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# Chirality-mediated bistability and strong frequency downshifting of the gyrotropic resonance of a magnetic vortex due to dynamic destiffening

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We demonstrate an enhanced, bidirectional, in-plane magnetic field tuning of the gyrotropic resonance frequency of a magnetic vortex within a ferromagnetic disk by introducing a flat edge. When the core is in its vicinity, the flat edge locally reduces the core's directional dynamic stiffness for movement parallel to the edge. This strongly reduces the net dynamic core stiffness, leading to the gyrotropic frequency being significantly less than when the core is centered (or located near the round edge). This leads to the measurable range of gyrotropic frequencies being more than doubled and also results in a clear chirality-mediated bistability of the gyrotropic resonance frequency due to what is effectively a chirality dependence of the core's confining potential.

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Magnetic vortices are curled magnetization configurations that arise naturally in thin magnetic elements with lateral dimensions from ~0.1  $\mu$ m to a few  $\mu$ m [1–4]. They are characterized by an in-plane, curling magnetization which surrounds an out-of-plane magnetized nanoscale region known as the vortex core [Fig. 1(a)]. Magnetic vortices are examples of topological solitons or defects and can display dynamic behavior which is intrinsically nonlinear [5–9], a characteristic which has generated significant theoretical interest.

The potential for device applications [10-12], which include tuneable rf signal generators and detectors [13–15] and data storage devices [10], has strongly motivated studies in tuning the frequency of the gyrotropic resonance of magnetic vortices,  $f_G$ . This resonance involves the vortex core following an orbitlike path around its equilibrium position [16-20]. The gyrotropic resonance frequency is proportional to the vortex stiffness [17],  $\kappa$ , which is typically determined by a geometrically induced, primarily magnetostatic [17,21], core confining potential (there can also be non-negligible contributions from exchange interactions [22] or current-generated Oersted fields [23]). Although the confining potential can be treated as harmonic for small radial core displacements  $(\Delta E = \frac{1}{2}\kappa X^2$  where E is the system energy and X is the radial core displacement), it is typically anharmonic [24], meaning that  $\kappa$ , and thus  $f_G$ , are both dependent on the position of the vortex core. For example, in circular [24-26] disks (as well as in elliptical disks, although the behavior there is slightly more complex [27]), the gyrotropic frequency becomes higher as the core is displaced from the disk's center due to a core stiffening.

In this Rapid Communication we present results on vortex core dynamics in a ferromagnetic disk that has one side which has been made flat ("chopped") [Fig. 1(b)]. The flat edge enables control over the vortex chirality [28-34] which describes the direction of the [clockwise (CW) or anticlockwise (ACW)] curling magnetization. The chirality is critical in this Rapid Communication as it determines the lateral direction that a core will be displaced under the action of a given static in-plane magnetic field [28]. Chirality control thus enables core displacement control. Despite both the flat and round edges being repulsive to the core under static displacements towards the edge, we show that a core undergoing gyrotropic motion near the flat edge exhibits a strongly reduced dynamic stiffness when moving along the flat edge (i.e., perpendicular to the direction of the static displacement). As a result, the net dynamic core stiffness [27] is also reduced, leading to  $f_G$  at the flat edge being lower than  $f_G$  for the disk-centered core.  $f_G$  can thus either be strongly increased (by shifting the core towards the disk's round edge) or decreased (by moving the core towards the flat edge). This leads to the range of accessible  $f_G$  values being approximately doubled (i.e., we can both significantly increase and decrease  $f_G$  relative to its value for a nondisplaced vortex in zero field). We note that frequency downshifting has also been observed in square ferromagnetic elements [35,36] and, to a lesser degree, in triangular elements [37] when moving the core towards a flat edge within the element.

A final consequence of the geometrical asymmetry in our system is that the vortex is characterized by a clear chiralityinduced, dynamic bistability. Indeed, for a given, finite, static in-plane magnetic field (applied such that it acts to displace the core perpendicular to the disk's flat edge), two values of  $f_G$  can be observed depending on the vortex chirality. This is reminiscent of the polarity-induced bistability studied by de Loubens *et al.* [38]. Here however, it is chirality mediated and arises because, for a given in-plane field polarity, the chirality determines which part of the asymmetric confining potential the gyrating core is subject to.

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FIG. 1. Simulated vortex configurations in (a) circular and (b) chopped NiFe-like disks in zero external magnetic field. The diameter of the circular disk is  $2 \mu m$ . The geometry of the chopped disk matches that shown in (c). (c) Schematic of the experimental setup used for probing the core dynamics including a scanning electron micrograph showing the lateral dimensions of a chopped disk used in our experiments. (d) Experimentally obtained resonance peak at  $H_{\parallel} = 0$ . Simulated transition from the (e) right- and (f) left-oriented saturated states to, respectively, an anticlockwise (ACW) and clockwise (CW) vortex state ( $H_{\parallel} = 0$ ).  $H_{sat}$  is used experimentally to approach the saturated state and controllably produce CW or ACW vortex configurations.

A scanning electron microscope image of a chopped disk is shown in Fig. 1(c). The distance from the disk's center to the round edge is  $1 \,\mu m$  (radius of the circular part of the disk) while the shortest distance from the disk's center to the flat edge is  $0.7 \,\mu$ m. Disks were fabricated from a continuous sputtered NiFe (30 nm)/Au (8 nm) layer via argon ion milling using a hard Ti mask defined by electron-beam lithography (NanoBeam Limited). Evaporated lateral contacts were defined using electron-beam lithography and liftoff. Auger spectroscopy suggests that approximately 30 nm of Ti remains on the top of the NiFe/Au chopped disk [26]. The measured device was wire bonded to a sample mount which was placed between the poles of an electromagnet in such a way that a static, in-plane magnetic field,  $H_{||}$ , could be applied along the flat edge of the disk (note that simulations detailed below will suggest the presence of a small misalignment of  $\sim 3^{\circ}$ between the field and the disk's flat edge). A nanovoltmeter (200-ms integration time) was used to measure the voltage across the device in the presence of injected dc or rf currents [Fig. 1(c)]. The rf source output power was -14 dBm.

An rf current injected across the device generates a transverse, rf Oersted field in the lower NiFe layer which can drive gyrotropic core motion [26]. On resonance, this generates an oscillation in the sample's resistance (via anisotropic magnetoresistance) which can mix with the input rf current to generate a measurable rectified voltage and enable the electrical identification of  $f_G$  [25,26,39–42]. In Fig. 1(d) we



FIG. 2. Experimentally obtained magnetoresistive rectification traces demonstrating chiral bistability of the gyrotropic resonance frequency in a chopped disk at  $\mu_0 H_{||}$  values of (a) +10.6 mT and (b) -10.6mT for CW (dashed black line) and ACW (solid red line) vortices. Insets show simulated at-equilibrium vortex configurations with shifted cores ( $\mu_0 H_{||} = \pm 10$  mT). For simplicity, each peak is shown with a negative polarity (the peak polarity will depend on the core polarity [26,41], which was not controlled in these experiments).

show the rectification peak obtained in the chopped disk at zero applied field from which we can extract  $f_G \approx 126$  MHz. This value matches closely with the simulated  $f_G = 128$  MHz at  $H_{||} = 0$  (see below). Note that in circular disks a rectification peak is not generated for  $H_{||} = 0$  due to the symmetry of the core trajectory around the center of the disk which results in the generated voltage time averaging to zero [26,43]. In contrast, the chopped disk geometry leads to an asymmetric orbit and the core's equilibrium position being shifted away from the circular center of the element which enables the generation of a finite amplitude peak even for  $H_{||} = 0$ . This result is discussed further in Fig. 1 of Ref. [44].

The vortex chirality defines the direction of the core shift for a given  $H_{\parallel}$  [28]. For example, a positive  $H_{\parallel}$  shifts the core to the round edge for an ACW vortex but shifts it to the flat edge for a CW vortex [insets of Fig. 2]. Micromagnetic simulations performed using the MUMAX3 micromagnetic code [45] demonstrate the ability to choose the vortex chirality in the chopped disk by starting from an in-plane saturated state and then returning the field to zero [Figs. 1(e) and 1(f)]. In the simulations, we used 30-nm-thick cells with lateral dimensions of  $\sim 3.9 \times 3.9$  nm<sup>2</sup> (512×512 cells for the  $2 \times 2 \cdot \mu m^2$  simulation region) [46]. We then initialized the system with a uniform magnetization parallel to the flat edge and let the magnetization evolve towards a final, converged state in zero magnetic field with damping parameter  $\alpha = 0.01$ [saturation magnetization = 800 kA/m; exchange stiffness = 13 pJ/m; nil anisotropy;  $\gamma = 1.7595 \times 10^{11} \text{ rad}(\text{T s})^{-1}$ , which is within  $\sim 5\%$  of the experimentally determined value [47]]. We find that the initial direction of the magnetization along

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the flat edge remains fixed upon the return to zero field and thus defines the chirality of the relaxed, curled vortex state [Figs. 1(e) and 1(f)]. Note that the simulated transition to the single vortex state proceeds via a nontrivial intermediate state analogous to that seen in Co disks with widths >800 nm [32]. Experimentally, the left and right saturated magnetic states are approximated by applying an in-plane saturating field,  $H_{sat} = \pm 0.6$  T, along the flat edge of the disk [Figs. 1(e) and 1(f)]. In Fig. 2 of Ref. [44] we confirm our ability to choose the core chirality by exploiting differences in the vortex annihilation fields at the flat and round edges [29] (as well as differences in the quasistatic magnetization reversal process). Dynamic results presented below will also confirm our ability to set the chirality and controllably displace the core towards the flat or round edge of the disk.

We now use the on-resonance rectification to experimentally measure the influence of the core's equilibrium position on  $f_G$ . We first set a CW vortex chirality, return to zero field, and then apply  $\mu_0 H_{\parallel} = +10.6 \,\mathrm{mT}$ . This shifts the core towards the disk's flat edge [Fig. 2(a), left]. An rf signal is then injected across the disk, sweeping from low frequency to high frequency, enabling us to determine  $f_G = 108 \text{ MHz}$ [black dashed lines in Fig. 2(a)]. Note that the measured frequency is significantly lower than the value found at  $H_{\parallel} = 0$ in Fig. 1(d) ( $\approx$  126 MHz). Repeating the measurement for an ACW chirality at the same field allows us to probe core dynamics at the round edge of the disk [Fig. 2(a), right] for which we find  $f_G = 140 \text{ MHz}$  [solid red line in Fig. 2(a)]. This confirms the chiral bistability in that we can observe two different values of  $f_G$  for a fixed  $H_{||}$ , depending on the vortex chirality. Changing the polarity of  $H_{||}$  changes the direction of the core displacement for a given chirality. As such, for  $\mu_0 H_{||} = -10.6 \text{ mT}$  [Fig. 2(b)], it is now the CW vortex core which moves to the round edge of the disk, resulting in it having the higher  $f_G$ .

The results of experiments carried out for both chiralities are given in Fig. 3, showing the full evolution of  $f_G$  with  $H_{||}$ . Examples of peaks obtained by carrying out field sweeps at fixed frequency (field-resolved measurements) are also shown as insets in Fig. 3 and show good agreement with the frequency-resolved data. Note that there are two data sets in Fig. 3 corresponding to CW (filled squares) and ACW (filled circles) vortices. Here, it is again clear that for a given finite in-plane field  $f_G$  can be either above or below the zero-field value of  $f_G$  depending on the vortex chirality with low frequencies obtained when the core is shifted towards the flat edge ( $H_{||} < 0$  for an ACW vortex and  $H_{||} > 0$  for a CW vortex). Also note that the difference between  $f_G$  values for the two chiralities increases with  $H_{\parallel}$  as the core is pushed further away from the disk's center. Simulated gyrotropic frequencies (open circles) for different chiralities and  $H_{\parallel}$ values are also shown in Fig. 3 with good agreement between the simulation and experimental results. Note, however, that the best agreement is obtained by including a misalignment of 3° between  $H_{||}$  and the flat edge (this causes the core to be slightly displaced towards the point where the flat edge meets the disk's round edge, slightly increasing the stiffness and thus  $f_G$ ; see Fig. 3 of Ref. [44]). To obtain simulated  $f_G$  values, we performed field-pulse-driven "ringdown" simulations [48] (e.g., Refs. [49,50]) for a number of  $H_{\parallel}$  values.

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FIG. 3. Experimental data showing the gyrotropic resonance frequency as a function of  $H_{||}$  for CW (solid squares) and ACW (solid circles) vortices. Four data points obtained from field-swept measurements (see insets) at 140 and 110 MHz are plotted as open triangles. The plot also shows simulated gyrotropic frequencies for a perfect alignment of the flat edge and  $H_{||}$  (0 deg, shown for both chiralities) and for a misalignment of 3° (3 deg, shown for ACW).

To understand the observed dropoff in  $f_G$  for cores at the flat edge of the disk, we look at the relationship between  $f_G$  and the core stiffness, the latter depending not only on the location of the core but also on the direction of core movement [27]:

$$f_G = \frac{\sqrt{\kappa_x \kappa_y}}{2\pi G}.$$
 (1)

Above,  $\kappa_x$  and  $\kappa_y$  correspond to the local core stiffness in the x and y directions [defined in Figs. 1(a) and 1(b)] and G is the gyroconstant [17,51,52] (considered field independent here). Note that in a circularly symmetric system [17,21]  $f_G$ is simply given by  $\kappa/2\pi G$  with  $\sqrt{\kappa_x \kappa_y}$  here replacing the otherwise direction-independent  $\kappa \equiv \kappa_{tot}$ . The stiffness coefficient along an axis x is defined via  $\Delta E = \frac{1}{2}\kappa_x x^2$  (valid for small [24] x) where E is the energy of the system. An accurate description of dynamics must, however, take into account the energy of the moving core rather than static displacements [22,27]. To extract the dynamic  $\kappa$  from micromagnetic simulations, core dynamics were driven using an in-plane sinusoidal field with an amplitude of 5  $\mu$ T and frequency equal to  $f_G$  as obtained from the ringdown simulations [50].  $\kappa_x$  and  $\kappa_{v}$  were then extracted from parabolic fits to the total system energy as a function of core displacement along the x and y directions, respectively.

Figure 4(a) shows the extracted  $\kappa_x$  and  $\kappa_y$  values versus in-plane field for an ACW vortex for which a negative  $H_{||}$ will displace the core toward the disk's flat edge. Although  $\kappa_y$  is relatively symmetric about  $\mu_0 H_{||} = 0$  mT,  $\kappa_x$ , related to dynamic displacement parallel to the flat edge of the disk, is clearly asymmetric and lowest when the core is located near the flat edge ( $H_{||} < 0$ ). This is despite the edge of the disk being repulsive in terms of static displacements of the core towards it [i.e., the equilibrium position of the static core at  $H_{||} = 0$  remains relatively close to the disk's center; Fig. 1(b)].



FIG. 4. (a)  $\kappa_x$  and  $\kappa_y$  and (b)  $\kappa_{tot} = \sqrt{\kappa_x \kappa_y}$  as extracted from simulations for an ACW vortex as a function of  $H_{||}$ . (c) Simulated, calculated [via Eq. (1)], and experimental values of  $f_G$  as a function of  $H_{||}$  for the ACW vortex. (d) Demagnetizing energy profile extracted from simulation for a core displacing approximately along the flat edge (solid triangles) and round edge (open circles). The energy is shown as a function of equilibrium core displacement along the x direction (induced by application of a stepped field along the ydirection, i.e., perpendicular to the flat edge). Insets in (b) show the core trajectory at resonance when the core is displaced towards the flat edge ( $\mu_0 H_{||} = -15 \text{ mT}$ ) or towards the round edge ( $\mu_0 H_{||} =$ +15 mT).

The asymmetry in  $\kappa_x$  is critical to understand the dropoff in  $f_G$  as it leads to a strong local reduction in the  $\sqrt{\kappa_x \kappa_y} \equiv \kappa_{\text{tot}}$  term [Fig. 4(b)] which in turn leads to a strong reduction in  $f_G$  as per Eq. (1). Indeed the  $f_G$  predicted from the extracted  $\kappa_x$  and  $\kappa_y$  values using Eq. (1) can be used to accurately reproduce the simulated frequencies which in turn approximate the measured frequencies well [Fig. 4(c)]. As noted above and seen in Fig. 3 of Ref. [44], a better match between simulation and experiment can be obtained by including a 3° in-plane field misalignment.

The reduced value of  $\kappa_x$  at the disk's flat edge is primarily due to a weaker dependence of the demagnetizing-energy on the *x* position of the core at that side of the element (contributions from demagnetizing, exchange, and Zeeman energies are compared in Fig. 4 of Ref. [44] for the chopped and unchopped disk). This weaker dependence can be directly visualized in Fig. 4(d) where we show the change in the system's demagnetizing energy for a core that is quasistatically shifted approximately laterally along the flat and round edges via a *y*-oriented magnetic field. One sees that small lateral displacements near the curved edge lead to larger changes in the

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demagnetizing energy (per unit displacement) than do lateral displacements along the flat edge. At least for static magnetization configurations with laterally shifted cores, the demagnetizing energy (as well as the displacement-induced change in the demagnetizing energy) is concentrated within lines that join the core to positions which are close to the meeting points of the flat and curved edges of the disk (these lines are essentially domain walls; see Fig. 5 of Ref. [44]). As an aside, we note that the reduced  $\kappa_x$  at the flat edge also has a strong effect on the simulated orbit, with simulations predicting that the orbit will be strongly elongated in the *x* direction [lower inset in Fig. 4(b)] as compared to the orbit of the core when it is located near the curved edge [upper inset in Fig. 4(b)].

In conclusion, we have shown that the introduction of a flat edge into a magnetic disk can generate a chirality-driven bistability of the vortex gyrotropic resonance frequency as well as an increased range of accessible gyrotropic resonance frequencies. Indeed, depending on the vortex chirality, a static in-plane magnetic field can drive the core either towards the disk's round edge (where the gyrotropic frequency is known to increase) or towards its flat edge (which is shown here to reduce the gyrotropic frequency). The latter frequency downshifting is demonstrated to be a dynamic effect related to the core moving both parallel and perpendicularly to the flat edge during gyrotropic motion. Calculations of the stiffness of the resonating core demonstrate that the core's dynamic stiffness along the flat edge  $(\kappa_x)$  is strongly reduced when the core is close to the flat edge, resulting in a lower net dynamic stiffness ( $\propto \sqrt{\kappa_x}$ ) and thus the lowered gyrotropic resonance frequencies that we observe in experiment.

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