## **Anisotropic anomalous Hall effect in triangular itinerant ferromagnet Fe3GeTe2**

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Magnetic frustrated materials are of great interest for their novel spin-dependent transport properties. We report an anisotropic anomalous Hall effect in the triangular itinerant ferromagnet  $Fe<sub>3</sub>GeTe<sub>2</sub>$ . When the current flows along the *ab* plane, Fe<sub>3</sub>GeTe<sub>2</sub> exhibits the conventional anomalous Hall effect below the Curie temperature *Tc*, which can be depicted by Karplus–Luttinger theory. On the other hand, the topological Hall effect shows up below *Tc* with current along the *c* axis. The enhancement of Hall resistivity can be attributed to the chiral effect during the spin-flop process.

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# **I. INTRODUCTION**

The anomalous Hall effect (AHE) is a common phenomenon in ferromagnetic (FM) materials. It is generally accepted that two terms contribute to the AHE: one is induced by the Lorentz force, and the other is caused by the spin-orbit interaction (SOI) [\[1\]](#page-5-0). Thus, the Hall resistivity  $\rho_{xy}$  can be described by an empirical formula [\[2\]](#page-5-0)

$$
\rho_{xy} = R_0 \mu_0 H + R_s M, \qquad (1)
$$

where  $R_0$  and  $R_s$  represent the ordinary and anomalous Hall coefficients, respectively. The AHE is not only observed in ferromagnets but can also appear in materials which show large localized magnetic moment, such as strongly paramagnetic (PM) or antiferromagnetic (AFM) metals [\[2\]](#page-5-0). Recently, attention has been paid to magnetic frustrated materials exhibiting the topological Hall effect (THE), such as  $PdCrO<sub>2</sub>$  and  $Fe<sub>1.3</sub>Sb$ with a triangular lattice  $[3,4]$ ,  $Pr_2Ir_2O_7$  and  $Nd_2Mo_2O_7$  with a pyrochlore lattice  $[5,6]$ , Mn<sub>3</sub>Sn and Mn<sub>3</sub>Ge with a Kagomé lattice [\[7–10\]](#page-5-0), and antiferromagnets with noncollinear spin structures  $[11-13]$ . In these materials, the anomalous Hall resistivity is not proportional to magnetization, which cannot be explained by conventional AHE mechanisms, including Karplus–Luttinger (K-L) theory [\[14\]](#page-5-0), skew scattering [\[15,16\]](#page-5-0), and side jump [\[17\]](#page-5-0). As a consequence, Berry-phase-related mechanisms are developed, which in turn are adopted to explain the THE in magnetic frustrated materials [\[18–23\]](#page-5-0).

The archetypal example of magnetic frustrated systems is AFM interacting spins in a triangular lattice. When two of the spins are pairwise anti-aligned, the remaining one cannot point in a direction that satisfies AFM interactions simultaneously with the former two spins, which gives rise to a large degeneracy of the system ground states [\[24,25\]](#page-5-0). Therefore, the spins in magnetic frustrated materials tend to form noncoplanar textures; namely, spin chirality, which endows the conduction electrons with a phase factor and acts as a fictitious magnetic field that leads to the THE [\[19–21,26\]](#page-5-0). However, because the fictitious magnetic field over the whole lattice sites generally balances out [\[27,28\]](#page-5-0), the THE is not a common feature among magnetic frustrated materials. Consequently, searching for materials exhibiting the THE will contribute to understanding and verifying the THE mechanisms.

 $Fe<sub>3</sub>GeTe<sub>2</sub>$  has a hexagonal crystal structure with a space group *P*63*/mmc* [\[29\]](#page-5-0), and is known as a quasi-twodimensional (quasi-2D) itinerant ferromagnet with a Curie temperature  $T_c$  ranging from 150 to 220 K that depends on the Fe concentration [\[30\]](#page-5-0). There are triangular lattices formed by iron atoms and are parallel to the *c* axis, indicating that frustrated structure exists in  $Fe<sub>3</sub>GeTe<sub>2</sub>$ . Large susceptibility anisotropy has been reported with the magnetic field along the *c* axis and the *ab* plane [\[31\]](#page-5-0), respectively. Moreover, recent magnetic measurements reveal a competing AFM state along the *c* axis [\[32\]](#page-5-0). As the temperature cools from 300 to 2 K, the ground states along the *c* axis vary successively from PM to AFM coexisting with FM, then to AFM. Whereas in the *ab* plane, the ground states vary from PM to FM [\[32\]](#page-5-0). All the results above remind us that  $Fe<sub>3</sub>GeTe<sub>2</sub>$  may be a good candidate to investigate the THE.

In this study, we grew  $Fe<sub>3</sub>GeTe<sub>2</sub>$  single crystals and performed transport measurements. Obvious magnetization and electronic transport anisotropy was observed. In particular, we found a THE in Fe<sub>3</sub>GeTe<sub>2</sub> with current along the *c* axis. The Hall resistivity shows strong enhancement at low field below the Curie temperature. This behavior sharply contrasts with the behavior expressed by aforementioned empirical formula, and can be explained by chiral effect in magnetic frustrated material.

### **II. EXPERIMENTAL DETAILS**

Single crystals of  $Fe<sub>3</sub>GeTe<sub>2</sub>$  were grown by the chemical vapor transport method, referring to procedures described in the literature [\[31\]](#page-5-0). To get large single crystals for transport measurements, the transport agent  $I_2$  is replaced by TeCl4. The structure was characterized by x-ray diffraction

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<span id="page-1-0"></span>(XRD) analysis with Cu  $K_{\alpha}$  radiation at room temperature by using a diffractometer (Rigaku-TTR3). Magnetic and electrical transport measurements were carried out by using a Quantum Design 7 T Magnetic Property Measurement System (SQUID-VSM3) and an Oxford Instrument TeslatronPT cryogenic system with the dc four-probe method, respectively. High-quality plate-like single crystals were used for these measurements to minimize the misalignment of samples. Both top and bottom surfaces of the samples are flat and parallel with each other. Before transport measurements, calibration of angle was performed to reach the best precision of experiments. All experiments were repeated to verify that the error from misalignment of sample mounting is negligible. For the measurement of magnetoresistance and Hall resistivity, single crystals were cut into rectangles with dimensions of  $2 \times 1.5 \times 0.15$  mm<sup>3</sup>. Details about transport measurements are given in Part I of the supplementary material [\[33\]](#page-5-0). To eliminate misalignment of electrodes, the resistivity and Hall resistivity were measured at both positive and negative fields.

## **III. RESULTS AND DISCUSSION**

The crystal structure of  $Fe<sub>3</sub>GeTe<sub>2</sub>$  is depicted in Figs. 1(a) and  $1(b)$ . Layered Fe<sub>3</sub>Ge substructures are sandwiched by two layers of Te atoms with a van der Waals bond between adjacent Te layers. Within the substructure, seven Fe atoms share one vertex, forming three regular triangles, which imply that the frustrated feature exists in this material. Figure  $1(c)$  shows the XRD pattern of a Fe<sub>3</sub>GeTe<sub>2</sub> single crystal. Only the (00*l*) Bragg peaks are observed, demonstrating that the exposed



FIG. 1. (a) Crystal structure of  $Fe<sub>3</sub>GeTe<sub>2</sub>$ . (b) Top view of  $Fe<sub>3</sub>GeTe<sub>2</sub>$ . (c) XRD pattern of  $Fe<sub>3</sub>GeTe<sub>2</sub>$  single crystal. The inset shows a photograph of  $Fe<sub>3</sub>GeTe<sub>2</sub>$  single crystals on a 1 mm grid.



FIG. 2. (a), (b) Temperature dependence of susceptibility *χ* (left ordinate) and  $1/(\chi - \chi_0)$  vs *T* behavior (right ordinate) with *H*  $\parallel$  *c* axis and  $H \parallel ab$  plane. The solid line indicates the fit with the modified Curie–Weiss law for temperatures ranging from 240 to 300 K. (c), (d) Field dependence of magnetization at indicated temperatures with  $H \parallel c$  axis and  $H \parallel ab$  plane.

surface is *ab* plane. The lattice parameter along the *c* axis is estimated to be  $16.376 \text{ Å}$  by using Bragg's law, which is consistent with reported values  $[29-31]$ . The inset of Fig.  $1(c)$ shows two pieces of  $Fe<sub>3</sub>GeTe<sub>2</sub>$  single crystals on a 1 mm grid. A typical crystal size is  $2 \times 2 \times 0.15$  mm<sup>3</sup> with a hexagonal plate-like shape.

To understand the magnetic properties of  $Fe<sub>3</sub>GeTe<sub>2</sub>$ , temperature dependence of susceptibility  $\chi$  is measured at 0.1 T and shown in Figs.  $2(a)$  and  $2(b)$ . Rapid upturns are observed at 201 K for the field along the *c* axis ( $H \parallel c$  axis) and 196 K for a field along the *ab* plane ( $H \parallel ab$  plane), which demonstrates magnetic transitions occur at these temperatures [\[31\]](#page-5-0). Below the transition temperature, the susceptibility  $\chi_c$  for *H*  $\parallel$  *c* axis is about ten times larger than  $\chi_{ab}$  for  $H \parallel ab$  plane, which is in accord with reported data and indicates the anisotropic magnetic property in Fe<sub>3</sub>GeTe<sub>2</sub> [\[31,32\]](#page-5-0). The  $1/(\chi - \chi_0)$  vs *T* curves above 240 K can be fit by a modified Curie–Weiss law,

$$
\chi(T) = \chi_0 + \frac{C}{T - \theta_p},\tag{2}
$$

where  $\chi_0$  is a *T*-independent contribution to  $\chi(T)$ , *C* is the Curie constant, and  $\theta_p$  is the Weiss temperature. The fits over the temperature ranging from 240 to 300 K using Eq. (2) are shown as solid blue curves in Figs.  $2(a)$  and  $2(b)$ . The parameters  $\chi_0$ , *C*, and  $\theta_p$  obtained from the fits are listed in Table [I.](#page-2-0) The effective moment derived from the fits is  $4.74\mu_B$ /Fe for *H*  $\parallel$  *c* axis and  $4.59\mu_B$ /Fe for *H*  $\parallel$  *ab* plane, which are consistent with literature values [\[31\]](#page-5-0) and close to the theoretical value of 4.90 $\mu_B$ /Fe for free Fe<sup>+2</sup> ions with spin *S* = 2. This result indicates that all Fe ions in  $Fe<sub>3</sub>GeTe<sub>2</sub>$  crystals

<span id="page-2-0"></span>TABLE I. FM ordering temperatures obtained from  $1/(\chi - \chi_0)$ vs *T* data and the parameters obtained from fits of the  $1/(\chi - \chi_0)$  vs  $T$  data for Fe<sub>3</sub>GeTe<sub>2</sub> single crystals by using Eq. [\(2\)](#page-1-0).

Field direction $(K)$	$T_c$	Fit $T$ range (K)	$\chi_0$	$\mathcal{C}$ (emu/mol) (emu $K/mol$ ) (K)	$\theta_n$
		<i>H</i> $ c \t201.1 \t240 \le T \le 300 - 4.25 \times 10^{-3}$ H    ab   196.1 240 $\leq T \leq 300 - 1.38 \times 10^{-2}$		8.412 7.914	208.4 204.3

are in the divalent state. The positive Weiss temperatures for both directions suggest FM correlations in this material.

Figures  $2(c)$  and  $2(d)$  show magnetization as a function of effective magnetic field  $\mu_0 H_{\text{eff}}$  at different temperatures with *H*  $\parallel$  *c* axis and *H*  $\parallel$  *ab* plane, respectively. Here,  $\mu_0 H_{\text{eff}} =$  $\mu_0(H - N_dM)$ , where  $N_d$  is the demagnetization factor. A method devoted to calculating  $N_d$  in rectangular ferromagnetic prism was used, with details given in Ref. [\[34\]](#page-5-0). Saturation behavior is observed for both directions. The saturation fields at 2 K are  $H_s^c = 0.4$  T for  $H \parallel c$  axis and  $H_s^{ab} = 3.5$  T for  $H \parallel ab$  plane, which indicates the easy magnetization direction is the *c* axis. Moreover, the saturation magnetic moments at 2 K is  $M_s^c = 4.1 \mu_B$ /formula for *H* || *c* axis, and  $M_s^{ab} = 3.8 \mu_B$ /formula for *H* || *ab* plane. Similar magnetic anisotropy has also been observed in both frustrated and nonfrustrated materials, such as  $Pr<sub>2</sub>Ir<sub>2</sub>O<sub>7</sub>$ , Mn<sub>3</sub>Sn, and DyScO<sub>3</sub>. However, the microscopic mechanisms of the magnetization and its anisotropy differ [\[5,8,35\]](#page-5-0). To solve the above problem, detailed studies on magnetic structures with  $H \parallel c$  axis and  $H \parallel ab$  plane are still needed. In addition, field dependence of magnetizations along different directions in *ab* plane were also measured. This is because, from the perspective of crystal structure, it is not identical along different directions in the *ab* plane. However, no in-plane magnetic anisotropy was observed (see Fig. S2 in the supplementary material [\[33\]](#page-5-0)). Consequently, the Hall resistivity anomaly discussed below with  $I \parallel c$  axis is not related to the in-plane magnetization behavior.

Figure  $3(a)$  exhibits the temperature dependence of the in-plane ( $\rho_{xx}$ ) and out-of-plane ( $\rho_{zz}$ ) resistivity. Both curves



FIG. 3. (a) Temperature dependence of in-plane and out-of-plane resistivity for single crystal  $Fe<sub>3</sub>GeTe<sub>2</sub>$ . The inset shows that the resistivity anisotropy ( $\rho_{zz}/\rho_{xx}$ ). (b), (c) Field dependence of in-plane and out-of-plane resistivities.



FIG. 4. (a) Field dependence of Hall resistivity with  $I \parallel ab$  plane at indicated temperatures. (b) Temperature dependence of  $R_0$  and *Rs*. Error bars indicate the standard error. (c) Hall conductivity plotted against the magnetization below  $T_c$ . (d) The  $\rho_{xy}/\mu_0H$  vs  $\rho_{xx}^2 M / \mu_0 H$  curves at indicated temperatures. The curves have been offset subsequently by  $1 \times 10^{-11}$  m<sup>3</sup>/C for clarity. Lines represent linear fits of data at different temperatures.

show metallic behavior with temperatures ranging from 2 to 300 K. For both directions, clear anomalies are found at ∼204 K, corresponding well with *T<sub>c</sub>* obtained from susceptibility measurements. The resistivity anisotropy  $\rho_{zz}/\rho_{xx}$  [inset in Fig.  $3(a)$ ] is as large as 15, indicating the system is quasi-2D. This conclusion is consistent with magnetic measurement results [\[31\]](#page-5-0). In addition, the ratio  $\rho_{zz}/\rho_{xx}$  is independent of temperature, which suggests that the in-plane and out-of-plane transports share the same scattering mechanism. Figures 3(b) and  $3(c)$  exhibit the field dependence of  $\rho_{xx}$  and  $\rho_{zz}$  with current perpendicular to magnetic field, at the same time, parallel to the *ab* plane (*I*  $\parallel$  *ab* plane) and *c* axis (*I*  $\parallel$  *c* axis), respectively. Negative magnetoresistance behavior is presented with  $I \parallel ab$  plane, indicating the spin-scattering is suppressed with increasing magnetic field. This phenomenon is common in ferromagnetic materials [\[36,37\]](#page-5-0). In addition,  $\rho_{xx}$  and  $\rho_{zz}$  are featureless and smaller than 1.5% at temperatures below *Tc*.

Figure  $4(a)$  represents the field dependence of Hall resistivity  $\rho_{xy}$  at different temperatures with *I* || *ab* plane. The  $\rho_{xy}$  vs *H* curves share similar shape features with *M* vs *H* curves in Fig.  $2(c)$ . At low temperature  $(2 K)$ , with increasing magnetic field,  $\rho_{xy}$  increases dramatically and saturates at 0.4 T, corresponding well with  $H_s^{ab}$  shown in Fig. [2\(c\).](#page-1-0) This result demonstrates that the magnetization dominates the AHE in Fe<sub>3</sub>GeTe<sub>2</sub> with *I* || *ab* plane. The ordinary Hall coefficient  $R_0$ and anomalous Hall coefficient *Rs* are separated by procedures described in Part III of the supplementary materials [\[33\]](#page-5-0). As shown in Fig.  $4(b)$ ,  $R_0$  is positive, indicating that the hole-type carrier is dominant in  $Fe<sub>3</sub>GeTe<sub>2</sub>$ . In addition, the value of  $R_0$  increases steadily as the temperature increases, which indicates that the carrier density is sensitive to temperature. In contrast,  $R_s$  reaches a maximum at about 110 K, a temperature <span id="page-3-0"></span>that deviates from Curie temperature. Similar temperature dependence of  $R_s$  is also observed in Ni and  $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ single crystals [\[38,39\]](#page-5-0), and  $Mn_5Si_3$  and  $Mn_5Ge_3$  films [\[12,40\]](#page-5-0). Generally speaking,  $R_s$  exhibits a broad peak at  $0.7T_c-0.8T_c$ , and then decreases to zero in the paramagnetic state [\[18,41,42\]](#page-5-0). Furthermore,  $R_s$  is about two orders of magnitude larger than  $R_0$ . All the results above demonstrate that the AHE in Fe<sub>3</sub>GeTe<sub>2</sub> with *I*  $\parallel$  *ab* plane is conventional.

In general, the AHE can be depicted by conventional mechanisms  $[14-17]$ . Figure [4\(c\)](#page-2-0) shows Hall conductivity  $\sigma_{xy}$ plotted against magnetization  $M$  below  $T_c$ . It is distinct that the  $\sigma_{xy}$  of Fe<sub>3</sub>GeTe<sub>2</sub> with *I* || *ab* plane is proportional to *M*. The relation is expected by K-L theory [\[14\]](#page-5-0) and has also been observed in La<sub>0.7</sub>Sr<sub>0.3</sub>MnO<sub>3</sub> [\[39\]](#page-5-0). What is more, the linear-*M* Hall conductivity is also recognized as an evidence of the dissipationless nature of anomalous Hall current [\[43\]](#page-5-0). We note that the experimental data deviate from a linear fit below 30 K. This phenomenon is related to characteristic change of  $\rho_{xx}$  vs *T* curve at low temperature, which probably is caused by the scattering of conduction electrons due to magnetic impurities.

In Eq. [\(1\)](#page-0-0), the anomalous Hall coefficient  $R_s$  is dependent on both magnetization *M* and resistivity  $\rho_{xx}$ , especially in materials exhibiting large magnetoresistance [\[44–48\]](#page-5-0). Consequently, the field dependence of resistivity should also be taken into consideration. Hence Eq. [\(1\)](#page-0-0) can be written as

$$
\rho_{xy} = R_0 \mu_0 H + S_H \rho_{xx}^2 M,\qquad (3)
$$

where  $S_H$  is a material-specific scale factor  $[44,47]$ . The linear-*M* Hall conductivity indicates that Hall effect in  $Fe<sub>3</sub>GeTe<sub>2</sub>$ with  $I \parallel ab$  plane is expected to be explained by K-L theory. Equation (3) can be used to check the above conclusion over the whole temperature-magnetic-field range below  $T_c$ . Here the  $\rho_{xy}/\mu_0 H$  vs  $\rho_{xx}^2 M/\mu_0 H$  curves are shown in Fig. [4\(d\),](#page-2-0) which is motivated by a modification of Eq.  $(3)$ : Dividing Eq. (3) by  $\mu_0H$  [\[47\]](#page-5-0). For clarity, the curves in Fig. [4\(d\)](#page-2-0) have been offset subsequently by  $1 \times 10^{-11}$  m<sup>3</sup>/C. The good linear fits of data at different temperature confirm the conclusion that the AHE in Fe<sub>3</sub>GeTe<sub>2</sub> with *I*  $\parallel$  *ab* plane is best described by K-L theory.

Figure  $5(a)$  shows the field dependence of the Hall resistivity  $\rho_{xz}$  at indicated temperatures with  $I \parallel c$  axis. When  $T > T_c$ , the magnitude of  $\rho_{xz}$  increases in proportion to *M*, which indicates the spin-orbit coupling induced AHE dominates the Hall resistivity. Below  $T_c$ ,  $\rho_{xz}$  increases linearly at low field, and then decreases gently and tends to saturate at high field, which shows striking contrast to *M* vs *H* curves along the *ab* plane [Fig.  $2(d)$ ].

Figure 5(b) exhibits a subset of field dependence of  $\rho_{xz}$  with  $I \parallel ab$  plane. The solid lines are the fitting curves using the relation  $\rho_{xz} = R_0 \mu_0 H + S_H \rho_{zz}^2 M$  with the fitting parameter  $R_0$  and  $S_H$  [\[45\]](#page-5-0). However, the estimates cannot explain the *ρxz* behavior at low field. Similar unconventional behavior has also been found in several magnetic frustrated materials [\[3,11\]](#page-5-0), in which the Hall resistivity anomalies are attributed to the chiral effect induced by noncoplanar spin textures  $[4,5]$ . If we label the chiral contribution as  $\rho_{xz}^T$ , the Hall resistivity  $\rho_{xz}$ for Fe<sub>3</sub>GeTe<sub>2</sub> with *I*  $\parallel$  *c* axis can be depicted by an equation



FIG. 5. (a) Field dependence of Hall resistivity with  $I \parallel ab$  plane at indicated temperatures. (b) Field dependence of Hall resistivity with  $I \parallel ab$  plane at indicated temperatures. For clarity, only a subset of data is shown. (c) Field dependence of the chiral effect to Hall resistivity  $\rho_{xz}$  at indicated temperatures. (d) The anisotropic field dependence of Hall resistivity  $\rho_{xy}$  and  $\rho_{xz}$  at 2 K with magnetic field along *c* axis and *ab* plane. (e), (f) Magnetic structure of the Fe sublattice during magnetization process with field along *ab* plane and *c* axis, respectively.

We note that the saturation behavior persists for a magnetic field up to 14 T (Fig. S4 in the supplementary material [\[33\]](#page-5-0)). Accordingly, it is reasonable to propose that the chiral effect disappears at high field. Then  $\rho_{xz}^T$  can be obtained by subtracting the ordinary and anomalous part from the total Hall resistivity  $\rho_{xz}$  and shown in Fig. 5(c). Below  $T_c$ ,  $\rho_{xz}^T$  shows a maximum at low field and decreases as the field increases. Figure  $5(d)$ shows the field dependence of Hall resistivity at 2 K with  $I \parallel$ *ab* plane and *I*  $\parallel$  *c* axis. Obvious anisotropy is observed, indicating the different AHE mechanisms for the two directions.

In theory, the chiral effect is usually derived from noncoplanar spin textures and acts as a fictitious magnetic field in real space [\[20,26\]](#page-5-0). However, due to the compensation of fictitious magnetic field, the THE has only been observed in several magnetic frustrated materials [\[27,28\]](#page-5-0). From the perspective of the  $Fe<sub>3</sub>GeTe<sub>2</sub>$  crystal structure, seven iron atoms share one vertex, forming three regular triangles that are parallel to *c* axis [Fig.  $1(a)$ ]. This peculiar structure prevents the compensation of the fictitious magnetic field, as discussed below.

Figure  $5(e)$  shows the spin structure during the magnetization process with *H*  $\parallel$  *ab* plane, and  $\alpha$  is defined as the angle between the fictitious magnetic field *b* and external magnetic

field  $H$ . Because the *ab* plane is a hard direction for  $Fe<sub>3</sub>GeTe<sub>2</sub>$ , the spins in iron atoms will flop from the easy axis (*c* axis) to the  $ab$  plane below  $T_c$ . During the spin-flop process, the spins are noncoplanar. As a result, the chiral effect appears and is represented as

$$
\chi_{i,j,k} = S_i \cdot (S_j \times S_k), \tag{5}
$$

where  $S_i$ ,  $S_j$ , and  $S_k$  are three noncoplanar spins in a triangular formed by iron atoms [\[11\]](#page-5-0). The chiral effect acts as a fictitious magnetic field  $\boldsymbol{b}$ , which has a component  $b \cos \alpha$ along direction of the external magnetic field. Consequently, a strong enhancement of  $\rho_{xz}$  is observed at low field. As the field increases further, the spins tend to align parallel because of the FM coupling along the *ab* plane, leading to the decrease of chiral effect and the fictitious magnetic field. As a result, *ρxz* decreases and tends to saturate at high field. Although there are no obvious anomalies in the  $\rho_{xz}$  vs *H* curves at high field (Fig. S4 in the supplementary material [\[33\]](#page-5-0)), we still note that a small tilting angle of spins can also lead to the fictitious magnetic field in several materials such as  $Nd<sub>2</sub>Mo<sub>2</sub>O<sub>7</sub>$ [\[6\]](#page-5-0). Hence further investigations about the in-plane magnetic structure with  $H \parallel ab$  plane are needed.

As the origin of the Hall resistivity anomaly at low field with  $I \parallel c$  axis, one may consider the possibility that  $R_s$  becomes field dependent. As shown in Fig. S5 of the supplementary material [\[33\]](#page-5-0) and Fig. [5\(b\),](#page-3-0) both the equation  $\rho_{xz} = R_0 \mu_0 H +$  $S_A \rho_{zz} M$  (skew scattering) and  $\rho_{xz} = R_0 \mu_0 H + S_H \rho_{zz}^2 M$  (K-L theory or side jump) cannot give a good fit to  $\rho_{xz}$  vs *H* curves. Therefore, the anomalous Hall coefficient  $R_s$  seems insensitive to the magnetic field, and another contribution is expected to give an enhancement to  $\rho_{xz}$ . Although the spin chirality mechanism can properly explain the unconventional behavior of Hall resistivity with  $H \parallel ab$  plane, other possibilities should also be taken into consideration because of the uncertainty of the magnetic structure at low field and the absence of theoretical calculation. For example, the skyrmion state or DM interaction may influence the Hall resistivity [\[4,46,49\]](#page-5-0). For the present material  $Fe<sub>3</sub>GeTe<sub>2</sub>$ , further investigations are still expected. In addition, the competition [\[32\]](#page-5-0) of AFM and FM in this material has no reflection in the  $\rho_{xz}$  vs *H* curves. This is probably because, when the magnetic field is applied along *ab* plane, the spins in each single layer will flop from the easy axis (*c* axis) to the *ab* plane and give rise to a fictitious magnetic field *b* regardless the AFM or FM order.

Figure [5\(f\)](#page-3-0) shows the magnetic structure of iron lattice during magnetization process with  $H \parallel c$  axis. Because the *c* axis is an easy axis of Fe<sub>3</sub>GeTe<sub>2</sub>, the spins are collinear and parallel with each other. Hence the chiral effect quenches, and only the conventional AHE appears.

According to reported data [\[31,32\]](#page-5-0) and the present work, magnetic phase diagrams with  $H \parallel c$  axis and  $H \parallel ab$  plane were made and are shown in Fig. 6. For both directions with  $T > T_c$ , Fe<sub>3</sub>GeTe<sub>2</sub> shows paramagnetic behavior and ordinary Hall effect in this temperature range. When  $T < T_c$ , the spins tend to arrange along the easy axis (*c* axis). Similar to a traditional ferromagnet,  $Fe<sub>3</sub>GeTe<sub>2</sub>$  shows the anomalous Hall effect with *H*  $\parallel$  *c* axis, as presented in Fig. 6(a). While for  $H \parallel ab$  plane, as shown in Fig. 6(b), the triangular lattice formed by iron atoms is crossed by the magnetic field and the spins will flop from easy axis to the hard axis (*ab* plane). In the



FIG. 6. Magnetic phase diagrams with (a)  $H \parallel c$  axis and (b)  $H \parallel ab$  plane. The circles denote the saturation fields  $H_s$  in *M* vs *H* curves.

low-field region, the spins are noncoplanar during the spin-flop process. In this area, the THE shows up. As the field increases, the spins tend to become parallel, leading to the suppression of the THE.

According to Ref. [\[32\]](#page-5-0), an AFM ground state was observed with magnetic moments parallel to the *c* axis at low ac magnetic field (3.9 Oe). However, the magnetic structure remains unknown with a large applied field along the *c* axis. Furthermore, the field dependence of *M* and  $\rho_{xy}$  show similar behavior as a ferromagnet. Consequently, we tend to define the magnetic phase to be FM with *H*  $\parallel$  *c* axis below  $T_c = 201.1$  K. More detailed investigations about magnetic structures with the field along the *c* axis and the *ab* plane are necessary.

### **IV. CONCLUSIONS**

In summary, we prepared and investigated the transport properties of  $Fe<sub>3</sub>GeTe<sub>2</sub>$  single crystals. Magnetization and resistivity measurements reveal an obvious anisotropy in this material. The conventional AHE shows up with  $I \parallel ab$ plane. The Hall conductivity  $\sigma_{xy}$  is proportional to *M*, which conforms with the behavior expressed by K-L theory. On the other hand, an obvious enhancement of Hall resistivity shows up at low field with  $I \parallel c$  axis and is likely explained by the chiral effect originating from the noncoplanar spin textures during the spin-flop process. For this reason,  $Fe<sub>3</sub>GeTe<sub>2</sub>$  is expected to serve as an archetypal material to study the THE mechanism. Moreover, theoretical calculation and detailed experimental studies on magnetic structures below  $T_c$  with

<span id="page-5-0"></span>field along *c* axis and *ab* plane are desired to deepen our understanding of the origin of the anisotropic AHE.

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