Magnetic transitions under ultrahigh magnetic fields of up to 130 T in the breathing pyrochlore antiferromagnet $LiInCr₄O₈$

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The magnetization processes of the spin-3/2 antiferromagnet $LiInCr_4O_8$ comprising a "breathing" pyrochlore lattice, which is an alternating array of small and large tetrahedra, are studied under ultrahigh magnetic fields of up to 130 T using state-of-the-art pulsed magnets. A half magnetization plateau is observed above 90 T to 130 T, suggesting that $LiInCr_4O_8$ has a strong spin-lattice coupling, similar to conventional chromium spinel oxides. The magnetization of $LiGa_{0.125}In_{0.875}Cr_4O_8$, in which the structural and magnetic transitions at low temperatures have been completely suppressed, shows a sudden increase above 13 T, indicating that a spin gap of 2.2 meV exists between a tetramer singlet ground state and an excited state with total spin 1, with the latter being stabilized by the application of a magnetic field. The breathing pyrochlore antiferromagnet is found to be a unique frustrated system with strong spin-lattice coupling and bond alternation.

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I. INTRODUCTION

The chromium spinel oxide $ACr₂O₄$ with a nonmagnetic A^{2+} ion, such as Zn^{2+} , Mg^{2+} , Cd^{2+} , or Hg^{2+} , is one of the most intensively studied geometrically frustrated magnets [\[1\]](#page-3-0). Cr^{3+} ions with three localized 3*d* electrons carrying an $S = 3/2$ Heisenberg spin form a pyrochlore lattice, in which antiferromagnetic interactions are dominant. $ACr₂O₄$ undergoes a long-range magnetic order with a complex spin structure, accompanied by a structural distortion, although the transition temperature is lowered due to geometrical frustration of the pyrochlore lattice [\[2–4\]](#page-3-0). Another distinctive feature of $ACr₂O₄$ is its magnetic phase transitions induced by applying a magnetic field. $ACr₂O₄$ with A = Cd and Hg exhibits magnetic transitions at magnetic fields of 28 and 10 T, respectively [\[5,6\]](#page-3-0). Above this field, magnetization curves show a plateau at half the saturation magnetization, *M*s, known as the half magnetization plateau. Neutron diffraction measurements under magnetic fields revealed a common magnetic structure at the plateau phase, namely, a ferrimagnetic order maintaining cubic crystal symmetry with each tetrahedron having a 3-up-1 down collinear spin configuration $[7,8]$. ACr₂O₄ single crystals with $A = Zn$ and Mg are also found to show half magnetization plateaus above approximately 140 T $[9-12]$. Common to the aforementioned four spinel oxides, half magnetization plateaus are formed in wide magnetic-field ranges of several tens of tesla [\[6,13–16\]](#page-3-0), in contrast to the narrow ones observed in Ising pyrochlore magnets, such as $Ho_2Ti_2O_7$ [\[17\]](#page-3-0). Theoretical studies suggest the important role of spin-lattice coupling in stabilizing the wide magnetization plateaus in $ACr₂O₄$ [\[18](#page-3-0)[,19\]](#page-4-0).

Here we focus on an A-site ordered Cr spinel oxide LiInCr₄O₈. In LiInCr₄O₈, Li⁺ and In³⁺ ions form a zincblende type order [\[20,21\]](#page-4-0). This atomic order causes chemical pressure on the Cr^{3+} pyrochlore lattice, resulting in an alternation in the size of adjacent Cr_4 tetrahedra, as shown

 $LiInCr₄O₈$ shows spin-gap behavior below 65 K with the magnetic susceptibility strongly decreasing with decreasing temperature. In this temperature region, four spins on a small tetrahedron form a tetramer singlet with the total spin on a small tetrahedron $S_t = 0$. As discussed in the studies of the pseudospin-1/2 breathing pyrochlore antiferromagnet $Ba_3Yb_2Zn_5O_{11}$, the tetramer singlet has a ground state degeneracy caused by the tetrahedral symmetry [\[22–24\]](#page-4-0). At approximately 15 K, LiInCr₄O₈ is found to exhibit successive structural and magnetic phase transitions and go into an antiferromagnetically ordered ground state on the distorted breathing pyrochlore lattice, suggestive of the presence of a strong spin-lattice coupling similar to the case of $ACr₂O₄$ [\[25–27\]](#page-4-0).

These phase transitions in $LiInCr₄O₈$ are suppressed by Ga substitutions. LiGa_{0.125}In_{0.875}Cr₄O₈ shows a similar magnetic susceptibility to that of $LiInCr_4O_8$, suggesting that the magnetic interactions are almost identical [\[28\]](#page-4-0). However, there is no peak in the heat capacity data of $LiGa_{0.125}In_{0.875}Cr_4O_8$ down to 0.5 K, indicating that no phase transitions take place. Moreover, the magnetic susceptibility shows spingap behavior continuing down to 2 K without glass-type hysteresis. This is probably because the structural transition

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in the inset of Fig. $1(a)$, and a reduction in crystal symmetry from cubic $Fd\overline{3}m$ to another cubic space group, $F\overline{4}3m$. This bond-alternated pyrochlore lattice is known as the "breathing" pyrochlore lattice $[21]$. There are antiferromagnetic couplings between neighboring Cr^{3+} spins, as indicated by a negative Weiss temperature of $\theta_{\rm W} = -332$ K [\[21\]](#page-4-0). The magnitudes of antiferromagnetic interactions on the small and large tetrahedra, J and J' , respectively, are quite different. We estimated the ratio of J and J' , defined as the breathing factor, $B_f = J'/J$, to be approximately 0.1 for LiInCr₄O₈ deduced from an empirical relationship between the strength of magnetic interactions and the Cr-Cr distances [\[21\]](#page-4-0). This small B_f indicates that $LiInCr_4O_8$ lies close to the isolated tetrahedra limit ($B_f = 0$) rather than the uniform pyrochlore limit $(B_f = 1)$.

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FIG. 1. Magnetization curves of powder samples of (a) LiInCr₄O₈ and (b) LiGa_{0.125}In_{0.875}Cr₄O₈. Measurements were performed up to 15, 58, and 72 T at 1.4 K using a multilayered pulsed magnet. The highest magnetic field for each measurement is indicated by an arrow. The inset shows a breathing pyrochlore lattice made of Cr^{3+} ions.

has been suppressed by the substitution, which enables us to study the intrinsic properties of the breathing pyrochlore antiferromagnets, such as the effects of high magnetic field on the tetramer singlet, different from $LiInCr_4O_8$.

In this study, we report state-of-the-art high-field magnetization measurements on powder samples of $LiInCr₄O₈$ and LiGa_{0.125}In_{0.875}Cr₄O₈ using nondestructive and destructive pulsed magnets. They show significantly different magnetization processes reflecting the different zero-field magnetic states. The magnetization of $LiInCr₄O₈$ monotonically increases with increasing magnetic fields up to 72 T, which is the highest magnetic field measured by the nondestructive pulsed magnet. In contrast, that of LiGa_{0.125}In_{0.875}Cr₄O₈ is smaller in a low magnetic field region and strongly increases above 13 T, corresponding to the closing of the spin gap. Moreover, we discovered a half magnetization plateau in the magnetization curve of $LiInCr₄O₈$ above 90 T. This finding indicates the presence of strong spin-lattice coupling in $LiInCr₄O₈$.

II. EXPERIMENTAL DETAILS

High-resolution magnetization measurements up to 72 T on powder samples of $LiInCr_4O_8$ and $LiGa_{0.125}In_{0.875}Cr_4O_8$ were performed using a multilayered nondestructive pulsed magnet with a duration time of 4 ms. Each sample was prepared from the same batch as used in Ref. [\[28\]](#page-4-0). These samples show the sharp diffraction peaks in powder x-ray and neutron diffraction patterns, indicative of the good crystallinity [\[21,28\]](#page-4-0). The very small Curie tails in magnetic susceptibility data suggest that the surface states and lattice defects, giving rise to the orphan spins, in the samples are quite few [\[28\]](#page-4-0). The magnetizations were measured at 1.4 K by the electromagnetic induction method employing a coaxial pickup coil. Since it is difficult to obtain the absolute values of magnetization using this method, we have calibrated the data to fit other magnetization curves measured on the same samples up to 7 T using a Magnetic Property Measurement System (Quantum Design).

A magnetization process of $LiInCr₄O₈$ at ultrahigh magnetic fields of up to 130 T was measured using a destructive single-turn-coil mega-Gauss generator equipped with 200 kJ and 50 kV fast-condenser banks [\[29\]](#page-4-0). The sample used in this measurement is identical to that used in the above measurements. The pulse field duration is about 6*.*5*μ*s and the magnetic field reaches its maximum value in approximately 2.5 μ s. The magnetization curve was obtained by the electromagnetic induction method with a coaxial self-compensated magnetic pickup coil. Details of the measurement techniques will be reported elsewhere, but their essence is similar to those reported in Ref. [\[30\]](#page-4-0), except the configuration of the pickup coil (changed from a parallel pair to coaxial). The pickup coil was set in a He-flow type cryostat solely made of glass-epoxy (FRP, G-10) with special low-temperature glue (Nitofix SK-229, NITTO DENKO Co. Ltd.). The cryostat with its outermost tube diameter of 7.0 mm is inserted precisely into the 12 mm bore single-turn coil. Pairs of measurements with and without the sample in the identical coil under the exactly same discharging conditions were carried out to eliminate background noises superposed on the intrinsic signal from the sample.

III. RESULTS AND DISCUSSION

A. Magnetization processes measured by employing a nondestructive pulsed magnet

Figure $1(a)$ shows magnetization curves of a LiInCr₄O₈ powder sample measured up to 72 T at 1.4 K. The data measured up to 15, 58, and 72 T completely overlap with each other. The magnetization M increases with increasing magnetic field *H* and reaches 0.49μ _B/Cr at 72 T. This *M* corresponds to 0*.*17*M*s, as shown in Fig. [2,](#page-2-0) providing a saturation magnetization of $M_s = gS\mu_B = 2.964\mu_B/Cr$, estimated from the Lande *g* factor, $g = 1.976$, determined by electron spin resonance experiments [\[27\]](#page-4-0). As seen in the top panel of Fig. [2,](#page-2-0) the dM/dH of LiInCr₄O₈ shows a small peak at 7 T, indicating that the slope of the $M - H$ curve takes a local maximum at this *H*, where there may be a small change in the magnetic structure. Above 20 T, the $M - H$ curves of $LiInCr₄O₈$ show slightly concave-upward behavior, probably related to the increase of *M* towards a half magnetization plateau, as discussed later.

The magnetization process of $LiGa_{0.125}In_{0.875}Cr₄O₈$ is significantly different from that of $LiInCr_4O_8$. As shown in Fig. 1(b), the magnetization curves of a $LiGa_{0.125}In_{0.875}Cr₄O₈$

FIG. 2. Normalized magnetization curves of powder samples of LiInCr₄O₈ and LiGa_{0.125}In_{0.875}Cr₄O₈ measured up to 72 T at 1.4 K. The data for LiGa_{0.125}In_{0.875}Cr₄O₈ after the removal of the orphan spin contribution are shown as a dotted curve. *dM/dH* of the *M* − *H* curves and d^2M/dH^2 of that of LiGa_{0.125}In_{0.875}Cr₄O₈ are shown at the top and in the upper inset, respectively. The lower inset shows the low magnetic-field region of the LiGa_{0.125}In_{0.875}Cr₄O₈ data.

powder sample measured up to 15, 58, and 72 T completely overlap with each other. The *M* − *H* curve of $LiGa_{0.125}In_{0.875}Cr₄O₈$ is concave downward below 10 T. This behavior suggests the presence of nearly free spins, which are most likely orphan spins appearing around crystal defects of the spin-singlet tetramers [\[31\]](#page-4-0). The number of orphan spins are estimated by fitting the magnetization curve to the Brillouin function for $S = 3/2$; 0.26% of all Cr^{3+} spins. This value is nearly equal to 0.2%, as estimated by the Curie-Weiss fit of the temperature dependence of magnetic susceptibility [\[28\]](#page-4-0). The magnetization of $LiGa_{0.125}In_{0.875}Cr₄O₈$ after subtracting the orphan spin contribution is very small in the low magnetic field region, as shown in Fig. 2, suggesting that $LiGa_{0.125}In_{0.875}Cr₄O₈ remains in the tetramer singlet$ state at 1.4 K.

The magnetization of $LiGa_{0.125}In_{0.875}Cr₄O₈$ rapidly increases with increasing magnetic field above approximately 13 T. As shown in the inset of Fig. 2, the d^2M/dH^2 of $LiGa_{0.125}In_{0.875}Cr₄O₈$ shows a maximum at 13 T, meaning that the *M* increases most steeply at this *H*. This steep increase reflects the fact that the energy gap Δ between the tetramer singlet state with $S_t = 0$ and the excited state with $S_t = 1$ becomes zero when applying the magnetic field. The energy scale of the $\mu_0 H = 13$ T corresponds to $\Delta =$ 2.2 meV (Δ/k_B = 26 K), given the values of *g* and *S* in this compound. This energy scale is not far from the energy gap of $\Delta/k_B \sim 30$ K, estimated from the temperature dependence

FIG. 3. Magnetization curves of a $LiInCr₄O₈$ powder sample obtained by a single-turn coil mega-Gauss generator in magnetic fields of up to 130 T at approximately 10 K. The left- and righthand-side panels present the $M - H$ curves obtained in elevating and descending processes of a pulse magnetic field, respectively. The broken lines are the $M - H$ curve measured by a nondestructive magnet at 1.4 K, as shown in Fig. $1(a)$. The horizontal dotted line indicates half the M_s . The shaded area is regarded as a background contribution increasing over time, which is caused by the time evolution of the inhomogeneity of the magnetic field in an expanding single-turn coil.

of $1/T_1$ of ⁷Li-NMR in the paramagnetic phase of LiInCr₄O₈ [\[25\]](#page-4-0), suggestive of the same origin.

Above 13 T, the *M* of $LiGa_{0.125}In_{0.875}Cr₄O₈ monotonically$ increases with increasing *H* and reaches $0.55\mu_B/Cr = 0.19M_s$ at 72 T. This *M* is already larger than *M*s*/*6, which is the magnetization when $S_t = 1$ spins are fully polarized along the applied magnetic field. In general, breathing pyrochlore antiferromagnets with small B_f are expected to show stepwise *M* − *H* curves at sufficiently low temperature, in which plateaus appear at $M = nM_s/4S$, where *n* is an integer between zero and 4*S*, the same as in the isolated tetrahedra case. In fact, the $M - H$ curve of the pseudospin- $1/2$ Ba₃Yb₂Zn₅O₁₁ with $J/k_B = 7$ K measured at 0.5 K is stepwise and shows a plateau at $M_s/2$ [\[23\]](#page-4-0), which remain as anomalies corresponding to the closing of the spin gap and the transition to the plateau in 1.8 K data [\[22\]](#page-4-0). It is not clear why there is no signature corresponding to the *M*s*/*6 plateau in the $LiGa_{0.125}In_{0.875}Cr₄O₈ data measured at 1.4 K, which has$ a much smaller energy scale than $J/k_B = 60 \text{ K}$ [\[28\]](#page-4-0). The *J* larger than that in $Ba_3Yb_2Zn_5O_{11}$ may have an important role in the absence of the $M_s/6$ plateau in LiGa_{0.125}In_{0.875}Cr₄O₈.

B. Magnetization processes measured by the single-turn coil method

Figure 3 shows a magnetization process of a $LiInCr₄O₈$ powder sample measured up to 130 T at approximately 10 K by the single-turn coil method. The *M* jumps to $1.5\mu_B/Cr$ at approximately 90 T, indicating a magnetic transition occurs at this *H*. From the transition field to the highest measured field of 130 T, the *M* is almost constant at $1.5\mu_B/Cr$. This *M* corresponds to 0*.*50*M*s, given the values of *g* and *S* of LiInCr₄O₈, indicating that LiInCr₄O₈ is in a half magnetization plateau state in this magnetic field region. A closer look at the magnetization process shown in Fig. [3](#page-2-0) reveals that the jumps of *M* occur at 95–100 T and 85–90 T with increasing and decreasing *H*, respectively, indicative of the presence of hysteresis in this transition. This result suggests that the magnetic transition to the half magnetization plateau occurs as a first-order phase transition.

The half-magnetization plateau formed over a wide *H* region and the first-order transition to the plateau are identical to the behavior of $ACr₂O₄$. These features strongly suggest for the $M_s/2$ plateau phase of $LiInCr_4O_8$ that the 3-up-1-down spin configuration for each tetrahedron, same as in $ACr₂O₄$ [7,8], is realized and the tetrahedra are distorted to stabilize this spin configuration due to the strong spin-lattice coupling, even though there is a strong bond alternation indicated by the small B_f of approximately 0.1. In addition, this is in contrast to the absence of the $M_s/6$ plateau in LiGa_{0.125}In_{0.875}Cr₄O₈, indicating that the spin-lattice coupling does not help to form the *M*s*/*6 plateau.

Finally, we note the magnetization curve just below the half magnetization plateau. The magnetizations of $ZnCr_2O_4$ and MgCr₂O₄, which have large Weiss temperatures of -300 to -400 K, comparable to that of LiInCr₄O₈, linearly increase with increasing *H* just below the half magnetization plateau [12,16]. In contrast, the $M - H$ curve of LiInCr₄O₈ does not show such behavior, but shows a discontinuous jump to the half magnetization plateau. Note that a similar jump has been observed in the $M - H$ curve of CdCr₂O₄ with a much weaker antiferromagnetic interaction ($\theta_{\text{W}} = -70$ K) [5]. Theoretically, the linearly increasing region preceding the plateau appears when the spin-lattice coupling is relatively weak compared to the strength of antiferromagnetic interaction [18]. Therefore, the spin-lattice coupling of this compound must be unusually strong compared to that in $ZnCr_2O_4$ and $MgCr_2O_4$. It is important to clarify the effect of bond alternation on the spin-lattice coupling in the breathing pyrochlore lattice.

IV. SUMMARY

We have reported the magnetization processes of spin-3*/*2 breathing pyrochlore antiferromagnets, measured up to 72 T by employing a nondestructive multilayered pulsed magnet and up to 130 T by the single-turn coil method. The magnetization of $LiInCr₄O₈$, which exhibits an antiferromagnetic order at 15 K, monotonically increases with increasing magnetic field up to 72 T. In contrast, the intrinsic magnetization of $LiGa_{0.125}In_{0.875}Cr₄O₈$, which shows a spin-gap-like magnetic susceptibility down to 2 K, is very small at a low magnetic field, while strongly increasing above 13 T, reflecting the closing of the spin gap between the tetramer singlet state and the excited state by applying a magnetic field. At approximately 90 T, the magnetization of $LiInCr₄O₈$ jumps to the half magnetization plateau, which continues to the highest measured field of $\mu_0 H = 130$ T. This result indicates the presence of considerably strong spin-lattice coupling in $LiInCr₄O₈$ and suggests that this compound is a unique system for realizing an intriguing magnetic property induced by strong spin-lattice coupling and bond alternation.

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- [1] S.-H. Lee, H. Takagi, D. Louca, M. Matsuda, S. Ji, H. Ueda, Y. Ueda, T. Katsufuji, J.-H. Chung, S. Park, S.-W. Cheong, and C. Broholm, [J. Phys. Soc. Jpn.](https://doi.org/10.1143/JPSJ.79.011004) **[79](https://doi.org/10.1143/JPSJ.79.011004)**, [011004](https://doi.org/10.1143/JPSJ.79.011004) [\(2010\)](https://doi.org/10.1143/JPSJ.79.011004).
- [2] S.-H. Lee, C. Broholm, T. H. Kim, W. Ratcliff II, and S.-W. Cheong, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.84.3718) **[84](https://doi.org/10.1103/PhysRevLett.84.3718)**, [3718](https://doi.org/10.1103/PhysRevLett.84.3718) [\(2000\)](https://doi.org/10.1103/PhysRevLett.84.3718).
- [3] J.-H. Chung, M. Matsuda, S.-H. Lee, K. Kakurai, H. Ueda, T. J. Sato, H. Takagi, K.-P. Hong, and S. Park, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.95.247204) **[95](https://doi.org/10.1103/PhysRevLett.95.247204)**, [247204](https://doi.org/10.1103/PhysRevLett.95.247204) [\(2005\)](https://doi.org/10.1103/PhysRevLett.95.247204).
- [4] S. Ji, S.-H. Lee, C. Broholm, T. Y. Koo, W. Ratcliff, S.-W. Cheong, and P. Zschack, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.103.037201) **[103](https://doi.org/10.1103/PhysRevLett.103.037201)**, [037201](https://doi.org/10.1103/PhysRevLett.103.037201) [\(2009\)](https://doi.org/10.1103/PhysRevLett.103.037201).
- [5] H. Ueda, H. A. Katori, H. Mitamura, T. Goto, and H. Takagi, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.94.047202) **[94](https://doi.org/10.1103/PhysRevLett.94.047202)**, [047202](https://doi.org/10.1103/PhysRevLett.94.047202) [\(2005\)](https://doi.org/10.1103/PhysRevLett.94.047202).
- [6] H. Ueda, H. Mitamura, T. Goto, and Y. Ueda, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.73.094415) **[73](https://doi.org/10.1103/PhysRevB.73.094415)**, [094415](https://doi.org/10.1103/PhysRevB.73.094415) [\(2006\)](https://doi.org/10.1103/PhysRevB.73.094415).
- [7] M. Matsuda, H. Ueda, A. Kikkawa, Y. Tanaka, K. Katsumata, Y. Narumi, T. Inami, Y. Ueda, and S.-H. Lee, [Nat. Phys.](https://doi.org/10.1038/nphys586) **[3](https://doi.org/10.1038/nphys586)**, [397](https://doi.org/10.1038/nphys586) [\(2007\)](https://doi.org/10.1038/nphys586).
- [8] M. Matsuda, K. Ohoyama, S. Yoshii, H. Nojiri, P. Frings, F. Duc, B. Vignolle, G. L. J. A. Rikken, L.-P. Regnault, S.-H. Lee, H. Ueda, and Y. Ueda, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.104.047201) **[104](https://doi.org/10.1103/PhysRevLett.104.047201)**, [047201](https://doi.org/10.1103/PhysRevLett.104.047201) [\(2010\)](https://doi.org/10.1103/PhysRevLett.104.047201).
- [9] E. Kojima, A. Miyata, Y. Motome, H. Ueda, Y. Ueda, and S. Takeyama, [J. Low Temp. Phys.](https://doi.org/10.1007/s10909-009-0069-7) **[159](https://doi.org/10.1007/s10909-009-0069-7)**, [3](https://doi.org/10.1007/s10909-009-0069-7) [\(2010\)](https://doi.org/10.1007/s10909-009-0069-7).
- [10] A. Miyata, H. Ueda, Y. Ueda, H. Sawabe, and S. Takeyama, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.107.207203) **[107](https://doi.org/10.1103/PhysRevLett.107.207203)**, [207203](https://doi.org/10.1103/PhysRevLett.107.207203) [\(2011\)](https://doi.org/10.1103/PhysRevLett.107.207203).
- [11] A. Miyata, H. Ueda, Y. Ueda, Y. Motome, N. Shannon, K. Penc, and S. Takeyama, [J. Phys. Soc. Jpn.](https://doi.org/10.1143/JPSJ.81.114701) **[81](https://doi.org/10.1143/JPSJ.81.114701)**, [114701](https://doi.org/10.1143/JPSJ.81.114701) [\(2012\)](https://doi.org/10.1143/JPSJ.81.114701).
- [12] A. Miyata, H. Ueda, and S. Takeyama, [J. Phys. Soc. Jpn.](https://doi.org/10.7566/JPSJ.83.063702) **[83](https://doi.org/10.7566/JPSJ.83.063702)**, [063702](https://doi.org/10.7566/JPSJ.83.063702) [\(2014\)](https://doi.org/10.7566/JPSJ.83.063702).
- [13] H. Mitamura, H. Ueda, H. A. Katori, S. Takeyama, T. Sakakibara, Y. Ueda, and H. Takagi, [J. Phys. Soc. Jpn.](https://doi.org/10.1143/JPSJ.76.085001) **[76](https://doi.org/10.1143/JPSJ.76.085001)**, [085001](https://doi.org/10.1143/JPSJ.76.085001) [\(2007\)](https://doi.org/10.1143/JPSJ.76.085001).
- [14] E. Kojima, A. Miyata, S. Miyabe, S. Takeyama, H. Ueda, and Y. Ueda, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.77.212408) **[77](https://doi.org/10.1103/PhysRevB.77.212408)**, [212408](https://doi.org/10.1103/PhysRevB.77.212408) [\(2008\)](https://doi.org/10.1103/PhysRevB.77.212408).
- [15] A. Miyata, S. Takeyama, and H. Ueda, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.87.214424) **[87](https://doi.org/10.1103/PhysRevB.87.214424)**, [214424](https://doi.org/10.1103/PhysRevB.87.214424) [\(2013\)](https://doi.org/10.1103/PhysRevB.87.214424).
- [16] A. Miyata, H. Ueda, Y. Ueda, Y. Motome, N. Shannon, K. Penc, and S. Takeyama, [J. Phys. Soc. Jpn.](https://doi.org/10.1143/JPSJ.80.074709) **[80](https://doi.org/10.1143/JPSJ.80.074709)**, [074709](https://doi.org/10.1143/JPSJ.80.074709) [\(2011\)](https://doi.org/10.1143/JPSJ.80.074709).
- [17] A. L. Cornelius and J. S. Gardner, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.64.060406) **[64](https://doi.org/10.1103/PhysRevB.64.060406)**, [060406\(R\)](https://doi.org/10.1103/PhysRevB.64.060406) [\(2001\)](https://doi.org/10.1103/PhysRevB.64.060406).
- [18] K. Penc, N. Shannon, and H. Shiba, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.93.197203) **[93](https://doi.org/10.1103/PhysRevLett.93.197203)**, [197203](https://doi.org/10.1103/PhysRevLett.93.197203) [\(2004\)](https://doi.org/10.1103/PhysRevLett.93.197203).
- [19] N. Shannon, H. Ueda, Y. Motome, K. Penc, H. Shiba, and H. Takagi, [J. Phys. Conf. Ser.](https://doi.org/10.1088/1742-6596/51/1/005) **[51](https://doi.org/10.1088/1742-6596/51/1/005)**, [31](https://doi.org/10.1088/1742-6596/51/1/005) [\(2006\)](https://doi.org/10.1088/1742-6596/51/1/005).
- [20] J.-C. Joubert and A. Durif, Bull. Soc. Fr. Mineral. Cristallogr. **89**, 26 (1966).
- [21] [Y. Okamoto, G. J. Nilsen, J. P. Attfield, and Z. Hiroi,](https://doi.org/10.1103/PhysRevLett.110.097203) *Phys. Rev.* Lett. **[110](https://doi.org/10.1103/PhysRevLett.110.097203)**, [097203](https://doi.org/10.1103/PhysRevLett.110.097203) [\(2013\)](https://doi.org/10.1103/PhysRevLett.110.097203).
- [22] K. Kimura, S. Nakatsuji, and T. Kimura, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.90.060414)**[90](https://doi.org/10.1103/PhysRevB.90.060414)**, [060414](https://doi.org/10.1103/PhysRevB.90.060414) [\(2014\)](https://doi.org/10.1103/PhysRevB.90.060414).
- [23] T. Haku, K. Kimura, Y. Matsumoto, M. Soda, M. Sera, D. Yu, R. A. Mole, T. Takeuchi, S. Nakatsuji, Y. Kono, T. Sakakibara, L.-J. Chang, and T. Masuda, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.93.220407) **[93](https://doi.org/10.1103/PhysRevB.93.220407)**, [220407\(R\)](https://doi.org/10.1103/PhysRevB.93.220407) [\(2016\)](https://doi.org/10.1103/PhysRevB.93.220407).
- [24] A. J. García-Adeva and D. L. Huber, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.85.4598) **[85](https://doi.org/10.1103/PhysRevLett.85.4598)**, [4598](https://doi.org/10.1103/PhysRevLett.85.4598) [\(2000\)](https://doi.org/10.1103/PhysRevLett.85.4598).
- [25] Y. Tanaka, M. Yoshida, M. Takigawa, Y. Okamoto, and Z. Hiroi, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.113.227204) **[113](https://doi.org/10.1103/PhysRevLett.113.227204)**, [227204](https://doi.org/10.1103/PhysRevLett.113.227204) [\(2014\)](https://doi.org/10.1103/PhysRevLett.113.227204).
- [26] G. J. Nilsen, Y. Okamoto, T. Masuda, J. Rodriguez-Carvajal, H. Mutka, T. Hansen, and Z. Hiroi, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.91.174435) **[91](https://doi.org/10.1103/PhysRevB.91.174435)**, [174435](https://doi.org/10.1103/PhysRevB.91.174435) [\(2015\)](https://doi.org/10.1103/PhysRevB.91.174435).
- [27] S. Lee, S.-H. Do, W.-J. Lee, Y. S. Choi, M. Lee, E. S. Choi, A. P. [Reyes, P. L. Kuhns, A. Ozarowski, and K.-Y. Choi,](https://doi.org/10.1103/PhysRevB.93.174402) Phys. Rev. B **[93](https://doi.org/10.1103/PhysRevB.93.174402)**, [174402](https://doi.org/10.1103/PhysRevB.93.174402) [\(2016\)](https://doi.org/10.1103/PhysRevB.93.174402).
- [28] [Y. Okamoto, G. J. Nilsen, T. Nakazono, and Z. Hiroi,](https://doi.org/10.7566/JPSJ.84.043707) J. Phys. Soc. Jpn. **[84](https://doi.org/10.7566/JPSJ.84.043707)**, [043707](https://doi.org/10.7566/JPSJ.84.043707) [\(2015\)](https://doi.org/10.7566/JPSJ.84.043707).
- [29] N. Miura, T. Osada, and S. Takeyama, [J. Low Temp. Phys.](https://doi.org/10.1023/A:1025689218138) **[133](https://doi.org/10.1023/A:1025689218138)**, [139](https://doi.org/10.1023/A:1025689218138) [\(2003\)](https://doi.org/10.1023/A:1025689218138).
- [30] S. Takeyama, R. Sakakura, Y. H. Matsuda, A. Miyata, and M. Tokunaga, [J. Phys. Soc. Jpn.](https://doi.org/10.1143/JPSJ.81.014702) **[81](https://doi.org/10.1143/JPSJ.81.014702)**, [014702](https://doi.org/10.1143/JPSJ.81.014702) [\(2012\)](https://doi.org/10.1143/JPSJ.81.014702).
- [31] P. Schiffer and I. Daruka, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.56.13712) **[56](https://doi.org/10.1103/PhysRevB.56.13712)**, [13712](https://doi.org/10.1103/PhysRevB.56.13712) [\(1997\)](https://doi.org/10.1103/PhysRevB.56.13712).