# Spin dynamics of the magnetocaloric compound MnFe<sub>4</sub>Si<sub>3</sub>

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The magnetic excitation spectrum of the magnetocaloric compound  $MnFe_4Si_3$  has been investigated by means of polarized and unpolarized inelastic neutron scattering on single crystals. Spectra were collected in the ferromagnetic phase ( $T_C \approx 305$  K), as well as in the paramagnetic state, in order to understand the nature of the magnetism in  $MnFe_4Si_3$ . Spin-wave measurements at 1.5 K reveal a strong anisotropy of the magnetic exchange interactions along the (h00) and (001) reciprocal directions of the hexagonal system, which also manifests itself in the q-dependent linewidths in the paramagnetic state. The correlation lengths indicate a short-range order, while the average linewidth is of the order of  $k_BT_C$  pointing to a behavior typical of many ferromagnets. In addition, the in- and out-of-plane spin fluctuations are found to be isotropic around  $T_C$  and can be suppressed by a magnetic field of 2 T.

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### I. INTRODUCTION

One possibility for an environmentally friendly and more efficient use of energy in daily life is the use of magnetic refrigeration technologies, which are based on the magnetocaloric effect (MCE) [1]. MCE is the reversible temperature change of a magnetic material upon the isothermal application of a magnetic field and its adiabatic removal [2]. Since the early demonstration of magnetocaloric (MC) cooling near room temperature in the ferromagnetic (FM) material gadolinium [3] and the more recent discovery of giant MCE in Gd<sub>5</sub>Si<sub>2</sub>Ge<sub>2</sub> [4], the research publications on MC cooling have increased greatly. Nowadays, a significant number of materials with magnetic phase transition near room temperature have been proposed for applications [5,6]. Such materials should combine a high adiabatic temperature change  $(\Delta T_{ad})$  with a large isothermal entropy change ( $\Delta S_{iso}$ ). In addition, a good candidate material should consist of environmentally friendly, abundant, low-cost, and nontoxic elements.

Among the suggested MC compounds for applications, the  $Mn_{5-x}Fe_xSi_3$  ( $0 \le x \le 5$ )-based systems exhibit moderate MCE at low magnetic fields and at different temperatures depending on x [7]. Early studies reported that they crystallize in a hexagonal structure with the space group  $P6_3/mcm$ , with two distinguished crystallographic sites-Wyckoff positions (WP) 6g and 4d—occupied by Mn and Fe in different ratios depending on composition [8]. From this series, MnFe<sub>4</sub>Si<sub>3</sub> is a promising candidate material since a transformation from the paramagnetic (PM) state to the FM phase occurs at the Curie temperature  $(T_C) \approx 300 \text{ K}$  [9–11] with  $\Delta S_{\text{iso}} \approx 2 \text{ JK}^{-1} \text{kg}^{-1}$ for a field change from 0 to 2 T [7,9]. The order of the FM transition seems not to be fully established. Hysteresis loops point to a first-order FM transition [9]. Recent measurements of hyperfine fields with Mössbauer spectroscopy propose that the type of the magnetic transition cannot be strictly characterized as first or second order [12]. In this framework, it is worthwhile to note that, in Fe<sub>2</sub>P-based MC materials, the order of the FM transition changes from first to second order depending on composition [13].

According to recent x-ray and neutron diffraction experiments performed on single crystals of MnFe<sub>4</sub>Si<sub>3</sub>, a partial ordering of Mn and Fe atoms was observed on the sites of mixed occupancy, which leads to reduction of symmetry from space group  $P6_3/mcm$  to  $P\overline{6}$  [9]. For the present experimental study, the higher symmetric  $P6_3/mcm$  structure [8] proved to be a sufficient approximation. In this structure (see Fig. 1), the WP 4d is occupied by Fe atoms surrounded by six Si atoms at a distance  $\approx 2.4$  Å in the form of a distorted octahedra [FeSi<sub>6</sub>]. The WP 6g has a mixed occupancy of Fe-Mn (Fe occupancy  $\approx$ 67%, Mn occupancy  $\approx$ 33%) and forms triangular units in the *ab* plane (interatomic distance  $\approx 2.775$  Å). The triangular units are stacked along the c direction, forming empty distorted [MnFe]<sub>6</sub> octahedra. The magnetic moments on the WP 6g lie in the basal plane of the hexagonal system with a magnitude of 1.5(2)  $\mu_B$ , while no significant magnetic moment could be determined on WP 4d [9]. The direction of the magnetic moments is consistent with magnetization measurements performed on single crystals, where a strong anisotropy is found with the easy axis of magnetization lying perpendicular to the c axis [9].

MCE potentially occurs in any magnetic ordering process. Although different scenarios are well-known for specific systems, no microscopic mechanism based on key ingredients such as coupling of spin, lattice, and electronic degrees of freedom has been experimentally proven. Inelastic Neutron Scattering (INS) measurements, which microscopically probe the magnetization dynamics, can tackle this question and shed light onto the fundamental mechanism of MCE. To this aim, the spin dynamics of the MC compound  $MnFe_4Si_3$  have been investigated above and below  $T_C$  as a function of the wave



FIG. 1. Projection on the hexagonal plane of the crystal structure of MnFe<sub>4</sub>Si<sub>3</sub> in  $P6_3/mcm$  space group. Sites occupied by Mn and Fe (WP 6g, large magenta) carry magnetic moments 1.5  $\mu_B$  parallel to b axis; sites occupied by Fe (WP 4d, large yellow) and Si atoms (small blue) carry no magnetic moments. Yellow lines ( $J_0$ ) connect atoms in the same plane, red lines ( $J_1$ ), black lines, ( $J_2$ ), and green lines ( $J_3$ ) in different planes.

vector  $\mathbf{Q}$  and the energy E. This compound is a suitable candidate for detailed INS experiments, since large single crystals can be grown [9].

## **II. EXPERIMENTAL DETAILS**

The single crystal of MnFe<sub>4</sub>Si<sub>3</sub> was grown by the Czochralski method [9] and two samples of this batch with a mass of about 7 g each were mounted on an aluminium sample holder and oriented in the (a\*,c) and (a\*,b\*) scattering plane of the hexagonal lattice, respectively. The linewidths of the Rocking curve of each sample consist of a single Gaussian peak and is of about 0.3 degrees as measured by neutron scattering.

INS measurements were carried out on the cold and thermal triple-axis spectrometers (TAS) IN12 [14] and IN22 at the Institut Laue Langevin, as well as on MIRA [15] and PUMA [16] at the Heinz Maier-Leibnitz Zentrum. The spectrometers used for INS studies were set up in W configuration with a fixed final energy and a fully focusing setup. MIRA was used in elastic TAS mode with 60' secondary collimation. The corresponding integration in energy covers the range from -0.1 to 0.1 meV. Additional information regarding each configuration is given in Table I.

For unpolarized INS measurements below  $T_C$ , the sample was cooled down to the base temperature  $T \approx 1.5$  K with an orange or closed-cycle cryostat (configurations A and B in Table I) while, for measurements above  $T_C$ , a cryofurnace was used to cover the temperature region of  $80 \le T \le 500$  K (configuration C in Table I). Elastic measurements on MIRA were performed using a 2.2 T vertical field magnet with the field applied in the plane (configuration F).

For INS measurements with polarized neutrons, the incident neutron beam spin state was prepared for IN12 with a transmission polarizing cavity [14] located after the velocity selector and for IN22 with a Heusler monochromator. All along

TABLE I. Instrument configurations. "PG(002)" and "Heusler" refer to pyrolytic graphite and  $Cu_2MnAl(111)$ , respectively. Higher order contamination was removed using a PG filter in the scattered neutron beam on IN22 and PUMA. On IN12 and MIRA a velocity selector (VS) was employed before and a cooled Be filter after the monochromator, respectively. The symbol " \* " refers to polarized setups.

| Config. | TAS   | Monoch. | Anal.   | $k_f (\text{\AA}^{-1})$ | Filter |  |
|---------|-------|---------|---------|-------------------------|--------|--|
| A       | IN12  | PG(002) | PG(002) | 2                       | VS     |  |
| В       | PUMA  | PG(002) | PG(002) | 1.971                   | PG     |  |
| С       | IN12  | PG(002) | PG(002) | 1.3                     | VS     |  |
| D       | IN12* | PG(002) | Heusler | 2                       | VS     |  |
| Е       | IN22* | Heusler | Heusler | 2.662                   | PG     |  |
| F       | MIRA  | PG(002) | PG(002) | 1.4                     | Be     |  |

the neutron path, guide fields were installed to maintain the polarization of the beam. In order to investigate the spin-wave scattering, the sample was placed in a 2.5 T vertical field magnet. The single crystal was first heated up above  $T_C$  to 316 K and then cooled down to 1.5 K under a vertical magnetic field of  $H_z = 1$  T applied parallel to the *b* axis of the hexagonal system of the sample, corresponding to an axis within the easy plane of magnetization [9]. This results in a single domain state of the sample. The scattered beam was analyzed by a combination of a Mezei spin flipper and a horizontally focusing Heusler analyzer set at fixed  $k_f$  (configurations D and E in Table I). The PM scattering was also investigated in detail at T = 316 K using the spherical polarization analysis setup CRYOPAD and configuration E. For all measurements with polarized neutron beam (configurations D and E), a flipping ratio of about 14 has been measured on a graphite sample.

#### **III. SPIN-WAVE SCATTERING**

Magnetic excitations were measured around the zone centers  $\tau = (2, 0, 0)$ ,  $\tau = (0, 2, 0)$ , and  $\tau = (0, 0, 2)$  with configuration A and B [17]. There, the calculated magnetic form factors for Fe and Mn are expected to have significant magnitude. To extract acoustic magnon branches, constant energy and constant **Q** scans were carried out at energy transfers below 20 meV at T = 1.5 K along the high symmetry reciprocal directions (h00), (hh0), and (001) of the hexagonal system. Specific scans were repeated above  $T_C$ , e.g., at T = 313 K, in order to establish the magnetic nature of the excitations. Typical representatives of such measurements are shown in Fig. 2 at **Q** = (2.3, 0, 0), where the peak observed at T = 1.5 K is replaced by a broad quasielastic signal above the ordering temperature at T = 313 K.

Further experiments with polarized neutrons were performed along the (h00) and (001) directions at 1.5 K using instrument configurations D and E. Figure 3 shows a characteristic constant energy scan performed for an energy transfer of 5 meV where the peak observed in the spin flip (SF<sub>zz</sub>) channel vanishes in the non-spin flip (NSF<sub>zz</sub>) channel (see Appendix A). Measurements with polarized neutrons are crucial in such a ferromagnet as acoustic phonon, and magnon modes originate from the same Brillouin zone center.



FIG. 2. Energy spectra at  $\mathbf{Q} = (2.3, 0, 0)$  measured at IN12 spectrometer with unpolarized setup at 313 K (squares) and 1.5 K (circles). Neutron intensity for data at 1.5 K and 313 K is given on the left and right vertical axis, respectively. The solid line corresponds to a Gaussian function fit and the dashed line is a guide for the eyes.

Moreover, all spectra were examined carefully for spurious scattering, especially aluminium and copper contamination, and the corresponding regions were masked during the data evaluation. Magnetic excitations, both for the constant Q (Fig. 2) and constant E (Fig. 3) scans, were fitted with Gaussian functions.

The obtained magnon dispersion along the main three symmetry directions [(h00), (001), and (hh0)] is shown in Fig. 4. While the magnon branches are found to be rather isotropic in the two basal plane directions, (h00) and (hh0), a much steeper dispersion develops along (001). The experimental spin-wave spectrum at low energies ( $E \le 5 \text{ meV}$ ) can be described by a quadratic dispersion,  $E = \Delta + D_{(hkl)}q^2$ , where  $\Delta$  is the energy gap,  $D_{(hkl)}$  is the spin-wave stiffness, and q is the momentum transfer. The obtained values are  $\Delta = 0.71(25) \text{ meV}$ ,  $D_{(h00)} \simeq D_{(hh0)} = 43(7) \text{ meV}Å^2$ , and  $D_{(00l)} = 310(30) \text{ meV}Å^2$  for the in- and out-of-plane magnon



FIG. 3. Polarized inelastic neutron scattering spectra obtained at IN12 around  $\mathbf{Q} = (2, 0, Q_l)$  at constant energy transfer of 5 meV at T = 1.5 K from spin flip and non-spin flip channel. The solid line represents a fit with a Gaussian function.



FIG. 4. Magnon dispersion at T = 1.5 K along (001), (h00), and (hh0) directions from polarized (circles) and unpolarized (triangles) INS measurements. The color-coded intensity corresponds to spin-wave simulation as described in the text.

branch, respectively. However, the obtained value for the spin gap is within the instrument resolution, which is approximately 0.5 meV for configuration A.

To describe the spin-wave spectrum, and to extract the relevant exchange interactions of this compound, the SpinWave software package was used [18]. Since our experimental data revealed only the lower energy acoustic magnon dispersion for each direction, a simplified spin model was employed. Given the experimental uncertainty on the magnetic moment on the 4d site [9], we considered one type of magnetic atoms carrying a spin S on the 6g sites of mixed occupancy. As no significant differences are observed between the dispersion measured along the (h00) and (001) directions at zero field and for H = 1 T applied along the b axis, we assume for simplicity that the magnetic moments are lying along the baxis. Furthermore, the Zeeman effect is negligible, being of the order of 0.09 meV for a magnetic moment of 1.5  $\mu_B$  under a magnetic field of 1 T. The spin model is described by a Heisenberg-type Hamiltonian,  $H_H = \sum_{i,j} J_{ij} S_i S_j$ , where  $J_{ij}$ denotes the exchange couplings between sites i and j.

The exchange interactions between the nearest neighboring magnetic atoms located at WP 6g are shown in Fig. 1 and are described in Table II. First, the coupling between magnetic atoms in the same distorted [MnFe]<sub>6</sub> octahedra are considered. This concerns  $2SJ_0$ , the exchange between the spins located on a triangle (distance 2.775 Å),  $2SJ_2$  and  $2SJ_3$  that couples two spin located on adjacent triangles separated by c/2 with distances 2.885 and 3.981 Å, respectively. Second, the exchange  $2SJ_1$  concerns the shortest distance (4.304 Å) between spins located on adjacent distorted [MnFe]<sub>6</sub> octahedra. The

TABLE II. Exchange constant values, number of neighbors between magnetic sites  $(z_n)$ , in-plane (IPP), and out-of-plane projections (OPP) of the vector linking the magnetic sites and distances between magnetic atoms (see Fig. 1). The symbol "—" means that the exchange interactions cannot be determined in the present work.

| Exchange           | Value<br>(meV) | Zn | IPP   | OPP | Distance<br>(Å) |
|--------------------|----------------|----|-------|-----|-----------------|
| $\overline{2SJ_0}$ | _              | 2  | 0.409 | 0   | 2.775           |
| $2SJ_1$            | -4             | 2  | 0.528 | 0.5 | 4.304           |
| $2SJ_2$            | -18            | 4  | 0.236 | 0.5 | 2.855           |
| $2SJ_3$            | _              | 2  | 0.472 | 0.5 | 3.981           |

experimental fact that the magnon dispersion is much steeper along the (001) direction than in the basal plane, imposes that the exchange interaction with the highest ratio of out-of-plane to in-plane component,  $2SJ_2$ , is the dominant one. The second most important interaction concerning acoustic spin waves is the one that connects the different octahedra,  $2SJ_1$ , which is mandatory to create the in-plane dispersion. The calculated dispersion using only the  $2SJ_1$  and  $2SJ_2$  interactions with the values indicated in Table II is shown in Fig. 4. This simplified model describes well the experimental dispersion; including further interactions is not relevant, given the present set of data. In this respect, it should be pointed out that  $2SJ_0$  does not participate in the out-of-plane dispersion by nature. Our simulations show further that it does not contribute to the in-plane acoustic modes but only to the optic modes. Since these modes were not experimentally observed in the present study,  $2SJ_0$  cannot be determined. In addition, it is found that the effect of  $2SJ_3$  is redundant with the one of  $2SJ_1$  and  $2SJ_2$ and cannot be disentangled.

#### IV. PARAMAGNETIC SCATTERING

The spin dynamics of the MC compound MnFe<sub>4</sub>Si<sub>3</sub> in the PM state was investigated with INS measurements, which were carried out with the scattering vectors along the (h00) and (001) directions. For determining the extent of the spin fluctuations in the PM region, spectra have been collected with an unpolarized neutron beam at small q, using instrument configuration C. The measured intensity was corrected by the Bose factor and a constant background was subtracted so that the obtained results correspond to the imaginary part of the dynamical spin susceptibility  $\chi''(\mathbf{Q},\omega)$ . A typical temperature dependence for  $\mathbf{Q} = (0.25, 0, 0)$  for an energy transfer of E = 0.3 meV is shown in Fig. 5. The spin fluctuations show their maximum at  $T_C$  and extend for temperatures higher than  $1.5T_C$ . The inset in Fig. 5 shows the temperature dependence of the beam polarization P. Measurements were performed with the use of



FIG. 5. Temperature dependence of dynamical spin susceptibility  $\chi''(\mathbf{Q},\omega)$  at  $\mathbf{Q} = (0.25, 0, 0)$  and E = 0.3 meV measured with unpolarized neutrons at IN12. The dashed vertical line and the red arrow indicate  $T_C \approx 305$  K and  $1.036T_C \approx 316$  K, respectively. The inset shows the temperature dependence of the beam polarization at  $\mathbf{Q} = (0, 0, 2)$  Bragg peak.



FIG. 6. Evolution of elastic scattering at Q =  $0.05 \text{ Å}^{-1}$  measured at MIRA as a function of magnetic field at three temperatures. Lines can be used as guides for the eyes. The inset shows a calculation of the field dependence of  $\chi_q(H,T_C)$  following Ref. [19].

CRYOPAD and configuration E in non-spin flip NSF<sub>xx</sub> and spin flip channel SF<sub>xx</sub> at the  $\mathbf{Q} = (0, 0, 2)$  Bragg peak. The calculated beam polarization was obtained by:

$$P = \frac{\text{NSF}_{xx} - \text{SF}_{xx}}{\text{NSF}_{xx} + \text{SF}_{xx}}.$$
 (1)

It is clearly seen that a considerable beam depolarization occurs for  $T \leq T_C$  due to the magnetic domain structure, indicating the transition from the PM state to the FM phase at  $T_C = 305$  K.

Figure 6 shows the evolution of elastic scattering measured with configuration F as a function of magnetic field at three temperatures: close to  $T_C$ , above  $T_C$ , and below  $T_C$  at the lowest accessible Q range. In this very low Q range, the contribution to the intensity in the obtained spectra is attributed mainly to magnetic scattering. Consistently with Fig. 5, the magnetic scattering is significantly reduced at 110 and 480 K compared to 300 K. Around the critical temperature, a field of 2 T is sufficient to suppress the magnetic fluctuations. The spectra at 300 K for ramping the magnetic field in a positive or negative direction are offset by the coercive field ( $\approx 0.03$  T). To get a qualitative description of the suppression of the magnetic fluctuations, the model of Ref. [19] was used and the calculated *q*-dependent susceptibility at  $T_C$  as a function of field is shown in the inset in Fig. 6 (see Discussion).

To get insight into the spin dynamics near room temperature and above  $T_c$ , the PM scattering was studied at T = 316 K corresponding to  $1.036 \times T_c$  along the (h00) and (001) directions with constant **Q** scans using instrument configuration E. Spectra were collected in two non-spin flip channels NSF<sub>yy</sub> and NSF<sub>xx</sub> around the  $\tau = (2, 0, 0)$  and  $\tau = (0, 0, 2)$  zone centers. The magnetic fluctuations were extracted by taking the difference of intensity of the two non-spin flip channels taking into account higher order corrections of the monitor counts of each polarization channel. This gives access to the spin fluctuations along the *c* axis,  $\langle \delta M_c \rangle$  (see Appendix A). A typical measurement is depicted in Fig. 7, where energy scans at **Q** = (2.2, 0, 0) and **Q** = (2.3, 0, 0) are shown. As expected, the intensity decreases when *q* increases. The obtained spectra were convoluted with the 1D-instrument resolution and values



FIG. 7. Spin fluctuations  $\langle \delta M_c \rangle$  obtained at IN22 and measured at **Q** = (2.2, 0, 0) (black circles) and **Q** = (2.3, 0, 0) (red squares) at 1.036*T<sub>c</sub>*. Solid lines represent fits as explained in the text.

for the *q*-dependent susceptibility  $\chi_q$  and linewidth  $\Gamma_q$  were extracted as described in Appendix B.

The obtained values for  $\chi_q$  and  $\Gamma_q$  for (001) and (h00) directions at 316 K are shown in Fig. 8.  $\chi_q$  decreases faster along the (001) direction compared to (h00), indicating a shorter inverse correlation length. A Lorentzian fit for the *q*-dependent susceptibility  $\chi_q$  gives values for the inverse correlation lengths  $\kappa_q$ :  $\kappa_{(00l)} = 0.054(3) \text{ Å}^{-1}$  and  $\kappa_{(h00)} = 0.14(1) \text{ Å}^{-1}$ . The energy range of the spin fluctuations is of the same order of magnitude as the one of the spin waves along these high symmetry directions. For q = 0 the linewidth extrapolates to zero. To describe the experimental data for  $\Gamma_q$  at  $1.036T_c$ , two different



FIG. 8. *q*-dependent susceptibility  $\chi_q$  (top) and linewidth  $\Gamma_q$  (bottom) in the (001) and (h00) directions at 316 K. The solid black lines for  $\chi_q$  correspond to Lorentzian fits as described in the text. The solid black and dashed red line for  $\Gamma_q$  correspond to the localized and weak itinerant model of ferromagnetism, respectively.



FIG. 9. Subtracted spin fluctuations spectra from constant energy scans at 1.5 meV at 316 K along (h00) (top) and (001) (bottom) directions obtained at IN22. The indices *i* in  $\langle \delta M_i \rangle$  indicates the direction of fluctuations (*a*<sup>\*</sup>, *b*, and *c*). Solid lines correspond to fits with Lorentzian functions.

models were used. For localized Heisenberg ferromagnets, the linewidth of the magnetic fluctuations can be expressed as  $\Gamma_q = A_{\rm loc}q^{2.5}$  [20]. On the other hand, for the weak itinerant model the expression is  $\Gamma_q = A_{\rm wi}q[1 + (q/\kappa)^2]$ , where  $\kappa$  refers to the inverse correlation length [20]. The obtained values for the (001) direction are  $A_{\rm loc} = 183(6) \,\mathrm{meV} \text{\AA}^{2.5}$ ,  $A_{\rm wi} = 1.3(5) \,\mathrm{meV} \text{\AA}$ , and  $\kappa_{(00l)} = 0.054(12) \,\text{\AA}^{-1}$ ; for the (h00) direction  $A_{\rm loc} = 35.2(8) \,\mathrm{meV} \text{\AA}^{2.5}$ ,  $A_{\rm wi} = 0.93(25) \,\mathrm{meV} \text{\AA}$ , and  $\kappa_{(h00)} = 0.14(2) \,\text{\AA}^{-1}$ .

Constant energy scans were performed for an energy transfer of 1.5 meV along the directions (h00) and (001) at 316 K in three non-spin flip channels NSF<sub>xx</sub>, NSF<sub>yy</sub>, and NSF<sub>zz</sub> around the  $\tau = (2, 0, 0)$  and  $\tau = (0, 0, 2)$  zone centers. The in-plane and out-of-plane components of the magnetic fluctuations were separately obtained using canonical subtraction of intensities measured in the different polarization channels (see Appendix A). They are shown in Fig. 9. As can be seen, the in-plane  $\langle \delta M_b \rangle$  and the out-of plane fluctuations  $\langle \delta M_c \rangle$  are found to be isotropic (Fig. 9, top). The different in-plane components,  $\langle \delta M_{a^*} \rangle$  and  $\langle \delta M_b \rangle$ , are also isotropic (Fig. 9, bottom). For this energy of 1.5 meV, the spectra show a maximum at a specific wave-vector  $\mathbf{q} = (0.23, 0, 0)$  along (h00) and  $\mathbf{q} = (0, 0, 0.08)$  along (001)

direction, respectively. This mimics the spin-wave dispersion. However, the PM scattering is quasielastic, as can be seen in Fig. 7, since there is no well-defined inelastic mode associated with a given wave vector. Such "ridge" structure in (**Q**, *E*) space, i.e., maxima in constant-*E* spectra at finite *q* away from the  $\Gamma$ -point and maxima in constant-**Q** spectra for *E* = 0, is typical of PM scattering [20,21]. One can also see that the peak widths are very anisotropic between the basal plane, where a broad peak spans the whole Brillouin zone (Fig. 9, top) and perpendicular to the *c* axis, where a narrow peak shape is found (Fig. 9, bottom). The spectra measured at a constant energy of 1.5 meV were fitted by Lorentzian line shapes. The obtained effective inverse correlation lengths are  $\kappa_{(h00)}^* = 0.139(2) \text{ Å}^{-1}$  and  $\kappa_{(001)}^* = 0.0825(4) \text{ Å}^{-1}$ . They compare well with the correlation lengths obtained through the *q* dependence of the energy-integrated PM scattering (see above and Fig. 8).

#### V. DISCUSSION

Polarized and unpolarized INS measurements performed on single crystals of the MC compound MnFe<sub>4</sub>Si<sub>3</sub> reveal a strong anisotropy in the exchange interactions between the (h00) and (001) directions of the hexagonal system, while the magnetic fluctuations (dynamical susceptibilities) in the PM state at  $T = 1.036T_C = 316$  K are found to be isotropic. This anisotropy is reflected in the magnon spectrum as well as in the q-dependent linewidths  $\Gamma_q$  (see Figs. 4 and 8). The ratio of the spin-wave stiffness D and the constant  $A_{loc}$  for the two directions is about of the same magnitude  $(D_{(00l)}/D_{(h00)}) =$ 7.2(1.4) and  $(A_{loc}^{(00l)}/A_{loc}^{(h00)}) = 5.2(2)$ . The obtained data at 1.5 K indicate that the magnetic exchange interactions within the basal plane between the (h00) and (hh0) directions are isotropic. The experimental data collected at 1.5 K could be well described by a Heisenberg-type Hamiltonian. In the used effective spin-wave model, this translates into two FM exchange parameters with values  $2SJ_2 = -18$  meV and  $2SJ_1$ = -4 meV.

Strong anisotropy in the magnetic exchange interactions between the (h00) and (001) directions has been reported for other FM compounds with hexagonal structure and lattice parameters comparable to MnFe<sub>4</sub>Si<sub>3</sub>, e.g., MnBi [22], MnSb [23,24], MnP [25,26] and Fe<sub>2</sub>P [27]. Selected microscopic properties for representative hexagonal FM compounds are given in Table III. A striking feature is the large value of  $D_{(00l)}$  and the related strong anisotropy for MnFe<sub>4</sub>Si<sub>3</sub>. For the isostructural MnT ferromagnets (T = Bi, Sb, P) decreasing the size of the T-ion leads to a decrease of interatomic Mn-Mn distance resulting in lower magnetic moments and Curie temperatures. This behavior might be attributed to a systematic shift from dominant itinerant to short-range exchange interactions with decreasing size of the T-ion [22]. In MnFe<sub>4</sub>Si<sub>3</sub>, the magnetic atoms that carry moments in WP 6g, which has a mixed occupancy of Mn and Fe, have an interatomic shortest nearest neighbors distance of  $\approx 2.775$  Å comparable to MnP. This could hint to short range exchange magnetic interactions in MnFe<sub>4</sub>Si<sub>3</sub>.

Further insight can be gained from the calculation of the correlation lengths. The order of the FM transition is not clarified and since, experimentally, no discontinuity of the temperature dependence of magnetization was reported [9,12] and strong critical fluctuations are observed (Fig. 5), the inverse of the spin correlation length  $\kappa$  can be assumed to follow a critical law:

$$\kappa = \kappa_0 \left(\frac{|T - T_C|}{T_C}\right)^{\nu}.$$
 (2)

In this formula,  $\kappa_0$  refers to the inverse spin correlation length at 0 K and the exponent  $\nu$  equals 0.5 and 0.7 for a Heisenberg model within the mean-field approximation and for critical scattering, respectively. The calculated values  $\kappa_0$  for  $\nu = 0.5$  result to:  $\kappa_0^{(h00)} = 0.74(5) \text{ Å}^{-1}$  and  $\kappa_0^{(00l)} =$  $0.284(16) \text{ Å}^{-1}$  and for  $\nu = 0.7$  to:  $\kappa_0^{(h00)} = 1.4(1) \text{ Å}^{-1}$  and  $\kappa_0^{(00l)} = 0.55(3) \text{ Å}^{-1}$ . One alternative model for calculating the inverse spin correlation lengths  $\kappa_0$  by taking into account the spin-wave stiffness and the transition temperature is the following [21]:

$$\kappa_0 = \left(\frac{3k_B T_C}{(S+1)D}\right)^{0.5},\tag{3}$$

which gives  $\kappa_0^{(h00)} = 0.96(8) \text{ Å}^{-1}$  and  $\kappa_0^{(00l)} = 0.357(17) \text{ Å}^{-1}$ . These values are of the same order of magnitude as the ones obtained by Eq. (2). It is clearly seen that the corresponding correlation lengths  $\xi_0 = \kappa_0^{-1}$  are smaller than the lattice parameters a and c, which points to a localized feature of the magnetism of MnFe<sub>4</sub>Si<sub>3</sub>. On the other hand, for itinerant magnetic systems  $\xi_0$  are expected to be significantly larger [20,21].

Additional information can be given by the linewidths  $\Gamma_q$ . The experimental data for the  $\Gamma_q$  obtained at 316 K for the (h00) and (001) directions could be well described both with a model for localized Heisenberg ferromagnets ( $\Gamma_q = A_{\rm loc}q^{2.5}$ ) as well as a model for weak itinerant ferromagnets ( $\Gamma_q = A_{\rm wi}q[1 + (q/\kappa)^2]$ ). The difficulty to distinguish between both models near  $T_C$  was reported previously for Ni<sub>3</sub>Al [28].

The maximum value for  $\Gamma_q$  in the zone boundary (q = 0.5)for each direction is  $\Gamma_{loc,max}^{(h00)} = 5.15(12)$  meV and  $\Gamma_{loc,max}^{(00)} = 62(2)$  meV, which means that the overall  $\langle \Gamma_q \rangle$  is not expected to be higher than  $2k_BT_C$ . Based on the fact that the characteristic linewidths are higher than  $k_BT_C$ , we could expect an itinerant contribution to the magnetism. This is in agreement with Ref. [9], where the Rhodes-Wohlfarth model for the ratio of magnetic moments obtained from the Curie-Weiss law  $(M_c)$ to the low temperature saturation magnetization  $(M_s), M_c/M_s$ = 1.7 points to itinerant magnetism. To summarize, in our study, the obtained correlation lengths and linewidths point to both itinerant and localized contributions of the magnetism in the MC compound MnFe<sub>4</sub>Si<sub>3</sub>, a behavior typical of many ferromagnets [20].

Short-range magnetic correlations in the PM state were also observed in Fe<sub>2</sub>P-based MC materials [31] and their importance for the MCE is not clearly demonstrated. However, our study shows that the temperature and the magnetic field ranges, where the change of entropy is sizable, matches the ones where the magnetic fluctuations are either critical (near  $T_C$ ) or suppressed (near H = 2 T). This points to the importance of such fluctuations for the MCE. In particular, the critical scattering observed near  $T_C$  is strongly suppressed by a

| TABLE III. Properties of selected ferromagnetic materials with hexagonal structure. Lattice parameters are given at around 300 K. M     |
|---|
| refers to the saturated magnetic moments. For MnP compound, the parameters are given in the distorted hexagonal NiAs-type structure. Th |
| lattice parameters for MnFe <sub>4</sub> Si <sub>3</sub> are the ones obtained in the present study and are in agreement with Ref. [9]. |

| Compound                          | <i>Т<sub>С</sub></i><br>(К) | $M_s \ \mu_B$ | a<br>(Å) | c<br>(Å) | c/a   | $D_{(h00)}$<br>(meVÅ <sup>2</sup> ) | $\frac{D_{(00l)}}{(\text{meVÅ}^2)}$ | $D_{(00l)}/D_{(h00)}$ | Easy axis of magnetization |
|-----------------------------------|-----------------------------|---------------|----------|----------|-------|-------------------------------------|-------------------------------------|-----------------------|----------------------------|
| Fe <sub>2</sub> P [27,29,30]      | 209                         | 1.46          | 5.88     | 3.44     | 0.585 | 42                                  | 76                                  | 1.81 (at 77 K)        | С                          |
| MnP [25]                          | 292                         | 1.33          | 3.17     | 5.26     | 1.659 | 70                                  | 145                                 | 2.07 (at 150 K)       | а                          |
| MnFe <sub>4</sub> Si <sub>3</sub> | 305                         | 1.5           | 6.78     | 4.72     | 0.696 | 43                                  | 310                                 | 7.2 (at 1.5 K)        | b                          |

magnetic field of 2 T. To get insight into the observed behavior, a comparison with the model of Ref. [19] has been performed. This model estimates the q-dependent susceptibility under a finite external magnetic field using the Landau theory for the magnetic fluctuations. The measurements shown in Fig. 6 probe the sum of the susceptibilities parallel and perpendicular to the field. In the vicinity of  $T_C$ , the expressions of Ref. [19] are given by:

$$\chi_q^{\parallel}(H, T_C) = \frac{\chi_q(0, T_C)}{1 + \left(\frac{27}{30}\right)^{1/3} \left(\frac{\kappa_0}{q}\right)^2 \left(\frac{g\mu_B H}{k_B T_C}\right)^{2/3}}$$
(4)

$$\chi_q^{\perp}(H, T_C) = \frac{\chi_q(0, T_C)}{1 + \left(\frac{1}{30}\right)^{1/3} \left(\frac{\kappa_0}{q}\right)^2 \left(\frac{g\mu_B H}{k_B T_C}\right)^{2/3}}.$$
 (5)

The field-dependent susceptibility is calculated by inserting the parameters obtained above for v = 0.5 and by averaging the in- and out-of-plane correlation lengths (giving  $(\frac{\kappa_0}{a})^2 \approx$ 100). The obtained calculation is shown in the inset of Fig. 6 with an overall scale factor as the only free parameter. The calculated function describes qualitatively well the data, but the observed decrease with magnetic field is quantitatively stronger. Such disagreement could be attributed to different reasons: the finite integration in energy of our data ( $-0.1 \leq$  $E \leq 0.1 \text{ meV}$ ), the isotropic nature of spin correlations in the model of Ref. [19], or a fluctuations pattern beyond the Landau theory. Since such studies on the effect of a magnetic field on the critical fluctuations are scarce, it is difficult to draw firm conclusions. The same model was used to describe the suppression of the critical fluctuations in Gd [32] and here also the agreement is semiqualitative. In this context, further studies on the effect of the magnetic field on the magnetic critical fluctuations are necessary regarding their potential importance for the MCE.

## **VI. CONCLUSION**

Our detailed study of the spin dynamics of the MC compound  $MnFe_4Si_3$  provides key microscopic information concerning the nature of the magnetism in this system. Among the specific features highlighted in the present study are the isotropic dynamical spin susceptibilities in the PM state, strong anisotropy between in- and out-of-plane magnetic exchange interactions, short-range correlation lengths compared to typical distances, and extended characteristic linewidths compared to  $T_C$ . So far it is not clear which ingredient is favorable to produce a large MCE. Our study suggests that the strong response of the critical fluctuations in the PM state to a magnetic field of 2 T is an important feature.

Thus a systematic study of the spin dynamics of various MC compounds to highlight the major components at play and to finally optimize the materials in view of applications is highly needed.

### APPENDIX A: POLARIZED NEUTRON MEASUREMENTS

For polarized neutron experiments, the usual convention is to define a cartesian coordinate system with the *x* axis parallel to **Q**, the *y* axis perpendicular to **Q** in the scattering plane, and the *z* axis perpendicular to the scattering plane. Since neutron scattering experiments probe only the magnetism perpendicular to the scattering vector **Q**, the measured magnetic fluctuations are therefore  $\langle \delta M_y \rangle$  and  $\langle \delta M_z \rangle$ , where

$$\langle \delta M_{\beta} \rangle = \frac{1}{2\pi} \int \langle \delta M(-Q)_{\beta}^{\perp}(0) \delta M(Q)_{\beta}^{\perp}(t) \rangle e^{-i\omega t} dt.$$
 (A1)

 $\delta M(Q)^{\perp}_{\beta}(t)$  is the  $\beta$  component of the Fourier component of the magnetic fluctuations perpendicular to **Q** and  $\langle ... \rangle$  is the quantum statistical expectation value.

In our experiments, longitudinal polarization analysis was performed: the initial polarization of the neutron beam **P** lies along x, y, or z and only the scattering events where the final polarization lies either parallel—non-spin flip channel (NSF)—or antiparallel—spin flip channel (SF)—to **P** are measured. Magnetic fluctuations parallel to **P** give rise to NSF scattering and magnetic fluctuations perpendicular to **P** give rise to SF scattering. Given the high polarization, no polarization corrections were applied to the data.

### 1. Spin-wave scattering

The polarization is along the direction of the applied vertical magnetic field, z, which corresponds to the direction of the ordered magnetic moments in the single domain sample. Spin waves correspond to precession perpendicular to the ordered moment with, therefore, a unique component  $\langle \delta M_y \rangle$ . The neutron scattering double differential cross sections are:

$$\text{NSF}_{zz} : \left(\frac{d^2\sigma}{d\Omega dE}\right)_{\text{NSF}}^z \propto BG_{\text{NSF}} + \langle N \rangle \qquad (A2)$$

$$\mathrm{SF}_{zz} : \left(\frac{d^2\sigma}{d\Omega dE}\right)_{\mathrm{SF}}^z \propto BG_{\mathrm{SF}} + \langle \delta M_y \rangle$$
 (A3)

where  $\langle N \rangle$  is the nuclear scattering and  $BG_{\rm NSF}$  and  $BG_{\rm SF}$  are the background in the NSF and SF channel, respectively. In the crystal frame and for **Q** in the (a<sup>\*</sup>,c) plane, the cross sections

become:

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^z \propto BG_{\rm NSF} + \langle N \rangle \tag{A4}$$
$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm SF}^z \propto BG_{\rm SF} + \cos^2\theta \langle \delta M_c \rangle + \sin^2\theta \langle \delta M_{a^*} \rangle \tag{A5}$$

with  $\theta$  the angle between **Q** and the (h00) direction.

#### 2. Paramagnetic scattering

In this part, NSF scattering was measured with the double differential cross-sections:

$$\mathrm{NSF}_{xx} : \left(\frac{d^2\sigma}{d\Omega dE}\right)_{\mathrm{NSF}}^x \propto BG_{\mathrm{NSF}} + \langle N \rangle \tag{A6}$$

$$\mathrm{NSF}_{yy} : \left(\frac{d^2\sigma}{d\Omega dE}\right)_{\mathrm{NSF}}^{y} \propto BG_{\mathrm{NSF}} + \langle N \rangle + \langle \delta M_{y} \rangle \qquad (A7)$$

$$\mathrm{NSF}_{zz} : \left(\frac{d^2\sigma}{d\Omega dE}\right)_{\mathrm{NSF}}^z \propto BG_{\mathrm{NSF}} + \langle N \rangle + \langle \delta M_z \rangle.$$
(A8)

For scattering vectors  $\mathbf{Q}$  parallel to (h00), the scattering cross sections are for (a<sup>\*</sup>,c) plane:

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^x \propto BG_{\rm NSF} + \langle N\rangle \tag{A9}$$

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^{\rm y} \propto BG_{\rm NSF} + \langle N \rangle + \langle \delta M_c \rangle \qquad (A10)$$

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^z \propto BG_{\rm NSF} + \langle N \rangle + \langle \delta M_b \rangle.$$
(A11)

It is possible to determine  $\langle \delta M_c \rangle$  and  $\langle \delta M_b \rangle$  by making the subtraction Eqs. (A10)–(A9) and Eqs. (A11)–(A9), respectively. For scattering vectors **Q** parallel to (001), the scattering cross sections are for (a<sup>\*</sup>,c) plane:

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^x \propto BG_{\rm NSF} + \langle N \rangle \tag{A12}$$

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^{\rm y} \propto BG_{\rm NSF} + \langle N \rangle + \langle \delta M_{a^*} \rangle \qquad (A13)$$

$$\left(\frac{d^2\sigma}{d\Omega dE}\right)_{\rm NSF}^z \propto BG_{\rm NSF} + \langle N \rangle + \langle \delta M_b \rangle. \tag{A14}$$

It is possible to determine  $\langle \delta M_{a^*} \rangle$  and  $\langle \delta M_b \rangle$  by making the subtraction Eqs. (A13)–(A12) and Eqs. (A14)–(A12), respectively.

## APPENDIX B: SCATTERING FUNCTIONS

The measured intensity  $I(\mathbf{Q}, \omega)$  is the convolution of the resolution function  $F(\mathbf{Q}, \omega)$  and the scattering function  $S(\mathbf{Q}, \omega)$ :  $I(\mathbf{Q}, \omega) = F(\mathbf{Q}, \omega) \otimes S(\mathbf{Q}, \omega)$ . In this paper, the constant  $\mathbf{Q}$  spectra at T = 316 K were convoluted with a one-dimensional resolution in the  $\omega$  direction. We assumed that the resolution function has a Gaussian shape with widths defined from measurements on a vanadium sample. The scattering function and the imaginary part of the dynamical spin susceptibility  $\chi''(\mathbf{Q}, \omega)$  are connected through the following relation:

$$S(\mathbf{Q},\omega) = \frac{1}{1 - e^{-\omega/T}} \chi''(\mathbf{Q},\omega), \qquad (B1)$$

where  $\omega$  and *T* are given in units of  $\hbar$  and  $k_B$ , respectively. The paramagnetic scattering can be described with the Lorentzian-like equation  $\chi''(\mathbf{q}, \omega)$ :

$$\chi''(\mathbf{q},\omega) = \frac{\chi_0}{1 + (q/\kappa)^2} \frac{\omega\Gamma_q}{\omega^2 + \Gamma_q^2} = \chi_q \frac{\omega\Gamma_q}{\omega^2 + \Gamma_q^2}, \quad (B2)$$

where  $\chi_q$ ,  $\Gamma_q$ , and  $\kappa$  are the *q*-dependent susceptibility, linewidth, and inverse correlation length and  $\chi_0$  the static susceptibility. For all the obtained constant **Q** spectra at  $1.036T_C \approx 316$  K (e.g., Fig. 7) the energy transfer was between  $-5 \leq E \leq 5$  meV. For this energy range and temperature, Eq. (B1) combined with Eq. (B2) is simplified to the double Lorentzian form:

$$S(\mathbf{q},\omega) = T \frac{\chi_0}{1 + (q/\kappa)^2} \frac{\Gamma_q}{\omega^2 + \Gamma_q^2} = T \chi_q \frac{\Gamma_q}{\omega^2 + \Gamma_q^2}.$$
 (B3)

The resulting fit for the measured intensity  $I(\mathbf{Q},\omega)$  can be realized as a Voigt function. From the Voigt's function amplitude  $\chi_q$  can be extracted and the width of the Lorentzian part (HWHM) corresponds to  $\Gamma_q$ . The width of the Gaussian part is fixed to a constant value, defined from the vanadium sample measurement.

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