## **Optical activity of quantum wells**

L. V. Kotova,<sup>1,2</sup> A. V. Platonov,<sup>1</sup> V. N. Kats,<sup>1</sup> V. P. Kochereshko,<sup>1</sup> S. V. Sorokin,<sup>1</sup> S. V. Ivanov,<sup>1</sup> and L. E. Golub<sup>1</sup>

<sup>1</sup>*Ioffe Institute, 194021 St. Petersburg, Russia* <sup>2</sup>*ITMO University, 197101 St. Petersburg, Russia* (Received 7 July 2016; published 19 October 2016)

We report on the observation of optical activity of quantum wells resulting in the conversion of the light polarization state controlled by the light propagation direction. The polarization conversion is detected in reflection measurements. We show that a pure *s*-polarized light incident on a quantum well is reflected as an elliptically polarized wave. The signal is drastically enhanced in the vicinity of the light-hole exciton resonance. We show that the polarization conversion is caused by the spin-orbit splitting of the light hole states and the birefringence of the studied structure. The bulk inversion asymmetry constant  $\beta_h \approx 0.14$  eV Å is determined for the ground light hole subband in a 10 nm ZnSe/ZnMgSSe quantum well.

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Studies of polarization-sensitive optical effects allow creating optical devices and give access to fundamental properties of material systems. A very important effect intensively investigated and widely used in practice is a conversion of light polarization state [1,2]. Examples are the rotation of a linear polarization plane and the transformation of a pure linearly or circularly polarized wave into an elliptically polarized light. A possibility for the polarization conversion exists in systems of sufficiently low spatial symmetry. For example, birefringent media effectively rotate light polarization plane and produce light helicity. Basic examples are half- and quarter-wave plates made of birefringent crystals widely used in both laboratories and in industry. Recently, polarization conversion has been observed in metamaterials [2-4], twisted photonic crystal fibers [5], and microcavities [6]. While metamaterials convert light polarization due to a special design of building blocks, semiconductor nanostructures are birefringent as-grown. The polarization conversion has been demonstrated in a number of experiments on quantum wells (QWs) [7-11] and quantum dots [12,13]. The low symmetry of QWs can be caused by in-plane deformations [7,8,10] or by microscopic structure of interfaces [14,15], while the birefringence of self-assembled quantum dots appears due to their anisotropic shape [13].

Optical activity is an effect responsible for the polarization conversion controlled by the light propagation direction. It is present even in homogeneous systems whose point group symmetry belongs to a gyrotropic class, i.e., allows for a linear coupling between components of a vector and a pseudovector. Recently it has been shown that optical activity of metals is closely related to their band topology and Berry phase [16,17]. Optical activity in the visible spectral range is useful to investigate in semiconductors where they are greatly enhanced in the vicinity of exciton resonances [18]. Optical activity of bulk gyrotropic semiconductors is well established [19,20] being, however, still a topic of recent studies [21]. QWs grown of cubic semiconductors are gyrotropic: for the growth direction (001), point symmetry group of a QW is  $D_{2d}$  or  $C_{2v}$  depending on a presence of the structure inversion symmetry [22,23]. Recent theoretical studies showed that QWs are optically active in both cases [24,25]. However, experimental detection of optical activity has not been reported so far for OWs.

In this work, we address the fundamental question of whether real QWs are optically active. We report on the observation and study of optical activity in QWs. We demonstrate a resonant enhancement of the polarization conversion in the vicinity of the exciton transitions.

Before discussing the experimental results we address the basic physics of the optical activity and determine requirements to the experimental geometry. The optical activity induced polarization conversion can be conveniently described by an effective magnetic field  $B_{\rm eff}$  linear in the photon wave vector  $\boldsymbol{q}$ .  $\boldsymbol{B}_{\text{eff}}$  affects polarization of the reflected light similar to a real magnetic field in the magneto-optical Kerr effect. The effective magnetic field is nonzero due to bulk and structure inversion asymmetries of the QW [23,26]. Effective magnetic field results in a variety of remarkable effects in exciton physics, mostly studied in double QWs [27-29]. Optical activity is caused by the part of  $B_{\rm eff}$  which has a nonzero projection on q, Fig. 1(a). Therefore, structure inversion asymmetry resulting in  $B_{\rm eff} \perp q$  [23] does not manifest itself in optical activity. Bulk and interface inversion asymmetries in the  $D_{2d}$  point group result in the effective magnetic field lying in the QW plane. Therefore, optical activity can be observed only at oblique light incidence. Direction of  $B_{eff}$  depends on the orientation of the photon wave vector in respect to crystallographic axes, Fig. 1(b). The maximal value of the polarization conversion is achieved when the incidence plane contains one of cubic axes  $\langle 100 \rangle$ .

In order to investigate optical activity, we measure light reflection from a QW.<sup>1</sup> This method has been used for investigations of optical activity of gyrotropic bulk semiconductors [19,21]. Study of reflection allows for detecting the optical activity of QWs in special experimental geometries [25]. In particular, taking into account the in-plane components of the photon wave vector we derive that the electric field component  $E_z$  transforms according to the same representation ( $B_2$ ) of the  $D_{2d}$  point group as the combination  $q_x E_y + q_y E_x$ , while the pairs ( $E_x, E_y$ ) and ( $q_y E_z, q_x E_z$ ) transform according to the same representation (E). Therefore, an interaction

<sup>&</sup>lt;sup>1</sup>A possible reason why the optical activity has not been observed in QWs so far is that typically it is detected by the rotation of the light polarization as it propagates through a medium. Measurements of this kind are hardly realizable in real QWs due to a small transmission through a substrate.



FIG. 1. (a) Experimental geometry for optical activity registration. The effective magnetic field  $B_{\rm eff}$  linear in the light wave vector results in the elliptical polarization of the reflected wave. (b) Directions of  $B_{\rm eff}$  caused by the bulk inversion asymmetry at various orientations of the light wave vector. (c) Sample sketch. The widths of the barriers and QW are L = 110 nm and a = 10 nm. (d) Reflectance spectrum of *s*-polarized light incident at angle  $\theta = 35^{\circ}$  (symbols) and the fit (solid line). The heavy-hole and light-hole exciton resonances are indicated.

of the QW with the electric field normal component  $E_z$  is necessary for detection of optical activity. As a result, the optical activity is present for the light-hole excitons which have a dipole moment along the growth direction rather than for the heavy-hole excitons which are insensitive to zpolarization. Therefore, we choose ZnSe-based QWs where the light-hole exciton is easily observable [30]. Polarized spectra of exciton reflection were measured from single QW structures ZnSe/Zn<sub>0.82</sub>Mg<sub>0.18</sub>S<sub>0.18</sub>Se<sub>0.82</sub>. The samples were grown by molecular beam epitaxy on GaAs epitaxial buffer layers pseudomorphically to GaAs (100) substrates, Fig. 1(c). The growth of ZnMgSSe barriers proceeded at 270 °C under the stoichiometric conditions corresponding to equivalent fluxes of the group VI and II elements.<sup>2</sup> The total structure thickness including barriers and the QW is 230 nm, which corresponds to  $5\lambda/4$  where  $\lambda$  is the light wavelength at the exciton frequency in ZnSe. This allows for achieving almost complete compensation of reflections from the sample surface and the substrate leading to the pronounced increase of the relative exciton contribution to the reflection (see Supplemental Material [31]).

We studied the dependencies of the reflected light polarization state on the incidence angle and on orientation of the incidence plane relative to the crystallographic axes. The measurements were performed in a glass cylindrical cryostat which allows for investigating reflection at arbitrary angles of incidence. The sample holder allowed us to rotate the sample around the normal by an angle up to 360°. For measuring reflection spectra, we used a halogen lamp as a light source. The parallel light beam was formed by using lenses and slits. The light spot size exceeded the sample diameter by about two times. The light incident on the sample was linearly polarized perpendicular to the plane of incidence (s polarization). All six polarization components of the reflected light were measured. Namely, two circular intensities  $I_{\sigma_{\pm}}$ , two linear ones  $I_{s,p}$  that correspond to s and p polarizations, and two linear components in the axes rotated by  $\pm 45^{\circ}$  relative to the plane of incidence,  $\tilde{I}_{1,2}$ . The spectra were registered by using a 0.5 m monochromator and a CCD camera. We estimate the polarization degree measurements accuracy as 0.1%. Polarization state of the reflected light was determined via the Stokes parameters:

$$P_{circ} = \frac{I_{\sigma_{+}} - I_{\sigma_{-}}}{I_{\sigma_{+}} + I_{\sigma_{-}}}, \quad \tilde{P}_{lin} = \frac{\tilde{I}_{1} - \tilde{I}_{2}}{\tilde{I}_{1} + \tilde{I}_{2}}.$$
 (1)

The latter is related to the angle  $\alpha$  in Fig. 1(a) by  $\tilde{P}_{lin} = \sin 2\alpha$ .

The reflection spectrum at oblique incidence of *s*-polarized light is shown in Fig. 1(d). Two clearly seen resonances are due to heavy-hole  $(X_{hh})$  and light-hole  $(X_{lh})$  excitons. The spectra do not change qualitatively at variation of the incidence angle  $\theta$ . The exciton contribution to the reflectance is big enough owing to a minimum in the background reflection near the exciton frequencies (see Supplemental Material [31]). The resonant frequency behavior of the exciton reflection coefficient is well described by the pole function characterized by the radiative and nonradiative dampings [32]. Using this approach, we determine the radiative and nonradiative dampings of the light-hole exciton from the reflection spectrum (see Supplemental Material [31]). They are found to be  $\hbar\Gamma_0 = 0.05$  meV and  $\hbar\Gamma = 2.35$  meV, respectively.

A presence of the optical activity results in an appearance of the *p*-polarized component as well as helicity in the reflected wave at incidence of purely *s*-polarized light, Fig. 1(a). Therefore, two Stokes parameters that are absent in the incident wave,  $P_{circ}$  and  $\tilde{P}_{lin}$ , are nonzero in the reflected light. These two values measured at reflection from our sample are presented in Fig. 2. Resonant features at the  $X_{lh}$  frequency are clearly seen in spectral dependencies of  $P_{circ}$  and  $\tilde{P}_{lin}$ , Figs. 2(a) and 2(b). Variation of the Stokes parameters with incidence angle are presented in Figs. 2(c) and 2(d). The maximal polarization conversion takes place at  $\theta \approx 45^{\circ}$ , where it reaches  $\approx 2.5\%$ .

Our measurements show that the Stokes parameters of the reflected light depend on the incidence plane orientation. Figure 3 presents the measured dependence  $P_{circ}(\varphi)$  where  $\varphi$ is an angle between the plane of incidence and the axis [100]. Absolute value of the signal is maximal when the incidence plane contains cubic axes [100], [010].  $P_{circ}$  changes its sign at rotation by 90° and reduces to zero at  $q_{\parallel}$  oriented along  $\langle 110 \rangle$  directions. This behavior reflects the system symmetry

<sup>&</sup>lt;sup>2</sup>Special four-period ZnSSe/MgSe superlattices with the same average composition as the bulk  $Zn_{0.82}Mg_{0.18}S_{0.18}Se_{0.82}$  barrier and the total thickness of 10 nm each were grown at both interfaces of the ZnSe QW to improve the interface flatness.



FIG. 2. Spectra of polarization degrees of reflected light  $P_{circ}$  (a) and  $\tilde{P}_{lin}$  (b) in the vicinity of the  $X_{lh}$  resonance. The wave incident at an angle  $\theta = 35^{\circ}$  is *s*-polarized. Incidence angle dependencies of  $P_{circ}$  (c) and  $\tilde{P}_{lin}$  (d) amplitudes indicated by arrows in panels (a) and (b), respectively. Solid lines show fit by Eqs. (9).

and corresponds to the anisotropy of the effective magnetic field  $B_{\text{eff}}$ , Fig. 1(b).

While the explanation of the optical activity effects has been given in a qualitative way above, we resort now to a microscopic description based on the equations for the exciton dielectric polarization P in a QW. Near the light exciton resonance, the microscopic reason for the effective magnetic field resulting in the optical activity is the bulk inversion asymmetry induced spin-orbit interaction. It yields the linear in electron and light hole in-plane momenta  $k^{e,h}$  contributions to the single-particle Hamiltonians:

$$H_i = \beta_i \left( \sigma_x^i k_x^i - \sigma_y^i k_y^i \right), \quad i = e, h, \tag{2}$$

where  $\sigma_{x,y}^i$  are the Pauli matrices acting on the spin of the *i*th particle,  $x \parallel [100]$ ,  $y \parallel [010]$  are cubic axes, and the growth direction is  $z \parallel [001]$ . At oblique incidence, the in-plane



FIG. 3. Dependence of the circular polarization degree of reflected light on the incidence plane orientation relative to crystallographic axes. Solid line is a fit by  $P_{circ}(\varphi) = A \cos 2\varphi$ .

component of light wave vector is related to  $\mathbf{k}^{e,h}$  via  $\mathbf{q}_{\parallel} = \mathbf{k}^e + \mathbf{k}^h$ . The term  $H_e$  mixes the electron states  $S \uparrow$  and  $S \downarrow$ , and  $H_h$  mixes the light hole states  $\uparrow (X - iY)/\sqrt{6} + \downarrow \sqrt{2/3}Z$  and  $\downarrow (X + iY)/\sqrt{6} + \uparrow \sqrt{2/3}Z$ , where *S* is the Bloch orbital in the conduction band, *X*, *Y*, *Z* are the Bloch orbitals in the valence band, and  $\uparrow$ ,  $\downarrow$  are the spinors  $\pm 1/2$ . As a result of this mixing, interband transitions are allowed in both in-plane and out-of-plane polarizations, which leads to the polarization conversion, i.e., optical activity. We stress that the effect is absent for the heavy-hole excitons where the Bloch function has no *Z* orbital. The bulk inversion asymmetry results in  $\mathbf{q}$ -linear terms in the equations for the exciton electric polarization [19,33]:

$$(\omega_{\perp}^{0} - \omega)P_{x,y} - i\frac{\beta}{\hbar}\sqrt{\frac{d_{\perp}}{d_{\parallel}}}q_{y,x}P_{z}$$

$$= d_{\perp}\Phi(z)\int_{-\infty}^{\infty}dz'\Phi(z')E_{x,y}(z'), \qquad (3)$$

$$(\omega_{\parallel}^{0} - \omega)P_{z} + i\frac{\beta}{\hbar}\sqrt{\frac{d_{\parallel}}{d_{\perp}}}(q_{x}P_{y} + q_{y}P_{x})$$

$$= d_{\parallel} \Phi(z) \int_{-\infty}^{\infty} dz' \Phi(z') E_z(z').$$
<sup>(4)</sup>

Here E is the total electric field in the system, the real function  $\Phi(z)$  is the wave function of the exciton size quantization at coinciding coordinates of electron and hole, and  $\omega_{\perp,\parallel}^0$  and  $d_{\perp,\parallel}$  are the frequencies and the squared matrix elements of the light excitons with dipole moments oriented in the QW plane and along z, respectively  $(d_{\parallel}/d_{\perp} = 4)$ . The exciton bulk inversion asymmetry constant is related to  $\beta_{e,h}$  introduced in Eq. (2) by

$$\beta = \frac{\beta_e m_e + \beta_h m_h}{m_e + m_h},\tag{5}$$

where  $m_{e,h}$  are the electron and the light hole in-plane effective masses.

Solution of the Maxwell equations with the material relations (3), (4) between the polarization and electric field yields the amplitude  $E_p^{QW}$  of the *p*-polarized component reflected from the QW at incidence of *s*-polarized wave with the amplitude  $E_{0s}$ :  $E_p^{QW} = \mathcal{R}_{ps}^{\beta} E_{0s}$  (see Supplemental Material [31]). Here  $\mathcal{R}_{ps}^{\beta}$  is the reflection coefficient describing the polarization conversion linear in the spin-orbit exciton constant  $\beta$ :

$$\mathcal{R}_{ps}^{\beta} = \frac{\sin^2 \theta_1}{\cos \theta_1} \sqrt{\frac{d_{\parallel}}{d_{\perp}}} \frac{\beta q \, \cos 2\varphi \, \Gamma_0}{(\omega_{\perp} - \omega - i \, \Gamma)(\omega_{\parallel} - \omega - i \, \Gamma)}, \quad (6)$$

where  $\theta_1$  is the light propagation angle inside the structure, the radiative and nonradiative  $X_{lh}$  linewidths  $\Gamma_0$  and  $\Gamma$  were determined from the reflection spectrum, and  $\omega_{\perp,\parallel}$  are the light exciton frequencies slightly different from  $\omega_{\perp,\parallel}^0$  due to a radiative renormalization [32,34].

Equation (6) demonstrates that the polarization conversion is absent at normal incidence, and the amplitude  $E_p^{QW}$ increases as  $\theta^2$  at small  $\theta$ . However, the experimental results demonstrate the polarization conversion at normal incidence as well. This effect is not related with the effective magnetic field, but indicates birefringence caused by low symmetry of the real QW under study. One of the reasons for the polarization conversion at normal light incidence may be deformations in the QW plane. We describe this effect introducing a mixing of the in-plane components of the exciton polarization which does not depend on the wave vector:

$$(\omega_{\perp}^{0} - \omega)P_{x,y} + \delta P_{y,x} = d_{\perp}\Phi(z) \int_{-\infty}^{\infty} dz' \Phi(z') E_{x,y}(z').$$
(7)

Here real and imaginary parts of  $\delta$  describe, respectively, an energy splitting and a difference of dampings between the exciton states with dipole moments along [110] and [110] axes. Microscopically, the splitting is caused by an effect of in-plane deformations on the exchange interaction in the exciton as well as by the mixing of heavy- and light-hole states [32,35,36]. A finite value of  $\delta$  gives rise to the following contribution into the polarization conversion coefficient (see Supplemental Material [31]):

$$\mathcal{R}_{ps}^{\delta} = \frac{\delta \cos 2\varphi i \Gamma_0}{(\omega_{\perp} - \omega - i \Gamma)^2}.$$
(8)

The Stokes parameters Eq. (1) of the wave reflected from the whole studied structure are described by the complex reflection coefficient  $r_{ps}$  relating the amplitudes of the incident *s*- and reflected *p*-polarized light as follows (see Supplemental Material [31]):

$$P_{circ} = 2 \operatorname{Im}(r_{ps}/r_{ss}), \quad \tilde{P}_{lin} = 2 \operatorname{Re}(r_{ps}/r_{ss}), \quad (9)$$

where  $r_{ss}$  is the reflection coefficient for *s*-polarized light. In the studied structure, the resonant signal in the polarization conversion is caused by the QW only. Therefore,  $r_{ps}$  is proportional to the reflection coefficient describing polarization conversion by the QW:

$$r_{ps} = \left(\mathcal{R}^{\beta}_{ps} + \mathcal{R}^{\delta}_{ps}\right) F(\theta, \omega). \tag{10}$$

Here the function  $F(\theta, \omega)$  accounts for multiple reflections from the QW, the sample surface, and the interface with the substrate [Fig. 1(c)], as well as a conversion of polarization at transmission through the QW (see Supplemental Material [31]).

Comparison of the optical-activity and birefringence coefficients  $\mathcal{R}_{ps}^{\beta}$  and  $\mathcal{R}_{ps}^{\delta}$  shows that they have drastically different dependencies on the incidence angle. In contrast to  $\mathcal{R}_{ps}^{\beta}$  which is zero at normal incidence,  $\mathcal{R}_{ps}^{\delta}$  is independent of  $\theta$ . This difference allows us to separate the contributions of optical activity and birefringence into the polarization conversion (see Supplemental Material [31]). We have fitted both the spectral and incidence-angle dependencies of the Stokes parameters  $P_{circ}$  and  $\tilde{P}_{lin}$  by Eqs. (9) and (10). Figure 2 demonstrates that the developed theory describes all four dependencies very well. We stress that the experimental dependencies in Fig. 2 are fitted with just two fitting parameters. Some deviations of the linear polarization angular dependence at large incidence angles  $\theta > 55^{\circ}$  are caused by a low quality of the surface which affects the linear polarization degree of the reflected light, especially at nearly grazing incidence. From the data at normal incidence we determine the birefringence parameter  $\delta = (-0.11i + 0.022)$  meV. A larger imaginary value of  $\delta$ means that the birefringence of the studied structure is caused mainly by a 5% difference in the nonradiative dampings  $\Gamma$  for the excitons with dipole moments along [110] and  $[1\overline{1}0]$  directions rather than in their energy splitting. This damping anisotropy can be caused by a difference in scattering rates on anisotropic scattering centers at QW interfaces; see, e.g., Ref. [13]. The fact that we fitted both spectral and incidence-angle dependencies introducing the birefringence only from the QW exciton demonstrates that a possible barrier contribution to the birefringence which has another spectral dependence plays a minor role. The best fit of the data at oblique incidence shown in Fig. 2 is achieved at the spin-orbit exciton constant  $\beta = 0.07 \text{ eV}$ Å.

The  $\cos 2\varphi$  dependence of the Stokes parameters on the angle  $\varphi$  between the polarization plane of incident light and *x* axis is present in both  $\mathcal{R}_{ps}^{\beta}$  and  $\mathcal{R}_{ps}^{\delta}$ . This angular dependence perfectly describes the circular polarization degree of the reflected light presented in Fig. 3.

The value of the bulk inversion asymmetry constant  $\beta$  determined from our experiment is in a good agreement with theoretical estimates. The electron constant  $\beta_e$  determined in Ref. [37] for similar QWs is an order of magnitude smaller than  $\beta$  but, as it follows from Refs. [36,38], the light-hole spin-orbit splitting exceeds by far the electronic one. The enhancement of  $\beta_h$  is most dramatic in the QWs with close ground light-hole level *lh*1 and first excited heavy-hole level *hh*2. In the studied ZnSe-based 10 nm wide QW, *hh*2 and *lh*1 levels are indeed close to each other. Therefore, we conclude that the exciton constant is mainly determined by the *lh*1 constant via  $\beta \approx \beta_h m_h/(m_e + m_h)$ , which yields  $\beta_h \approx 0.14$  eV Å. This value agrees with theoretical estimates [36,38].

To summarize, we observed optical activity of semiconductor QWs. The developed theory demonstrates that the polarization conversion is caused by spin-orbit interaction and by birefringence of the studied QW structure. The observed effect has a strongly resonant behavior in the vicinity of the lightexciton transition. Studying the polarization state of reflected light, we determined the exciton spin-orbit splitting in the QW.

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