

## Switching of magnetic ground states across the $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$ alloy system

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(Received 2 May 2016; revised manuscript received 14 March 2017; published 24 April 2017)

We investigated the evolution of magnetism in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system by the systematic study of high-quality single crystals. Lattice parameters of both parent compounds are very similar, resulting in almost identical nearest interatomic uranium distances close to the Hill limit. We established the  $x$ - $T$  phase diagram of the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system and found a discontinuous antiferromagnetic/ferromagnetic boundary at  $x_{\text{crit}} = 0.56$ , where a local minimum in ordering temperature and maximum of the Sommerfeld coefficient  $\gamma \approx 175$  mJ/mol K<sup>2</sup> occurs in the  $\text{UCoGe-URhGe-UIrGe}$  system, signaling an increase in magnetic fluctuation. However, a quantum critical point is not realized because of the finite ordering temperature at  $x_{\text{crit}}$ . A magnon gap on the antiferromagnetic side abruptly suppresses magnetic fluctuations. We find a field-induced first order transition in the vicinity of the critical magnetic field along the  $b$  axis ( $H_{b,\text{crit}}$ ) in the entire  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system, including the ferromagnetic region  $\sim \text{UCo}_{0.6}\text{Rh}_{0.4}\text{Ge-URhGe}$ .

DOI: [10.1103/PhysRevB.95.155138](https://doi.org/10.1103/PhysRevB.95.155138)

### I. INTRODUCTION

Uranium intermetallics with  $5f$  electrons at the boundary between localized and itinerant characters are of continuing interest. The crossover was empirically established by Hill [1] at an interatomic uranium-uranium distance  $d_{\text{U-U}} \approx 3.5$  Å. Exotic electronic phenomena often appear in compounds satisfying this criterion. Ferromagnetic (FM) superconductors (SCs)  $\text{URhGe}$  [2] and  $\text{UCoGe}$  [3] are exemplary cases. Recent papers on the related isostructural  $\text{TiNiSi}$ -type  $\text{UTGe}$  ( $T$  = transition metal) compounds found their magnetism scaling according to the Hill criterion [4,5] and uncovered another promising candidate,  $\text{UIrGe}$ .

$\text{UIrGe}$  [6] has an almost identical nearest interatomic uranium-uranium distance to  $\text{URhGe}$  but orders antiferromagnetically [7] with Néel temperature  $T_{\text{N}} = 16.5$  K. The magnetic structure of  $\text{UIrGe}$  consists of FM zigzag chains along the  $a$  axis [8,9], resembling the magnetic structures of the FMs  $\text{UCoGe}$  [10–12] and  $\text{URhGe}$ . The chains are antiferromagnetically coupled. A spin-flop transition is induced in a magnetic field applied along the  $c$  axis of  $H_{c,\text{crit}} = 14$  T. A similar spin-flop mechanism was detected for the magnetization along the  $b$  axis at  $H_{b,\text{crit}} = 21$  T [13,14]. Then, the  $b$  axis becomes the easy magnetization axis, similar to the magnetic behavior of FM  $\text{URhGe}$ . Here the so-called intermediate  $b$  axis is characterized by a magnetic moment reorientation at a critical magnetic field  $H_{\text{R}} = 12$  T, which restores the SC state [5,15]. Recent papers revealed strong tricritical fluctuations in the vicinity of  $H_{\text{R}}$  [16,17] accompanied by a Lifshitz-type transition and enhancement of the coefficient  $\gamma$  [18–20].

We studied the magnetic properties and quantum critical phenomena in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system, which has an interesting FM/antiferromagnetic (AFM) boundary at low temperature. This AFM/FM boundary is of interest because

the AFM and FM are separated at this point throughout the whole orthorhombic  $\text{TiNiSi}$ -type  $\text{UTGe}$  system by the Hill limit [4]. Many studies have been conducted to determine the delicate balance of magnetic interactions in  $\text{UTGe}$  alloy systems, but they have been primarily on polycrystalline samples where the crucially important magnetocrystalline anisotropy remains hidden [4,21–26]. Our investigation of single crystals has allowed us to develop a general picture of the magnetism in the AFM part of the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system, which surprisingly preserves many of the magnetic features of the FM parent compounds  $\text{URhGe}$  and  $\text{UCoGe}$ . Our discussion and conclusions are based on a detailed analysis of the crystal structure, magnetization, and heat capacity.

### II. EXPERIMENTAL

High-quality single crystals were grown by Czochralski pulling in a tetra arc furnace from polycrystalline precursors of nominal concentrations listed in Table I. Pulling speeds of 6 mm/h was used for the alloy compounds. The single crystals were several-centimeter-long cylinders of 2–3-mm diameter. The pulled crystals were wrapped in Ta foil, sealed in quartz tubes under high vacuum, and annealed 14 d at 1000 °C. The residual resistivity ratio (RRR) was substantially increased by this annealing procedure in the case of  $\text{UIrGe}$  from 2–4 up to several tens [27]. The RRR of the substituted compounds remains unchanged, as observed in the other systems [4,12,21,24,25,28,29]. A precision spark erosion saw was used to cut appropriately shaped samples. An electron probe microanalyzer EPMA JXA-8900 (JEOL) has been used for the chemical analysis. Structural characterization was performed by single crystal x-ray diffraction using a Rigaku Rapid diffractometer. The recorded patterns were evaluated using ShelX software. The temperature and field dependent magnetization was measured along the principal crystallographic directions down to  $T = 1.8$  K in applied magnetic fields up to 7 T using a commercial magnetometer

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TABLE I. Chemical analyses of the studied single crystals in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system.

Nominal concentration	Microprobe analysis
AFM $\text{UIr}_{0.50}\text{Rh}_{0.50}\text{Ge}$	$\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}_{1.00}$
<sup>a</sup> AFM $\text{UIr}_{0.37}\text{Rh}_{0.63}\text{Ge}$	$\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}_{0.98}$
FM $\text{UIr}_{0.35}\text{Rh}_{0.65}\text{Ge}$	$\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}_{0.99}$
FM $\text{UIr}_{0.10}\text{Rh}_{0.90}\text{Ge}$	$\text{UIr}_{0.14}\text{Rh}_{0.86}\text{Ge}_{0.99}$

<sup>a</sup>Block 4 in Fig. 1. The compositions obtained by electron microprobe analyses are used in the text.

(Magnetic Property Measurement System [MPMS] 7 T and 5 T, Quantum Design). The heat capacity measurements were carried out down to 1.8 K with applied magnetic fields up to 9 T using a commercial Physical Property Measurement System (PPMS; Quantum Design DynaCool).

### III. EXPERIMENTAL RESULTS

#### A. Chemical analysis

The microprobe analysis of all the alloying single crystals revealed a higher concentration of Ir than the nominal composition of the melt. Table I summarizes the nominal concentrations and the results of electron microprobe analyses. This disproportion causes a weak gradient of the Ir-Rh ratio along the single crystal ingots. The upper parts of the ingots are richer in Ir. The Rh concentration increases toward the bottom due to the prior consumption of Ir during the growth process. Detailed chemical analysis has revealed a weak gradient of the Ir-Rh ratio  $\sim 1$  at. % (almost the detection limit of the method used) along the 40-mm-long ingot.

We cut the single crystal of composition  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$ , expected to have a robust AFM phase, into  $\sim 2$ -mm-long blocks and measured for each one the temperature dependent magnetization along the  $c$  axis. Upper blocks 1–13 show robust AFM, with Néel temperature determined from the magnetization maxima. Nonetheless, due to the weak Rh gradient, we found the first signature of the nascent FM phase as a broad hump with roughly  $T_C \approx 6.5$  K in block 14 of  $\text{UIr}_{0.44}\text{Rh}_{0.56}\text{Ge}$ . Simultaneously, the weak local maximum of the AFM phase still remains, fixed at  $T_N \approx 3.9$  K (see Fig. 1).

For the later research we used block 4 of composition  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  as the ultimate AFM compound. The weak Rh-Ir gradient in the other single crystals does not have any noticeable effect, causing only a tiny shift of the ordering temperature of the robust FM or AFM phase. One unique block of length  $\sim 2$  mm was always extracted from each single crystal and used for all experiments to avoid any effect of the gradient.

#### B. XRD characterization

The high quality of each single crystal was verified by Laue patterns showing sharp reflections. Structural analysis by single-crystal x-ray diffraction confirmed the orthorhombic  $\text{TiNiSi}$ -type structure and space group  $Pnma$  throughout the whole series. Results are summarized in Fig. 2 and the Appendix.

The AFM/FM boundary in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system is interesting from the standpoint that AFM  $\text{UIrGe}$  and FM

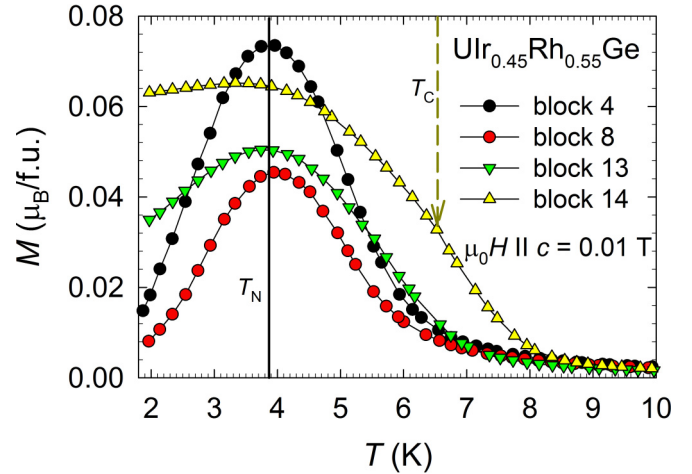


FIG. 1. Temperature dependent magnetization of selected blocks of the  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  single crystal. Increasing block numbers correspond to the direction from the neck to the end of the single crystal. The black line marks the lowest detectable  $T_N$ . The yellow dashed arrow marks the  $T_C$  of the nascent FM phase. f. u. = formula units.

$\text{URhGe}$  have very similar lattice parameters arising from almost identical radii of the transition element ions [30]. The lattice similarity is evident when the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  data are plotted together with the neighboring  $\text{UCoGe}$  and  $\text{UNiGe}$ , showing the growing  $d_{\text{U-U}}$  (Fig. 2). The unit cell volume of  $\text{UIrGe}$  is only about 0.07% larger than that of  $\text{URhGe}$  [6,31]. The very small change of the unit cell volume arises from nearly perfect cancellation of the weakly expanded lattice parameter  $c$  and shortened  $b$ . The crucial parameter  $a$  remains unchanged and reflects an almost constant  $d_{\text{U-U}}$  distance. The shortening of the  $b$  axis reduces the second nearest  $d_{\text{U-U}}$  distance from 3.758 Å ( $\text{URhGe}$ ) to 3.747 Å ( $\text{UIrGe}$ ), the zigzag chain separation being at distance  $b$ . The  $bc$  plane of the  $\text{TiNiSi}$ -type structure can be considered derived from a deformed hexagonal lattice. An angle of  $70.39^\circ$  characterizes the lattice of the  $\text{URhGe}$ , compared with the  $70.09(5)^\circ$  of  $\text{UIrGe}$ . The larger  $c$  of  $\text{UIrGe}$  sharpens the angle of the zigzag chains from the  $157.34(6)^\circ$  of  $\text{URhGe}$  to  $156.23(9)^\circ$ . However, these variations do not lead to obvious conclusions concerning the FM/AFM boundary in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  based on a simple structural analysis. Moreover, the lattice parameters  $b$  and  $c$  develop unsystematically from  $\text{UIrGe}$  to another AFM  $\text{UNiGe}$  (Fig. 2).

#### C. Magnetization

Magnetic ordering temperatures of all studied compounds were determined (Fig. 3, Table II). In the case of the parent  $\text{UIrGe}$  with the sharp AFM transition, we found clear agreement with  $T_N$  estimated as a position of the sudden drop in the electrical resistivity [27], the peak maximum in the temperature dependent susceptibility along the  $c$  axis, and onset of the  $\lambda$  anomaly in the heat capacity [14]. The identical procedure is applicable for electrical resistivity and heat capacity of the FM  $\text{URhGe}$  [31]. Thus, we strictly followed this procedure for all alloy compounds studied. The estimation method used for  $T_N$  as the maximum susceptibility also respects the method in the original polycrystalline paper

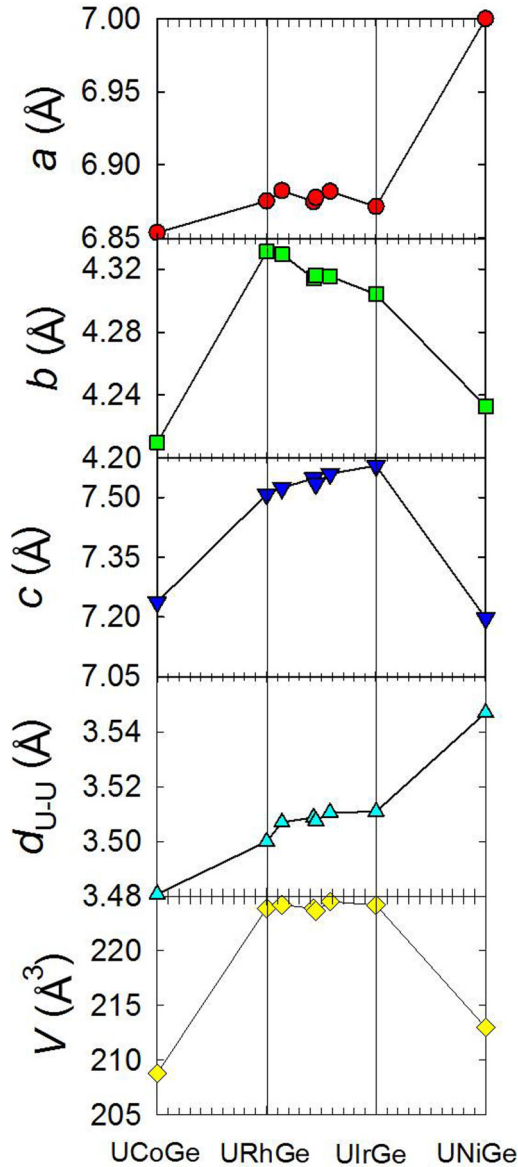


FIG. 2. Lattice parameters in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system as a function of concentration. Two neighboring compounds,  $\text{UCoGe}$  and  $\text{UNiGe}$ , are also plotted to show the gradually increasing nearest uranium-uranium distance  $d_{\text{U-U}}$  utilized in the Hill plots [4]. Refined structural parameters for the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system are available in the Appendix.

[32]. We found two FM compounds,  $\text{UIr}_{0.14}\text{Rh}_{0.86}\text{Ge}$  and  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ , with Curie temperatures  $T_C = 9.1$  K and 6.2 K, respectively. The plateau of the weakly decreasing  $T_C$  is broken by an acute fall to the Néel temperature  $T_N = 3.9$  K with the first AFM composition  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$ . We particularly note that the FM/AFM boundary arises with an infinitesimal concentration step of the substituent elements. Magnetization studies of the gradient crystals have never found  $T_C$  and  $T_N$  to merge continuously. A further increase of Ir concentration is accompanied by growth of  $T_N$ . A  $T_N = 7$  K was found in  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$ , increasing to the highest value  $T_N = 16.5$  K of parent  $\text{UIrGe}$  (Fig. 3). Ordering temperatures together with all the magnetic constants are summarized in Table II.

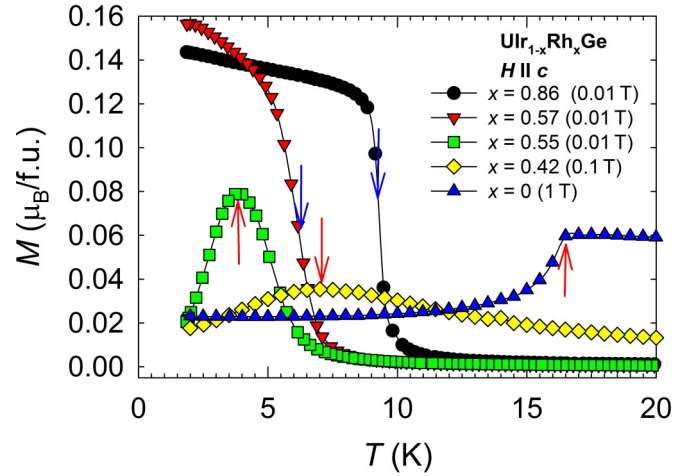


FIG. 3. Temperature dependent magnetization of all studied compounds in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system. The blue arrows indicate Curie temperatures and the red arrows Néel temperatures. The curve for  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  was multiplied by 5 and the curve for  $\text{UIrGe}$  by 3 for clarity because of the reduced magnetic moments compared with the FM members. Curie temperatures were taken as the inflection points in the magnetization curves and the Néel temperatures as the maxima of the peaks.

There is a discrepancy between our results and the original paper.  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  was reported as FM [32], while we still see a clear AFM order. We will show below that a magnetic field of 0.1 T [32] along the  $c$  axis was strong enough to initiate the spin-flop transition.

Magnetic anisotropy of the AFM  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  still points to a simple collinear magnetic structure with magnetic moment aligned along the  $c$  axis. In contrast, a reproducible drop of magnetization is detected along the  $a$  and  $b$  axes at  $T_N$  in  $\text{UIrGe}$  (Fig. 4). This may be evidence of canting of the magnetic moments, as predicted by neutron diffraction, close to the parent  $\text{UIrGe}$ .

Current knowledge about the magnetic structure of  $\text{UIrGe}$  is quite unclear. Neutron diffraction on a single crystal [8,33] suggested a component of magnetization along  $a$  which was not confirmed experimentally by magnetization up to 50 T [14]. Magnetic moment components in the  $bc$  plane were found for the isostructural AFM  $\text{UNiGe}$  and  $\text{UPdGe}$  [9]. The  $\text{UIrGe}$  state resembles the  $a$  axis component of the magnetic moment proposed in  $\text{UNiGe}$ , although the  $bc$  plane is magnetically soft, with a complex magnetic phase diagram [34,35].

Temperature dependent magnetization curves along the  $b$  axis show complex behavior. A broad maximum is located above  $T_N$  at  $T_{\text{max}} = 11, 12,$  and  $29$  K in  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$ ,  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$ , and  $\text{UIrGe}$ , respectively (Fig. 4).  $T_{\text{max}}$  is also observable as a sharp peak in the FM  $\text{UIr}_{0.14}\text{Rh}_{0.86}\text{Ge}$  [Fig. 5(a)], identical to parent  $\text{URhGe}$  [20], and as a broad peak in  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$  [Fig. 5(b)]. A general feature is that  $T_{\text{max}} \approx T_C$  for all FMs. In contrast,  $T_{\text{max}} > T_N$  for all AFMs (see Table II).  $T_{\text{max}}$  is shifted to lower temperatures with an increasing magnetic field along the  $b$  axis, demarking closed domes whose summits are located at higher fields than those available to our magnetometer. Data from Figs. 5 and 6 will be used below for construction of the  $H$ - $T$  phase diagrams.

TABLE II. Magnetic and thermodynamic constants of all studied compounds in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system. A dashed line separates the FM and AFM compounds. Nonetheless, evidence of the nascent FM phase was detected by heat capacity data in  $x = 0.55$ . Magnetic constants of URhGe with rather limited agreement are available in Ref. [31] by fitting the Curie-Weiss law, compared with our fitting by modified Curie-Weiss law.

$\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$	$x = 1$	$x = 0.86$	$x = 0.57$	$x = 0.55$	$x = 0.42$	$x = 0$
$T_C$ (K)	9.5	9.1	6.2	—	—	—
$T_N$ (K)	—	—	—	3.9	7	16.5
$T_{\max}$ (K)	$=T_C$	$=T_C$	$=T_C$	$\sim 11$	12	29
$T_{\max}/T_C$ ( $T_N$ )	1	1	1	2.8	1.71	1.75
$\mu_0 H_{c,\text{crit}}(T)$	—	—	—	0.085	1.6	14 [14]
$\mu_0 H_{b,\text{crit}}(T)$	12.5	12.1 <sup>a</sup>	8.3	6.6	7.7	21 [14]
$\mu_0 H_{b,\text{crit}}/T_C$ ( $T_N$ )	1.32	1.33 <sup>a</sup>	1.33	1.69	1.1	1.27
$\mu_0 H_{b,\text{crit}}/T_{\max}$	1.32	1.33 <sup>a</sup>	1.33	0.60	0.64	0.72
$\mu_{\text{eff}}(a)$ ( $\mu_B/\text{f.u.}$ )	—	1.55	1.51	1.42	1.29	1.02
$\mu_{\text{eff}}(b)$ ( $\mu_B/\text{f.u.}$ )	—	2.12	2.12	2.11	2.3	2.52
$\mu_{\text{eff}}(c)$ ( $\mu_B/\text{f.u.}$ )	—	1.78	1.73	1.73	1.67	1.66
$\mu_{\text{sp}}(\mu_B/\text{f.u.})$	0.43 [31]	0.39	0.24	—	—	—
$\theta_p(a)$ (K)	—	−109	−131	−118	−112	−97
$\theta_p(b)$ (K)	—	−17.2	−11.1	−13.7	−20.3	−34.1
$\theta_p(c)$ (K)	—	5.5	3.4	4.5	3.9	−10
$\chi_0(a)$ ( $10^{-8}$ mol/m <sup>3</sup> )	—	1.19	1.17	1.18	1.33	1.39
$\chi_0(b)$ ( $10^{-8}$ mol/m <sup>3</sup> )	—	0.88	0.91	0.88	0.58	0.25
$\chi_0(c)$ ( $10^{-8}$ mol/m <sup>3</sup> )	—	1.23	1.19	1.18	1.36	1.10
$\gamma$ (mJ/mol K <sup>2</sup> )	163 [20]	160	175	$\sim 120$	$\sim 70$	16
$\Delta C_p/T$ (mJ/mol K <sup>2</sup> )	200 [12]	180	75	$\sim 20$	$\sim 80$	750
$S_{\text{mag}}$ ( $R \ln 2$ )	0.2 [31]	0.17	0.073	—	—	0.23

<sup>a</sup>Values were estimated with assumption of a constant  $H_{b,\text{crit}}/T_C$  ratio deduced from the observed experimental values for FMs URhGe and  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ .

The temperature dependent inverse magnetic susceptibilities are strongly nonlinear up to 400 K. We had to use a modified Curie-Weiss law [36], which gives good agreement with the data in the interval  $\sim 30$ –400 K. Calculated magnetic constants for all materials are summarized in Table II.

Effective magnetic moments are reduced compared with free  $\text{U}^{3+}$  and  $\text{U}^{4+}$  ionic values in all compounds along all three axes. Magnetization isotherms show the hard magnetization  $a$  axis. The easy magnetization axis is the  $c$  axis. The spontaneous magnetic moment of the FM compounds  $\mu_{\text{sp}}$  gradually decreases with increasing Ir content, having almost

half the value at the AFM/FM boundary of that of parent URhGe (Table II). Hysteresis of the FM compounds at temperature 1.8 K is significantly suppressed to a value of only  $\sim 0.001$  T.

A metamagnetic jump instantly appears in the first AFM compound  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  at the critical field of the spin-flop transition  $\mu_0 H_{c,\text{crit}} = 0.085$  T [Fig. 7(c), inset]. The metamagnetic transition clearly disappears at  $T_N$ , which is strong evidence of the intrinsic bulk AFM. The  $H_{c,\text{crit}}$  of  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  is lower than that applied magnetic field in previous paper, which considered this compound to be FM.

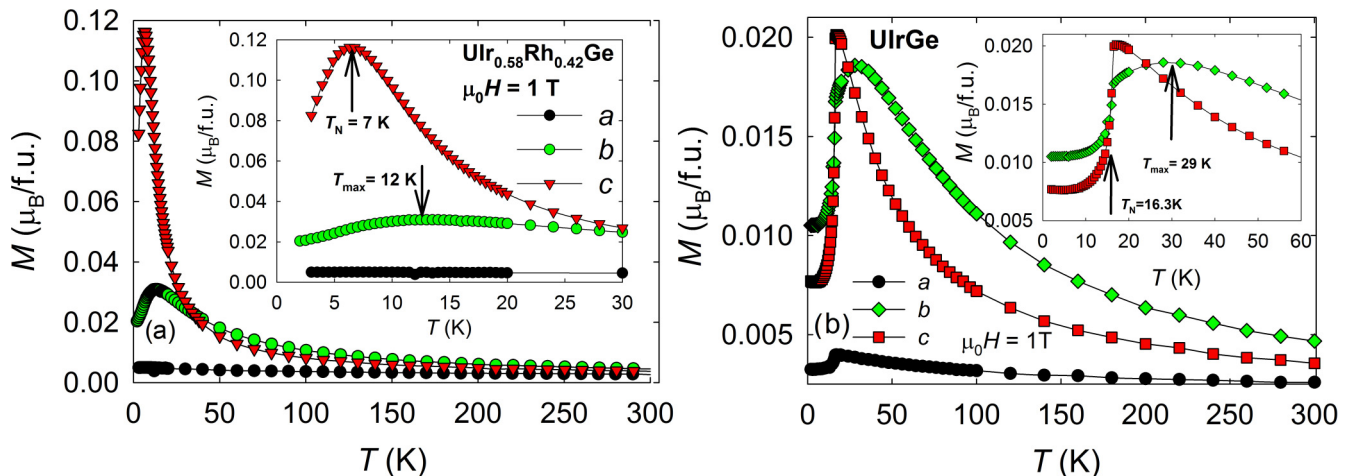


FIG. 4. Temperature dependent magnetization of AFM  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  (a) and  $\text{UIrGe}$  (b) along all three crystallographic axes.

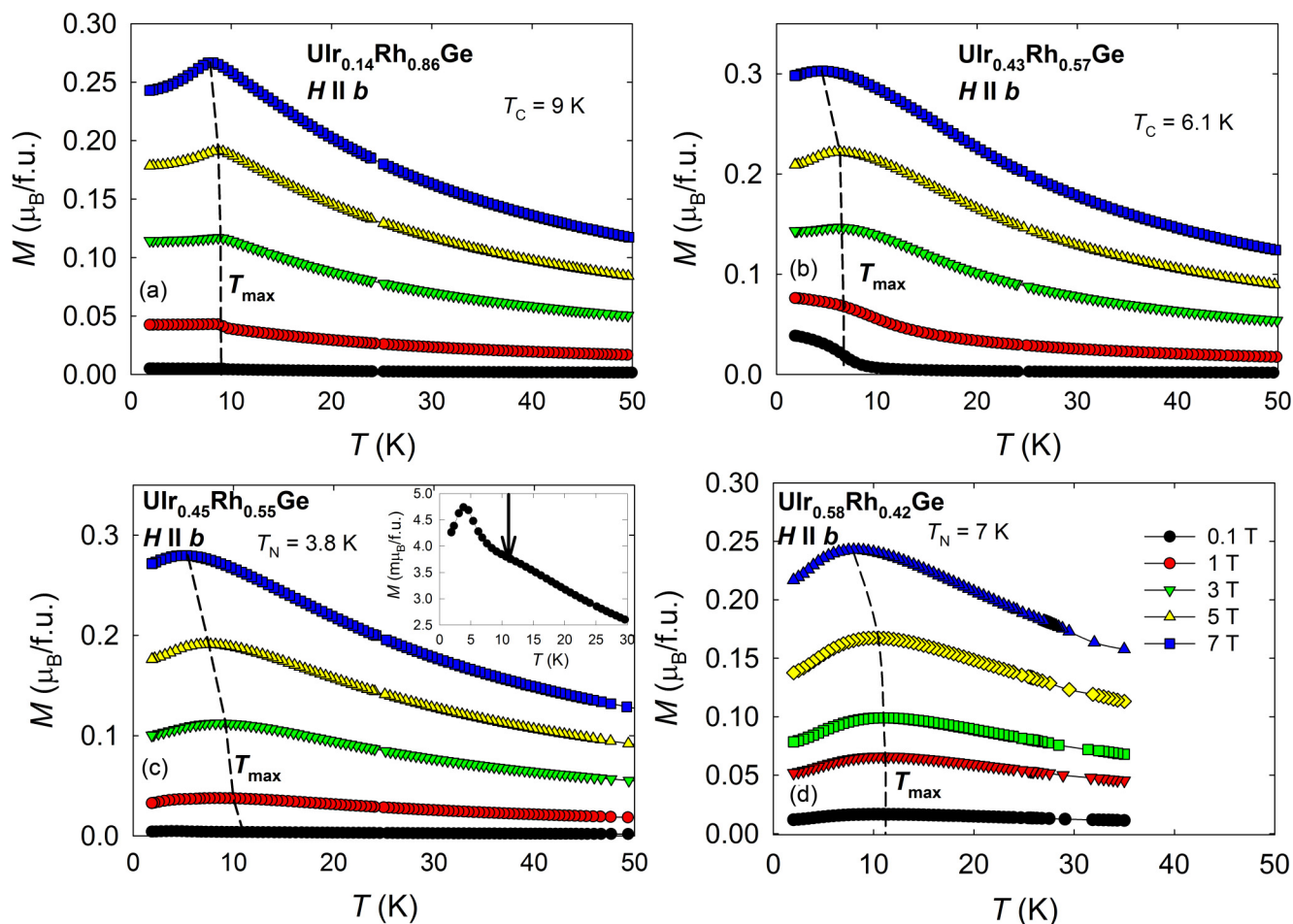


FIG. 5. Temperature dependent magnetization of all studied compounds along the  $b$  axis. The dashed lines tentatively mark the position of  $T_{\max}$  as a function of magnetic field. The inset in panel c shows the curve at 0.1 T in detail.  $T_{\max}$  is detected as a broad maximum. The peak at  $\sim 4$  K is a projection of the easy axis due to a small misalignment of the sample.

Approaching UIrGe strengthens  $H_{c,\text{crit}}$  up to a final value of 14 T (Table II).

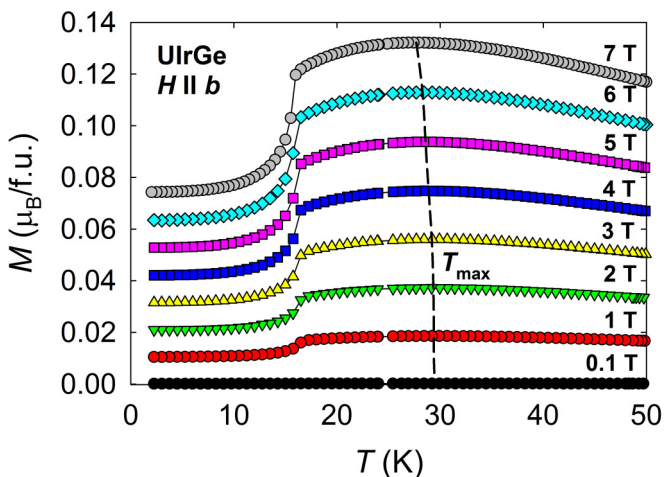


FIG. 6. Temperature dependent magnetization of UIrGe in a series of magnetic fields applied along the  $b$  axis. The dashed line tentatively marks the position of  $T_{\max}$  as a function of the magnetic field.

Magnetic moment reorientation along the  $b$  axis is a strongly studied phenomenon of URhGe because of the magnetic field-induced SC [37]. A similar spin-flip transition also appears at  $\mu_0 H_{b,\text{crit}} = 21$  T in UIrGe. We found the value of the critical field  $H_{b,\text{crit}}$  to be above the limit of a common superconducting quantum interference device (SQUID) magnetometer in  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$ . The metamagnetic transition can be inferred only just at the AFM/FM boundary by the tenuous increase of magnetization at the maximum available field [Figs. 7(b) and 7(c)]. A large value of  $H_{b,\text{crit}}$  evidently passes through the AFM/FM boundary, which will be established later by the heat capacity method.

In contrast to the  $c$  axis, the value of magnetization along the  $b$  axis grows even above  $T_N$  in the AFM compounds. Magnetization isotherms are characterized by convex curvature indicative of an additional metamagnetic transition existing above  $T_N$ . The maximum magnetization and linear character of the magnetization isotherms are reached at temperature  $T_{\max}$  (see the example in Fig. 8), which raises the question of whether the metamagnetic jump along the  $b$  axis is associated with  $T_N$  or  $T_{\max}$ . We will solve this issue later in our discussion of the  $H$ - $T$  phase diagrams.

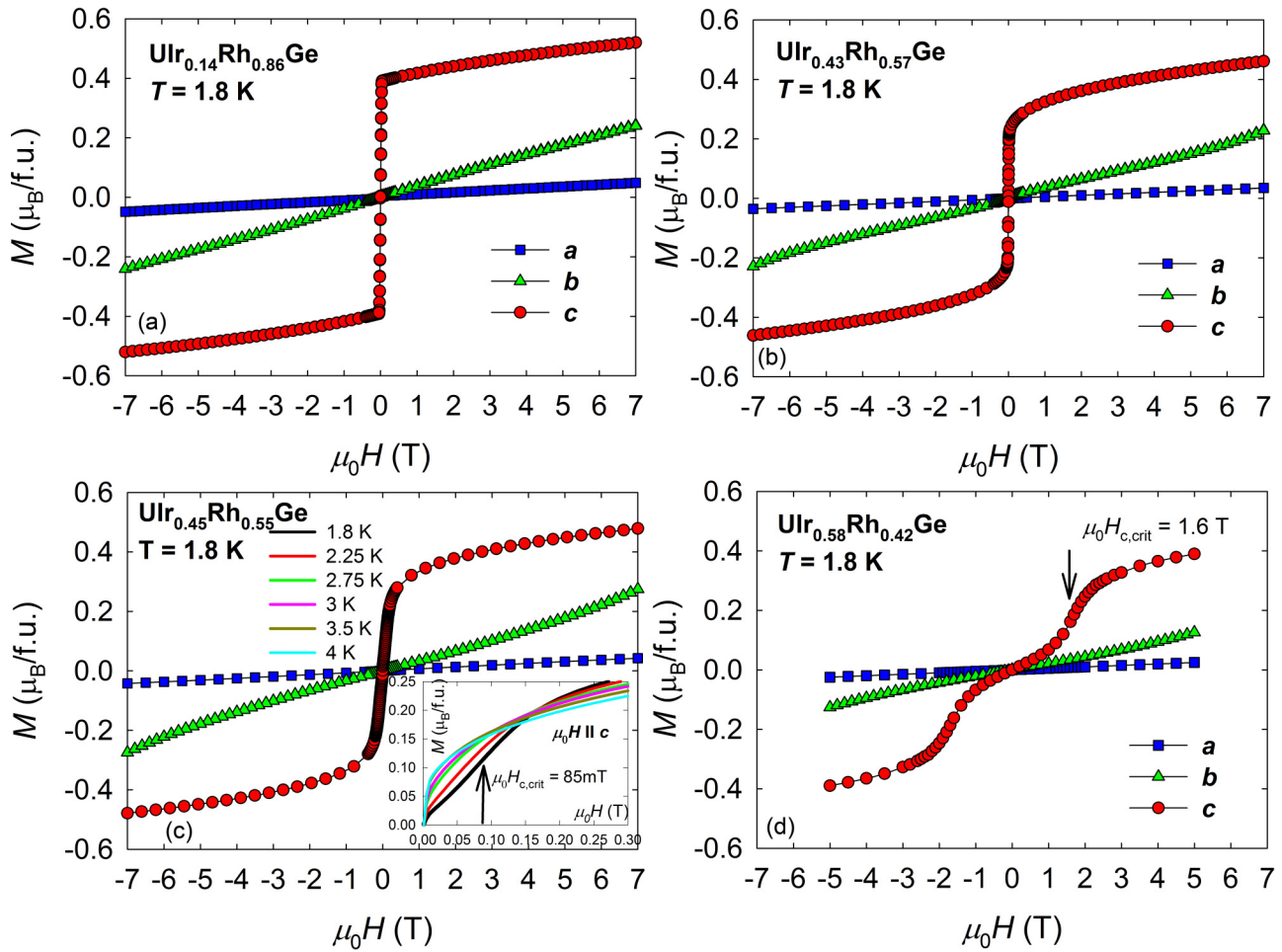


FIG. 7. Magnetization isotherms of the alloy compounds along all three crystallographic axes. The value of  $H_{c,crit}$  is taken as the inflection point of the metamagnetic jumps.

**D. Heat capacity**

Heat capacities of the FM compounds are characterized by a clear  $\lambda$ -type anomaly [Figs. 9(a) and 9(b)]. The shape

of the anomalies abruptly changes to a broad maximum on the AFM side, which gradually transforms into the  $\lambda$ -type anomaly of pure UIrGe [Figs. 9(c)–9(f) and 10]. Nevertheless, the rapid drop of the heat capacity below  $T_N$  typical for all AFM

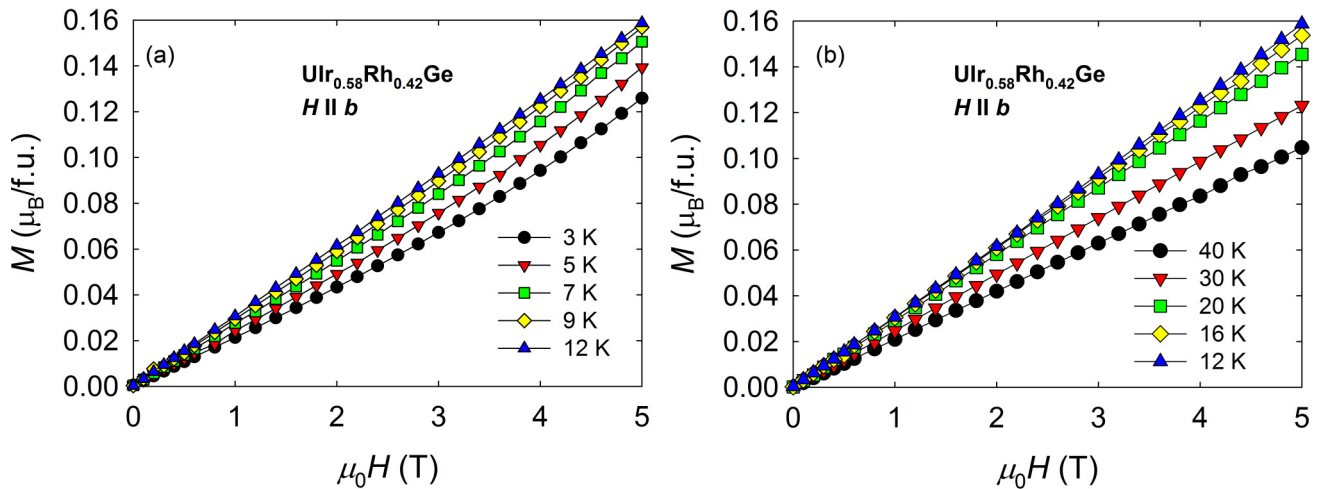


FIG. 8. Representative magnetization isotherms along the  $b$  axis. Maximum magnetization of  $UIr_{0.58}Rh_{0.42}Ge$  ( $T_N = 7$  K) along the  $b$  axis was reached at 12 K, corresponding to  $T_{max}$ . The isotherms have Brillouin characters above this characteristic temperature.

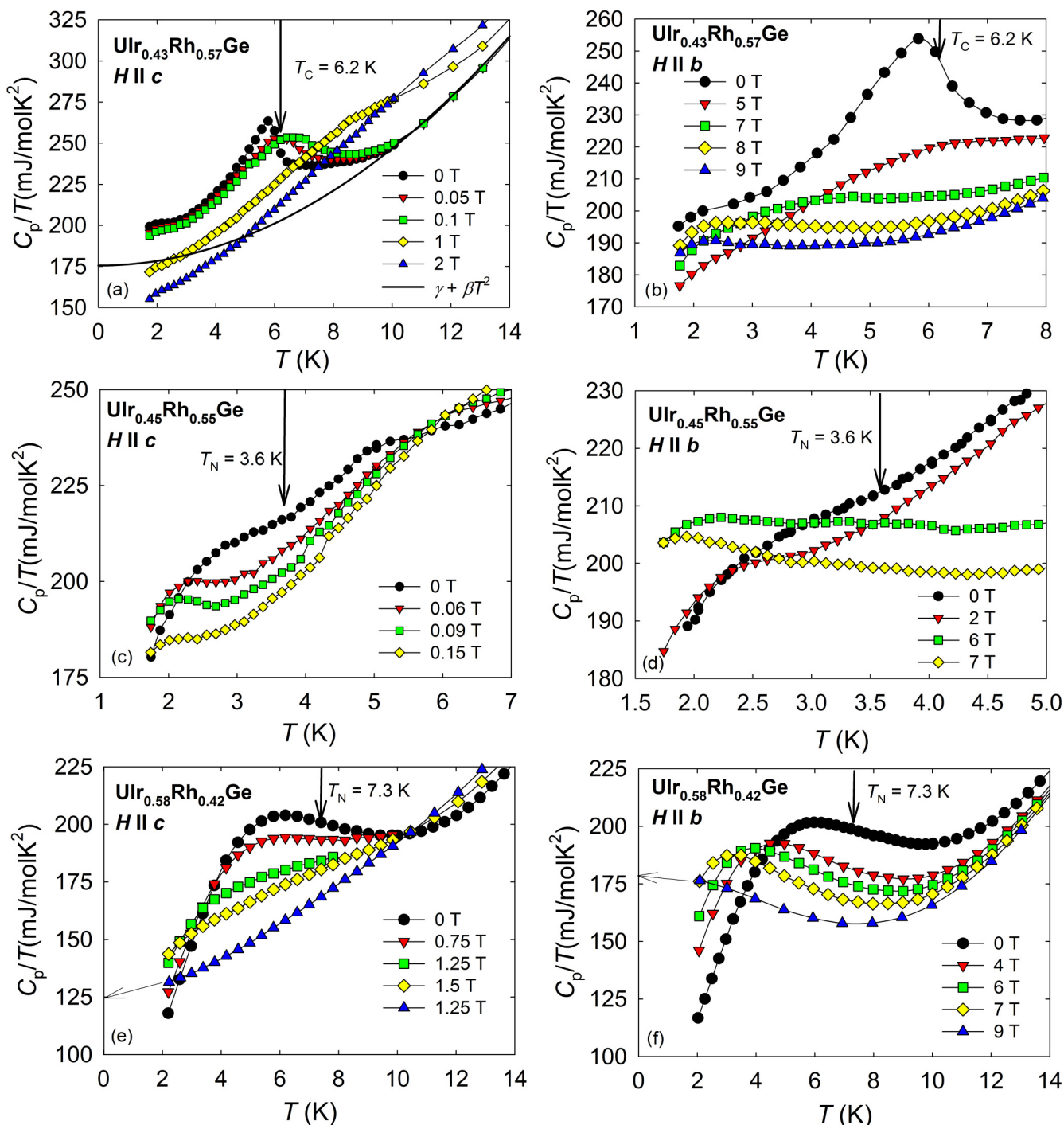


FIG. 9. Heat capacity of  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ ,  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$ , and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$ . Left panels show data in the magnetic field applied along the  $c$  axis, and the right panels show data in the magnetic field applied along the  $b$  axis. Black arrows mark the positions of the ordering temperatures. Two broad maxima are detected in the  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  data. The upper maximum is a result of the nascent FM phase, and the bottom maximum at 3.6 K represents the dominant AFM phase. We estimated the volume of the FM phase at  $\sim 15\%$  by considering the considerably reduced FM peak compared with pure FM  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ . There is also evidence of the restoration of the peak in the FM  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$  in panel b at 2.5 K and 9 T. The originally very broad maximum transforms to a narrow peak in  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$  at  $\sim 2$  K and in the magnetic field 0.09 and 7 T along the  $c$  and  $b$  axes visible in panels (c) and (d). The effect is less clear in  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$ .

$\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  is maintained, even though the  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  peak close to the boundary is rather weak. The ordering temperatures were established as the onsets of the peaks and are consistent with the results of magnetization data.  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  also provides evidence of the discontinuity

between the  $T_C$  and  $T_N$  [Figs. 9(c) and 9(d)]. We detected here a portion ( $\sim 15\%$ ) of the nascent FM phase with ordering temperature  $\sim 6$  K, while the predominant AFM phase has clearly decreased  $T_N = 3.7$  K with no sign of merging.

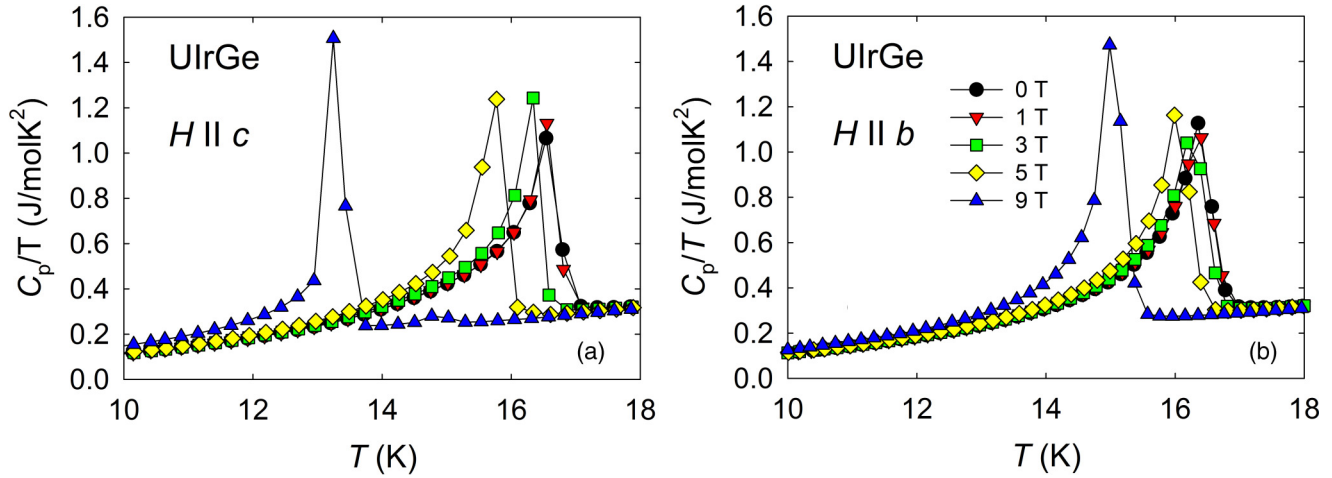


FIG. 10. Heat capacity of UIrGe. (a) Data with magnetic field applied along the  $c$  axis and (b) data with magnetic field applied along the  $b$  axis. There is evidence of narrowing and increase of peak height  $\Delta C_p/T_{\text{UIrGe}}$  at the maximum magnetic field in both panels.

Magnetic anomalies along the  $c$  axis rapidly vanish in a magnetic field in all compounds. A significantly larger magnetic field must be applied along the  $b$  axis (Fig. 9).

We extracted the phonon parts  $C_{\text{ph}}$  by an identical procedure used previously for URhGe and UIrGe [6,31]. The Debye model and the low temperature expression  $C_p/T = \gamma + \beta T^2$  are used to analyze the experimental data, giving similar Debye temperatures. The calculated magnetic entropy  $S_{\text{mag}}$  is reduced from  $0.2R \ln 2$  in URhGe downward to  $0.073R \ln 2$  in the ultimate FM UIr<sub>0.43</sub>Rh<sub>0.57</sub>Ge (Table II). Calculated Debye temperatures of 198 K and 202 K using the formula  $\theta_D^3 = 3(12\pi^4 R/5\beta)$ , where  $R$  is the gas constant and  $\beta$  is the phonon coupling constant, of FM UIr<sub>0.14</sub>Rh<sub>0.86</sub>Ge and UIr<sub>0.43</sub>Rh<sub>0.57</sub>Ge are similar to those of the parent compounds URhGe and UIrGe.

We point out a discrepancy with the previously published heat capacity data and the  $\Delta C_p/T_{\text{UIrGe}}$  parameter. A significantly lower and broader peak is reported by Prokes *et al.* [6] and Ramirez *et al.* [7] and a double peak anomaly probably due to a parasitic grain in Chang *et al.* [38], compared with Yoshii *et al.* [14]. Our experimental observation of  $\Delta C_p/T_{\text{UIrGe}} \approx 750 \text{ mJ/mol K}^2$  on a high-quality single crystal (RRR of 36) is in agreement with Yoshii *et al.* [14]. However,  $S_{\text{mag}} = 0.23R \ln 2$  is still in agreement with the Prokes *et al.* paper [6] due to the much narrower character of the peak. It seems that the high-quality samples narrow and increase the heat capacity peak, but magnetic entropy  $S_{\text{mag}}$  remains conserved.  $S_{\text{mag}}$  of UIrGe is the same as for URhGe, although  $\Delta C_p/T$  is almost four times larger. The high  $\Delta C_p/T_{\text{UIrGe}}$  is presumably the result of the opening of a large AFM gap at  $T_N$  [6].

A specific feature of the heat capacity is development of peak shapes of the transitions close to magnetic field  $H_{\text{crit}}$ , particularly in UIrGe. The original  $\lambda$ -type anomaly associated with the second order transition is transformed to a sharp peak of a first order–like transition of the considerably larger jump in  $\Delta C_p/T_{\text{UIrGe}}^{14\text{T}} \approx 2600 \text{ mJ/mol K}^2$ . Our experimental observations (Fig. 10) are in agreement with the data in Ref. [39]. The clear  $\lambda$ -type peak in the heat capacity data of FM UIr<sub>0.43</sub>Rh<sub>0.57</sub>G begins broad in the magnetic field along  $b$ . However, the peak restores at  $\sim 2.5$  K and magnetic fields

8 and 9 T [Fig. 9(b)]. Narrow peaks are also developed in the AFM UIr<sub>0.45</sub>Rh<sub>0.55</sub>Ge [Figs. 9(c) and 9(d)] at 2 K and magnetic field close to  $H_{\text{crit}}$  along the  $b$  and  $c$  axes. The effect was not observable in UIr<sub>0.58</sub>Rh<sub>0.42</sub>Ge [Figs. 9(e) and 9(f)].

We use heat capacity to estimate the value of the  $H_{\text{crit}}$ , which should be clearly detectable, in the thermodynamic Maxwell relation

$$\left(\frac{\partial S}{\partial H}\right)_T = \left(\frac{\partial M}{\partial T}\right)_H \quad (1)$$

Assuming the Fermi liquid state with  $\sim T^2$  dependence of  $M$ , one can obtain the field derivative of  $\gamma$  by the differentiation of Eq. (1) with respect to temperature.

$$\left(\frac{\partial \gamma}{\partial H}\right)_T = \left(\frac{\partial^2 M}{\partial T^2}\right)_H = 2\beta \quad (2)$$

We experimentally performed field dependent scans of the heat capacity within this theoretical approach (see the results in Fig. 11). Because of finite temperature, we plot the results as  $C_p/T$ . The using of a commercial PPMS <sup>3</sup>He heat capacity puck down to 0.4 K was impossible because of the strong mechanical force of the highly anisotropic samples in the magnetic field applied along the hard magnetization axes.  $H_{\text{crit}}$  is another quantity supporting the discontinuous AFM/FM boundary. A step of  $\sim 1.7$  T was observed between the  $H_{b,\text{crit}}$  values of FM UIr<sub>0.43</sub>Rh<sub>0.57</sub>Ge and AFM UIr<sub>0.45</sub>Rh<sub>0.55</sub>Ge. The magnetic field dependent heat capacity isotherms are also a tool to uncover the intrinsic character of the magnetic ground state of the each compound, particularly in the vicinity of the AFM/FM boundary. A decreasing character of  $C_p/T$  is observed only in the FM compounds in magnetic fields applied along the  $c$  axis [Fig. 11(a)]. In contrast, maxima corresponding to  $H_{c,\text{crit}}$  are seen in the heat capacity isotherms [Figs. 11(c) and 11(e)] of the AFM compounds, in agreement with the magnetization data (Table II). The height of the maxima along the  $c$  axis are approximately two-fifths the height along the  $b$  axis in both cases.

A curvature of the heat capacity isotherms along the  $b$  axis is maintained even above  $T_N$  [Figs. 11(d) and 11(f)]. This trend substantially weakens at temperatures close to  $T_{\text{max}}$ . The



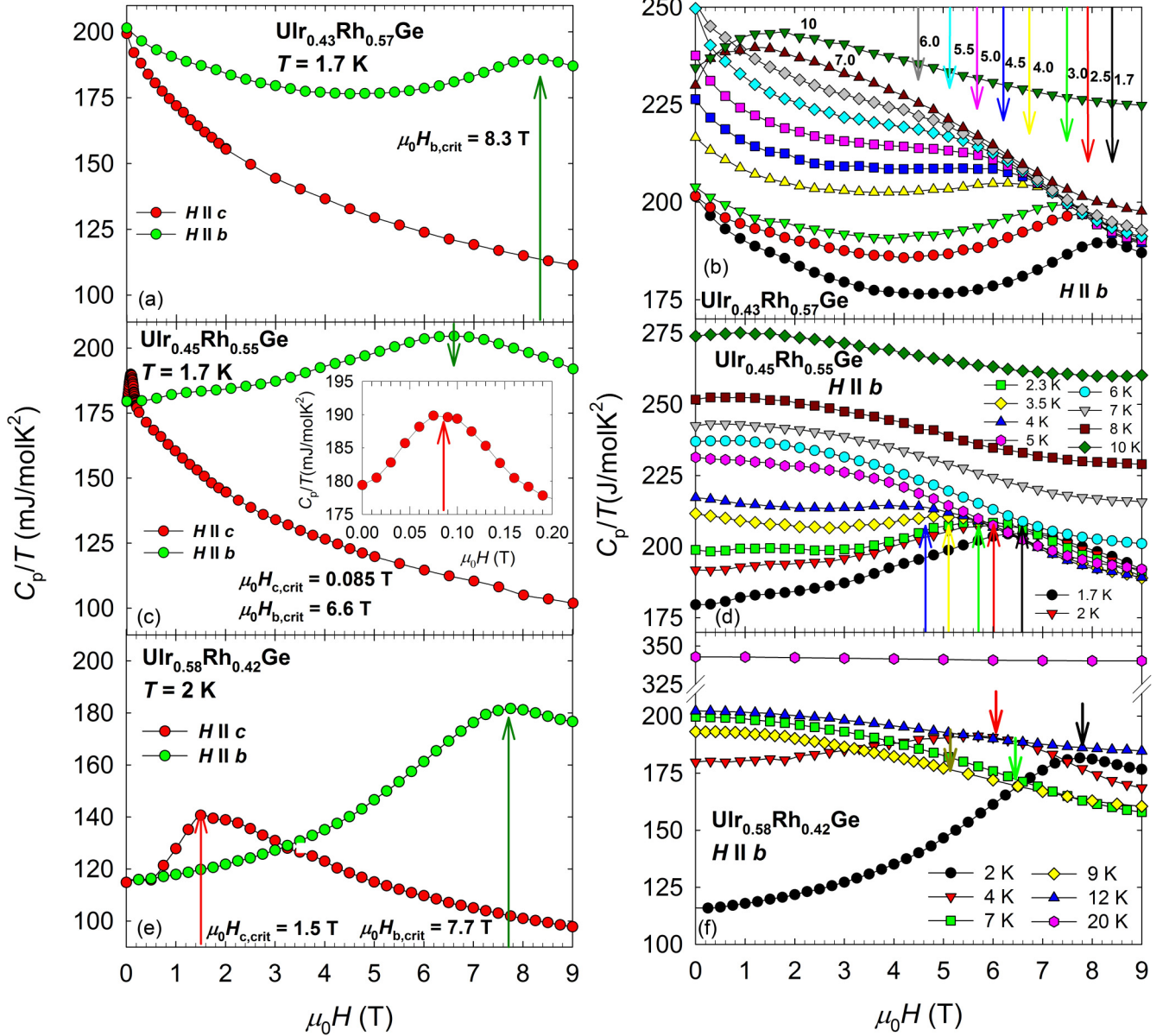


FIG. 11. Field dependent experimental heat capacity data  $C_p/T$  of  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$  (a,b),  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  (c,d), and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  (e,f) in an external magnetic field applied along the  $c$  and  $b$  axes at various temperatures. The arrows point to the values of  $H_{b,crit}$  used for later construction of the  $H$ - $T$  phase diagrams.

recorded isotherms will be used for later construction of the  $H$ - $T$  phase diagrams.

The FM  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  is characterized by an almost constant value of  $\gamma$  with weak growth toward the boundary (Fig. 12). Here, the  $\gamma$  coefficient suddenly falls and approaches  $\gamma_{\text{UIrGe}} = 16 \text{ mJ/mol K}^2$  (Table II).

The  $\gamma$  coefficient is rather reduced in value compared with the FM SCs  $\text{UCoGe}$  and  $\text{URhGe}$ , of  $\gamma \approx 60$  and  $160 \text{ mJ/mol K}^2$ , respectively [3,31]. On the other hand, extrapolation of the paramagnetic region of the  $C_p/T$  data to zero temperature using  $C_p/T = \gamma + \beta T^2$  points to a significantly larger value of  $\gamma_{\text{URhGe}}^{\text{band}} \approx 110 \text{ mJ/mol K}^2$  (Fig. 13). The  $\gamma_{\text{URhGe}} \approx 160 \text{ mJ/mol K}^2$  is  $\sim 50 \text{ mJ/mol K}^2$  higher than that of  $\gamma_{\text{URhGe}}^{\text{band}} \approx 110 \text{ mJ/mol K}^2$  [20]. On the other hand,  $\gamma_{\text{UIrGe}} \approx 16 \text{ mJ/mol K}^2$  is  $\sim 100 \text{ mJ/mol K}^2$  lower, indicative of a low density of  $5f$  states at the Fermi energy ( $E_F$ ),

probably due to opening of an AFM gap. We will discuss below the renewal of magnetic fluctuations in AFM compounds by magnetic fields along the  $b$  and  $c$  axes.

## IV. DISCUSSION

### A. The AFM/FM boundary in $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$

We collected magnetic parameters of all the studied compounds in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system and constructed a magnetic phase diagram (Fig. 14). The remarkable result is confirmation of the discontinuity in all magnetic quantities between the utmost AFM  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  and FM  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ . We detected the discontinuity in the ordering temperatures as well as in  $H_{b,crit}$  and a finite value of  $H_{c,crit}$  on the AFM side. The discontinuity of the first order transition between the FM and AFM at critical concentration of  $\sim \text{UIr}_{0.44}\text{Rh}_{0.56}\text{Ge}$  is also

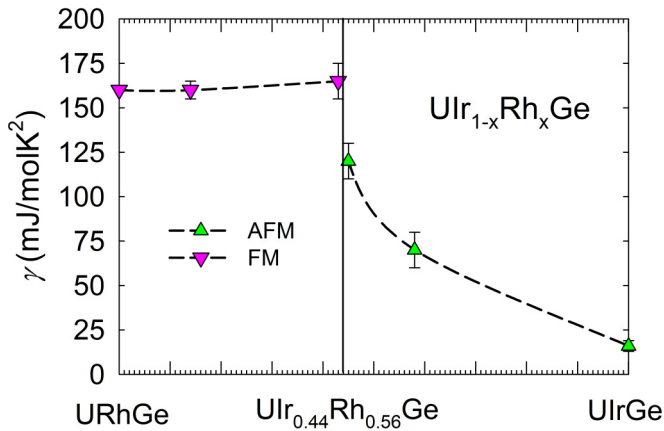


FIG. 12. Evolution of the Sommerfeld coefficient  $\gamma$  in the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system obtained by extrapolation of the data using  $C_p/T = \gamma + \beta T^2$ .  $\gamma$  of AFMs  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  were estimated by tentative extension of the broad peaks to zero temperature, resulting in larger error bars (Fig. 13).

supported by the heat capacity of the AFM  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  with a nascent FM phase with no sign of a merger of  $T_C$  and  $T_N$ . Instead, a clear gap of  $\sim 2.3$  K was detected. A particularly important issue is the evolution of  $T_{\max}$ . It is an intriguing property of  $\text{URhGe}$  where  $T_C \approx T_{\max}$  [15,20], and this trend is maintained toward the ultimate FM compound  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ .  $T_{\max}$  suddenly splits from  $T_N$  at the AFM border.

Consider the first order transition at the FM/AFM boundary; both  $T_N$  and  $T_C$  are finite at the boundary. Such a phase diagram could be realized in a system involving two independent magnetic intra- ( $J$ ) and inter- ( $J^*$ ) chain couplings along the  $a$

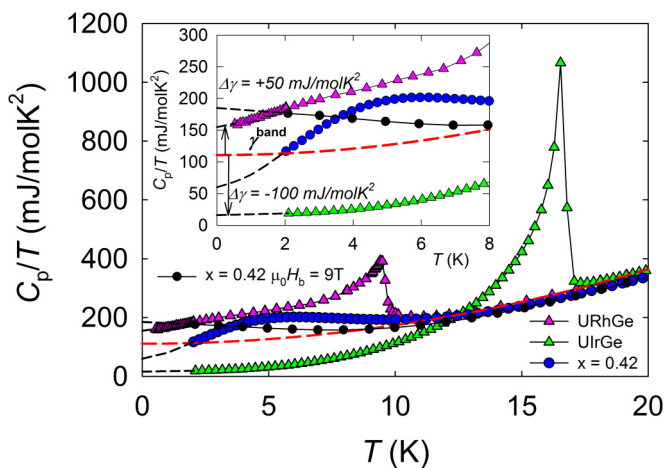


FIG. 13. Temperature dependent  $C_p/T$  of  $\text{URhGe}$ ,  $\text{UIrGe}$ , and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$ . The red line represents extrapolation of the paramagnetic part of the heat capacity of  $\text{URhGe}$  using  $C_p/T = \gamma + \beta T^2$  to zero temperature, giving a value of  $\gamma_{\text{URhGe}}^{\text{band}} \approx 110$  mJ/molK<sup>2</sup>. Other AFM compounds  $\text{UIrGe}$  and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  are characterized by almost identical values of  $\gamma^{\text{band}}$ . The inset shows the low temperature interval. The value of  $\gamma$  in the vicinity of  $H_{b,\text{crit}}$  of the  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  compound,  $\gamma_{b,\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}}^{9T} \approx 180$  mJ/molK<sup>2</sup>, is apparently enhanced compared with the value at zero field  $\gamma_{\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}} \approx 70$  mJ/molK<sup>2</sup> and  $\gamma^{\text{band}}$ .

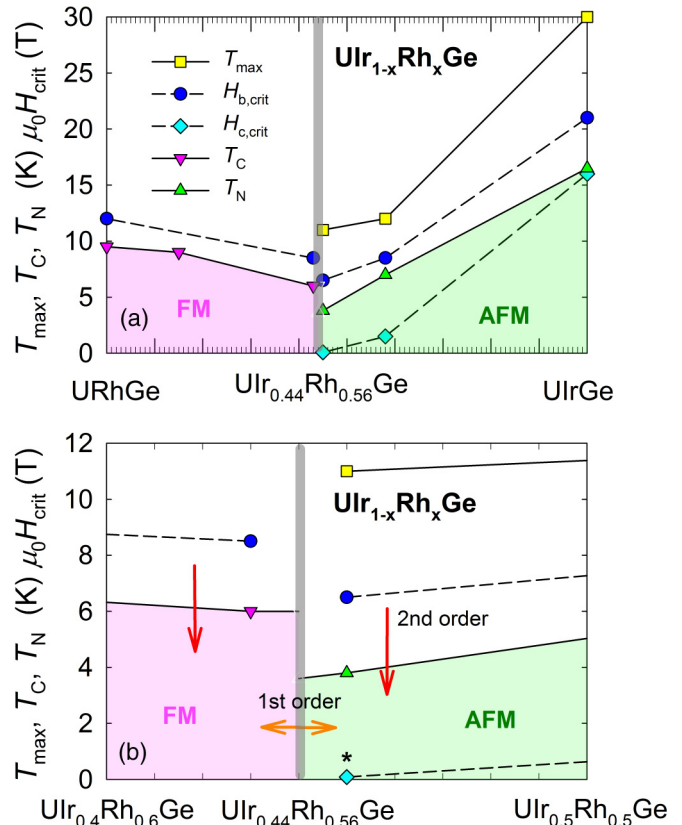


FIG. 14. Magnetic phase diagram of the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system: (a) Full concentration range and (b) area around the AFM/FM boundary in detail. The asterisk is 0.085 T (Table II). The critical concentration is tentatively established at  $x_{\text{crit}} = 0.56$ . The lines are guides to the eye.

axis. Indeed, U moments are aligned ferromagnetically along the chain in both  $\text{UIrGe}$  and  $\text{URhGe}$ . This indicates  $J > 0$  (FM) on both sides of the boundary. The AFM/FM boundary can then be defined as the point where only  $J^*$  changes sign from  $J^* < 0$  (AFM for Ir) to  $J^* > 0$  (FM for Rh). Because of the discontinuous transition,  $J^* \neq 0$ . Naturally, both  $T_N$  and  $T_C$  are finite with  $J > 0$ .

Room temperature crystal structure analysis does not provide any clear solution for variation of the  $J^*-J$  balance, but an abrupt change of the lattice parameters cannot be excluded, especially since the thermal expansion coefficients  $\alpha_i$  are not well known for  $\text{UIrGe}$  around  $T_N$  [40]. It is worth noting here that the  $\text{UIrGe}$  hydride is a ferromagnet of  $T_C = 28$  K that coincides with the position of  $T_{\max}$  in the parent  $\text{UIrGe}$  [41]. However, the magnetocrystalline anisotropy and detailed crystal and magnetic structures of the  $\text{UIrGe}$  hydride are not known to shine a light on the possible development of the  $J^*-J$  balance.

The second scenario considers the effect of bandwidth  $W_d$  of the valence  $4d$  and  $5d$  states of Rh and Ir [42], respectively, affecting  $5f$ - $d$  hybridization and the spin-orbit  $s$ - $o$  interaction of the much heavier Ir ion [43]. This should be verified by detailed electronic structure investigations by angle-resolved photoemission spectroscopy or de Haas-van Alphen (dHvA) effect in  $\text{UIrGe}$ .

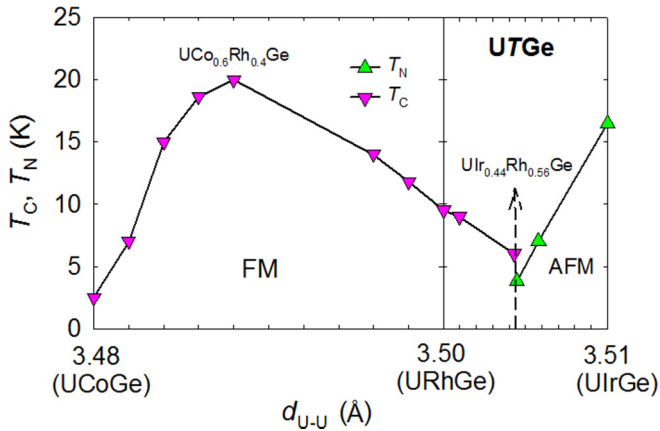


FIG. 15.  $d_{U-U}$ - $T$  phase diagram of the UCoGe-URhGe-UirGe system. The  $UCo_{1-x}Rh_xGe$  panel is constructed based on data in Ref. [23]. The width of the  $UCo_{1-x}Rh_xGe$  and  $UIr_{1-x}Rh_xGe$  panels corresponds to the nearest uranium ion distance  $d_{U-U}$ , assuming Vegard's law [45].

### B. QCP in the $UIr_{1-x}Rh_xGe$ system at $x_{crit}$

Evolution of the ordering temperature through the UCoGe-URhGe-UirGe system is displayed in the  $d_{U-U}$ - $T$  phase diagram (Fig. 15). We used the parameter  $d_{U-U}$  instead of common concentration  $x$  because the phase diagram connects together two different alloy systems. Nevertheless,  $d_{U-U}$  also is not a physically relevant parameter, and finding a better one is subject of further research.

Existence of quantum critical points (QCPs) were reported in the neighboring alloying FM-PM and AFM-paramagnetic (PM) systems  $URh_{1-x}Ru_xGe$  [29,44],  $UCo_{1-x}Fe_xGe$  [28],  $UCo_{1-x}Ru_xGe$  [4], or  $UPd_{1-x}Ru_xGe$  [21]. The  $UIr_{1-x}Rh_xGe$  system behaves like the other AFM/FM alloy system  $UPd_{1-x}Co_xGe$ , where magnetic order survives in the entire concentration range [22]. In contrast to  $UPd_{1-x}Co_xGe$ , a deep local minimum in the ordering temperatures is created at the AFM/FM boundary in  $UIr_{1-x}Rh_xGe$  almost at the level of

$T_C$  of UCoGe. Secondly, the analysis suggests here an enhancement of the coefficient  $\gamma_{UIr_{0.43}Rh_{0.57}Ge} \approx 175 \text{ mJ/mol K}^2$  (Fig. 12), the highest in the UCoGe-URhGe-UirGe system, indicating enhancement of the magnetic fluctuations typical for the development of a QCP reported in the above-listed alloy systems. However, magnetic fluctuations are interrupted in  $UIr_{1-x}Rh_xGe$  by a very stable AFM phase, and a QCP is not realized. In particular, the evolution of the  $\gamma$  coefficient in Fig. 12 confirms a sudden reconstruction of the electronic structure, probably by the AFM gap opening in the magnetic Brillouin zone.

### C. $H$ - $T$ phase diagrams

$H_b$ - $T$  phase diagrams of the FM compounds are displayed in Fig. 16. A gradual increase of Ir concentration in URhGe suppresses both  $T_C$  and  $H_{b,crit}$ . Moreover, the phase diagram in Fig. 14 has suggested uniformly decreasing  $T_C$  in the wide interval from  $\sim UCo_{0.6}Rh_{0.4}Ge$  down to  $UIr_{0.43}Rh_{0.57}Ge$ . Thus, the temperature dependence of an order parameter and energy scale of the magnetic interactions in all of these compounds seem to be of the same nature as seen in the normalized phase diagram with overlap of all curves. It has also allowed us to tentatively draw the phase diagram of  $UIr_{0.14}Rh_{0.86}Ge$ , whose critical field  $H_{b,crit}$  was higher than that of available magnetic fields in the instruments used.

The normalized phase diagram together with the recovered heat capacity anomaly of  $UIr_{0.43}Rh_{0.57}Ge$  at low temperature and magnetic field close to  $H_{b,crit}$  [Fig. 9(b)] raise a fundamental question concerning the development of the first order transition in the proximity of  $H_{b,crit}$  through the  $\sim UCo_{0.6}Rh_{0.4}Ge$ - $UIr_{0.43}Rh_{0.57}Ge$  region characterized by a monotonous decrease of  $T_C$ . Recent studies of URhGe confirmed the transformation of the second order to a first order FM/PM transition at the tricritical point (TCP) located at finite temperature with characteristic bifurcation to the wing structure phase diagram [47]. Surprisingly, a similar wing structure phase diagram was confirmed by a detailed NMR investigation of the alloying compound  $UCo_{0.1}Rh_{0.9}Ge$

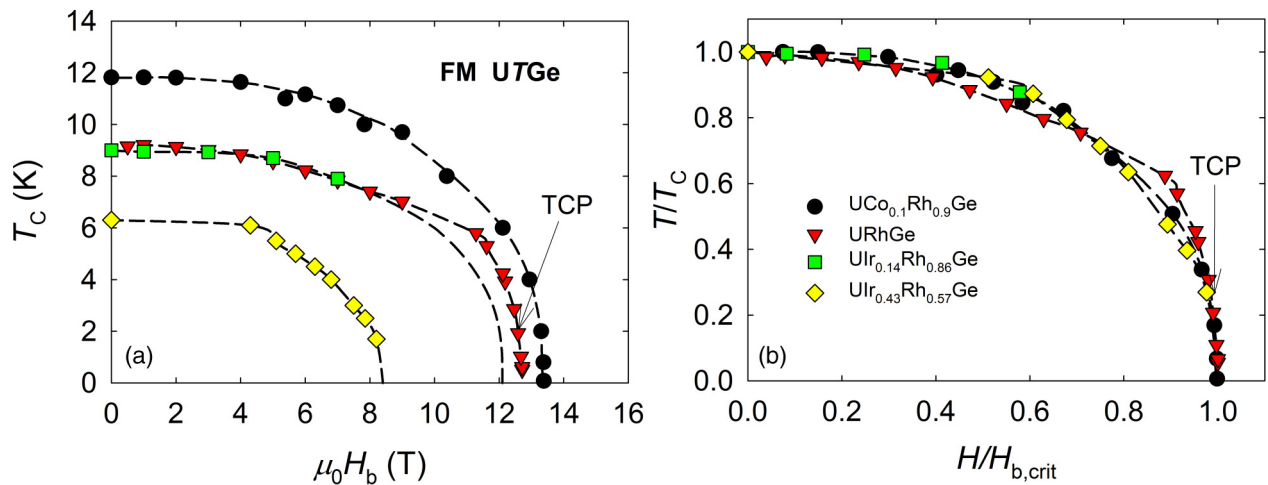


FIG. 16. (a)  $H_b$ - $T$  phase diagram of the FM compounds in the  $UIr_{1-x}Rh_xGe$  system extended about FMs  $UCo_{0.1}Rh_{0.9}Ge$  [17] and URhGe [46]. Scaling of the magnetization data was used for construction of the phase diagram of  $UIr_{0.14}Rh_{0.86}Ge$ . (b) The normalized  $H_b$ - $T$  phase diagram. The normalization parameters were taken from Table II. The dashed lines are guides to the eye. The arrows point to the location of the tricritical point (TCP) reported in URhGe [47].

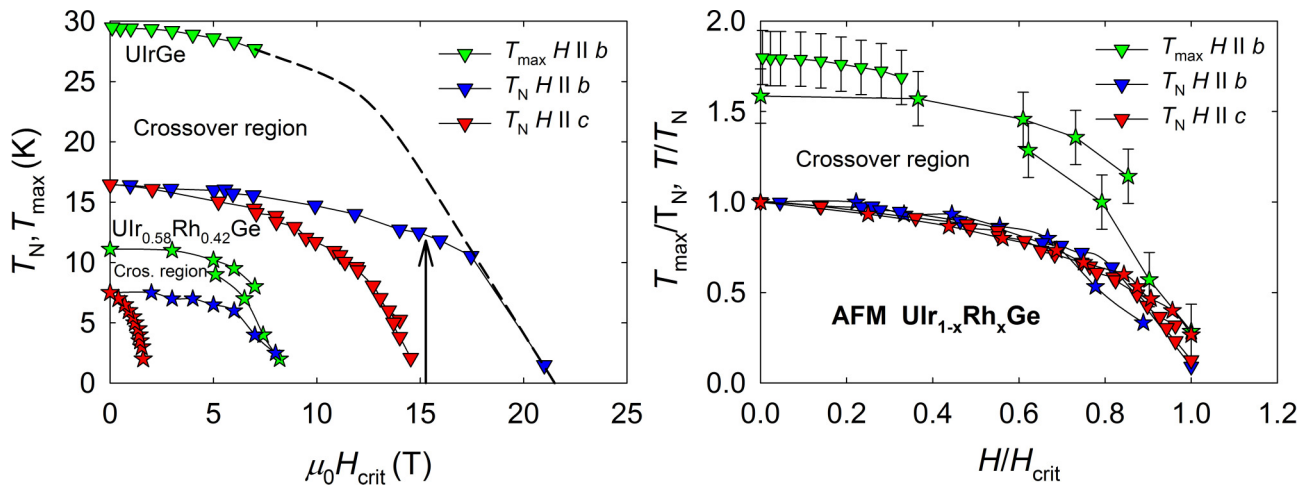


FIG. 17. (Left)  $H$ - $T$  phase diagram of UIrGe (triangles) and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  (stars) using identical color schemes. Evolution of the  $T_N$  of UIrGe was extracted from Ref. [14] and  $T_{\text{max}}$  from our magnetization data. Dashed line tentatively marks evolution of  $T_{\text{max}}$  in high magnetic fields. Complete dome of the  $T_{\text{max}}$  of  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  was constructed using the magnetization and heat capacity data. (Right) Normalized version of the  $H$ - $T$  phase diagram. The normalization parameters were taken from Table II. The black arrow marks the magnetic field  $H_b$  where the peak-like anomaly signaling a first order transition is reported in Ref. [14]. The crossover region is clearly demarked by  $T_{\text{max}}$  and  $T_N$  in the magnetic field along the  $b$  axis.

[17], which is incorporated in Fig. 16. It is in contrast to the prediction for the FM/PM quantum phase transition in the disordered FM metallic systems where a continuous second order phase transition is maintained down to zero temperature [48,49].

$\text{UCo}_{1-x}\text{Rh}_x\text{Ge}$  and  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  may represent a particular case where the first order transition is attainable in a magnetic field along the  $b$  axis at finite disorder strength, because there are essential differences compared with the alloy systems with QCP. First,  $\text{UCo}_{1-x}\text{Rh}_x\text{Ge}$  and  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  represent alloying between isoelectronic transition metals. Another specific feature of the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system is the almost negligible variation of the ionic diameter of Rh and Ir reflected in a very weak change in the lattice parameters which inhibits a local structural disorder. Such closeness of the magnetic features was already observed in other Rh-Ir alloy systems [50,51], but we simultaneously avoid generalization of the suggested scenario of the possible first order transition for all types of isoelectronic alloy systems. Taking into account the scaling parameter  $H_{b,\text{crit}}/T_C$ , the phase diagrams in Fig. 15, and the recovered heat capacity anomaly [Fig. 9(b)] in the vicinity of  $H_{b,\text{crit}}$ , we can assume the scenario of the first order transition for all the compositions in the region of  $\sim\text{UCo}_{0.6}\text{Rh}_{0.4}\text{Ge}$ - $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ .

We constructed an identical set of  $H$ - $T$  phase diagrams for the AFM part of  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  (Fig. 17) to test the potential propagation of the first order transition near  $H_{b,\text{crit}}$  from the FM to AFM phase. We omitted  $\text{UIr}_{0.45}\text{Rh}_{0.55}\text{Ge}$  because we cannot exclude the influence of the nascent FM phase detected in the analysis. The  $H$ - $T$  phase diagram of the AFM part had to be extended by two parameters -  $H_{c,\text{crit}}$  and, especially, the characteristic temperature  $T_{\text{max}}$ , where  $T_{\text{max}} > T_N$  compared with FM  $\text{UIr}_{0.43}\text{Rh}_{0.57}\text{Ge}$ ,  $\text{UIr}_{0.86}\text{Rh}_{0.14}\text{Ge}$ ,  $\text{URhGe}$ , and, we surmise, up to  $\sim\text{UCo}_{0.6}\text{Rh}_{0.4}\text{Ge}$ . We performed a similar analysis of the scaling parameters  $T_{\text{max}}/T_N$ ,  $H_{b,\text{crit}}/T_N$ , and  $H_{b,\text{crit}}/T_{\text{max}}$  and found overlap between both compounds

$\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  and UIrGe (Fig. 17), signaling the presence of an identical order parameter, which is, however, different from the FM part because of the first order AFM/FM transition. The phase diagram also shows coincidence of the critical field  $H_{b,\text{crit}}$  for  $T_N$  and  $T_{\text{max}}$  of  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$ .  $T_N$  and  $T_{\text{max}}$  circumscribe a crossover region separating the AFM phase from the PM phase. The  $H_{b,\text{crit}}$  of UIrGe is too high to see the merger of  $T_N$  and  $T_{\text{max}}$  near  $H_{b,\text{crit}}$ . Taking into account the normalized phase diagram, we propose the same scenario here.

#### D. Crossover region

The constructed phase diagram in Fig. 17 opens the question as to whether the  $b$  axis crossover region circumscribed by  $T_N$  and  $T_{\text{max}}$  is a product of a specific feature of the uranium magnetism or is related to a heavy fermion phase. It seems that the crossover region is substantially reduced or does not exist in the URhGe because  $T_{\text{max}} \approx T_C$ . Then, critical field  $H_{b,\text{crit}}$  and  $T_{\text{max}}$  and  $T_C$  are proportional to a constant factor  $H_{b,\text{crit}}/T_{\text{max}} = H_{b,\text{crit}}/T_C \approx 1.33$ . On the other hand, we surmise a large area of the crossover region existing between the  $\text{UCoGe}$ ,  $\sim\text{UCo}_{0.6}\text{Rh}_{0.4}\text{Ge}$ , where  $T_{\text{max}} > T_C$ . Very high  $H_{b,\text{crit}} \sim 50$  T of  $\text{UCoGe}$  seems to be connected with  $T_{\text{max}}$  not having any relation to  $T_C$ . Identically,  $T_{\text{max}} > T_N$  in the AFM  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$ , but both seem to have one common  $H_{b,\text{crit}}$ . Thus, the relation between  $T_C$ ,  $T_N$ ,  $T_{\text{max}}$ , and  $H_{b,\text{crit}}$  evidently varies through the system and is summarized in Fig. 18. A manuscript supporting the scenario of  $T_{\text{max}}$  evolution through the  $\text{UCoGe}$ - $\text{URhGe}$  system is in preparation.

$T_{\text{max}}$  is certainly related to the energy scale of AFM ordering with relation  $T_{\text{max}} \sim 1.8T_N$  at zero field, as observed in the present paper (Fig. 17). The appearance of  $T_{\text{max}}$  is a characteristic of an itinerant magnet; a maximum of  $\chi$  can be caused due to an increase of spin fluctuation amplitude  $\langle \delta m^2 \rangle$  when a certain Fermi surface condition is satisfied [52]. In

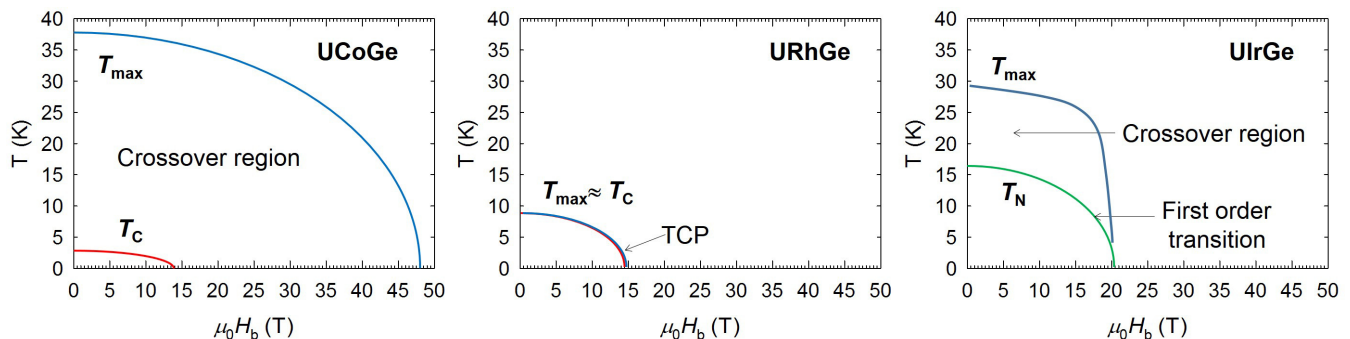


FIG. 18. Schematic  $H_b$ - $T$  phase diagrams of UCoGe, URhGe, and UIrGe. The UCoGe diagram was constructed using data from other papers [15,46], the URhGe diagram is from Ref. [15], and UIrGe diagram is from our data and the paper in Ref. [14]. The position of the TCP in URhGe was taken from Ref. [47]. The transformation from the second to first order transition in UIrGe was deduced from the heat capacity data in Ref. [14].

heavy fermion systems,  $T_{\max}$  is sometimes connected with the beginning of heavy electron formation. However, in such a case,  $T_{\max}$  is observed for the easy axis [53–57], which is not the case for the UCoGe-URhGe-UIrGe system. As  $T_{\max}$  is not observed for the  $c$  axis, but exclusively along the  $b$  axis, it may be connected rather to a particular shape of the Fermi surface.

It may be interesting to consider UCoGe, which shows high  $T_{\max} \gg T_C = 2.5$  K. As  $T_{\max}$  is observed, this compound is considered to be far from the TCP at zero field. If reentrant superconductivity does not appear at  $H_{b,\text{crit}}$  in UCoGe, it may be connected to this lack of tricriticality. Actually, in the  $\text{UCo}_{1-x}\text{Rh}_x\text{Ge}$  system, the maximum  $T_C$  appears around  $\text{UCo}_{0.6}\text{Rh}_{0.4}\text{Ge}$ , implying that tricritical and mono-FM fluctuations are enhanced around  $x = 1$  and  $0$ , respectively, which reduce  $T_C$  but are balanced out around  $\text{UCo}_{0.6}\text{Rh}_{0.4}\text{Ge}$  with the highest  $T_C$ .

### E. Magnetic fluctuation development in the AFM side of the $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$ system

Both AFM compounds UIrGe and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  were found with rather low values of the  $\gamma$  coefficient compared with common heavy fermion systems. However, the  $\gamma$  coefficient is strongly enhanced when the magnetic field is applied along the  $b$  and  $c$  axes. The  $\gamma_{c,\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}}^{2T} \approx 125$  mJ/mol K<sup>2</sup> [Fig. 9(e)] is in reasonable agreement with  $\gamma^{\text{band}} \approx 110$  mJ/mol K<sup>2</sup> (Fig. 13). An enhanced value  $\gamma_{b,\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}}^{9T} \approx 175$  mJ/mol K<sup>2</sup> was found along the  $b$  axis exceeding significantly the extrapolated  $\gamma^{\text{band}}$ .

It was shown by Hardy *et al.* [20] and Miyake *et al.* [58] that the effective mass  $m$  can be described by

$$m^* = m^{\text{band}} + m^{**},$$

where  $m^{\text{band}}$  is the renormalized band mass and  $m^{**}$  is the correlated mass associated with the magnetic instability. UIrGe and  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  are specific cases where extrapolated paramagnetic  $\gamma^{\text{band}}$  is significantly higher than real  $\gamma = 16$  or  $70$  mJ/mol K<sup>2</sup> (Fig. 13). When AFM order vanishes in  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  because of the critical magnetic field  $H_{c,\text{crit}}$  along the  $c$  axis, we received a system where  $\gamma_{c,\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}}^{2T} \approx \gamma^{\text{band}}$ . On the other hand, when the critical magnetic field  $H_{b,\text{crit}}$

is applied along the  $b$  axis, then  $\gamma_{b,\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}}^{9T} > \gamma^{\text{band}}$ , giving the magnetic instability term  $\gamma^{**} = \gamma_{b,\text{UIr}_{0.62}\text{Rh}_{0.38}\text{Ge}}^{9T} - \gamma^{\text{band}} \approx 65$  mJ/mol K<sup>2</sup>. Magnetic field along the  $b$  axis enhances fluctuations, and a magnetic instability term  $\gamma^{**}$  must be taken into account. The origin of the  $\gamma^{**}$  term in AFM  $\text{UIr}_{0.58}\text{Rh}_{0.42}\text{Ge}$  may be connected with  $T_{\max}$ , because  $T_N$  merges with  $T_{\max}$  in the vicinity of  $H_{b,\text{crit}}$  and creates the crossover region (Figs. 17 and 18). We suppose a similar scenario for the parent UIrGe at  $H_{b,\text{crit}} = 21$  T, which must be verified by a high magnetic field experiment. We note that  $m^{\text{band}}$  in the AFM state may be quite different from that in the PM state, because the Fermi surface in the AFM state is reconstructed due to the AFM magnetic Brillouin zone. The large decrease of the  $C_p/T$  in UIrGe below  $T_N$  supports this.

## V. CONCLUSIONS

We constructed the magnetic phase diagram of the  $\text{UIr}_{1-x}\text{Rh}_x\text{Ge}$  system and found discontinuity at  $x_{\text{crit}} = 0.56$  in all the magnetic parameters between the FM and AFM phase typical for the first order transition. QCP is not realized at  $x_{\text{crit}}$  because of finite  $T_C$  and  $T_N$ . However, magnetic fluctuations are moderately enhanced in the FM limit deduced from the highest  $\gamma$  through the FM phase. Magnetic fluctuations are suddenly decreased in the AFM phase. The recovery of the magnetic fluctuations in the AFM compounds is possible in applied magnetic field along the  $b$  and  $c$  axes. Stronger fluctuations are expected along the  $b$  axis, probably due to  $T_{\max}$ . We found the dome of the crossover region in the AFM compounds. Based on these findings, we constructed the  $d_{\text{U-U}}-T$  magnetic phase diagram of the UCoGe-URhGe-UIrGe system and schematic phase diagrams of the parent compounds. The relation between  $T_{\max}$  and  $T_C$ ,  $T_N$ , and  $H_{b,\text{crit}}$  seems to be an important feature of the magnetism of the UTGe compounds. Advanced high-magnetic field specific heat and dHvA measurements are desirable to further elucidate field-induced transitions in the UCoGe-URhGe-UIrGe systems.

## ACKNOWLEDGMENTS

The authors thank Z. Fisk for fruitful discussion of the experimental data. This paper was supported by Japan Society

for the Promotion of Science (JSPS) KAKENHI Grants No. 15H05884 (J-Physics), No. 16K05463, No. 15KK0149, No. 15K05156, and No. JP15H05852 and the REIMEI Research Program of Japan Atomic Energy Agency (JAEA). This paper was also supported by a Grant-in-Aid for Scientific Research C (Grant No. 25400386).

## APPENDIX

Crystal structure parameters of UIrGe.

$a$ (Å)	$b$ (Å)	$c$ (Å)	$V$ (Å <sup>3</sup> )	$d_{U-U}$ (Å)
6.8714(4)	4.3039(3)	7.5793(5)	224.15(6)	3.511
Site	$x/a$	$y/b$	$z/c$	Occ.
U ( $4c$ )	0.0067(20)	0.25	0.7023(19)	1
Ir ( $4c$ )	0.2815(20)	0.25	0.0854(19)	1
Ge ( $4c$ )	0.1831(7)	0.25	0.4132(6)	1

Crystal structure parameters of UIr<sub>0.58</sub>Rh<sub>0.42</sub>Ge.

$a$ (Å)	$b$ (Å)	$c$ (Å)	$V$ (Å <sup>3</sup> )	$d_{U-U}$ (Å)
6.8819(5)	4.3154(3)	7.5590(6)	224.494	3.511
Site	$x/a$	$y/b$	$z/c$	Occ.
U ( $4c$ )	0.0071(20)	0.25	0.7960(19)	1
Ir ( $4c$ )	0.2823(3)	0.25	0.0863(20)	0.61(2)
Rh ( $4c$ )	0.2823(3)	0.25	0.0863(20)	0.39(2)
Ge ( $4c$ )	0.1864(6)	0.25	0.4137(6)	1

Crystal structure parameters of UIr<sub>0.45</sub>Rh<sub>0.55</sub>Ge.

$a$ (Å)	$b$ (Å)	$c$ (Å)	$V$ (Å <sup>3</sup> )	$d_{U-U}$ (Å)
6.8776(5)	4.3160(3)	7.5335(7)	223.622	3.508
Site	$x/a$	$y/b$	$z/c$	Occ.
U ( $4c$ )	0.0067(3)	0.25	0.7959(3)	1
Ir ( $4c$ )	0.2825(5)	0.25	0.0858(4)	0.43(4)
Rh ( $4c$ )	0.2825(5)	0.25	0.0858(4)	0.57(4)
Ge ( $4c$ )	0.1889(10)	0.25	0.4136(9)	1

Crystal structure parameters of UIr<sub>0.43</sub>Rh<sub>0.57</sub>Ge.

$a$ (Å)	$b$ (Å)	$c$ (Å)	$V$ (Å <sup>3</sup> )	$d_{U-U}$ (Å)
6.8747(3)	4.3141(15)	7.5476(3)	223.848	3.509
Site	$x/a$	$y/b$	$z/c$	Occ.
U ( $4c$ )	0.0072(9)	0.25	0.7967(8)	1
Ir ( $4c$ )	0.2836(12)	0.25	0.0861(11)	0.54(1)
Rh ( $4c$ )	0.2836(12)	0.25	0.0861(11)	0.47(1)
Ge ( $4c$ )	0.1875(3)	0.25	0.4141(3)	1

Crystal structure parameters of UIr<sub>0.14</sub>Rh<sub>0.86</sub>Ge.

$a$ (Å)	$b$ (Å)	$c$ (Å)	$V$ (Å <sup>3</sup> )	$d_{U-U}$ (Å)
6.8823(5)	4.3294(3)	7.5236(6)	224.1749	3.507
Site	$x/a$	$y/b$	$z/c$	Occ.
U ( $4c$ )	0.0077(3)	0.25	0.7950(3)	1
Ir ( $4c$ )	0.2848(6)	0.25	0.0850(5)	0.15(3)
Rh ( $4c$ )	0.2848(6)	0.25	0.0850(5)	0.85(3)
Ge ( $4c$ )	0.1899(10)	0.25	0.4131(7)	1

- [1] H. H. Hill, *Plutonium 1970 and Other Actinides*, edited by W. N. Miner (American Institute of Mining, Metallurgical, and Petroleum Engineers, New York, 1970), p. 2.
- [2] D. Aoki, A. Huxley, E. Ressouche, D. Braithwaite, J. Flouquet, J. P. Brison, E. Lhotel, and C. Paulsen, *Nature* **413**, 613 (2001).
- [3] N. T. Huy, A. Gasparini, D. E. de Nijs, Y. Huang, J. C. P. Klaasse, T. Gortenmulder, A. de Visser, A. Hamann, T. Gorlach, and H. von Löhneysen, *Phys. Rev. Lett.* **99**, 067006 (2007).
- [4] M. Vališka, J. Pospíšil, M. Diviš, J. Prokleška, V. Sechovský, and M. M. Abd-Elmeguid, *Phys. Rev. B* **92**, 045114 (2015).
- [5] D. Aoki and J. Flouquet, *J. Phys. Soc. Jpn.* **81**, 011003 (2012).
- [6] K. Prokes, T. Tahara, T. Fujita, H. Goshima, T. Takabatake, M. Mihalik, A. A. Menovsky, S. Fukuda, and J. Sakurai, *Phys. Rev. B* **60**, 9532 (1999).
- [7] A. P. Ramirez, B. Batlogg, and E. Bucher, *J. Appl. Phys.* **61**, 3189 (1987).
- [8] K. Prokes, V. Sechovsky, F. R. de Boer, and A. V. Andreev, *J. Phys. Condens. Matter* **20**, 104221 (2008).
- [9] S. Kawamata, K. Ishimoto, Y. Yamaguchi, and T. Komatsubara, *J. Magn. Magn. Mater.* **104–107**, 51 (1992).
- [10] K. Prokes, A. de Visser, Y. K. Huang, B. Fak, and E. Ressouche, *Phys. Rev. B* **81**, 180407(R) (2010).
- [11] M. Taupin, J.-P. Sanchez, J. P. Brison, D. Aoki, G. Lapertot, F. Wilhelm, and A. Rogalev, *Phys. Rev. B* **92**, 035124 (2015).
- [12] M. Vališka, J. Pospíšil, A. Stunault, Y. Takeda, B. Gillon, Y. Haga, K. Prokeš, M. M. Abd-Elmeguid, G. Nenert, T. Okane, H. Yamagami, L. Chapon, A. Gukasov, A. Cousson, E. Yamamoto, and V. Sechovský, *J. Phys. Soc. Jpn.* **84**, 084707 (2015).
- [13] A. V. Andreev, Y. Skourski, S. Yasin, S. Zherlitsyn, and J. Wosnitzer, *J. Magn. Magn. Mater.* **324**, 3413 (2012).
- [14] S. Yoshii, A. V. Andreev, E. Brück, J. C. P. Klaasse, K. Prokeš, F. R. de Boer, M. Hagiwara, K. Kindo, and V. Sechovský, *J. Phys. Conf. Ser.* **51**, 151 (2006).
- [15] W. Knafo, T. D. Matsuda, D. Aoki, F. Hardy, G. W. Scheerer, G. Ballon, M. Nardone, A. Zitouni, C. Meingast, and J. Flouquet, *Phys. Rev. B* **86**, 184416 (2012).
- [16] F. Levy, I. Sheikin, and A. Huxley, *Nat. Phys.* **3**, 460 (2007).
- [17] Y. Tokunaga, D. Aoki, H. Mayaffre, S. Kramer, M. H. Julien, C. Berthier, M. Horvatic, H. Sakai, S. Kambe, and S. Araki, *Phys. Rev. Lett.* **114**, 216401 (2015).
- [18] D. Aoki and J. Flouquet, *J. Phys. Soc. Jpn.* **83**, 061011 (2014).

- [19] E. A. Yelland, J. M. Barraclough, W. Wang, K. V. Kamenev, and A. D. Huxley, *Nat. Phys.* **7**, 890 (2011).
- [20] F. Hardy, D. Aoki, C. Meingast, P. Schweiss, P. Burger, H. Von Lohneysen, and J. Flouquet, *Phys. Rev. B* **83**, 195107 (2011).
- [21] D. Gralak and V. H. Tran, *J. Solid State Chem.* **226**, 50 (2015).
- [22] D. Gralak, A. J. Zaleski, and V. H. Tran, *J. Solid State Chem.* **242**, 175 (2016).
- [23] N. T. Huy and A. de Visser, *Solid State Commun.* **149**, 703 (2009).
- [24] J. Pospíšil, J. P. Vejpravová, M. Diviš, and V. Sechovský, *J. Appl. Phys.* **105**, 07E114 (2009).
- [25] S. Sakarya, N. T. Huy, N. H. van Dijk, A. de Visser, M. Wagemaker, A. C. Moleman, T. J. Gortenmulder, J. C. P. Klaasse, M. Uhlarz, and H. Löhneysen, *J. Alloys Compd.* **457**, 51 (2008).
- [26] S. Sakarya, N. H. van Dijk, N. T. Huy, and A. de Visser, *Phys. B: Condens. Matter* **378–380**, 970 (2006).
- [27] J. Pospíšil, J. Gouchi, Y. Haga, F. Honda, Y. Uwatoko, N. Tateiwa, S. Kambe, S. Nagasaki, Y. Homma, and E. Yamamoto, *J. Phys. Soc. Jpn.* **86**, 044709 (2017).
- [28] K. Huang, J. J. Hamlin, R. E. Baumbach, M. Janoschek, N. Kanchanavatee, D. A. Zocco, F. Ronning, and M. B. Maple, *Phys. Rev. B* **87**, 054513 (2013).
- [29] N. T. Huy, A. Gasparini, J. C. P. Klaasse, A. de Visser, S. Sakarya, and N. H. van Dijk, *Phys. Rev. B* **75**, 212405 (2007).
- [30] B. Cordero, V. Gomez, A. E. Platero-Prats, M. Reves, J. Echeverria, E. Cremades, F. Barragan, and S. Alvarez, *Dalton Trans.* **21**, 2832 (2008).
- [31] K. Prokes, T. Tahara, Y. Echizen, T. Takabatake, T. Fujita, I. H. Hagmusa, J. C. P. Klaasse, E. Brück, F. R. de Boer, M. Divis, and V. Sechovsky, *Phys. B: Condens. Matter* **311**, 220 (2002).
- [32] B. Chevalier, E. Hickey, and J. Etourneau, *J. Magn. Magn. Mater.* **90–91**, 499 (1990).
- [33] K. Prokes, H. Nakotte, V. Sechovsky, M. Mihalik, and A. V. Andreev, *Phys. B: Condens. Matter* **350**, E199 (2004).
- [34] F. R. de Boer, K. Prokes, H. Nakotte, E. Brück, M. Hilbers, P. Svoboda, V. Sechovsky, L. Havela, and H. Maletta, *Phys. B: Condens. Matter* **201**, 251 (1994).
- [35] K. Prokes, P. F. de Chatel, E. Brück, F. R. de Boer, K. Ayuel, H. Nakotte, and V. Sechovsky, *Phys. Rev. B* **65**, 144429 (2002).
- [36] J. Pospíšil, P. Opletal, M. Vališka, Y. Tokunaga, A. Stunault, Y. Haga, N. Tateiwa, B. Gillon, F. Honda, T. Yamamura, V. Niznansky, E. Yamamoto, and D. Aoki, *J. Phys. Soc. Jpn.* **85**, 034710 (2016).
- [37] F. Levy, I. Sheikin, B. Grenier, and A. D. Huxley, *Science* **309**, 1343 (2005).
- [38] S. Chang, M. H. Jung, H. Nakotte, E. Bruck, J. C. P. Klaasse, M. Mihalik, A. H. Lacerda, K. Prokes, M. S. Torikachvili, and A. J. Schultz, *J. Appl. Phys.* **89**, 7186 (2001).
- [39] V. Sechovsky, J. Vejpravova, A. Andreev, F. Honda, K. Prokes, and E. Santava, *Phys. B: Condens. Matter* **359**, 1126 (2005).
- [40] S. Maskova, A. M. Adamska, L. Havela, N. T. H. Kim-Ngan, J. Przewoznik, S. Danis, K. Kothapalli, A. V. Kolomiets, S. Heathman, H. Nakotte, and H. Bordallo, *J. Alloys Compd.* **522**, 130 (2012).
- [41] A. M. Adamska, L. Havela, Y. Skourski, and A. V. Andreev, *J. Alloys Compd.* **515**, 171 (2012).
- [42] G. H. Lander, M. S. S. Brooks, and B. Johansson, *Phys. Rev. B* **43**, 13672 (1991).
- [43] T. Kawai, H. Muranaka, T. Endo, N. D. Dung, Y. Doi, S. Ikeda, T. D. Matsuda, Y. Haga, H. Harima, R. Setta, and Y. Onuki, *J. Phys. Soc. Jpn.* **77**, 064717 (2008).
- [44] N. T. Huy, D. E. De Nijs, A. Gasparini, J. C. P. Klaasse, A. de Visser, and N. H. van Dijk, *Phys. B: Condens. Matter* **403**, 1260 (2008).
- [45] L. Vegard, *Z. Phys.* **5**, 17 (1921).
- [46] D. Aoki, F. Hardy, A. Miyake, V. Taufour, T. D. Matsuda, and J. Flouquet, *C. R. Phys.* **12**, 573 (2011).
- [47] A. Gourgout, A. Pourret, G. Knebel, D. Aoki, G. Seyfarth, and J. Flouquet, *Phys. Rev. Lett.* **117**, 046401 (2016).
- [48] M. Brando, D. Belitz, F. M. Grosche, and T. R. Kirkpatrick, *Rev. Mod. Phys.* **88**, 025006 (2016).
- [49] Y. Sang, D. Belitz, and T. R. Kirkpatrick, *Phys. Rev. Lett.* **113**, 207201 (2014).
- [50] P. G. Pagliuso, R. Movshovich, A. D. Bianchi, M. Nicklas, N. O. Moreno, J. D. Thompson, M. F. Hundley, J. L. Sarrao, and Z. Fisk, *Phys. B: Condens. Matter* **312**, 129 (2002).
- [51] P. G. Pagliuso, C. Petrovic, R. Movshovich, D. Hall, M. F. Hundley, J. L. Sarrao, J. D. Thompson, and Z. Fisk, *Phys. Rev. B* **64**, 100503 (2001).
- [52] H. Yamada, *Phys. Rev. B* **47**, 11211 (1993).
- [53] H. Nohara, H. Kotegawa, H. Tou, T. D. Matsuda, E. Yamamoto, Y. Haga, Z. Fisk, Y. Onuki, D. Aoki, and J. Flouquet, *J. Phys. Soc. Jpn.* **80**, 093707 (2011).
- [54] C. Geibel, C. Schank, S. Thies, H. Kitazawa, C. D. Bredl, A. Bohm, M. Rau, A. Grauel, R. Caspary, R. Helfrich, U. Ahlheim, G. Weber, and F. Steglich, *Z. Phys. B* **84**, 1 (1991).
- [55] A. De Visser, A. Menovsky, and J. J. M. Franse, *Physica B+C* **147**, 81 (1987).
- [56] K. Sugiyama, M. Nakashima, M. Futoh, H. Ohkuni, T. Inoue, K. Kindo, N. Kimura, E. Yamamoto, Y. Haga, T. Honma, R. Settai, and Y. Onuki, *Phys. B: Condens. Matter* **281**, 244 (2000).
- [57] N. Tateiwa, S. Ikeda, Y. Haga, T. D. Matsuda, E. Yamamoto, K. Sugiyama, M. Hagiwara, K. Kindo, and Y. Onuki, *J. Phys. Soc. Jpn.* **80**, 014706 (2011).
- [58] A. Miyake, D. Aoki, and J. Flouquet, *J. Phys. Soc. Jpn.* **77**, 094709 (2008).