

## Control of bulk superconductivity in a BCS superconductor by surface charge doping via electrochemical gating

E. Piatti,<sup>1</sup> D. Daghero,<sup>1</sup> G. A. Ummarino,<sup>1,2</sup> F. Laviano,<sup>1</sup> J. R. Nair,<sup>1</sup> R. Cristiano,<sup>3</sup> A. Casaburi,<sup>4</sup> C. Portesi,<sup>5</sup> A. Sola,<sup>5</sup> and R. S. Gonnelli<sup>1,\*</sup>

<sup>1</sup>*Department of Applied Science and Technology, Politecnico di Torino, Torino, Italy*

<sup>2</sup>*National Research Nuclear University MEPhI, Moscow Engineering Physics Institute, Moscow, Russia*

<sup>3</sup>*CNR-SPIN Institute of Superconductors, Innovative Materials and Devices, UOS-Napoli, Napoli, Italy*

<sup>4</sup>*School of Engineering, University of Glasgow, Glasgow, United Kingdom*

<sup>5</sup>*INRIM—Istituto Nazionale di Ricerca Metrologica, Torino, Italy*

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The electrochemical gating technique is a powerful tool to tune the surface conduction properties of various materials by means of pure charge doping, but its efficiency is thought to be hampered in materials with a good electronic screening. We show that, if applied to a metallic superconductor (NbN thin films), this approach allows the observation of reversible enhancements or suppressions of the bulk superconducting transition temperature, which vary with the thickness of the films. These results are interpreted in terms of a proximity effect, and indicate that the effective screening length depends on the induced charge density, becoming much larger than that predicted by a standard screening theory at very high electric fields.

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The field effect (i.e., the modulation of the conduction properties of a material by means of a transverse electric field) is widely used in semiconducting electronic devices, namely, field-effect transistors (FETs). Recently, unprecedented intensities of the electric field—and thus densities of induced charge—have been reached by exploiting the formation of an electric double layer (EDL) at the interface between an electrolyte and the solid, when a voltage is applied between the latter and a gate electrode immersed in the electrolyte. The EDL acts as a nanoscale capacitor with a nanometric spacing between the “plates”, so that the electric field can be orders of magnitude higher than in standard field-effect (FE) devices. In these extreme conditions, new phases (including superconductivity) have been discovered in various materials, mostly semiconducting or insulating in their native state [1–5]. Instead, high-carrier-density systems such as metals and standard BCS superconductors have so far received little attention, because the electronic screening strongly limits the FE. A few works on gold [6,7] and other noble metals [8] remain the only literature about EDL gating on normal metals. More exotic metallic systems, i.e., two-dimensional (2D) materials of different classes [9–13] and complex oxides [14–20], were explored more extensively. In particular, the microscopic mechanism behind the carrier density modulation in EDL-gated oxides remains a subject of investigation [19,21–23].

The FE on BCS superconductors was investigated in the 1960's via solid dielectric [24] and ferroelectric [25] gating, and small (positive or negative) variations of the superconducting transition temperature ( $T_c$ ) were observed on increasing/decreasing the charge carrier density. Recent EDL gating experiments in Nb thin films [26] gave evidence of completely reversible  $T_c$  shifts about three orders of magnitude larger than in Refs. [24,25], though still smaller than 0.1 K. Despite the very effective electronic screening (due to unpaired electrons) the suppression of  $T_c$  was visible also in films

as thick as 120 nm. This means that the superconducting properties of the bulk were somehow changed by the applied gate voltage; otherwise, the surface layer with reduced  $T_c$  would have been shunted by the underlying bulk, giving no visible effect on the transition. A proper understanding of how this could happen is, however, still lacking [26].

In this Rapid Communication we suggest a solution to this problem—that first appeared in the literature more than 50 years ago [24,25]—by studying the  $T_c$  modulation of NbN thin films under EDL gating for different values of the film thickness  $t$ . We find that the  $T_c$  shift depends on  $t$ , thus proving that the whole bulk comes into play. If the proximity effect is taken into account within the strong-coupling limit of the standard BCS theory, this finding turns out to be compatible with a charge induction limited to the surface. We also find evidence suggesting that the volume density of the induced charge  $\Delta n_{3D}$  does not increase indefinitely with the gate voltage, but saturates at a maximum of about 0.4 electrons per unit cell—while no saturation occurs in the surface charge density  $\Delta n_{2D}$ . Thus, the electrostatic screening length increases with the gate voltage, becoming much larger than the Thomas-Fermi screening length  $\lambda_{TF}$  when  $\Delta n_{2D} > 2 \times 10^{15} \text{ cm}^{-2}$ .

NbN thin films were grown on insulating MgO substrates by reactive magnetron sputtering. The device geometry was defined by photolithography and subsequent wet etching in a 1:1 HF:HNO<sub>3</sub> solution. The inset to Fig. 1(a) shows the scheme of the samples: The strip is 135  $\mu\text{m}$  wide, with current pads on each end and four voltage contacts on each side, spaced by 946  $\mu\text{m}$  from one another. This geometry allows one to measure the voltage drop across different portions of the strip at the same time, thus defining an active (gated) and a reference (ungated) channel.

The film thickness  $t$  was measured by atomic force microscopy (AFM). Figure 1(a) shows the sheet resistance  $R_{\square}$  of the pristine film ( $t = 39.2 \pm 0.8 \text{ nm}$ ) versus temperature. The nonmonotonic behavior of  $R_{\square}(T)$  and the residual resistivity ratio  $\text{RRR} = R(300 \text{ K})/R(16 \text{ K}) = 1.05$  are characteristic of

\*renato.gonnelli@polito.it

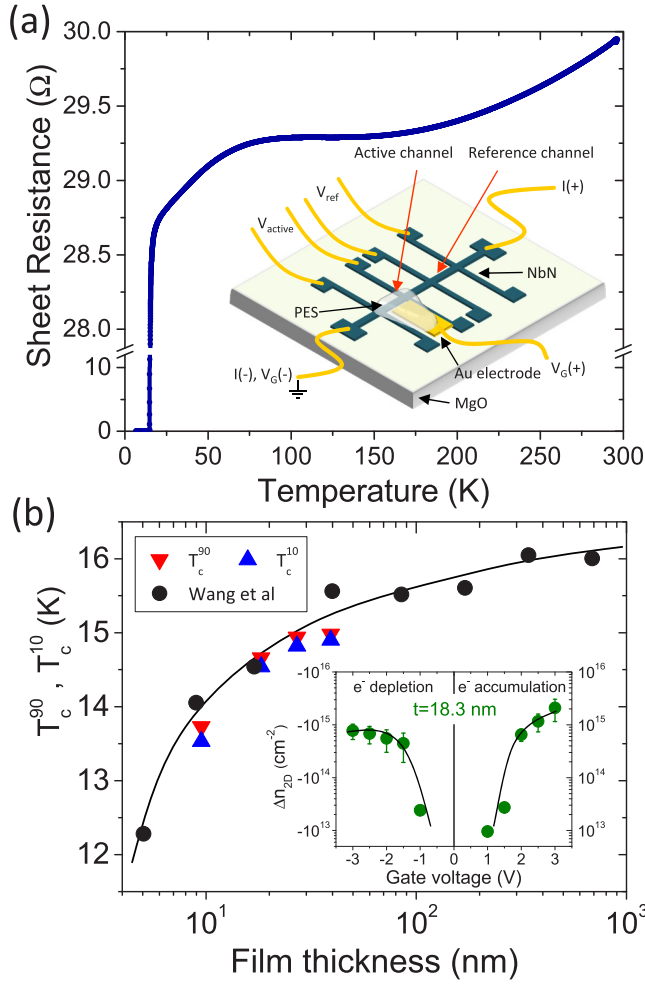


FIG. 1. (a) Sheet resistance  $R_{\square}$  as a function of temperature for the pristine 39.2-nm-thick device (prior to the PES deposition). The inset shows a scheme of the complete device. (b)  $T_c$  as a function of the film thickness: Both  $T_c^{90}$  (down triangles) and  $T_c^{10}$  (up triangles) are reported to show the variation in the transition width. Black dots are data taken from the literature [29]. Inset: Typical  $\Delta n_{2D}$  vs  $V_G$  curve determined by chronocoulometry.

granular NbN films of fairly high quality [27]. Subsequent steps of Ar-ion milling were used to reduce the thickness to  $27.1 \pm 1.5$ ,  $18.3 \pm 1.7$ , and finally  $9.5 \pm 1.8$  nm [28]. On reducing  $t$ ,  $T_c$  was suppressed [in good agreement with the curve for NbN films reported in the literature [29]; see Fig. 1(b)] and the transition width slightly increased. Both these effects are consistent with the fact that  $t$  approaches the coherence length of the material [29].

To perform EDL gating measurements, we covered the active channel and the gate counterelectrode placed on its side [made of a thin Au flake; see the inset to Fig. 1(a)] with the liquid precursor of the cross-linked polymer electrolyte system (PES), which was later UV cured.

Nb-based compounds always present a thin oxide layer at the surface (see Ref. [30] and references therein); in NbN this layer is less than 1 nm thick [30], and does not significantly reduce the gate capacitance. Indeed, EDL gating experiments performed through a thin insulating layer [13,31] indicate that

it actually minimizes the (unwanted) electrochemical reactions between sample and electrolyte.

To determine the surface electron density  $\Delta n_{2D}$  induced by a gate voltage  $V_G$ , we used the well-established electrochemical technique called double-step chronocoulometry [32]. We applied a given  $V_G$  at room temperature (above the glass transition of the PES, which occurs below 230 K) as a step perturbation, and then removed it. As shown in Ref. [33], an analysis of the gate current as a function of time allowed us to separate the contribution due to diffusion of electroreactants from that due to the EDL buildup; from the latter, one can determine the charge stored in the EDL and thus  $\Delta n_{2D}$ . A typical  $\Delta n_{2D}$  vs  $V_G$  curve is shown in the inset to Fig. 1(b). The reproducibility of the  $\Delta n_{2D}$  estimation for multiple subsequent applications of the same  $V_G$  is within  $\sim 30\%$  of the value, comparable with the uncertainty on  $\Delta n_{2D}$  of the technique itself [6].

To measure the effect of a given  $V_G$  on the transition temperature, we applied  $V_G$  at room temperature and kept it constant while cooling the device down to 2.7 K in a pulse-tube cryocooler. The voltage drops across the active and the reference channel,  $V_{\text{active}}$  and  $V_{\text{ref}}$  [see the inset to Fig. 1(a)], were then measured simultaneously during the very slow, quasistatic heating up to room temperature in the presence of a source-drain dc current of a few  $\mu\text{A}$ . By comparing the  $R_{\square}(T)$  curves of the active and reference channels measured at the same time, we were able to eliminate the possible small differences in critical temperature measured in different heating runs, and thus to detect shifts in  $T_c$  due to EDL gating as small as a few mK. For instance, the  $T_c$  shift due to  $V_G = +3$  V was evaluated as  $\Delta T_c(3 \text{ V}) = [T_c^{\text{active}} - T_c^{\text{ref}}]_{V_G=3 \text{ V}} - [T_c^{\text{active}} - T_c^{\text{ref}}]_{V_G=0 \text{ V}}$ .

Figure 2(a) shows, as an example, the effect of a gate voltage ranging between +3 and  $-3$  V on the superconducting transition of the 18.3-nm-thick film. The horizontal scale is the temperature normalized to the midpoint of the transition in the reference channel, i.e.,  $[T - T_c^{\text{ref}}]_{V_G} - [T_c^{\text{active}} - T_c^{\text{ref}}]_0$ . As for all thicknesses, the gate voltage reproducibly produces a rigid shift of the transition to a lower (higher) temperature for positive (negative)  $V_G$ , respectively. The amplitude of the reversible shift [28] is clearly correlated with the induced charge density.

Figure 2(b) shows that the amplitude of the  $T_c$  shift produced by a given gate voltage (here, +3.0 and  $-3.0$  V) is enhanced when the thickness  $t$  is reduced. This (together with the detection of negative  $T_c$  shifts for positive  $V_G$ ) suggests that the superconducting properties of the whole bulk are affected by the surface charge induction. The values of  $\Delta T_c$  vs  $\Delta n_{2D}$  for the different thicknesses are shown in Fig. 3.

Interestingly, the transition width depends on  $t$  but not on the gate voltage, indicating that the superconducting properties of the film are homogeneously modulated by the charge induction. The question then is how the electric field can induce this homogeneous perturbation in the whole thickness even in the presence of a strong electronic screening.

It is generally accepted that, at least in the limit of “weak” perturbations and linear response, the screening length in the superconducting state is the same as in the normal state, i.e., the Thomas-Fermi length [34]. This is certainly true in proximity

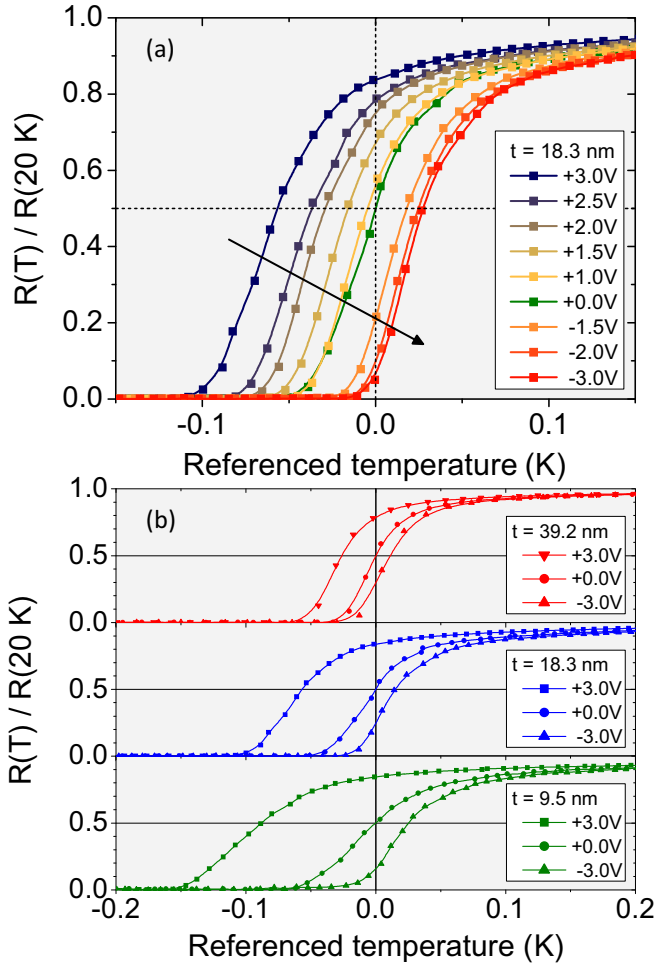


FIG. 2. (a) Normalized resistance  $R(T)/R(20\text{ K})$  of the active channel of a 18.3-nm-thick device, as a function of referenced temperature  $T^*$ , i.e.,  $T^* = [T - T_c^{\text{ref}}]_{V_G} - [T_c^{\text{active}} - T_c^{\text{ref}}]_0$ , at different gate voltages in the range  $[-3\text{ V}, +3\text{ V}]$ . (b) Effect of a gate voltage  $V_G = \pm 3\text{ V}$  on the  $R(T)/R(20\text{ K})$  vs  $T$  curve for three values of thickness: 39.2, 18.3, and 9.5 nm.

of  $T_c$  (i.e., at most 100 mK below it), where the screening is dominated by unpaired electrons since the superfluid density is very small [35]. We can thus safely assume that the electric field should decay at the NbN surface within a depth of the order of  $\lambda_{\text{TF}} \simeq 1\text{ \AA}$ .

The most likely mechanism able to turn the perturbation of the carrier density in a thin surface layer into a homogeneous perturbation of the bulk superconducting properties is the proximity effect at a normal metal/superconductor interface. In general, this is observed as the induction of a superconducting order parameter in the normal bank (close to the interface) accompanied by its suppression in the superconducting one [36]. Moreover, when the thicknesses of the two banks are sufficiently small (Cooper limit [37]), the compound slab behaves as a homogeneous superconductor whose effective electron-phonon coupling constant  $\langle \lambda \rangle$  is a weighted average of the coupling constants in the superconductor and in the normal metal [36,37]. From a scaling analysis of  $\Delta T_c$  on the thicknesses of the two banks (as explained below), we determine that the models for the proximity effect in the

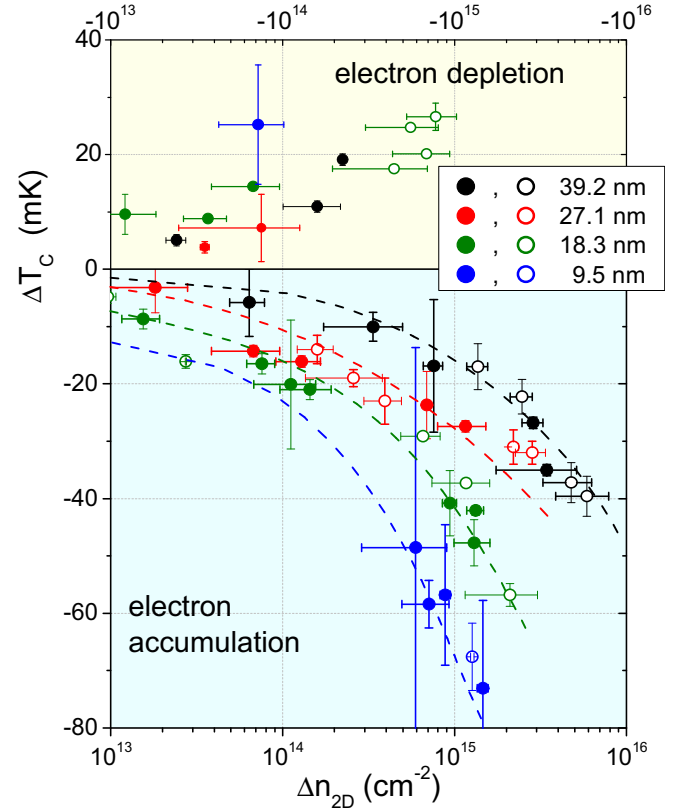


FIG. 3.  $T_c$  shift,  $\Delta T_c$ , as a function of the induced surface electron density  $\Delta n_{2D}$ , for all the film thicknesses. Dashed lines are only guides to the eye.

Cooper limit can be applied to our films [38]. Since NbN is a strong-coupling superconductor, we will actually use the strong-coupling version of the relevant model.

As a first approximation we can assume that both the characteristic temperature  $\Theta$  (representative of the phonon spectrum and thus related to the Debye temperature) and the Coulomb pseudopotential  $\mu^*$  are unaffected by the applied electric field, so that they can be obtained from literature [39]. Hence the model of Ref. [38] gives for the critical temperature of the compound slab,

$$T_{c,\text{comp}} = \frac{\Theta}{1.45} \exp \left[ -\frac{1 + \langle \lambda \rangle}{\langle \lambda \rangle - \mu^*} \right], \quad (1)$$

where

$$\langle \lambda \rangle = \frac{\lambda_s N_s d_s + \lambda_b N_b d_b}{N_s d_s + N_b d_b} = \beta_s \lambda_s + \beta_b \lambda_b. \quad (2)$$

Here, the subscripts  $s$  and  $b$  refer to surface and bulk,  $N_{s,b}$  are the densities of states (DOS) at the Fermi level,  $\lambda_{s,b}$  the electron-phonon coupling constants, and  $d_{s,b}$  the thicknesses of the layers, such that  $d_s + d_b = t$ . The condition under which the Cooper-limit model can be used [38] is that  $\Delta T_c$  scales on the ratio  $d_b/d_s$ , which is true in our case (see Fig. S5) [28]. We assume the effect of the induced charge on  $T_c$  to be mainly due to the modulation of  $N_s/N_b$ : Therefore, the coupling strength can be expressed in the simplest way as  $\lambda_s = \lambda_b(N_s/N_b)$ ,  $\lambda_b$  being calculated from the unperturbed  $T_c$  through the McMillan equation. The only remaining unknown

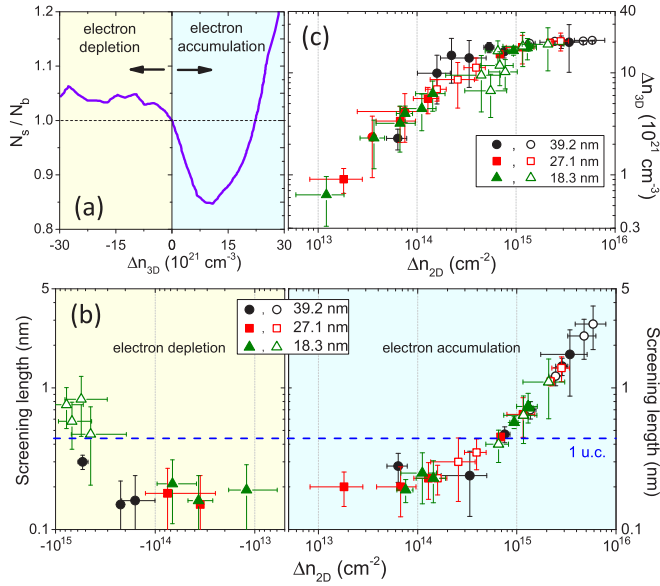


FIG. 4. (a) DOS ratio  $N_s/N_b$  of NbN as a function of  $\Delta n_{3D}$  (i.e.,  $\Delta n_{3D} = 0$  corresponds to native NbN). (b) Thickness of the perturbed surface layer  $d_s$  vs  $\Delta n_{2D}$  for both electron accumulation and depletion. The horizontal dashed line indicates the size of one unit cell of NbN. (c) Absolute value of the volume density of induced electrons (in the surface layer)  $\Delta n_{3D}$  as a function of  $\Delta n_{2D}$ .

quantity is thus the DOS ratio  $N_s/N_b$ , which can be calculated via density functional theory (DFT) once the shift of the Fermi level from the ungated value is known [see Fig. 4(a)]. This shift is determined by the volume density of induced carriers  $\Delta n_{3D}$ , while double-step chronocoulometry is able to measure the surface charge density  $\Delta n_{2D} = \int_0^t \Delta n_{3D}(z) dz$  [6]. An ansatz about how the volume charge density distributes across the thickness is thus required to determine  $N_s/N_b$ .

Since within the model in Ref. [38] the two layers of the compound slab are homogeneous, we choose for  $\Delta n_{3D}(z)$  a step profile, i.e., we assume the induced charge to be uniformly distributed in a thickness  $d_s$ , which is an adjustable parameter of our model.  $d_s$  can thus be considered an effective electrostatic screening length. For any value of  $\Delta n_{2D}$ , the choice of  $d_s$  determines  $\Delta n_{3D}$  and, consequently, (i) (by DFT calculations) the shift of the Fermi level and the perturbed DOS ratio at the surface  $N_s/N_b$ , (ii) the electron-phonon coupling strength  $\lambda_s$ , (iii) the value of  $T_{c,s}$ , and finally the critical temperature of the compound slab  $T_{c,\text{comp}}$  which has to agree with the experimental  $T_c$ .

The values of  $d_s$  that allow fitting the experimental  $T_c$  shifts are plotted as a function of  $\Delta n_{2D}$  in Fig. 4(b). Symbols of different shapes refer to different film thicknesses  $t$ . We excluded from our analysis the data for  $t = 9.5 \text{ nm}$  as we

deem the measured  $T_c$  shift not to be reliable enough due to a pronounced hysteresis of the field effect [28]. It is clearly seen that  $d_s$  does not depend on  $t$ , which is reasonable, but must vary with  $\Delta n_{2D}$ . Let us focus on the electron accumulation side, where the trend is clearer. In the low-carrier-density region,  $d_s$  roughly agrees with the Thomas-Fermi screening length  $\lambda_{\text{TF}}$  if the density of quasiparticles at  $T \simeq T_c$  is used, but already at  $7 \times 10^{14} \text{ cm}^{-2}$  it becomes as large as one unit cell ( $4.4 \text{ \AA}$ ). Without this increase in  $d_s$ , the volume charge density  $\Delta n_{3D}$  would become so large that the Fermi level would be shifted well beyond the local minimum in the DOS [see Fig. 4(a)], resulting in an increase in  $N_s$  and thus in a positive  $\Delta T_c$ , which is not the experimental result. The increase of  $d_s$  and the consequent existence of an upper limit for  $\Delta n_{3D}$  are thus qualitatively independent on the details of the proximity effect model [28]. For larger values of  $\Delta n_{2D}$ ,  $d_s$  further expands, finally reaching 4–5 unit cells. For  $\Delta n_{2D} > 5 \times 10^{14} \text{ cm}^{-2}$  the dependence of  $d_s$  on  $\Delta n_{2D}$  is remarkably linear. Note that the increase in  $d_s$  is not fast enough to keep the volume density of induced electrons  $\Delta n_{3D}$  constant [see Fig. 4(c)]; in this range,  $\Delta n_{3D}$  increases from  $1 \times 10^{22} \text{ cm}^{-3}$  ( $\sim 0.2 e^-/\text{u.c.}$ ) and tends to saturate around  $2 \times 10^{22} \text{ cm}^{-3}$  ( $\sim 0.4 e^-/\text{u.c.}$ ).

These results suggest that  $\Delta n_{3D}$  cannot exceed  $2 \times 10^{22} \text{ cm}^{-3}$  ( $\sim 0.4 e^-/\text{u.c.}$ ), and that the thickness of the surface layer departs from a Thomas-Fermi value [see Fig. 4(b)] when  $\Delta n_{3D}$  approaches this limit [see Fig. 4(c)], as if the surface layer of thickness  $\approx \lambda_{\text{TF}}$  was unable to accommodate all the induced charges. To look for an explanation of this effect, one has to abandon the Thomas-Fermi approximation: In this high charge-density regime the assumptions of weak perturbation and linear response are no longer valid since the surface potential  $\phi(z=0)$  does no longer fulfill the condition  $|e\phi(z=0)| \ll E_F$ . The screening theory beyond the linear regime [40] correctly explains the observed increase of  $d_s$  up to about  $3.6 \text{ \AA}$  when  $\Delta n_{2D} \simeq 5 \times 10^{14} \text{ cm}^{-2}$ , but above this doping value the appropriate theory is lacking [28].

In summary, we have experimentally proven that a surface charge induced by electrochemical gating can give rise to modifications of the *bulk* superconducting properties (and not only of the surface ones). This is true, surprisingly, in conventional BCS-like superconductors with a large electronic screening, and can be explained in terms of a proximity effect between the surface layer and the underlying part of the sample. We have also unveiled an increase in the effective electronic screening length that departs from the Thomas-Fermi value and increases, suggesting the existence of an upper limit for the volume charge density. These findings severely impact the study of the effects of EDL gating on high-carrier-density systems in general, and metallic superconductors in particular.

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