# **Magnetochromic sensing and size-dependent collective excitations in iron oxide nanoparticles**

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We combine optical and magneto-optical spectroscopies with complementary vibrational and magnetic property measurements to reveal finite length scale effects in nanoscale  $α$ -Fe<sub>2</sub>O<sub>3</sub>. Analysis of the *d*-to-*d* on-site excitations uncovers enhanced color contrast at particle sizes below approximately 75 nm due to size-induced changes in spin-charge coupling that are suppressed again below the superparamagnetic limit. These findings provide a general strategy for amplifying magnetochromism in  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> and other iron-containing nanomaterials that may be useful for advanced sensing applications. We also unravel the size dependence of collective excitations in this iconic antiferromagnet.

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### **I. INTRODUCTION**

The interplay between charge, structure, and magnetism is the origin of rich functionality in complex materials. Competing interactions are particularly strong in oxides, giving rise to elaborate *T* -*H*-*P*-*hν* phase diagrams, often with exotic states that derive from delicately balanced coupling [\[1,2\]](#page-4-0). Small external perturbations, for instance, magnetic field, pressure, or light, can change important energy and length scales, driving these flexible materials into new areas of phase space with very different properties [\[3–9\]](#page-4-0). These competing states are interesting and useful because of their different functionalities. Finite length scale effects also influence the interaction between charge, structure, and magnetism [\[10–](#page-4-0) [12\]](#page-4-0). Nanoscale oxides like MnO and  $\text{CoFe}_2\text{O}_4$ , for instance, sport modified chemical bonding, displacive transitions, and spin-lattice couplings compared to their bulk analogs [\[13–15\]](#page-5-0). Less is known, however, about how size can be used to control spin-charge interactions.

We identified  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>, commonly known as hematite, as a model antiferromagnet with which to test these ideas. This system displays a spin-flop transition that is driven by both temperature ( $T_M$  = 263 K) and magnetic field ( $H_{SF}$  = 6 and 16 T for the easy and hard axis, respectively) [\[16–18\]](#page-5-0). Applied field creates color contrast (red  $\rightarrow$  red') via a spin-charge coupling mechanism by amplifying changes in the  ${}^{6}A_{1g} \rightarrow {}^{4}T_{1}$ , on-site excitation across the spin-flop transition [19.20]  ${}^{4}T_{1g}$  on-site excitation across the spin-flop transition [\[19,20\]](#page-5-0). Analysis of the collective excitations on the leading edge of the *d*-to-*d* transition also reveals magnetic symmetry [\[20\]](#page-5-0). Confinement reduces the overall energy scales—a trend that is easily recognized by the decreased ordering temperatures and critical fields at small sizes  $[21-23]$ . It also modifies magnetization [\[24–28\]](#page-5-0), optical properties [\[29,30\]](#page-5-0), phonon frequencies [\[31,32\]](#page-5-0), and vibronic coupling [\[10\]](#page-4-0). Complex experimental probes of the fundamental electronic excitations in nanoscale  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> and an understanding of how the energy transfer processes involving the charge channel change with size [\[33,34\]](#page-5-0) are, however, still missing. At the same time, materials that possess a large generalized susceptibility (i.e., a strong response to a small stimulus) are promising candidates for novel device applications. The magnetochromic sensing capabilities explored here thus complement well-known medical and environmental uses of iron oxide nanoparticles [\[35–38\]](#page-5-0).

In this work, we combine magneto-optical spectroscopy with vibrational and magnetic property measurements to more deeply investigate magnetoelectric coupling in nanoscale hematite. We find stronger field-induced color contrast below approximately 75 nm due to enhanced spin-charge coupling that is suppressed below the super-paramagnetic regime [\[39\]](#page-5-0). The spin-charge coupling mechanism also accounts for systematic shifts in the magnon sideband frequency, from which we extract precisely how the fundamental exciton softens with decreasing size. These findings are important for generating large field-induced color contrast in iron-containing earthabundant materials and emerging magnetochromic sensor applications [\[40–42\]](#page-5-0).

#### **II. METHODS**

Several sizes and shapes of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> nanoparticles were prepared by hydrothermal methods [\[43–45\]](#page-5-0). Details on the synthesis, size and distribution analysis, and structural characterization are presented in Ref. [\[46\]](#page-5-0). A bulk powder with large micrometer-sized grains was purchased from Alfa Aeser (99.999%) for comparison. The dc magnetization of the *α*-Fe2O3 nanoparticles sealed inside gelatin capsules with paraffin wax was measured after both zero-field cooling and field cooling in a Quantum Design Magnetic Properties Measurement System from 1.8 to 300 K under an applied field of 500 Oe. These results are also shown in the Supplemental

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<span id="page-1-0"></span>Information. For optical transmittance measurements (8700– 17 000 cm−1, 2 cm−<sup>1</sup> resolution), samples were mixed with a matrix and pressed into pellets. Particle concentrations were low, such that interparticle interactions can be neglected. Absorption was calculated as  $\alpha(\omega) = \frac{-1}{hd} \ln[T(\omega)]$ , where  $T(\omega)$  is the measured transmittance, *h* is the sample loading, and *d* is thickness. Oscillator strength was calculated as  $f = \frac{2c}{N_e \pi \omega_p^2} \int_{\omega_1}^{\omega_2} n \alpha(\omega) d\omega$ , where  $N_e = 5$  is the number of electrons per Fe site,  $n \approx 2.23$  is the refractive index,  $\omega_\rho$  is the plasma frequency  $\omega_{\rho} \equiv \sqrt{\frac{e^2 \rho}{m \epsilon_0}}, e$  and *m* are the charge and mass of an electron,  $\epsilon_0$  is the vacuum dielectric constant, *ρ* is the density of Fe sites, *c* is the speed of light, and  $ω<sub>1</sub>$  and  $ω<sub>2</sub>$  are the frequency limits of integration [\[47\]](#page-5-0). The integration range is 10 000–11,000 cm<sup>-1</sup> for the magnon sideband, and 11 000–14 000 cm−<sup>1</sup> for the *d*-to-*d* excitation. High-field optical (9000–20 800 cm<sup>-1</sup>, 5 cm<sup>-1</sup> resolution) and infrared measurements (20–650 cm<sup>-1</sup>, 2 cm<sup>-1</sup> resolution) were performed at 4.2 K using a resistive magnet (0–35 T) at the National High Magnetic Field Laboratory in Tallahassee, FL. Raman measurements were taken with a 473-nm laser at 50 mW power and 1800 g/mm grating, integrated between 30 and 60 seconds and averaged three times.

#### **III. RESULTS AND DISCUSSION**

#### **A. Magneto-optical properties of hematite nanoparticles**

Figures  $1(a)$ – $1(c)$  displays the absorption of polycrystalline  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> as well as the response of two different sizes of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> nanoparticles. We assign the broad absorption band

centered at 11 600 cm<sup>-1</sup> as the <sup>6</sup>A<sub>1*g*</sub>  $\rightarrow$  <sup>4</sup>T<sub>1*g*</sub> Fe<sup>3+</sup> on-site excitation [\[19\]](#page-5-0) and the smaller feature on the leading edge of this structure (at  $10\,470\,\text{cm}^{-1}$ ) as a magnon sideband [\[48\]](#page-5-0). The former is activated by vibronic coupling and interaction with odd parity phonons whereas the latter is a characteristic dipoleallowed transition that appears in a number of antiferromagnets [\[19,49–51\]](#page-5-0). The collective nature of the magnon sideband makes it a superb probe of spin-charge coupling and magnetic quantum phase transitions [\[20,42\]](#page-5-0). The magneto-optical response of these materials [also in Figs.  $1(a)$ – $1(c)$ ] is shown as a full field absorption difference:  $\Delta \alpha = \alpha(35 \text{ T}) - \alpha(0 \text{ T})$ . This rendering highlights field-induced spectral changes by eliminating commonalities.

Inspection reveals that the absorption difference spectra have the same general shape regardless of particle size, with field-induced changes to both the *d*-to-*d* excitation and the magnon side band. A partial sum rule analysis [\[47\]](#page-5-0) over the appropriate energy windows quantifies these trends [Figs.  $1(d)$ – $1(f)$ ]. Prior magneto-optical work on single crystals reveals clear optical contrast through the spin-flop transition with enhancement (and softening) of the magnon sideband and diminution of the on-site excitation due to spin-charge interactions [\[20\]](#page-5-0). A remnant of these effects appears in polycrystalline  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> and the various nanoparticles of interest here [\[52\]](#page-5-0). For example, the oscillator strength of the *d*-to-*d* excitation in the bulk powder begins to decrease around 6 T and reaches its steepest slope near 16 T, consistent with the easy and hard axis critical fields of the single crystal [\[18\]](#page-5-0). The nanorhombohedra display similar effects although here, the oscillator strength of the color band begins to decrease



FIG. 1. (a)–(c) 4.2-K absorption spectrum of polycrystalline hematite and selected nanorhombohedra beneath the full field absorption difference spectrum,  $\Delta \alpha = \alpha(35 \text{ T}) - \alpha(0 \text{ T})$ , for comparison. The full data set is available in Ref. [\[46\]](#page-5-0). (d)–(f) Change in oscillator strength  $(\Delta f)$  of the *d*-to-*d* on-site excitation (green squares) and magnon sideband (violet circles) vs magnetic field for these materials. Blue lines guide the eye.

<span id="page-2-0"></span>TABLE I. Summary of the shape, size, and full field absorption difference  $\Delta \alpha_{\text{max}} = \left[\frac{\alpha(35 \text{ T}) - \alpha(0 \text{ T})}{\alpha(0 \text{ T})}\right] \times 100$  calculated at the position of the highest absorption, ( $\approx$ 11 600 cm<sup>-1</sup>) of the hematite nanomaterials used in this work.

material	particle length (nm)	particle width $(nm)$	$\Delta \alpha_{\rm max}(\%)$
bulk powder	$\approx$ 1000	$\approx$ 1000	$-1.2$
cubes	$450 \pm 60$	$450 \pm 60$	$-1.6$
polyhedra	$320 \pm 90$	$320 \pm 90$	$-1.2$
rice	$148 \pm 32$	$67 \pm 10$	$\Omega$
rhombohedra $(2x)$	$105 \pm 16$	$84 \pm 12$	$-1.5$
rhombohedra (L)	$75 \pm 8$	$50 \pm 7$	$-2.1$
rhombohedra (M)	$59 \pm 9$	$59 \pm 8$	$-3.1$
rhombohedra (S)	$50 \pm 8$	$35 \pm 7$	$-1.9$

at lower fields, indicating that smaller fields drive the color change. This is because the critical fields are smaller, in line with direct measurements of  $H_c$  [\[22\]](#page-5-0). At the same time, a portion of this oscillator strength is transferred to the magnon sideband, which grows with increasing field [Figs.  $1(d) - 1(f)$ ].

Table I summarizes the magnetochromic response of the full suite of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> nanomaterials of interest (see Fig. S4 in Ref. [\[46\]](#page-5-0) for data on all samples) [\[10\]](#page-4-0). Here, we use the field-induced change in the absorption spectrum ( $\Delta \alpha_{\text{max}}$ ) at the center position of the on-site excitation  $(11\,600\,\text{cm}^{-1})$  and highest available field (35 T) to quantitatively compare how the color band changes with size. Inspection of the last column in Table I reveals that, in general, spectral contrast (understood as  $|\Delta \alpha_{\text{max}}|$ ) increases with decreasing size—independent of shape.

Figure 2 displays the same data in graphical form. It is easy to identify three distinct regimes: a bulklike regime, a small size range, and an area below the superparamagnetic limit. At large sizes, the field-induced color change is nearly constant and on the order of 1.3% [\[53\]](#page-5-0). This is true for the single- and polycrystal as well as for several of the larger nanoparticles including cubes and polyhedra, suggesting that spin-charge coupling (which activates the field-induced color change) is of similar order of magnitude. Things are different when the characteristic particle size drops below about 75 nm (≈60 unit cells). Here, the spectral contrast increases to nearly 3% before dropping back down as the system approaches the super-paramagnetic region [\[39\]](#page-5-0). A similar trend emerges for the contrast of the magnon sideband. The enhanced contrast at small size suggests that spin-charge coupling is changing in critical ways - either by systematic enhancement (and subsequent diminishment at the smallest size) or by involving additional degrees of freedom (besides the spin and charge channels). We test these mechanistic scenarios below and find, to our surprise, that spin-charge coupling not only describes the overall trend but provides a plausible explanation for (i) the curious behavior of the smallest nanorhombohedra in this study and (ii) the rigidity of the *d*-to-*d* excitation in the nanorice.

## **B.** Mechanism of the field-induced color contrast in  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> **nanoparticles**

It is well established that magnetic field-induced color contrast in hematite single crystals derives from spin-charge



FIG. 2. Full field color contrast,  $|\Delta \alpha_{\text{max}}| = |\frac{\alpha(35 \text{ T}) - \alpha(0 \text{ T})}{\alpha(0 \text{ T})}| \times$ 100%, evaluated at 11 600 cm−<sup>1</sup> (which corresponds to the maximum of the *d*-to-*d* absorption) at 4.2 K. A photo of the single crystal and scanning electron microscope images of select nanoparticles are included. The three different size regimes [bulklike, small size, and superparamagnetic (SP)] are indicated. The red line guides the eye, with the dashed region approximating what may happen at smaller sizes.

coupling that is strongly amplified across the spin-flop transition [\[20\]](#page-5-0). It is therefore reasonable to anticipate that a similar mechanism will be relevant to the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> nanoparticles. Our work provides three independent checks of this scenario. The first test involves the behavior of the smallest nanorhombohedra and evaluates the role of the collective transition. Below about 40 nm (close to the size of the smallest rhombohedra), the spin-flop transition does not force spins to lie perfectly along the *c* axis (as in larger particles) but instead allows a 28◦ off-axis orientation [\[54\]](#page-5-0). This scenario is consistent with the significant moment below the spin-flop transition observed in magnetization measurements of our  $35 \times 50$  nm<sup>2</sup> particles (see Fig. S6 in Ref. [\[46\]](#page-5-0)), and it suggests that a degraded spin-flop transition might impact magnetochromism. The second check concerns the nanorice sample and even more firmly establishes the importance of the collective transition. Magnetic property measurements of the nanorice reveal no spin-flop transition (see Fig. S7 in Ref. [\[46\]](#page-5-0)), and correspondingly, magnetooptical experiments up to 35 T (and even test runs to 45 T) show no field-induced absorption difference. In other words, the absence of a spin-flop transition quenches the color contrast. Together, these two results demonstrate that a robust collective transition—in which the spins fully reorient—is required to modify the *d*-to-*d* excitation. The final check of the spin-charge coupling mechanism in hematite nanoparticles involves ruling out a lattice contribution. Since the *d*-to-*d* excitation is activated by coupling with an odd parity phonon [\[10\]](#page-4-0), any spin-lattice coupling is expected to involve an infrared-active mode. Direct magneto-infrared measurements <span id="page-3-0"></span>of the smallest rhombohedra up to 35 T, however, reveal no local lattice distortions (see Fig. S8 in Ref. [\[46\]](#page-5-0)), implying that the spin-flop transition occurs without any commensurate changes to the lattice. Taken together, these results show that spin and charge are intimately coupled in  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> and can interact directly—without involving the lattice.

#### **C. Magnetochromic sensing applications**

In the discussion above, we describe a general strategy for creating enhanced magnetochromic contrast in magnetic nanoparticles like  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>. It is important to point out that there are a number of applications that can make use of this technology—especially when the color contrast is visible to the human eye. Earth-abundant materials like hematite are inexpensive, safe, and stable. Moreover, small nanoparticles can be mixed into inks and embedded into fibers to provide very subtle and hard-to-duplicate forms of identification of the type that may be useful for anti-counterfeiting purposes. In  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>, our measurements suggest that particle sizes near 75 nm are likely to produce maximum red  $\rightarrow$  red' magnetochromic color contrast. The magnetic energy scales (as measured by the Morin temperature, for instance) are also relatively high and may be able to support room temperature operation. The latter assumes that the residual spin-spin correlations at room temperature are sufficient to provide a remnant of the collective transition—a supposition that has yet to be tested. Other iron oxides like  $Fe<sub>3</sub>O<sub>4</sub>$  or  $CoFe<sub>2</sub>O<sub>4</sub>$  will have somewhat different sweet spots, but our research suggests that the size regime just above the transition to the superparamagnetic state is the place to search for enhanced color contrast that can be observed with a hand-held spectrometer or (even better) by the naked eye. This discovery clearly opens the door to completely new types of sensing from magnetic nanoparticles.

# **D.** Collective excitations and fine structure in  $α$ -Fe<sub>2</sub>O<sub>3</sub> **nanoparticles**

Antiferromagnets traditionally offer foundational opportunities for investigating collective excitations like excitons and magnons as well as features like magnon sidebands that arise from charge-spin coupling [\[50,51,55\]](#page-5-0). The latter arises from the dipole-allowed combination of an exciton and a magnon ( $\omega_{MS} = \omega_E + \omega_M$ ) and is commonly observed on the leading edge of a  $d$ -to- $d$  band  $[20,48,50,55,56]$ . Exciton



FIG. 3. (a) Magnon sideband for the (blue) largest and (red) smallest rhombohedra. (b) Magnon sideband position vs field for the rhombohedral samples at 4.2 K. (c) Raman-active two magnon mode for the (blue) largest and (red) smallest rhombohedra at 300 K from which the magnon energy was determined. (d) Magnon sideband position vs particle size at 4.2 K and zero field. The equation reveals the limiting "zero size" value of the magnon sideband position and its systematic shift with particle size *D* in nanometers. (e) Change in magnon sideband position at 35 T vs size. Note that the smallest size particles are close to the super-paramagnetic region. (f) Magnon energy vs size. The limiting "zero size" position of the magnon and estimated linear size-dependent shift are extracted from the indicated fit. The sample specifications are given in Table [I.](#page-2-0)

<span id="page-4-0"></span>splitting and magnon sideband trends are incisive probes of symmetry, and their behavior can even be used to develop temperature-magnetic field phase diagrams [\[20,56,57\]](#page-5-0). While much is known about excitons, magnons, and magnon sidebands in antiferromagnets under external stimuli, there have been few opportunities to reveal finite length scale effects on the behavior of collective excitations. Our suite of hematite nanoparticles provides a superb platform for such tests [\[20,48,58\]](#page-5-0).

Figure [3](#page-3-0) summarizes how the collective excitations in nanohematite change with size. An obvious linear correlation exists between particle size and magnon sideband position in the absence of magnetic field [Figs.  $3(a)$  and  $3(d)$ ]. As particle size decreases, the frequency of the magnon sideband is reduced. This trend is due to the combined size dependence of the exciton and magnon that compose it and, in the discussion below, we separate the two effects. The magnon sideband position also softens through the field-driven spin-flop transition [Fig.  $3(b)$ ]. The degree to which the field-induced softening of the magnon sideband  $\Delta \omega_{MS}$  depends upon size is interesting [Fig.  $3(e)$ ].  $\Delta \omega_{MS}$  increases linearly in the small size regime but weakens again as the superparamagnetic regime is approached. This is because only a remnant of the spin-flop transition survives below the superparamagnetic limit, a situation that we already established as inconsistent with maximum spin-charge coupling [\[54,59\]](#page-5-0).

Magnons are a type of spin wave commonly found in magnetic materials [\[60,61\]](#page-5-0) and are typically explored with neutron and Raman scattering techniques. The two-magnon mode, in particular, is Raman-active [\[62,63\]](#page-5-0). It is straightforward to estimate the magnon frequency  $\omega_M$  from measurements of the two magnon mode as  $\omega_{2M} = 2\omega_M$ . In  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> single crystals, this yields  $\omega_M = 782$  cm<sup>-1</sup> [\[20,64,65\]](#page-5-0). Figures [3\(c\)](#page-3-0) and [3\(f\)](#page-3-0) displays the Raman-active two-magnon peak and the size dependence of  $\omega_M$  (see Fig. S5 in Ref. [\[46\]](#page-5-0) for all spectra). At least within the rhombohedral sub-class,  $\omega_M$  is nearly rigid [\[66\]](#page-5-0). Since  $\omega_{MS} = \omega_E + \omega_M$ , simple subtraction reveals that the exciton frequency must also decrease as particle size is reduced. We find  $\omega_E = 9631 + (0.14 \text{ cm}^{-1}/\text{nm})D$ , where *D* is particle size in nanometers. Comparison of the relative slopes reveals that the exciton is much more sensitive to size than the magnon  $[67]$ .

## **IV. CONCLUSION**

We measured the magneto-optical properties of a series of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> nanoparticles in order to reveal finite length scale effects on the fundamental electronic excitations. Decreasing the particle size below 75 nm amplifies the field-induced color contrast due to enhanced spin-charge coupling—until the onset of superparamagnetism quenches the effect. Various mechanistic tests, including the analysis of similar trends in nanorice samples and direct measurement of spin-lattice coupling with magneto-infrared spectroscopy, demonstrate the importance of a robust spin-flop transition; when the spin-flop is incomplete or absent, the color contrast is reduced or suppressed, respectively. We also took the opportunity to explore finite length scale effects on the collective excitations in  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> from which we learn that the exciton is much more susceptible to confinement than the magnon. This work advances the understanding of size effects on the color properties of multifunctional materials, motivates the extension to nanoanalogs of materials where different color change mechanisms are at work, and provides a general strategy for creating enhanced magnetochromic responses that are visible to the human eye.

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