Two-stage pressure-induced Yb valence change in the hexagonal Laves phase YbAg₂: Investigation by time differential perturbed angular $\gamma - \gamma$ correlation spectroscopy method and density functional calculations

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We have studied the C14 hexagonal Laves phase of YbAg₂ at normal conditions and under external pressure up to 19 GPa by the time-differential perturbed angular $\gamma-\gamma$ correlation spectroscopy (TDPAC) using ¹¹¹Cd probe nuclei. Under pressure the valence of Yb undergoes a two-stage transition from 2.8 to 3. The two-stage scenario is characterized by two distinct quadrupole frequencies of ¹¹¹Cd probes in a silver sublattice, monotonically increasing with pressure and saturating at 8 and 16 GPa. Our experimental data are compared with the density functional studies of the electron band structure of YbAg₂, whose results are used for discussion and interpretation of these experiments. We have found that there are two different electric field gradients at inequivalent silver sites and that 4d states of silver participate in metal bonding, allowing for the formation of the hexagonal Laves phase.

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I. INTRODUCTION

Ytterbium intermetallic compounds exhibit a rich variety of interesting physical phenomena such as intermediate valence, Kondo and heavy fermion behaviors, quantum critical behavior, and non-Fermi liquid behavior [1–3]. Herewith, their properties are highly sensitive to external pressure, magnetic field, or temperature as well as to chemical environment of ytterbium ions. This is due to the fact that in the atomic ground state, Yb is divalent with a filled $4f^{14}(sd)^2$ shell, but in the solid state, the f electron may experience the electronic transition from the $4f^{14}(sd)^2$ configuration to the $4f^{13}(sd)^3$ configuration (Yb is trivalent). As a consequence, the total f occupancy can be noninteger and fall in between 14 and 13, with the Yb ion valence varying from two to three. A high valence of ytterbium in elemental metal can be attained by application of pressure [4]. As pressure mounts from the normal value to 20 GPa, the ytterbium valence increases from two to an intermediate state (2.55 ± 0.05) reaching the value of three above 100 GPa [6]. Similarly to the pristine metal, in intermetallic compounds the Yb ion can exhibit a different integral valence (two or three) or be in the intermediate valence regime [7–14].

Changeable ytterbium valence is also observed in novel metastable compounds synthesised under high pressure and temperature conditions [15–18]. However, despite much experimental effort, the trivalent state of Yb in these intermetallic compounds has not been achieved even at sufficiently high pressures [17,19–21]. Here we report on our pressure studies of the novel hexagonal phase of the YbAg₂ compound, demonstrating a two-stage evolution of Yb valence, which

terminates at trivalent electronic state. Investigations of the effect of pressure on the valence of ytterbium in YbAg₂ are of particular interest since it is probably the best way to detect subtle changes in metallic bonding. Earlier we have shown that the effect of high pressure can be studied within the time-differential perturbed angular $\gamma - \gamma$ correlation spectroscopy (TDPAC) using ¹¹¹Cd probe nuclei [22], and established a linear correlation between the valence and the electric field gradient (or the quadrupole frequency ν_Q). Here we present a pressure-induced investigation where we have used a diamond anvil cell (see Fig. 1) to generate pressure up to 19 GPa.

At ambient pressure YbAg₂ has the orthorhombic structure of the CeCu₂ type [23], which is nonmagnetic with the divalent state of Yb. Since the divalent state of ytterbium implies conventional behavior, for our experiments we have chosen the hexagonal phase of YbAg₂ crystallized in the (C14) MgZn₂ structure (at pressure of 5 GPa), where the valence of ytterbium is 2.8 [18]. In the hexagonal phase a silver atom can be easily substituted with the ^{111}Cd probe and as a result we can create a relatively high density of ^{111}Cd nuclei required for the TDPAC measurements of hyperfine interactions parameters under high pressure.

The details of TDPAC measurements are given in Sec. II, the obtained results are discussed in Sec. III. For interpretation of the results in Sec. III we have used *ab initio* calculations of the electronic band structure of $YbAg_2$ and the related compound where some silver atoms are substituted with Cd probes.

II. EXPERIMENT AND THEORY

Experimental measurements were carried out by the TD-PAC method using the 171–245 keV $\gamma-\gamma$ cascade in ^{111}Cd populated through the 2.8 d isotope ^{111}In electron capture

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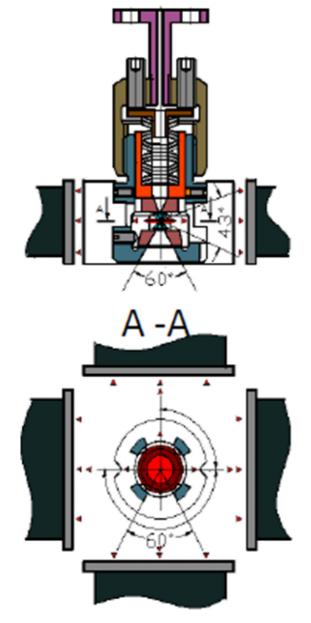


FIG. 1. Diamond anvil cell with four surrounding windows for four BaF₂ detectors. Lower panel represents the A-A cross section.

decay. The cascade proceeds via the 245 keV level with the half-life $\tau_{1/2}=84$ ns, spin I=5/2, and quadrupole moment Q=0.83(13) b [24]. The ¹¹¹In activity was produced via the ¹⁰⁹Ag $(\alpha,2n)$ ¹¹¹In reaction through irradiating a silver foil with the 32 MeV α beam at the Nuclear Physics Institute cyclotron (Moscow State University). The ¹¹¹In-¹¹¹Cd nuclear probes were introduced into the lattice of YbAg₂ by the high-pressure synthesis: the constituents (Yb and Ag) taken in proper amounts with an overall weight of about 600 mg were melted together with a piece of the irradiated silver foil (1 mg) in a special chamber under pressure of 5 GPa [18]. The x-ray diffraction pattern presented in Fig. 2 confirms the hexagonal Laves phase [18]. As the samples were polycrystalline and paramagnetic at temperatures above 4 K, the perturbation of the angular correlation can be described by the perturbation

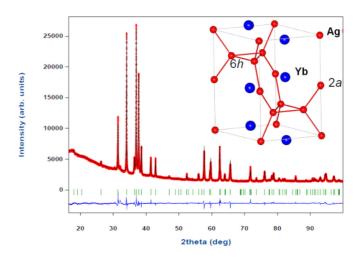


FIG. 2. X-ray powder diffraction profile (red) and its Rietveld refinement fit (black) for the hexagonal (C14) sample of $YbAg_2$ with ^{111}Cd probes. The difference plot (blue) and Bragg peaks (green) are plotted underneath. Inset shows the C14 hexagonal structure of $YbAg_2$.

factor G_{22} for the static electric quadrupole interaction (EQI) [25]:

$$G_{22}(t; \nu_{\mathcal{Q}}, \eta, \sigma) = \sum_{i} p_{i} \left(S_{20} + \sum_{n} S_{2n} \cos(\omega_{n} t) \right)$$

$$\times \exp\left(-\omega_{n}^{2} \sigma^{2} t^{2} / 2 \right). \tag{1}$$

Here p_i stands for the relative populations of nonequivalent sites of the probe nuclei; the hyperfine frequencies ω_n depend on the quadrupole coupling constant $v_Q = eQV_{zz}/h$ called below the quadrupole frequency (QF) and the asymmetry parameter $\eta = (V_{xx} - V_{yy})/V_{zz}$, where $V_{ii} = \frac{\partial^2 V}{\partial i^2}(i = x, y, z)$ are the principal-axis components of the tensor of the electric field gradient (EFG). The coefficients S_{2n} depend only on η (0 $\leq \eta \leq$ 1). For the nuclear spin I = 5/2 there are three transitions: n = 1,2,3. The exponential term is of the Gaussian form customarily used to represent a possible distribution of EFG and σ is the relative half-width of the Gaussian distribution. Here we restrict ourselves to the perturbation parameter of the second order since the unperturbed angular correlation coefficient $A_{44} \ll A_{22}$ ($A_{22} = -0.18$). The perturbation factor $G_{22}(t)$ describing a nuclear spin precession due to the hyperfine interaction, was determined in a usual way from the TDPAC spectrum R(t), measured by a four-detector spectrometer [26]. The TDPAC spectrum R(t) was obtained by combining the delayed coincidence spectra measured at the angles of $\pi/2$ and π between detectors $N(\pi/2,t)$ and $N(\pi,t)$ through the expression

$$R(t) = -A_{22}Q_2G_{22}(t). (2)$$

Here $Q_2 \approx 0.80$ is the solid-angle correction and

$$R(t) = -2\frac{N(\pi, t) - N(\pi/2, t)}{N(\pi, t) + 2N(\pi/2, t)}.$$
 (3)

External pressures up to 8 GPa were generated in a calibrated "toroid"-type device [27]. For pressures above

8 GPa we used a special high-pressure cell with diamond anvils with $\approx\!580~\mu m$ culet diameters and $\approx\!\pi/3$ aperture. The diamond anvil cell is shown schematically in Fig. 1. A 200 μm hole was drilled in the pre-indented stainless-steel gasket. Samples of YbAg₂ ($\approx\!75\times75\times25~\mu m^3$ in size), doped with $^{111}\text{In-}^{111}\text{Cd}$ and ruby chips were placed inside the gasket filled with sodium chloride as a pressure-transmitting medium. Pressure was measured by the ruby luminescence technique using the standard ruby calibration scale.

The quadrupole frequencies $v_Q(6h)$ (the ¹¹¹Cd localized in 6h sites) and $v_Q(2a)$ (the ¹¹¹Cd localized in 2a sites), where $v_Q = eQV_{zz}/h$ were measured as a function of pressure (up to 19 GPa) at room temperature and as a function of temperature at normal pressure.

Experimental data were analyzed with the DEPACK software [28].

The electronic band structure of YbAg₂ has been calculated using the linearized augmented plane wave method (LAPW) with the potential of general shape taking into account a semicore 5p band of Yb and the spin-orbit coupling splitting the 4f and 5p Yb band electron shells [29]. The C14 primitive unit cell is large: in total there are 12 atoms of three different types 4Yb, 2Ag(2a), 6Ag(6h) (a detailed discussion on two different silver sites is given in Sec. III). With the LAPW basis state cut-off parameter R_{MT}^{max} $K_{\text{max}} = 9$ we have 1131 basis functions for each point of the Brillouin zone. The number of k points was 215 for the self-consistent procedure and 1331 for the final run, with the number of calculated low-lying bands about 100. For calculation of the exchange-correlation potential and the exchange-correlation energy contribution we have used a variant of the local density approximation within the density functional theory (DFT) [30]. Calculations with Cd probe atom have been carried out by substituting Ag with Cd in the site 2a or 6h of the YbAg₂ unit cell.

III. RESULTS AND DISCUSSION

The x-ray diffraction measurements were carried out on a set of YbAg₂ powdered samples with the ¹¹¹Cd probes, from which the C14 hexagonal structure (the $P6_3/mmc$ space symmetry, the group number 194, Z=4) illustrated in Fig. 2 was confirmed [18]. The diffraction pattern and optimized structure obtained from Rietveld refinement (Fig. 2) yields the lattice constants a=b=5.6853(2) Å and c=9.3105(4) Å.

In the C14 phase there are two different sites of silver, Ag(2a) and Ag(6h), with the population ratio p(2a)/p(6h) =1:3 (see Fig. 2 and Table I). The Ag(2a) atom in the 2aposition is surrounded by six Ag(6h) and six Yb atoms. The Ag(6h) atom in the 6h position is surrounded by four Ag(6h) and two Ag(2a) atoms, and six Yb atoms. (Detailed information on neighboring shells for all atoms is given in Table I.) Ag(2a) and Ag(6h) sites have different local symmetry. The Ag(2a) site has the inversion symmetry while the Ag(6h) site does not. As a result, the electron density around the Ag(2a) site is expanded in spherical harmonics Y_L^m with even L (i.e., L = 0, 2, 4,...), while the electron density around Ag(6h) expands in spherical harmonics with even and odd L (i.e., L = 0, 1, 2, 3,...). Both silver sites [Ag(2a) and Ag(6h)] allow for a quadrupole electric component (l = 2)and a nonzero electric field gradient (EFG), which enables the

TABLE I. Nearest neighbor shells and distances (in Å) with the number of atoms in each shell for three nonequivalent atoms of YbAg₂. Last line shows lowest spherical harmonics used in the density expansion around each element.

Shell	Yb	Ag(2a)	Ag(6h)		
1	3.32812 6Ag(6h)	2.85482 6Ag(6h)	2.82435 2Ag(6h)		
2	3.33396 3Ag(2a)	3.33396 6Yb	2.85482 2Ag(2a)		
3	3.34977 3Ag(6h)	4.65998 2Ag(2a)	2.85718 2Ag(6h)		
4	3.46777 1Yb	4.91901 12Ag(6h)	3.32812 4Yb		
5	3.49017 3Yb	5.22254 6Yb	3.34977 2Yb		
Y_L^m	L = 1, 2, 3, 4,	L = 2, 4,	L = 1, 2, 3, 4,		

TDPAC signal. However, since the crystallographic sites and density expansion of the two silver sites are different, EFG for Ag(2a) and Ag(6h) are expected to be different too. This fact is confirmed by the electron band structure calculation of $YbAg_2$. In the TDPAC experiments we also observed nonequivalent EFGs on cadmium probe atoms inserted at sites 2a and 6h. The TDPAC spectra R(t) measured at the 111 Cd probe nuclei in $YbAg_2$ are given in Figs. 3 and 4, whose panels reproduce the evolutions of R(t) with temperature at normal pressure and with pressure at room temperature.

It is worth noting that the 111 Cd probe nuclei occupy exclusively sites of the Ag sublattice. This has been demonstrated previously for the YMn₂ compound synthesized in the same hexagonal structure at high pressure [31]. Another indication of this conclusion is that the experimentally observed occupation ratio p(6h)/p(2a) is close to three, clearly corresponding to the ratio of 6h/2a sites in the Ag sublattice [in the unit cell of the C14 structure there are two Ag(2a) atoms and six Ag(6h)

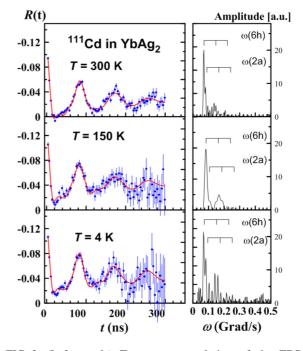


FIG. 3. (Left panels) Temperature evolution of the TDPAC spectrum R(t) of YbAg₂ taken from the ¹¹¹Cd nuclear probes located at crystallographically nonequivalent 2a and 6h sites of the Ag sublattice at normal pressure. (Right panels) Their Fourier transforms.

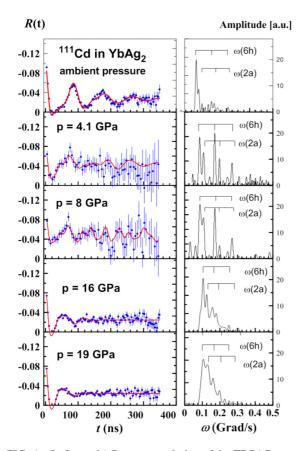


FIG. 4. (Left panels) Pressure evolution of the TDPAC spectrum R(t) of YbAg₂ taken from the ¹¹¹Cd nuclear probes located at crystallographically nonequivalent 2a and 6h sites of the Ag sublattice at room temperature. (Right panels) Their Fourier transforms. The spectra at 4.1 and 8 GPa have large errors because the measurements were carried out in a toroid-type chamber, for which a low signal-to-background ratio was observed.

atoms]. Since there are two types of Ag sites [Ag(2a)] and Ag(6h) having different values of EF gradients, there are two quadrupole frequencies $v_Q(2a)$ and $v_Q(6h)$ associated with the 111 Cd probe nuclei located at these sites. These frequencies as well as other characteristics of EFGs are quoted in Tables II and III.

From Fig. 3 showing the temperature evolution of the TDPAC data, it follows that the frequencies v_{Q1} and v_{Q2} practically do not change with temperature. Consequently, in

the region 4–300 K the valence of ytterbium is approximately temperature independent.

Another important finding is a variation of both quadrupole frequencies with pressure. The 6h site frequency $v_Q(6h)$ is increased from 76 to 93 MHz (at P=8 GPa), while the 2a site frequency $v_Q(2a)$ changes from 100 to 125 MHz (at P=16 GPa). These changes of $v_Q(6h)$ and $v_Q(2a)$ with pressure are summarized in Fig. 5. From Fig. 5 we see that a characteristic feature of both plots is a smooth rise to a certain value [93 MHz at 8 GPa for $v_Q(6h)$, 125 MHz at 16 GPa for $v_Q(2a)$], which then remains constant with further pressure increase. The constant value of $v_Q(2a,6h)$ is an indication that Yb in YbAg₂ has reached a stable monovalent state, which in our case is the trivalent one. Indeed, earlier it has been shown that GdAl₂ with the trivalent state of Gd shows no significant change of the quadrupole frequency [22].

In a mixed valent compound the pressure (P) or valence $[\upsilon = \upsilon(P)]$ dependence of the measured quadrupole frequency $v_O = v_O(v)$ is commonly described by the linear equation $v(v) = v_2 + (v_3 - v_2)(v - 2)$. In our case vis the valence of Yb (between two and three), while v_2 (v_3) is the frequency measured for the compound with the divalent (trivalent) ytterbium. In YbAg₂ at normal pressure $v_0 = 2.8$ [18], and for the divalent state of Yb we accept $v_2 = 5.7$ MHz. (This frequency can be extracted from data for CaAl2.) The linear relation then can be rewritten with respect to v_3 , $v_3 = v_2 + [v(v_0) - v_2]/(v_0 - 2)$. Substituting here the experimental (P = 0) quadrupole frequency values $v(v_0) = 97$ MHz for the 2a site and 76 MHz for the 6h site we obtain that $v_3 = 125$ and 93 MHz for the 2a and 6h site, respectively. These values are in good correspondence with the saturated frequencies $v_O(2a) \approx 125$ MHz and $v_O(6h) \approx$ 93 MHz shown in Fig. 5, indicating self-consistency of the obtained experimental results demonstrating the trivalent state of ytterbium.

It is worth mentioning that already at the pressure 8 GPa all ytterbium ions are trivalent with respect to the first 6h silver shell. However, since the quadrupole frequency for the 2a silver sites is not constant at this pressure (Fig. 5), we can use our formula which formally yields 2.97 for the ytterbium valence. We then conclude that in going from 8 to 16 GPa, the ytterbium valence changes from 2.97 to 3. Such a slow valence change characteristic of many rare earth compounds has been found in XAS L3-edge experiments, for example in YbAl₂ [19] and YbAl₃ [20]. In our case due to the local method used for valence determination, it is possible to probe the ytterbium valence selectively (i.e., with respect to different

TABLE II. Hyperfine quadrupole interaction parameters measured at the 111 Cd probe nuclei in YbAg₂ at various pressures at room temperature. $\nu_Q(6h)$, $\eta(6h)$, $\sigma(6h)$, $\rho(6h)$ and $\nu_Q(2a)$, $\eta(2a)$, $\sigma(2a)$, $\rho(2a)$ stand for the quadupolar frequency, the asymmetry parameter, the frequency distribution, and the relative population of the 111 Cd probes located at crystallographically nonequivalent 6h and 2a sites of the Ag sublattice, respectively.

P (GPa), T = 300 K	$v_Q(6h)$ (MHz)	$v_Q(2a)$ (MHz)	η(6h)	$\eta(2a)$	$\sigma(6h)$	$\sigma(2a)$	p(6h)	<i>p</i> (2 <i>a</i>)
0	76(1)	97(3)	0.2(1)	0.0(1)	0.1(1)	0.1(1)	0.8(1)	0.3(1)
4.1	80(2)	98(2)	0.4(1)	0.4(1)	0.2(1)	0.2(1)	0.8(1)	0.2(1)
8.0	93(2)	107(2)	0.4(1)	0.3(1)	0.05(2)	0.05(2)	0.5(1)	0.3(1)
16.0	93(3)	123(4)	0.5(1)	0.5(1)	0.15(5)	0.1(1)	0.7(1)	0.3(1)
19.0	91(3)	125(5)	0.4(1)	0.5(1)	0.18(4)	0.18(4)	0.7(1)	0.3(1)

TABLE III. Measured $(V_{zz}^{\rm expt})$ and calculated $(V_{zz}^{\rm calc})$ EFGs in $10^{21}~{\rm V/m^2}$ at P=0 and 19 GPa at room temperature.

YbAg ₂ (C14)	$V_{zz}^{ m expt}$:	V _{zz} at ¹¹¹ Cd		$V_{zz}^{ m calc}$ at Cd		$V_{zz}^{\rm calc}$ at Ag	
P, T	6 <i>h</i>	2 <i>a</i>	6 <i>h</i>	2 <i>a</i>	6 <i>h</i>	2 <i>a</i>	
0 GPa, 300 K 19 GPa, 300 K	3.8(6) 4.5(7)	5.0(8) 6.0(10)	1.9 2.0	4.1 4.7	6.1 6.9	8.0 9.1	

shells of neighbors) and even single out a crystallographic site completing the valence change.

The existence of two distinct frequencies $v_Q(2a)$ and $v_Q(6h)$ in YbAg₂ at normal and elevated pressure, Table II and Fig. 5, and their different pressure dependence lead to the conclusion that the electronic properties of silver at two crystallographically nonequivalent sites (6h and 2a) are fairly different and silver atoms located at the 6h and 2a sites behave to some extent as different elements.

The conclusion is fully confirmed by *ab initio* band structure calculations, whose main results are presented in Fig. 6. First, one can notice two very narrow group of band states centered around -1.57 and -0.24 eV, which correspond to splitted $4f_{5/2}$ and $4f_{7/2}$ electron levels. The region from -7 to -3 eV refers to the silver 4d states hybridized with other ytterbium states (mainly with 5d and 6s). Notice that the 4d states are not separated from the 5s and other Yb states by a gap of forbidden states, and therefore the 4d states fully participate in the formation of metal bonding in YbAg₂.

Our calculations have revealed a complex shape of the Fermi surface of $YbAg_2$, shown in Fig. 7. Its complexity reflects a relatively large intersections of the Fermi energy by valence electron bands. The calculated density of states (DOS) at the Fermi level is 3.86 state/eV or 9.09 mJ/mol K^2 . The last value should be compared with 12.9 mJ/mol K^2 found from the experimental fit of specific heat [18]. The discrepancy is usually accounted for by the electron-phonon interaction. In the present case there can be also an influence of the low temperature anomaly developed below 6 K (Fig. 5 of Ref. [18]).

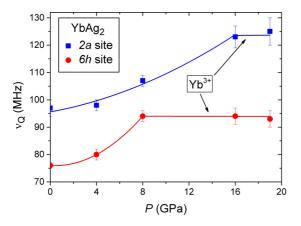


FIG. 5. Pressure evolution of the quadrupole frequencies v_Q for ¹¹¹Cd nuclear probes located at crystallographically nonequivalent sites (2*a* and 6*h*) of Ag in YbAg₂.

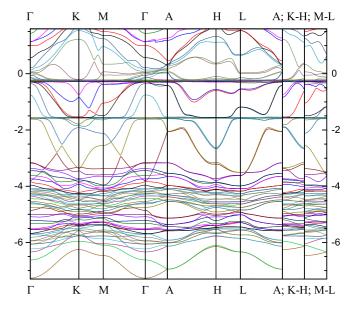


FIG. 6. Electron band structure of YbAg₂ along high symmetry lines. The Fermi level (E_F) corresponds to the zero energy. Calculated semicore 5p band of Yb lie about 27 eV below E_F (not shown).

Of particular interest is the partial density of states (DOS) of the two silver atoms and their difference shown in Fig. 8.

Notice that DOS of Ag(2a) is larger than DOS of Ag(6h)at the energy range from -5.45 to -5.68 eV and also around -5.24 and -4.74 eV, whereas at other energies the opposite takes place. Partial charges $(Q_l, \text{ where } l = s, p, d, f)$ of two silver atoms are close but nevertheless different. A typical difference is 0.01. At the 2a site the values of the partial charges Q_l with even l (i.e., Q_s , Q_d) are somewhat larger while at the 6h site Q_l with odd l (i.e., Q_p , Q_f) are larger. The total electron charge is slightly larger for Ag(2a). The difference between Ag(2a) and Ag(6h) is much more pronounced for multipole density distributions and charges, that is, for density components with $L \neq 0$. For example, the quadrupole electron density component at 2a site is described by the spherical component $Y_{l=2}^0$, whereas for 6h site it is given by two angular functions, $S_1 = -c_1 Y_{l=2}^0 + c_2 Y_{l=2}^{2,c}$ and $S_2 = c_2 Y_{l=2}^0 + c_1 Y_{l=2}^{2,c}$. Here $c_1 = 0.7559$, $c_2 = 0.6547$, and $Y_{l=2}^{2,c}$ stands for the real spherical harmonics of the cos type. Different quadrupole distribution of electron charges results in different EFG at

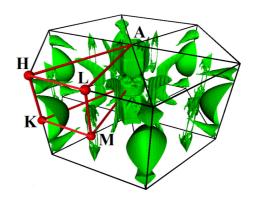


FIG. 7. The Fermi surface of YbAg₂.

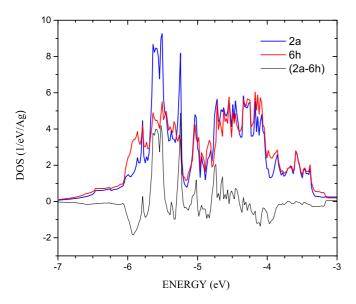


FIG. 8. Density of states (DOS) of two different silver atoms [Ag(2a) and Ag(6h), see text for details] in YbAg₂. Black line stands for the difference plot.

silver nuclei. For EFG at Ag(2a) we have $-8.04 \times 10^{21} \text{ V/m}^2$ and for EFG at Ag(6h) -6.12×10^{21} V/m². Calculations with Cd yield -4.11 V/m^2 for Cd at the 2a site and $-1.90 \times 10^{21} \text{ V/m}^2$ ($\eta = 0.1$) for Cd at the 6h site. (It should be noted that the calculation of Cd in the 6h site is less precise than in the 2a site. Such a calculation is only approximate because during the calculation we ignore a symmetry change induced by the probe Cd atom. The symmetry of the 2a site on the other hand does not change with substitution of Ag by Cd.) Therefore, EFG is larger at the 2a site in the correspondence with the experimental data. Since the electron density at the 6h site is described by two functions S_1 and S_2 with the azimuthal component m = 2, the matrix of gradients is not axially symmetric, and the EFG asymmetry parameter $\eta \neq 0$. This fact is also in correspondence with the EFG data measured at ¹¹¹Cd in 6h sites at normal conditions, Table II. We have $\eta = 0.8$ for Ag(6h) and $\eta = 0.1$ for Cd(6h). We have also calculated that the minimum of total energy of YbAg2 associated with the trivalent state of Yb around the 6h site of Ag and found that it corresponds to the unit cell volume $V(Yb^{+3}, 6h \text{ site}) = 245.3 \text{ Å}^3$. This volume is approximately 6% smaller than the experimental one at normal pressure and our estimations show that it can be reached under pressure of \approx 8.5 GPa. Notice that this pressure leads to the saturated value of the v_O at the 6h site marking the onset of the Yb trivalent state, Fig. 5. Calculations also confirm the experimental increase of EFG with pressure, Fig. 5 and Table III. The calculated values of EFG with $V(Yb^{+3}, 6h \text{ site})$ are $-9.07 \times 10^{21} \text{ V/m}^2$ at $Ag(2a), -6.94 \times 10^{21} \text{ V/m}^2$ with $\eta = 0.8$ at Ag(6h) for $YbAg_2$; $-4.69 \times 10^{21} \text{ V/m}^2$ at Cd(2a), and $-2.0 \times 10^{21} \text{ V/m}^2$ with $\eta = 0.46$ at Cd(6h) for Cd probes in YbAg₂. It should be mentioned that a slight increase of the asymmetry parameter η with pressure is also observed for the 2a site. This may be connected with deformation of the crystal lattice due to the nonhydrostatic properties of NaCl as pressure-transmitting medium.

The valence of ytterbium is found to be close to three at normal pressure. Formally, the number of 4f states $Q_f = 13.68$ per Yb atom. However, if following Ref. [32] we localize $13\ f$ electrons during the self-consistent procedure, then we obtain that the residual number of 4f band states is close to null. On the other hand, for elemental ytterbium which is in the divalent state, the number of 4f band states is very close to 14. These findings according to arguments of Ref. [32] implies that the ytterbium has an intermediate valence close to three.

Since there is only one crystallographic site of ytterbium, the question about its valence in the pressure region from 8 to 16 GPa arises, Fig. 5. The full trivalent state of ytterbium is realized at 16 GPa. However, the metallic bond of ytterbium is apparently sensitive to the direction of Yb-Ag bonding, which can be of Yb-Ag(2a) or Yb-Ag(6h) type. Based on Fig. 5 we observe that the Yb-Ag(6h) bond corresponding to slightly closer Yb-Ag distance (Table II) reaches saturation at a lower pressure (8 GPa) in comparison with the Yb-Ag(2a) bond where the saturation pressure is 16 GPa.

IV. CONCLUSIONS

Our TDPAC study confirms that the valence of ytterbium in the hexagonal C14 phase of YbAg₂ is intermediate (2.8 [18]) and close to three. The valence of Yb in the hexagonal phase is different from the divalent state of Yb found in the orthorhombic phase of the CeCu₂ structure. Under external pressure we observe an unusual behavior of quarupole frequencies shown in Fig. 5 which we characterize as a two-stage transition to the trivalent state of Yb. A saturation of the TDPAC quadrupole frequency first occurs for probes at the 6h sites at 8 GPa $[\nu_O(6h)]$ and then for probes at the 2a sites $[\nu_O(2a)]$ at a still higher pressure of 16 GPa. We attribute the two-stage transition to two different states of silver at the 2a and 6h sites of the C14 structure and correspondingly to two different states of the ¹¹¹Cd probes. A thorough discussion on this issue supported by DFT band structure calculations of YbAg₂ is presented in Sec. III. The 4d states of silver are involved in metal bonding, making silver in YbAg₂ analogous to other 4d transition metals (for example, Ru) with unoccupied 4d shell and allowing for the formation of the hexagonal Laves phase. It is also remarkable that the transition to the trivalent state takes place in YbAg₂ under a relatively moderate pressure of 8-16 GPa.

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- [1] P. Wachter, *Handbook on the Physics and Chemistry of Rare Earths* (North-Holland, Amsterdam, 1993), Vol. 19, Chap. 132.
- [2] M. S. Torikachvili, S. Jia, E. D. Mun, S. T. Hannahs, R. C. Black, W. K. Neils, Dinesh Martien, S. L. Bud'ko, and P. C. Canfield, Proc. Natl. Acad. Sci. USA 104, 9960 (2007).
- [3] S. Wada and A. Yamamoto, Physica B 403, 1202 (2008).
- [4] K. Syassen, G. Wortmann, J. Feldhaus, K. H. Frank, and G. Kaindl, Phys. Rev. B 26, 4745 (1982).
- [5] C. Dallera, O. Wessely, M. Colarieti-Tosti, O. Eriksson, R. Ahuja, B. Johansson, M. I. Katsnelson, E. Annese, J.-P. Rueff, G. Vanko, L. Braicovich, and M. Grioni, Phys. Rev. B 74, 081101(R) (2006).
- [6] G. N. Chesnut and Y. K. Vohra, Phys. Rev. Lett. 82, 1712 (1999).
- [7] J. M. Lawrence, G. H. Kwei, P. C. Canfield, J. G. DeWitt, and A. C. Lawson, Phys. Rev. B 49, 1627 (1994).
- [8] J. J. Joyce, A. B. Andrews, A. J. Arko, R. J. Bartlett, R. I. R. Blyth, C. G. Olson, P. J. Benning, P. C. Canfield, and D. M. Poirier, Phys. Rev. B 54, 17515 (1996).
- [9] H. Winkelmann, M. M. Abd-Elmeguid, H. Micklitz, J. P. Sanchez, C. Geibel, and F. Steglich, Phys. Rev. Lett. 81, 4947 (1998).
- [10] K. Alami-Yadri, H. Wilhelm, D. Jaccard, Physica B 259, 157 (1999).
- [11] C. Dallera, M. Grioni, A. Shukla, G. Vanko, J. L. Sarrao, J. P. Rueff, and D. L. Cox, Phys. Rev. Lett. 88, 196403 (2002).
- [12] Y. Singh, S. Ramakrishnan, Z. Hossain, and C. Geibel, Phys. Rev. B 66, 014415 (2002).
- [13] Y. Muro, K. Yamane, M. S. Kim, T. Takabatake, C. Godart, and P. Rogl, J. Phys. Soc. Jpn. 72, 1745 (2003).
- [14] T. Jeong, Physica B **390**, 309 (2007).
- [15] N. L. Eatough and H. T. Hall, Inorg. Chem. 11, 2608
- [16] A. V. Tsvyashchenko and S. V. Popova, J. Less-Common Met. 90, 211 (1983).
- [17] A. V. Tsvyashchenko, A. I. Velichkov, A. V. Salamatin, L. N. Fomicheva, D. A. Salamatin, G. K. Ryasny, A. V. Nikolaev, M. Budzynski, R. A. Sadykov, and A. V. Spasskiy, J. Alloys Compd. 552, 190 (2013).
- [18] A. V. Tsvyashchenko, A. P. Menushenkov, V. A. Sidorov, A. E. Petrova, L. N. Fomicheva, O. V. Chernysheva, Yu. B. Lebed,

- S. N. Axenov, S. L. Bud'ko, L. Sun, and Z. Zhao, J. Alloys Compd. **650**, 295 (2015).
- [19] C. Dallera, E. Annese, J.-P. Rueff, A. Palenzona, G. Vanko, L. Braicovich, A. Shukla, and M. Grioni, Phys. Rev. B 68, 245114 (2003).
- [20] R. S. Kumar, A. Svane, G. Vaitheeswaran, V. Kanchana, E. D. Bauer, M. Hu, M. F. Nicol, and A. L. Cornelius, Phys. Rev. B 78, 075117 (2008).
- [21] T. Watanuki, D. Kawana, A. Machida, and AnPang Tsai, J. Phys. Soc. Jpn. 80, SA087 (2011).
- [22] A. V. Tsvyashchenko, L. N. Fomicheva, V. B. Brudanin, O. I. Kochetov, A. V. Salamatin, A. Velichkov, M. Wiertel, M. Budzynski, A. A. Sorokin, G. K. Ryasniy, B. A. Komissarova, and M. Milanov, Phys. Rev. B 76, 045112 (2007).
- [23] K. H. J. Buschow, Rep. Prog. Phys. 42, 1373 (1979).
- [24] P. Herzog, K. Freitag, M. Reuschenbach, and H. Walitzki, Z. Phys. A 294, 13 (1980).
- [25] R. M. Steffen and H. Frauenfelder, in *Perturbed Angular Correlations*, edited by E. Karlsson, E. Matthias, and K. Siegbahn (North-Holland, Amsterdam, 1964).
- [26] V. B. Brudanin, D. V. Flossofov, O. I. Kochetov, N. A. Korolev, M. Milanov, V. Ostrovskiy, V. N. Pavlov, A. V. Salamatin, V. V. Timkin, A. I. Velichkov, L. N. Fomicheva, A. V. Tsvyashchenko, and Z. Z. Akselrod, Nucl. Instrum. Methods Phys. Res. Sect. A 547, 389 (2005).
- [27] L. G. Khvostantsev, L. F. Vereshchagin, and A. P. Novikov, High Temp. High Press. 9, 637 (1977).
- [28] B. Lindgren, DEPACK an interactive data analyses program. University of Uppsala, Institute of Physics Report, UUIP-1017, 1980
- [29] FLAPW-MOSCOW code [registration number 2015616990 (Russia) from 26 June 2015], A. V. Nikolaev, D. Lamoen, and B. Partoens, J. Chem. Phys. 145, 014101 (2016).
- [30] P. A. M. Dirac, Proc. Cambridge Philos. Soc. 26, 376 (2008);
 J. P. Perdew and Y. Wang, Phys. Rev. B 45, 13244 (1992).
- [31] B. A. Komissarova, G. K. Ryasny, A. A. Sorokin, L. G. Shpinkova, A. V. Tsvyashchenko, and L. N. Fomichova, Phys. Status Solidi B 213, 71 (1999).
- [32] P. Strange, A. Svane, W. M. Temmerman, Z. Szotek, and H. Winter, Nature (London) 399, 756 (1999).