Large magnetic anisotropy predicted for rare-earth-free Fe_{16-x}Co_xN₂ alloys

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Structures and magnetic properties of $Fe_{16-x}Co_xN_2$ are studied using adaptive genetic algorithm and firstprinciples calculations. We show that substituting Fe with Co in $Fe_{16}N_2$ with a Co/Fe ratio ≤ 1 can greatly improve the magnetic anisotropy of the material. The magnetocrystalline anisotropy energy from first-principles calculations reaches 3.18 MJ/m^3 (245.6 μ eV per metal atom) for $Fe_{12}Co_4N_2$, much larger than that of $Fe_{16}N_2$, and is one of the largest among the reported rare-earth-free magnets. From our systematic crystal structure searches, we show that there is a structure transition from tetragonal $Fe_{16}N_2$ to cubic $Co_{16}N_2$ in $Fe_{16-x}Co_xN_2$ as the Co concentration increases, which can be well explained by electron counting analysis. Different magnetic properties between the Fe-rich ($x \leq 8$) and Co-rich (x > 8) $Fe_{16-x}Co_xN_2$ is closely related to the structural transition.

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I. INTRODUCTION

Permanent magnets (PMs) are important energy and information storage and conversion materials, and play a crucial role in new energy economies. Currently, the most widely used PMs are $Nd_2Fe_{14}B$ and $SmCo_5$, both containing rare-earth (RE) elements. Because of the concerns on limited RE mineral resources and RE supplies, there has been increasing interest in discovering strong RE-free PM materials [1].

In addition to the microstructures, the performance of PMs relies on the intrinsic magnetic properties of their crystal structures, such as saturation magnetization, Curie temperature, and magnetocrystalline anisotropy energy (MAE). Among the RE-free magnets, the metastable tetragonal- α'' -Fe₁₆N₂ phase of iron nitrides has attracted considerable experimental and theoretical attention due to the low cost of Fe and high magnetization in α'' -Fe₁₆N₂ thin films [2]. In experiments, a very large value ($\sim 3 \mu_B$) of average Fe magnetic moment in Fe₁₆N₂ thin film was reported [2,3], which is much higher than that of pure bulk Fe (2.2 $\mu_{\rm B}$). The MAE of the tetragonal- $Fe_{16}N_2$ phase has been measured by several experiments [3-7], but the results are not conclusive, ranging from 0.44 to 2.0 MJ/m^3 . Because of the promising magnetic properties observed in thin films, efforts to synthesize bulk samples of the tetragonal- α'' -Fe₁₆N₂ phase have also been made [8–10]. In the α'' -Fe₁₆N₂ structure, the body-centered cubic (bcc) Fe lattice is expanded into a distorted body-centered tetragonal (bct) lattice due to the presence of N. Close to 500 K, the tetragonal- α'' -Fe₁₆N₂ phase decomposes into α -Fe and Fe₄N phases [11], making the thermal stability one of the major issues for its synthesis and application. It has been shown that adding a small amount of a third element, such as Co, Mn, or Ti, can stabilize the α'' -Fe₁₆N₂ phase in thin film samples [12,13]. Whether such a doping approach can stabilize the α'' -Fe₁₆N₂ in the synthesis of bulk samples is still under investigation [14].

Theoretically, many studies have also been devoted to exploring the origin of the magnetic moment and MAE enhancement in α'' -Fe₁₆N₂ [15–17]. Using density functional theory (DFT) and quasiparticle self-consistent *GW* calculations, Ke *et al.* studied the intrinsic magnetic properties of

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Fe₁₆N₂ and reported a magnetic moment of ~2.5 μ_B and Curie temperature of ~1300 K [17]. For MAE, they obtained a uniaxial magnetocrystalline anisotropy of 1.03 MJ/m³ by local density approximation (LDA) and 0.65 MJ/m³ by the generalized gradient approximation (GGA). Calculations by Ke *et al.* also indicate possible improvement of magnetocrystalline anisotropy by substituting a small amount (less than 15%) of Fe with Co or Ti in the α'' -Fe₁₆N₂ phase [17]. Nevertheless, the calculations were done using the α'' -Fe₁₆N₂ structure and the effect of transition metal (TM) substitution on the crystal structures and phase stabilities has not been investigated.

In this paper, we systematically study the structural evolution and magnetic properties of $Fe_{16-x}Co_xN_2$ with x ranging from 0 to 16. We show that substituting a minority of Fe by Co results in better magnetic properties; especially, a large value of MAE (~3.18 MJ/m³) is achieved at the composition of $Fe_{12}Co_4N_2$ (i.e., x = 4). We demonstrate that there is a tetragonal ($Fe_{16}N_2$) to cubic ($Co_{16}N_2$) structural transition in $Fe_{16-x}Co_xN_2$ as the Co concentration is increased. The changes in the magnetic properties with the Co concentration are strongly correlated with the structural changes.

II. CALCULATION DETAILS

Our crystal structure searches were performed using an adaptive genetic algorithm (AGA) [18,19] with real-space cut-and-paste operations for generating offspring structures [20]. No constraints were applied on the structure symmetries during the AGA search. We explored the crystal structures of $Fe_{16-x}Co_xN_2$ (18 atoms per unit cell) with x ranging from 0 to 16. During the AGA searches, an auxiliary classical potential based on the embedded-atom method [21] was used. The firstprinciples calculations were carried out using spin-polarized density functional theory (DFT). The generalized gradient approximation (GGA) in the form of PBE (Perdew, Burke, and Ernzerhof) [22] implemented in the VASP code [23] is used. Kinetic energy cutoff was set to be 520 eV. The Monkhorst-Pack's scheme [24] was used for Brillouin zone sampling with a k-point grid resolution of $2\pi \times 0.05 \text{ Å}^{-1}$ during the structure searches. In the final structure refinements, a denser grid of $2\pi \times 0.03$ Å⁻¹ was used and the ionic relaxations stop when the force on each atom is smaller than 0.01 eV/Å. Intrinsic

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FIG. 1. Crystal structures of (a) $Fe_{16}N_2$, space group I4/mmm with a = 5.68 Å, c = 6.22 Å, and N 2a (0.0, 0.0, 0.0), Fe 4d (0.0, 0.5, 0.25); (b) $Fe_{12}Co_4N_2$, space group I4/mmm with a = 5.64 Å, c = 6.24 Å, and N 2b (0.0, 0.0, 0.5), Co 4d (0.0, 0.5, 0.25), Fe 8h (0.255, 0.255, 0.0), Fe 4e (0.0, 0.0, 0.793); (c) $Co_{16}N_2$, space group Fm-3m with a = 7.19 Å and N 4a (0.0, 0.0, 0.0), Co 24e (0.260, 0.260, 0.260), Co 8c (0.25, 0.25). (d) Phonon density of states of the structures plotted in (a–c).

magnetic properties, such as magnetic moment and MAE, were also calculated by VASP based on the theoretically optimized structures. All symmetry operations are switched off completely when the spin-orbit coupling is turned on. Meanwhile, a much denser *k*-point grid $(2\pi \times 0.016 \text{ Å}^{-1})$ is used in the MAE calculations to achieve better *k*-point convergence.

III. RESULTS AND DISCUSSION

Based on the structures obtained from our AGA searches, we found that mixing Co with Fe can significantly enhance the magnetic anisotropy as compared to that of $Fe_{16}N_2$ when the Co concentration is smaller than that of Fe. A large value of MAE ($\sim 3.18 \text{ MJ/m}^3$) is found in one of the metastable Fe₁₂Co₄N₂ structures, which is the highest among the rareearth-free magnets reported so far. In Figs. 1(a)-1(c), the crystal structures of $Fe_{16}N_2$, $Fe_{12}Co_4N_2$ (the one with largest MAE), and Co₁₆N₂ are plotted. The Fe₁₂Co₄N₂ structure can be considered as a substituted Fe₁₆N₂ structure with Fe at the 4d sites being replaced by Co. For $Fe_{16}N_2$, our calculation gives an MAE of 50.1 $\mu eV/Fe$ atom (or 0.64 MJ/m³), consistent with Ref. [17] where a value of 52 μ eV/Fe atom (or 0.65 MJ/m³) was reported from GGA calculations using the theoretically optimized structure. The Co₁₆N₂ structure has nearly zero MAE due to its cubic symmetry.

To demonstrate that these structures are dynamically stable, in Fig. 1(d) the phonon density of states of each of these three structures is plotted. The phonon calculation was performed using a supercell approach by the PHONOPY code [25], where supercells with sizes of 324 atoms for $Fe_{16}N_2$ and $Fe_{12}Co_4N_2$ and 288 atoms for $Co_{16}N_2$ were used. The results show that there are no negative frequencies in all three structures, indicating these structures are dynamically stable.

In addition to the $Fe_{12}Co_4N_2$ structure, other metastable Fe-Co-N structures from our AGA searches also exhibit large MAE. The compositions, energies, and MAE of these structures are presented in Fig. 2. Different symbols used in Fig. 2 indicate structures with different MAE values:



FIG. 2. Formation energies and the structural evolution of $Fe_{16-x}Co_xN_2$ as the function of Co concentration *x*. The formation energy is calculated using $Fe_{16}N_2$ and $Co_{16}N_2$ as references: $E_f(Fe_{16-x}Co_xN_2) = \{E(Fe_{16-x}Co_xN_2) - (1 - x/16)[E(Fe_{16}N_2)] - x/16[E(Co_{16}N_2)]\}/18$. The solid blue line connects the $TM_{16}N_2$ -type structures (represented by the blue squares; see also text). The convex hull is shown by the black dashed line. Calculated structures with high MAEs are indicated by different symbols: green squares $(1.5 < MAE < 2.0 \text{ MJ/m}^3)$, black circles $(2.0 < MAE < 3.0 \text{ MJ/m}^3)$, and red stars $(MAE > 3.0 \text{ MJ/m}^3)$. Crystal structures are plotted for **a**, **b**, ..., **f** as labeled in the formation energy figure.



FIG. 3. (a) The c/a ratio and volume per formula unit (8 *TM* atoms, 1 N atom) of the $Fe_{16-x}Co_xN_2$ structures as a function of *x* from DFT calculations with spin polarization (solid blue and red lines) and without spin polarization (dashed blue and red lines). Black dashed line represents $c/a = \sqrt{2}$, which is the value for an ideal fcc structure. (b) Electronic density of state of the $Fe_{16}N_2$ in the cubic (Fe_8N -c) and tetragonal (Fe_8N -t) structures. Fermi level is indicated by the vertical dashed lines (two lines are very close). (c) Energy difference between the tetragonal (E_1) and cubic (E_c) phases evaluated using rigid-band analysis as a function of the electron doping. (d) The largest MAE values obtained at each composition and magnetic moment of the transition metal atoms calculated for the $TM_{16}N_2$ -type structures. In plots (a,d), the calculated volume and magnetic moment for the lowest-energy $Fe_8Co_8N_2$ structure are represented by green open squares.

1.5 $MJ/m^3 < MAE < 2.0 MJ/m^3$ (green squares), 2.0 $MJ/m^3 < MAE < 3.0 MJ/m^3$ (black circles), and $MAE > 3.0 MJ/m^3$ (red stars), respectively. From Fig. 2, it is clear that no structure in the Co-rich side has MAE larger than 1.5 MJ/m^3 . On the contrary, many structures in the Fe-rich side have high MAE. We will show that the trend of MAE is correlated with a structural transition as the function of Co concentration.

Based on the results from our AGA search, the lowestenergy structure of $Co_{16}N_2$ is cubic rather than tetragonal. In Fig. 2, $Co_{16}N_2$ is plotted in a different view so that its relationship to the tetragonal-Fe₁₆N₂ structure can be seen more clearly. The structure of Fe₁₆N₂ has larger distortion than $Co_{16}N_2$, causing the symmetry to be degraded to a tetragonal space group. In fact, Fe atoms in Fe₁₆N₂ have been considered to form distorted bct structure in previous studies [14,17]. In the Fe₁₆N₂ structure the bond length between each Fe and its 12 nearest neighbors varies gradually from 2.43 to 3.11 Å, while in the $Co_{16}N_2$ structure, the Co atoms are in a face-centered cubic (fcc) lattice; thus each Co bonds to 12 Co neighbors with almost the same bond length.

In order to build the connection between these two structures, we notice that the fcc structure of Co_{16}N_2 (a = 7.19 Å) can also be represented by a bct unit cell with $a' = a/\sqrt{2} = 5.08$ Å and c = a = 7.19 Å; i.e., the c/a ratio of the tetragonal cell equals $\sqrt{2}$. The Fe₁₆N₂ structure, on the other hand, is being squeezed along the *c* axis, and has a larger a (= 5.68 Å) and smaller c (= 6.22 Å). The c/a ratio in the Fe₁₆N₂ structure is about 1.09, much smaller than that of Co₁₆N₂. Despite the difference in the c/a ratio, these two structures can be classified as the same type of structure, which will be referred to as the $TM_{16}N_2$ type in the following discussions. As shown in Fig. 2, the lowest-energy structures at different compositions all belong to the $TM_{16}N_2$ -type structures (represented by the blue squares and connected by the blue line), except the lowest-energy structure of Fe₈Co₈N₂ which has a different prototype structure as shown in Fig. 2.

We note that there is a structural transition as the Co concentration increases. To obtain the transition point, we plot the c/a ratio and volume of the $TM_{16}N_2$ -type structures (represented by the blue squares in Fig. 2) as a function of Co concentration as shown in Fig. 3(a). For cubic structures such as $Co_{16}N_2$ and $Co_{12}Fe_4N_2$, the c/a value is $\sqrt{2}$ as explained above. The results in Fig. 3(a) clearly show a sudden increase in c/a at the composition of $Fe_8Co_8N_2$. For the Co-rich side, all the c/a ratios are close to $\sqrt{2}$, while on the Fe-rich side including Co : Fe = 1, the c/a drops to around 1.1. Note that the bct structures with c/a ratios of 1 and $\sqrt{2}$ are both cubic structures. In order to measure the tetragonality of the Fe_{16-x}Co_xN₂ structures, we define a parameter $\gamma = \sqrt{|(c/a - 1) \times (\sqrt{2} - c/a)|}$, which is the geometric mean of the distances between the c/a ratio of a given structure and that of the bcc (c/a = 1) and fcc $(c/a = \sqrt{2})$ structures. We found that γ is around 0.18 for $x \leq 8$, while it drops to ~0.0 for x > 8, thus serving as a clear indicator of the tetragonal-like to cubiclike structure transition. In addition to c/a, at the transition point from the Fe-rich side to the Co-rich side, there is a nearly 4% sudden drop in volume, which can also be considered as the signal of the structure transformation.

The sudden changes in c/a ratio (as well as γ) and volume at the transition can be attributed to the magnetic effects. It is interesting to note that without spin polarization, the abovementioned structure transition disappears as shown by the dashed lines in Fig. 3(a). All structures with different compositions have the c/a ratio close to $\sqrt{2}$ if spin polarization is turned off in the calculations. At the same time, the volume of the structures is much smaller and increases very slowly as the Co concentration increases. These results indicate that magnetism plays a crucial role for the structural transition in this system.

We further carried out a rigid-band perturbation analysis to better understand the mechanism of the structural transition upon TM substitution in $Fe_{16}N_2$. Figure 3(b) shows the electronic density of states of Fe₁₆N₂ in cubic and tetragonal phases. The electrostatic potential is aligned such that the band energy is equal to the total energy in each system, which was previously used in the development of the tight-binding potentials [26]. By valence electron counting, substitution of one Fe atom with a Mn, Co, or Ni atom corresponds to doping of one hole, one electron, or two electrons, respectively. If all Fe atoms are replaced, the structures will be $Mn_{16}N_2$, $Co_{16}N_2$, and $Ni_{16}N_2$, respectively. The difference of band energy between the tetragonal and cubic phases as the function of electron doping (i.e., the number of valence electrons per TM atom relative to that of Fe) in the system is shown by the solid line in Fig. 3(c). The trend predicted by the rigid-band analysis is remarkably consistent with the actual total energy calculation results shown by the stars where the atomic relaxations are also included. Similar analyses based on the Co₁₆N₂ cubic and tetragonal structures give the same trend, as shown by the dashed line in Fig. 3(c). Therefore the band structure effect through electron or hole doping by substitution of other TM atoms with similar atomic radius in Fe₁₆N₂ plays a dominant role in the structural transition of this series of compounds.

The structural transition from tetragonal-Fe₁₆N₂ to cubic-Co₁₆N₂ is strongly correlated with the magnetic properties of the system. The magnetic moments of the TM atoms calculated for the lowest-energy $TM_{16}N_2$ -type structures are plotted in Fig. 3(d), together with that of the Fe₈Co₈N₂ ground-state structure. It can be seen that the behavior of magnetic moment variation is almost the same as that of volume variation. A sudden decrease in magnetic moment near the structural transition point is also observed, which can be attributed to the well-known fact that larger volume gives larger moment [17,27]. For the magnetic anisotropy, as mentioned earlier,



FIG. 4. (a) Formation energies and (b) magnetic properties of the structures obtained from enumerating all the possible Fe/Co occupations in the tetragonal-Fe₁₆N₂ [for $x(Co) \leq 8$] and cubic-Co₁₆N₂ [for $x(Co) \leq 8$] structures using a unit cell size of 18 atoms. The energies of tetragonal-Fe₁₆N₂ and cubic-Co₁₆N₂ structures were used as reference in the formation energy calculation. "()" in (b) represents the averaged values: The magnetic moments were averaged over all the calculated structures, while the MAE numbers were averaged over the ten lowest-energy structures at each composition. Error bar represents one standard deviation.

after the structure transition, i.e., on the Co-rich side, no structure is found to have MAE larger than 1.5 MJ/m^3 , while before the transition structures are found to have much larger MAEs, which can also be seen from Fig. 3(d). This can now be explained from the perspective of crystal structures. The Co-rich structures prefer cubiclike structures, and thus are unlikely to have strong anisotropy. On the other hand, the shape anisotropy in the Fe-rich tetragonal structures can enhance the MAE.

It should be noted that the magnetic properties of the $TM_{16}N_2$ -type structures presented in Fig. 3(d) are for stoichiometric compounds. Since the energies of Fe-Co-N alloys with different Fe/Co site occupations are very close to each other, it is likely that at finite temperature disordered site occupation between Fe and Co would occur; thus an alloy of $Fe_{16-x}Co_xN_2$ will form instead of stoichiometric compounds. The effects of Fe and Co occupation disorder on the magnetic properties should be considered in material design and processing. As discussed above, there is a sharp structural phase transition at x = 8 between Fe-rich tetragonal and Co-rich cubic structures. Therefore, it is a good approximation to adopt the lattice parameters of tetragonal Fe₁₆N₂ for the Fe-rich alloys $(x \leq 8)$ and those of cubic Co_{16}N_2 for the Co-rich $(x \geq 8)$ $Fe_{16-x}Co_xN_2$ alloys. We enumerated all the possible Fe/Co occupations in the tetragonal-Fe₁₆N₂/cubic-Co₁₆N₂ structures using a unit cell size of 18 atoms. The atomic positions in the unit cells are fully relaxed by DFT calculations while the lattice parameters of the structures are kept fixed. The results are shown in Fig. 4. As one can see from Fig. 4(a), the energy spread due to the site occupation disorder can be as large as 50-60 meV/atoms. However, the magnetic moment as the function of composition averaged over all the structures at each composition as shown in Fig. 4(b) is very similar to that of the lowest-energy structure plotted in Fig. 3(d). Since the calculation of MAE is very costly, in Fig. 4(b) we plotted the MAE results averaged over the ten lowest-energy configurations for different Co concentrations. Although the averaged MAEs are slightly smaller than the results calculated for stoichiometric compounds, the maximum value appears at the same composition, i.e., Fe₁₂Co₄N₂. Between the MAE and magnetic moment, it is easy to notice that the error bar in MAE is much larger, indicating that magnetic anisotropy is more sensitive to the change of structures. We have also performed calculations in which both atomic position and lattice parameters are allowed to relax. The behavior of the magnetic moment and MAE as the function of Co concentration is essentially the same as in Fig. 4(b) except the transition at x(Co) = 8 is smoothed out when the lattice parameters are allowed to relax.

IV. CONCLUSION

In conclusion, our study on $Fe_{16-x}Co_xN_2$ reveals a structure transition as the Co concentration increases, which can be well explained by rigid-band perturbation analysis. From the cubic-Co₁₆N₂ structure to the tetragonal-Fe₁₆N₂ structure, magnetic

moments of the system increase while magnetocrystalline anisotropy is maximized at the composition near $Fe_{12}Co_4N_2$. The substantial improvement in the magnetic properties predicted for both ordered stoichiometric compounds and alloys with disordered Fe/Co occupations makes it possible for $Fe_{16-x}Co_xN_2$ to find applications as a rare-earth-free magnet. The stability of this system is still an important issue to consider. Although the structures discussed here are proven to be dynamically stable, we see that when using $Fe_{16}N_2$ and $Co_{16}N_2$ (which are metastable already) as references, only $Fe_4Co_{12}N_2$ is stable against decomposition. But it is also noticed that energies of the other structures are within 20 meV/atom above the convex hull, which may be attainable by synthesis techniques at far-from-equilibrium conditions.

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