normal state resistance only after the superconductivity is destroyed in the b-GST islands, namely, when the upper critical field of b-GST is reached.

V. CONCLUSIONS

To summarize, we demonstrated that polycrystalline $GeSb_2Te_4$ in the fcc phase becomes a superconductor at elevated pressure. The linear variation of the superconductor transition temperature versus pressure indicates a second-order quantum phase transition. Linear extrapolation to zero temperature gives the location of the quantum critical point, at a critical pressure of $P_{c,0} = 3.1$ GPa. In addition, we demonstrate that at higher pressures the f-GST goes through a structural phase transition via amorphization to b-GST, with all phases exhibiting superconductivity. We also provided a possible explanation for the magnetoresistance peak observed in the pressure range where an inhomogeneous mixture of a′-GST and b-GST is present.

[1] T. Siegrist, P. Jost, H. Volker, M. Woda, P. Merkelbach, C. Schlockermann, and M. Wuttig, Nat. Mater. **10**, 202 (2011).

[2] W. Zhang, A. Thiess, P. Zalden, R. Zeller, P. H. Dederichs, J.-Y. Raty, M. Wuttig, S. Blügel, and R. Mazzarello, Nat. Mater. **11**, 952 (2012).

[3] P. Nukala, R. Agarwal, X. Qian, M. H. Jang, S. Dhara, K. Kumar, A. T. C. Johnson, J. Li, and R. Agarwal, Nano Lett. **14**, 2201 (2014).

[4] N. P. Breznay, H. Volker, A. Palevski, R. Mazzarello, A. Kapitulnik, and M. Wuttig, Phys. Rev. B **86**, 205302 (2012).

[5] D. Loke, T. H. Lee, W. J. Wang, L. P. Shi, R. Zhao, Y. C. Yeo, T. C. Chong, and S. R. Elliott, Science **336**, 1566 (2012).

[6] D. Lencer, M. Salinga, and M. Wuttig, Adv. Mater. **23**, 2030 (2011).

[7] J. Hegedüs and S. R. Elliott, Nat. Mater. **7**, 399 (2008).

[8] N. Yamada and T. Matsunaga, J. Appl. Phys. **88**, 7020 (2000).

[9] X. Q. Liu, X. B. Li, L. Zhang, Y. Q. Cheng, Z. G. Yan, M. Xu, X. D. Han, S. B. Zhang, Z. Zhang, and E. Ma, Phys. Rev. Lett. **106**, 025501 (2011).

[10] P. W. Anderson, Phys. Rev. **109**, 1492 (1958).

[11] D. Lencer, M. Salinga, B. Grabowski, T. Hickel, J. Neugebauer, and M. Wuttig, Nat. Mater. **7**, 972 (2008).

[12] S. Caravati, M. Bernasconi, T.D. Kuhne, M. Krack, and M. Parrinello, Appl. Phys. Lett. **91**, 171906 (2007).

[13] Z. M. Sun, J. Zhou, A. Blomqvist, B. Johansson, and R. Ahuja, Phys. Rev. Lett. **102**, 075504 (2009).

[14] M. Krbal, A. V. Kolobov, J. Haines, P. Fons, C. Levelut, R. Le Parc, M. Hanfland, J. Tominaga, A. Pradel, and M. Ribes, Phys. Rev. Lett. **103**, 115502 (2009).

[15] E. Greenberg, B. Hen, S. Layek, I. Pozin, R. Friedman, V. Shelukhin, Y. Rosenberg, M. Karpovski, M. P. Pasternak, E. Sterer, Y. Dagan, G. Kh. Rozenberg, and A. Palevski, Phys. Rev. B **95**, 064514 (2017).

[16] E. Sterer, M. P. Pasternak, and R. D. Taylor, Rev. Sci. Instrum. **61**, 1117 (1990).

[17] C. Prescher and V. B. Prakapenka, High Pressure Res. **35**, 223 (2015).

[18] A. C. Larson and R. B. Von Dreele, General structure analysis system (GSAS), Los Alamos National Laboratory Report No. LAUR 86-748, 1994.

[19] B. H. Toby, J. Appl. Crystallogr. **34**, 210 (2001).

[20] B. Kalkan, S. Sen, and S. M. Clark, J. Chem. Phys. **135**, 124510 (2011).

[21] O. L. Anderson, *Equations of State of Solids for Geophysics and Ceramic Science* (Oxford University Press, New York, 1995).

[22] Z. Sun, J. Zhou, Y. Pan, Z. Song, H.-K. Mao, and R. Ahuja, Proc. Natl. Acad. Sci. U. S. A. **108**, 10410 (2011).

[23] Using the strong $T_c(P)$ dependence at the pressure range 4–10 GPa and the observed width ΔT_c of the transition temperature we can estimate the pressure inhomogeneity ΔP during the measurements. At 6, 6.6, and 8.4 GPa we find $\Delta P \sim 1.2$ GPa. Taking into account that the distance between the Ruby fragments [Fig. 2(b)] is much smaller than the sample size, the above value is consistent with the inhomogeneity depicted in Fig. 2(b).

[24] M. Tinkham, *Introduction to Superconductivity*, 2nd ed. (McGraw-Hill, New York, 1996).

[25] S. Sachdev, *Quantum Phase Transitions*, 2nd ed. (Cambridge University Press, Cambridge, 2011).

[26] N. F. Mott, *Metal-Insulator Transitions* (Taylor & Francis, London, 1990).

[27] M. Imada, A. Fujimori, and Y. Tokura, Rev. Mod. Phys. **70**, 1039 (1998).

[28] P. A. Lee and T. V. Ramakrishnan, Rev. Mod. Phys. **57**, 287 (1985).

[29] L. D. Jennings and C. A. Swenson, Phys. Rev. **112**, 31 (1958).

[30] I. S. Beloborodov, A. V. Lopatin, V. M. Vinokur, and K. B. Efetov, Rev. Mod. Phys. **79**, 469 (2007).

[31] V. Vinokur, T. Baturina, M. Fistul, A. Y. Mironov, M. Baklanov, and C. Strunk, Nature (London, U. K.) **452**, 613 (2008).

[32] Y. Dubi, Y. Meir, and Y. Avishai, Phys. Rev. B **73**, 054509 (2006).

[33] M. Steiner and A. Kapitulnik, Phys. C **422**, 16 (2005).

[34] M. Ovadia, D. Kalok, B. Sacepe, and D. Shahar, Nat. Phys. **9**, 415 (2013).

[35] T. I. Baturina, A. Yu. Mironov, V. M. Vinokur, M. R. Baklanov, and C. Strunk, Phys. Rev. Lett. **99**, 257003 (2007).

[36] T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Balkanov, and A. Satta, JETP Lett. **79**, 337 (2004).

[37] G. E. Blonder, M. Tinkham, and T. M. Klapwijk, Phys Rev B **25**, 4515 (1982).