# **Density functional theory study of bulk and single-layer magnetic semiconductor CrPS4**

Houlong L. Zhuang<sup>1,\*</sup> and Jia Zhou<sup>2,†</sup>

<sup>1</sup>*Department of Mechanical and Aerospace Engineering, Princeton University, Princeton, New Jersey 08544, USA* <sup>2</sup>*MIIT Key Laboratory of Critical Materials Technology for New Energy Coversion and Storage, School of Chemistry and Chemical Engineering, Harbin Institute of Technology, Harbin 1500001, China* (Received 9 September 2016; published 16 November 2016)

Searching for two-dimensional (2D) materials with multifunctionality is one of the main goals of current research in 2D materials. Magnetism and semiconducting are certainly two desirable functional properties for a single 2D material. In line with this goal, here we report a density functional theory (DFT) study of bulk and single-layer magnetic semiconductor CrPS4. We find that the ground-state magnetic structure of bulk CrPS4 exhibits the A-type antiferromagnetic ordering, which transforms to ferromagnetic (FM) ordering in single-layer CrPS4. The calculated formation energy and phonon spectrum confirm the stability of single-layer CrPS4. The band gaps of FM single-layer CrPS<sub>4</sub> calculated with a hybrid density functional are within the visible-light range. We also study the effects of FM ordering on the optical absorption spectra and band alignments for water splitting, indicating that single-layer CrPS4 could be a potential photocatalyst. Our work opens up ample opportunities of energy-related applications of single-layer CrPS4.

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# **I. INTRODUCTION**

Magnetic semiconductors are an important category of materials that exhibit magnetism in combination with semiconducting properties [\[1\]](#page-5-0). Typical examples of magnetic semiconductors include transition-metal oxides (e.g., NiO) [\[2,3\]](#page-5-0) and chalcogenides (e.g.,  $\text{FeCr}_2\text{S}_4$ ) [\[4\]](#page-6-0). Among many known magnetic semiconductors, the ones that possess layered structures (e.g.,  $CrXTe_3$ ;  $X = Si$ , Ge, and Sn) [\[5–9\]](#page-6-0) with a van der Waals (vdW) gap between the layers are of particular interest, as they could be thinned down to a single layer, which is often associated with improved properties due to the dimension reduction.

A number of single-layer magnetic semiconductors have been predicted via Kohn-Sham density functional theory (DFT) simulations [\[10–13\]](#page-6-0). Most of the proposed applications of the magnetic semiconductors center around employing the spin degree of freedom for spintronics devices [\[6\]](#page-6-0). By contrast, significantly fewer studies have explored solar-energy-related applications of single-layer magnetic semiconductors. To fill this gap, Zhang *et al.* recently computed the band-edge positions of single-layer antiferromagnetic (AFM) MnPSe<sub>3</sub> and suggested this single-layer material could be a promising photocatalyst for water splitting [\[14\]](#page-6-0).

Inspired by three previous experimental reports [\[15–17\]](#page-6-0), here we focus on a relatively less well known magnetic semiconductor CrPS<sub>4</sub>. Diehl and Carpentier [\[15\]](#page-6-0) first synthesized bulk CrPS<sub>4</sub> and determined its layered structure. Louisy *et al.* measured the magnetic susceptibility and optical spectra of bulk CrPS4 [\[16\]](#page-6-0). More recently, Pei *et al.* studied spin dynamics, electronic, and thermal transport properties of bulk CrPS4 [\[17\]](#page-6-0). In spite of these experimental studies of bulk CrPS4, theoretical perspectives on this compound are still lacking. Furthermore, although two of the experiments [\[16,17\]](#page-6-0)

have shown bulk  $CrPS<sub>4</sub>$  is AFM, no direct evidence exists to clarify a specific type of AFM ordering.

In this work, we perform DFT calculations on bulk CrPS4 with the ferromagnetic (FM) and four different types of AFM ordering. We find that the A-type AFM structure is the ground state, albeit the total energy of the FM structure is nearly degenerate. We further predict that single-layer  $CrPS<sub>4</sub>$  remains semiconducting, while the magnetic structure becomes FM. We show that the formation energy of single-layer  $CrPS<sub>4</sub>$  is sufficiently small, so that it could be obtained from mechanically exfoliating bulk  $CrPS<sub>4</sub>$ . The computed phonon spectrum of single-layer CrPS<sub>4</sub> confirms the dynamical stability. The band gaps of FM single-layer CrPS<sub>4</sub> are not only wider than those of bulk  $CrPS<sub>4</sub>$  but also within the range of visible light, which is promising for solar-energy-conversion applications. Finally, we demonstrate an example of these applications by showing that the band-edge positions of single-layer  $CrPS<sub>4</sub>$  are energetically favorable for splitting water to generate hydrogen.

#### **II. METHODS**

We perform spin-polarized DFT simulations on bulk and single-layer CrPS<sub>4</sub> using the Vienna Ab initio Simulation Package (VASP) [\[18,19\]](#page-6-0). We employ the Perdew-Burke-Ernzerhof (PBE) [\[20\]](#page-6-0) functional to describe the exchange and correlation. We also use the van der Waals density functional with optimized Becke88 parameterizations (vdW-DF-optB88) [\[21–24\]](#page-6-0) functional to account for the interlayer van der Waals interactions in bulk  $CrPS<sub>4</sub>$ . We employ the PBE version of the projector augmented-wave (PAW) [\[25,26\]](#page-6-0) potentials with the  $3s^23p^63d^54s^1$  states of Cr, the  $3s^23p^3$  states of P, and the  $3s<sup>2</sup>3p<sup>4</sup>$  states of S treated as valence electrons. The truncated plane-wave basis set has a cutoff energy of 500 eV. As the initial input geometry for the subsequent optimizations, the bulk CrPS<sub>4</sub> structure documented in the Inorganic Crystal Structure Database (ICSD) [\[27\]](#page-6-0) with the ID number 626520 is used. We use one layer of the bulk structure to build a supercell model for single-layer CrPS<sub>4</sub> with a vacuum spacing of 18  $\AA$ , which is sufficiently large to separate the image interactions

<sup>\*</sup>hzhuang@princeton.edu

<sup>†</sup> jiazhou@hit.edu.cn

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FIG. 1. Schematic illustration of (a) top and (b) side views of a unit cell of single-layer CrPS4.

between the layers. Figure 1 illustrates a single-layer CrPS<sub>4</sub> unit cell. The four Cr atoms in the unit cell on the *xy* plane form a trapezoidlike configuration. Each Cr atom locates at the center of a distorted octahedron with six neighboring S atoms. Viewed along the *y* direction, the crystal structure of single-layer CrPS4 is a quasi-one-dimensional structure with chains of distorted  $CrS_6$  octahedra bridged by P atoms. Integration over the first Brillouin zone is carried out on

 $6 \times 9 \times 1, 6 \times 9 \times 12, 6 \times 9 \times 12,$  and  $6 \times 9 \times 6$  *C*-centered Monkhorst-Pack [\[28\]](#page-6-0) grids for a 24-atom single-layer CrPS<sub>4</sub> unit cell, a 24-atom FM bulk CrPS<sub>4</sub> unit cell, 24-atom C-type AFM bulk  $CrPS<sub>4</sub>$  unit cell, and the other three 48-atom AFM bulk CrPS<sub>4</sub> supercells, respectively. The lattice parameters of bulk  $CrPS<sub>4</sub>$ , the in-plane lattice constants of single-layer CrPS4, and the atomic positions of all structures are completely relaxed using the conjugate gradient method until the convergence criterion that the residual interatomic forces are below 0.01 eV/ $\AA$  is satisfied.

To facilitate referencing various magnetic structures, we use notation to denote the arrangement of magnetic moments of Cr atoms. This notation combines the atom labels used in Fig. 1 with an upward or downward arrow in the subscript. The upward and downward arrows symbolize the spin-up and spin-down directions, respectively. The Cr atoms in a neighboring unit cell along the *z* direction are additionally labeled with a prime symbol in the superscript. With this notation, for example, the A-type AFM ordering is labeled by  $I_{\uparrow}II_{\uparrow}III_{\uparrow}IV_{\uparrow}I'_{\downarrow}III'_{\downarrow}IV'_{\downarrow}$ . Table I lists all the types of magnetic structures considered in this work and their corresponding notations.

We adopt the finite-displacement method [\[29\]](#page-6-0) as implemented in PHONOPY [\[30\]](#page-6-0) to calculate the phonon spectrum of single-layer CrPS4. The symmetry of single-layer CrPS4 results in thirty-six  $3 \times 3 \times 1$  supercells with inequivalent atomic displacements. For the force calculations with VASP, only the  $\Gamma$  point of each supercell is used.

### **III. RESULTS AND DISCUSSION**

We first examine whether the above simulation parameters are able to reproduce several basic properties of bulk CrPS4, including lattice parameters, ground-state magnetic structure, and electronic band gap, all of which have corresponding

TABLE I. Lattice parameters *a* (A), *b* (A), *c* (A), and  $\beta$  (degrees); energy difference  $\Delta E$  (meV per formula unit); band gap (eV); and electron magnetic moment *m* (in units of  $\mu_B$ ) per Cr atom of bulk CrPS<sub>4</sub> calculated with the PBE and vdW-DF-optB88 functionals. The energy difference is computed using the energy of the A-type AFM structure as the reference.

Magnetic ordering	Method	$\boldsymbol{a}$	b	$\boldsymbol{c}$	β	$\Delta E$	$E_{g}$	$\boldsymbol{m}$
FM	PBE	10.88	7.33	6.89	91.64	0.25	$1.10^{a}$ $1.35^{b}$	2.58
$I_{\uparrow}II_{\uparrow}III_{\uparrow}IV_{\uparrow}I'_{\uparrow}II'_{\uparrow}III'_{\uparrow}IV'_{\uparrow}$	vdW-DF-optB88	10.93	7.27	6.09	92.23	1.19	$1.01^{a}$ 1.17 <sup>b</sup>	2.58
A-type AFM	<b>PBE</b>	10.88	7.33	6.88	91.60	$\overline{0}$	0.79	2.58
$\mathbf{I}_\uparrow\mathbf{II}_\uparrow\mathbf{III}_\uparrow\mathbf{IV}_\uparrow\mathbf{I}'_\downarrow\mathbf{II}'_\downarrow\mathbf{III}'_\downarrow\mathbf{IV}'_\downarrow$	vdW-DF-optB88	10.93	7.27	6.09	92.21	$\Omega$	0.73	2.58
C-type AFM	<b>PBE</b>	10.93	7.24	6.88	91.25	19.35	1.32	2.51
$\mathbf{I}_{\uparrow}\mathbf{II}_{\downarrow}\mathbf{III}_{\uparrow}\mathbf{IV}_{\downarrow}\mathbf{I}'_{\uparrow}\mathbf{II}'_{\downarrow}\mathbf{III}'_{\uparrow}\mathbf{IV}'_{\perp}$	vdW-DF-optB88	10.98	7.19	6.11	91.80	10.40	1.23	2.51
E-type AFM	<b>PBE</b>	10.91	7.28	6.87	91.46	13.50	1.02	2.54
$\mathbf{I}_\uparrow\mathbf{II}_\uparrow\mathbf{III}_\downarrow\mathbf{IV}_\uparrow\mathbf{I}'_\downarrow\mathbf{II}'_\downarrow\mathbf{III}'_\uparrow\mathbf{IV}'_\downarrow$	vdW-DF-optB88	10.95	7.23	6.10	91.99	8.71	0.96	2.54
G-type AFM	<b>PBE</b>	10.94	7.24	6.89	91.22	19.07	1.28	2.51
$\mathbf{I}_{\uparrow}\mathbf{II}_{\downarrow}\mathbf{III}_{\uparrow}\mathbf{IV}_{\downarrow}\mathbf{I}'_{\perp}\mathbf{II}'_{\uparrow}\mathbf{III}'_{\perp}\mathbf{IV}'_{\uparrow}$	vdW-DF-optB88	10.98	7.19	6.11	91.79	11.23	1.16	2.51
NΜ	<b>PBE</b>	11.45	6.52	6.88	89.89	781.37	0 <sup>c</sup>	
	vdW-DF-optB88	11.45	6.59	6.17	89.05	671.27	0 <sup>c</sup>	
Undertermined	Experiment [15]	10.87	7.25	6.14	91.88			
AFM	Experiment $[16]$	10.86	7.25	6.14	91.87		1.40	
<b>AFM</b>	Experiment [17]	10.86	7.25	6.14	91.88		0.17	

a Spin up.

bSpin down.

c Metallic.

experimental data for comparison. Bulk  $CrPS<sub>4</sub>$  crystallizes as a monoclinic structure with the *C*2 space group [\[16\]](#page-6-0); it therefore has four independent lattice parameters: *a,b,c*, and angle *β*. Table [I](#page-1-0) reports the calculated lattice parameters using both the PBE and vdW-DF-optB88 functionals. For the completeness of comparison, we also list the results of the nonmagnetic (NM) structure, for which no spin-polarized DFT calculations are involved. As can be seen from Table [I,](#page-1-0) the resulting lattice parameters are nearly independent of the FM and AFM structures. We also observe that, although the PBE functional leads to  $a, b$ , and  $\beta$  that agree well with the experimental data, the lattice constant  $c$  seems to be overestimated. Including the vdW-DF-optB88 functional is thus important to obtain excellent agreement between the theoretical and experimental lattice constant *c*. The lattice parameters *a*, *b*, and  $\beta$  of the NM structure, on the other hand, are quite different from all of the FM, AFM, and experimental results.

We next compare the total energies of FM and four AFM bulk  $CrPS<sub>4</sub>$  structures. Table [I](#page-1-0) reveals the ground-state magnetic structure of bulk  $CrPS<sub>4</sub>$  exhibits the A-type AFM ordering because the energy differences between the other magnetic structures and the A-type AFM structure are all positive.We also notice that the total energy of the FM structure is nearly identical to that of the A-type AFM structure, and the NM structure shows much larger energy differences than the other structures. The predicted AFM ordering is, overall, consistent with the two above-mentioned experiments which measured the temperature-dependent magnetic susceptibility [\[16,17\]](#page-6-0). However, our predicted AFM type is different from the C type suggested in Ref. [\[17\]](#page-6-0). Table [I](#page-1-0) contrastingly shows the energy of C-type AFM structure is higher than that of the A-type AFM structure. Determination of the type of AFM ordering requires the neutron diffraction technique. Future experiments involving this technique are therefore called for to provide decisive evidence of the type of AFM ordering in bulk CrPS4. Given that the A-type AFM ordering exhibits the minimum total energy, we therefore use it as the reference to calculate the formation energy of single-layer bulk  $CrPS<sub>4</sub>$  (see below).

Figure 2 shows the density of states (DOS) of FM, AFM, and NM bulk  $CrPS<sub>4</sub>$  computed with the PBE and vdW-DF-optB88 functionals. All the magnetic structures except the NM one are semiconducting. Table [I](#page-1-0) summarizes the theoretical band gaps and available experimental data. The optical transmission spectra reported in Ref. [\[16\]](#page-6-0) show that bulk CrPS<sub>4</sub> is an indirect band gap semiconductor with a band gap of around 1.40 eV. The band gap (0.79 eV) of A-type AFM bulk CrPS4 calculated with the PBE functional is expectedly smaller than the experimental band gap since the PBE functional underestimates the band gap due to self-interaction errors [\[31–33\]](#page-6-0). Interestingly, Ref. [\[17\]](#page-6-0) reports a drastically smaller band gap (0.17 eV). In this reference, instead of measuring the optical spectra, the band gap is derived from the variation of electrical resistivity with temperature via the relation  $\rho \propto E g / k_B T$ . While this temperature dependence of the resistivity is true for an intrinsic semiconductor, a semiconductor is often an extrinsic one with a dominant (*n* or *p*) type of impurity. Therefore, the reported band gap in Ref. [\[17\]](#page-6-0) most likely corresponds to the donor or acceptor ionization energy, as a similar exponential relation



FIG. 2. DOS of bulk  $CrPS<sub>4</sub>$  with (a) and (b) FM, (c)–(j) four different types of AFM, and (k) and (l) NM structures obtained from DFT calculations with the PBE and vdW-DF-optB88 functionals.

exists between the resistivity, ionization energy, and temperature [\[34\]](#page-6-0).

A-type AFM bulk  $CrPS<sub>4</sub>$  exhibits FM ordering within each layer but AFM ordering between layers. We therefore expect the magnetic structure of single-layer  $CrPS<sub>4</sub>$  to become FM as the number of layers is reduced to one. Indeed, our PBE energy calculations show that single-layer  $CrPS<sub>4</sub>$  with FM ordering  $(I_1 II_1 II_1 IV_1)$  is more stable than other possible magnetic structures. For example, the PBE total energies of the  $I_{\uparrow}II_{\uparrow}III_{\downarrow}IV_{\downarrow}$  and  $I_{\uparrow}II_{\downarrow}III_{\downarrow}IV_{\uparrow}$  structures are, respectively, 4.56 and 27.07 meV*/*f.u. higher than that of the FM structure. The occurrence of FM ordering in single-layer CrPS<sub>4</sub> appears to contradict the remarkable Mermin-Wagner theorem claiming the absence of long-range order in a two-dimensional (2D) system [\[35\]](#page-6-0). However, noncollinear calculation including spin-orbit coupling shows single-layer CrPS<sub>4</sub> exhibits a sizable anisotropy energy of 40.0  $\mu$ eV per Cr atom with the spins favorably aligned along the out-of-plane (*z*) direction. This magnetocrystalline anisotropy implies single-layer CrPS4 belongs to the category of 2D Ising magnets, which are a notable exception of the Mermin-Wagner theorem [\[36\]](#page-6-0).

TABLE II. In-plane lattice constants  $a$  and  $b$  ( $\AA$ ) and electron magnetic moment *m* (in units of  $\mu_B$ , the Bohr magneton) per Cr atom and formation energy  $E_f^{\text{PBE}}$  (meV/atom) of single-layer CrPS<sub>4</sub> calculated with the DFT-PBE method. The formation energy  $E_f^{\text{vdW}}$ calculated with the vdW-DF-optB88 functional is also shown for comparison.

a		m	$E_{\rm f}^{\rm PBE}$	$E_{\rm f}^{\rm vdW}$	
10.86	7.32	2.58	1.44	71.60	

Table II lists the in-plane lattice constants (*a* and *b*) of single-layer  $CrPS<sub>4</sub>$  and the electron magnetic moment of each Cr atom. These parameters are very similar to the values they are in bulk CrPS<sub>4</sub>. The optimized Cr<sub>I</sub>-Cr<sub>IV</sub> and Cr<sub>II</sub>-Cr<sub>III</sub> distances are both 5.43  $\AA$ , which is much longer than the  $Cr_I-Cr_{II}$  and  $Cr_{III}-Cr_{IV}$  distances, which are 3.73 and 3.59 A, respectively.

We proceed to evaluate the stability of single-layer CrPS<sub>4</sub>. First, we adopt the common definition of the formation energy  $\Delta E_f$  for a 2D material; that is, the  $\Delta E_f$  of single-layer CrPS<sub>4</sub> is calculated via subtracting the energy of single-layer FM  $CrPS<sub>4</sub>$  from A-type AFM bulk  $CrPS<sub>4</sub>$  [\[37\]](#page-6-0). Table II shows that the  $\Delta E_f$  of single-layer CrPS<sub>4</sub> are 1.44 and 71.60 meV/atom calculated for the PBE and vdW-DF-optB88 functionals, respectively. These formation energies are sufficiently small, indicating that one feasible way of fabricating single-layer CrPS4 sheets is mechanically exfoliating synthesized bulk CrPS4. Second, we assess the dynamical stability of singlelayer CrPS<sub>4</sub>. Figure 3 shows the calculated phonon spectrum of single-layer CrPS<sub>4</sub>. The absence of imaginary phonon modes confirms the dynamical stability.

Having established the ground-state magnetic structure of single-layer  $CrPS<sub>4</sub>$ , we set out to understand the electronic origin that gives rise to FM ordering in the 2D structure. We notice that the electron magnetic moment of each Cr atom in bulk (Table [I\)](#page-1-0) and single-layer CrPS<sub>4</sub> (Table II) is



FIG. 3. Theoretical phonon spectrum of single-layer CrPS<sub>4</sub> obtained from DFT calculations with the PBE functional. The highsymmetry  $q$  points  $\Gamma$ ,  $X$ ,  $A$ , and  $Y$  have fractional coordinates of (0, 0), (1*/*2, 0), (1*/*2, 1*/*2), and (0, 1*/*2) of the 2D reciprocal lattice vectors, respectively.



FIG. 4. Charge-density difference between FM and AFM singlelayer CrPS4. Green and blue refer to electron accumulation and depletion, respectively. The isosurface value is set to 0.001  $e/a_0^3$ , with  $a_0$  being the Bohr radius.

close to  $3.0\mu_B$ , resulting from the oxidation state of  $+3$  in a Cr ion. The strongly localized magnetic moment suggests invoking exchange models to understand the mechanism of ferromagnetism. Along the *y* direction, the distance between Cr atoms is too large for the direct-exchange coupling to play an important role. The optimized  $Cr_{III}-S_V-Cr_V$  angle is 95.7°, which is near the ideal 90◦ bond angle usually associated with FM ordering, according to the Goodenough-Kanamori rules [\[38–40\]](#page-6-0). We therefore understand the exchange interactions between the Cr atoms through the superexchange interactions along the *y* direction. The exchange interactions along the *x* direction are more indirect because the Cr-Cr distance is even larger. This indirect exchange coupling is not only mediated by S atoms but also by P atoms, each of which is fourfold coordinated to surrounding S atoms. Figure 4 illustrates the total charge-density difference between the  $I_1 II_1 III_1 IV_1 (FM)$ and  $I_1I_2II_1II_1IV_1$  (AFM) magnetic structures. We observe significant charge redistributions around Cr and S atoms, implying strong exchange coupling along the *x* direction, which is also reflected by the above-shown sizable energy difference between the two magnetic structures.

Figure [5](#page-4-0) displays the PBE band structures of the spin-up and spin-down electrons. The spin-up band structure exhibits an indirect band gap of 1.13 eV with the conduction band minimum (CBM) located at the  $\Gamma$  point and the valence band maximum (VBM) at the *A* point. The CBM is twofold degenerate, with the effective masses of the heavy and light electrons being  $1.96 m_0$  and  $1.26 m_0$ , respectively, where  $m_0$ is the rest mass of the electron. The hole effective mass *mh* at the VBM is  $0.76 m_0$ , which is significantly smaller and only slightly heavier than that of single-layer  $MoS<sub>2</sub>$  with a theoretical  $m_h$  of 0.54 $m_0$  [\[41\]](#page-6-0). By contrast, the band gap of 1.42 eV in the spin-down band structure is direct and wider than that of the spin-up band gap. The electron and hole effective masses are  $0.87 m_0$  and  $1.52 m_0$ , respectively. Both spin-up and spin-down band gaps are significantly larger than the band gap of A-type AFM bulk  $CrPS<sub>4</sub>$  due to the quantum confinement effect. Owing to the much smaller hole effective

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FIG. 5. (a) Spin-up and (b) spin-down band structures of singlelayer CrPS<sub>4</sub> calculated with the DFT-PBE method. The Fermi level of the spin-up band structure is set to zero, while the spin-down band structure is shifted by the same magnitude of electron energy.

mass, we suggest*p*-type doping is an effective strategy to attain the highest carrier mobility when using single-layer  $CrPS<sub>4</sub>$  in electronic devices.

We also employ the Heyd-Scuseria-Ernzerhof [\[42,43\]](#page-6-0) (HSE06) hybrid density functional to obtain more accurate band gaps of single-layer CrPS<sub>4</sub>. Figure  $6(a)$  shows the resulting HSE06 spin-up and spin-down DOSs, with corresponding band gaps of 2.42 and 2.61 eV, respectively. These band gaps are within the visible-light spectrum, suggesting that single-layer  $CrPS<sub>4</sub>$  is a promising candidate for a variety of solar-energy-conversion applications. In addition to using the HSE06 functional, we attempt to calculate the band gaps of single-layer CrPS<sub>4</sub> using a computationally cheaper PBE + *U* method with the rotationally invariant  $U_{\text{eff}}$  [\[44\]](#page-6-0). We vary the  $U_{\text{eff}}$  parameters from 0 to 5.0 eV. Figure  $6(b)$  shows the *U*eff-dependent spin-up and spin-down band gaps. Both the spin-up and spin-down band gaps increase nearly linearly with the  $U_{\text{eff}}$  parameters. The two curves in Fig.  $6(b)$  are almost parallel to each other, showing that the difference between the two gaps is independent of the *U*eff parameter. The average increasing rate of the two band gaps is about 0.06; that is, adding 1.0 eV to the *U*eff only increases the band gaps by



FIG. 6. (a) DOS of single-layer bulk  $CrPS<sub>4</sub>$  calculated with the DFT-HSE06 method. (b) Variation of spin-up and spin-down band gaps with the  $U_{\text{eff}}$  parameters.

around 0.06 eV. As a result, if the HSE06 band gaps are used as the references and we assume a constant increasing rate of the band gaps with  $U_{\text{eff}}$ , an unphysically large  $U_{\text{eff}}$  parameter must be used in order to obtain the same magnitudes of the HSE06 band gaps.

Since single-layer  $CrPS<sub>4</sub>$  exhibits band gaps that are within the visible-light spectrum, we demonstrate an example of a potential solar-energy-conversion application of single-layer  $CrPS<sub>4</sub>$  as a photocatalyst for water splitting. Note that magnetism is not necessary for water splitting. However, we shall see that magnetism leads to spin-dependent optical properties. In the context of water splitting, two parameters, the optical absorption and band-edge positions, are of main relevance. For sunlight polarized within the plane of singlelayer material CrPS<sub>4</sub>, the optical absorbance  $A(\omega)$  is calculated as  $A(\omega) = \omega/cL\epsilon_{xx/yy}$  [\[45,46\]](#page-6-0), where *c* is the speed of light in vacuum and *L* is the length of the supercell in the *z* direction. The random-phase approximation and the PBE functional are adopted to calculate the *xx* and *yy* components of the imaginary part of the dielectric constant tensor [\[47\]](#page-6-0). Figure [7](#page-5-0) shows that the optical absorbance strongly depends not only on the polarization vectors of the light but also on the spin directions. The first absorption peaks in the optical absorption spectra originate from the excitations of the spin-up electrons. This is because the top valence band and the bottom conduction band in the spin-up band structure (Fig. 5) are almost parallel at most *k* points in the first Brillouin zone, which lead to a significantly enhanced joint density of states and the absorption peaks. The total optical absorbance of single-layer CrPS4

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FIG. 7. Optical absorbance of single-layer  $CrPS<sub>4</sub>$  transformed from the (a) *xx* and (b) *yy* components of the imaginary part of the dielectric constant tensor calculated at the DFT PBE level of theory.

around the first peaks ranges from 2% to 3%, which is similar to that (2.3%) of single-layer graphene [\[48\]](#page-6-0).

To determine the band-edge positions of single-layer CrPS4 with reference to the redox potentials of water splitting at  $pH = 0$ , we adopt Toroker's method [\[49\]](#page-6-0) to calculate the energy level of the band gap center (BGC)  $E_{BGC}$  of single-layer  $CrPS<sub>4</sub>$  with the assumption that the  $E_{BGC}$  is independent of the functionals used. The conduction and valence band edges are  $E_{BGC}$  +  $E_g/2$  and  $E_{BGC}$  –  $E_g/2$ , respectively. This method has been used to calculate the band-edge positions of a number of single-layer semiconductors [\[50,51\]](#page-6-0) such as group-III monochalcogenides [\[52\]](#page-6-0). Figure 8 illustrates the potential profiles and the corresponding spin-up and spindown  $E_{\text{BGC}}$  determined as  $-5.15$  and  $-5.65$  eV, respectively. The exchange-correlation potential is not included in the potential profiles, which are therefore spin independent. We use the HSE06 band gaps to evaluate the band-edge energy positions; then the conduction and valence band-edge energy levels for the spin-up electrons are −3*.*94 and −6*.*36 eV, respectively. Similarly, the conduction and valence band-edge energy levels for the spin-down electrons are −4*.*34 and −6*.*95 eV, respectively. The standard redox potentials (−4*.*44 and −5*.*67 eV) of the water-splitting reaction lie between



FIG. 8. Electrostatic potential profiles and  $E_{BGC}$  of single-layer CrPS4 calculated with the DFT-PBE method. The vacuum energy level is set to zero.

the calculated band-edge energy levels for both spin-up and spin-down electrons. We therefore suggest single-layer CrPS4 could be a suitable photocatalyst for solar water splitting.

## **IV. CONCLUSIONS**

In summary, we performed DFT calculations to show that the ground-state magnetic structure of bulk  $CrPS<sub>4</sub>$  is AFM, which is consistent with the experiment. We also found that the type of AFM ordering should be the A type. This prediction awaits experimental confirmation using the neutron diffraction technique. We further predicted that single-layer CrPS4 remains to be a semiconductor with enlarged spin-up and spin-down band gaps. However, the magnetic structure transforms to FM ordering due to the dimension reduction to an ultrathin layer. Finally, we showed a potential application of single-layer  $CrPS<sub>4</sub>$  as a photocatalyst for splitting water to generate hydrogen gas. We expect this work to stimulate interest in realizing single-layer CrPS<sub>4</sub> sheets in experiment. Future theoretical work includes studies of the magnetism effects on the other properties (e.g., thermoelectric and piezoelectric) of semiconducting single-layer CrPS4.

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