Metastability of Mn^{3+} in ZnO driven by strong d(Mn) intrashell Coulomb repulsion: Experiment and theory

A. Ciechan,¹ H. Przybylińska,¹ P. Bogusławski,^{1,2,*} A. Suchocki,^{1,2} A. Grochot,¹ A. Mycielski,¹ P. Skupiński,¹ and K. Grasza¹

¹Institute of Physics, Polish Academy of Sciences, al. Lotników 32/46, 02-668 Warsaw, Poland

²Institute of Physics, Kazimierz Wielki University, Powstanców Wielkopolskich 2, 85-064 Bydgoszcz, Poland

(Received 11 February 2016; revised manuscript received 20 September 2016; published 19 October 2016)

Depopulation of the Mn^{2+} state in ZnO:Mn upon illumination, monitored by quenching of the Mn^{2+} EPR signal intensity, was observed at temperatures below 80 K. Mn^{2+} photoquenching is shown to result from the $Mn^{2+} \rightarrow Mn^{3+}$ ionization transition, promoting one electron to the conduction band. Temperature dependence of this process indicates the existence of an energy barrier for electron recapture of the order of 1 meV. GGA + *U* calculations show that after ionization of Mn^{2+} a moderate breathing lattice relaxation in the 3+ charge state occurs, which increases energies of d(Mn) levels. At its equilibrium atomic configuration, Mn^{3+} is metastable since the direct capture of photoelectron is not possible. The metastability is mainly driven by the strong intrashell Coulomb repulsion between d(Mn) electrons. Both the estimated barrier for electron capture and the photoionization energy are in good agreement with the experimental values.

DOI: 10.1103/PhysRevB.94.165143

I. INTRODUCTION

ZnO is a promising material for photocatalysis [1] and photovoltaic applications [2,3]. Mn substituting for the divalent cation in ZnO introduces a Mn^{2+}/Mn^{3+} level located in the forbidden gap [4]. The midgap position of Mn^{2+} has been already practically utilized and powers the research on water splitting [1]. Mn-doped ZnO also exhibits a chromatographic effect: The undoped transparent crystals upon doping with Mn turn reddish brown due to the strong absorption interpreted as $Mn^{2+} \rightarrow (Mn^{3+}, e_{CB})$ photoionization transition [4], where e_{CB} denotes a photoelectron in the conduction band. This absorption is accompanied by photoconductivity [4]. The nature of this transition has been inferred only indirectly. Though the presence of Mn in the 2+ charge state in ZnO was detected with use of electron paramagnetic resonance (EPR) [5,6], no optical spectra related to intracenter transitions of Mn²⁺ were observed. Since these transitions can occur at energies higher than the observed photoionization band, it was concluded that the excited states of Mn²⁺ are degenerate with the conduction band of ZnO [7], consistent with the midgap position of the Mn²⁺ energy level. However, no direct evidence of the depopulation of the Mn^{2+} state under illumination was presented so far.

In this paper we study directly the occupancy of Mn^{2+} ions under illumination by means of photo-EPR spectroscopy. We observe a temperature dependent decrease of the EPR signal intensity under excitation with light of energies corresponding to the Mn-related absorption band. The kinetics of the EPR signal photoquenching points out to a process involving photocarriers and the Mn ions directly. First principles calculations indicate that the observed photoquenching is due to a transition of Mn^{3+} to a metastable state after photoionization of an electron to the conduction band. In our case, by metastability we understand the fact that the excited electron cannot directly recombine to the Mn ion because there is an energy barrier preventing the process. Metastability of defects and/or dopants typically originates in strong lattice relaxations accompanying the change of the defect charge state. More specifically, atomic configuration of a defect depends on its charge state, and defect metastability occurs when a direct change of the charge state (i.e., capture/emission of an electron by/from the defect) is prevented by an energy barrier. This can lead to, e.g., persistent photoconductivity. In the case of the As antisite in GaAs studied in the past (the EL2 center), optical excitation is followed by a large displacement, exceeding 1 Å, of the defect towards the metastable interstitial site [8,9]. A similar mechanism is operative also in the case of donors, which can acquire the DX configuration when a shallow donor captures an electron and becomes a deep one with a strongly localized electronic state in the band gap, [10-14] and in the case of native defects [15], where the (meta)stability is responsible for quenching of doping efficiency. A metastable configuration can also consist of a breathinglike displacement of the surrounding host atoms [16,17]. Here we show that metastability of Mn in ZnO also requires substantial lattice relaxations induced by the change of the charge state. However, unlike in the examples above, a second factor that drives metastability of Mn³⁺ is the strong intracenter Coulomb coupling between the d(Mn) electrons, which prevents the electron capture by Mn^{3+} followed by recombination. One should observe that considerable progress was recently achieved in understanding the electron capture process by advanced ab initio methods [18–21]. However, since this process is not the main topic of the present paper, we use a simplified approach based on adiabatic configuration coordinate diagram. Finally, regarding the absorption measurements, the calculations predict that intracenter transitions should occur at energies higher than photoionization, in agreement with experimental data.

The paper is organized in the following way: In Sec. II the experimental setup and results are presented and discussed. In Sec. III, details of the theoretical approach, based on the generalized gradient approximation (GGA) to the density functional theory, are given. The +U corrections [22–24] are applied to d(Zn), p(O), and the d(Mn) shell. The proposed mechanism of metastability of the photoionized Mn is presented in Sec. III D. Section IV summarizes the obtained results.

2469-9950/2016/94(16)/165143(12)

^{*}bogus@ifpan.edu.pl

II. RESULTS AND DISCUSSION

A. Experimental methods

Mn doped ZnO single crystals were grown by chemical vapor transport [25]. For the photo-EPR experiments the Mn concentration of 0.2% was chosen, as it ensures well resolved, narrow-line EPR spectra of Mn^{2+} . The EPR experiments were performed at 9.5 GHz, with use of a BRUKER ESP300 spectrometer equipped with an Oxford Instruments ESR 900 cryostat operating in the temperature range 1.8–300 K. The magnetic field was oriented perpendicular to the *c* axis of the crystal. The sample was illuminated at a right angle to the magnetic field direction with a set of laser diodes of wavelengths varying from 445 nm to 980 nm. For power dependent measurements a set of gray filters was employed.

B. Experimental results

The as-grown ZnO:Mn 0.2% sample is highly resistive, in contrast to the n-type conductivity of undoped ZnO crystals grown with the same method. A part of the Mn ions occurs in the Mn^{2+} charge state and can be easily detected by EPR. Annealing the crystal in hydrogen atmosphere leads to a substantial (more than fivefold) increase of the Mn^{2+} ion fraction accompanied by the appearance of n-type conductivity.

Figure 1(a) shows the EPR spectrum of Mn^{2+} in the as-grown ZnO:Mn sample at 3.8 K taken with the magnetic

field oriented perpendicular to the *c* axis of the crystal. The spectrum consists of 30 partly overlapped resonances grouped into five sextets. The five so-called fine structure groups stem from allowed $\Delta M_S = \pm 1$ transitions between electronic spin levels of a d^5 ion with the electronic spin of S = 5/2. Each group consist of six equally intense lines due to hyperfine interaction with the I = 5/2 nuclear spin of Mn⁵⁵. The spectrum is characteristic of isolated Mn²⁺ ions in ZnO. [5,6] Analysis of the angular dependence of the resonance peak positions measured [26] yields the spin Hamiltonian parameters $g = 2.0025 \pm 0.0003$, $D = -248.53 \pm 0.07$ G, $A_{\parallel} = 80.4 \pm 0.1$ G, $A_{\perp} = 80.3 \pm 0.3$ G, and $a = 3.9 \pm 0.1$ G at 3 K, consistent with earlier studies [4,27].

Apart from the EPR spectrum of isolated Mn^{2+} ions, no other EPR signals were detected in our crystals, in particular neither complexes of Mn^{2+} with other defects (up to second nearest neighbors) nor spectra related to Mn-Mn pairs were observed. Such defects, if present at concentrations exceeding the detection limit of the EPR spectrometer, should produce additional resonance signals in the magnetic field range shown in Fig. 1(a). The absence of lines other than that of Mn^{2+} implies the absence of defects with a *g* factor ranging from 1.5 to about 2.8.

Illumination with light in the 980–445 nm range leads to a drastic reduction of the detected EPR signal intensity of Mn^{2+} . Exemplary spectra recorded at 3.8 K under illumination with 532 nm and 850 nm laser lines are shown in Fig. 1(b). The



FIG. 1. (a) EPR spectrum of Mn^{2+} in ZnO with *B* perpendicular to the *c* axis. Black line shows the signals in the dark, green, and red traces are recorded under illumination with 532 nm (50 mW) and 850 nm (660 mW) laser lines, respectively. (b) EPR signal of (a) in the magnetic field range 4060–4160 G showing the shift of the line position and the change of the lineshape from Gaussian (in the dark) to Dysonian under illumination. (c),(d) EPR signal in the dark and under illumination measured in the thin (100 μ m) sample. The illumination conditions are the same as in Figs. 1(a) and 1(b).



FIG. 2. (a) Quenching of Mn^{2+} EPR intensity, ΔI_{EPR} , at T = 2.8 K as a function of excitation wavelength measured in the thin sample. (b) Spectral dependence of the absorption coefficient for both pure ZnO and ZnO doped with 0.5% Mn at 300 K.

laser power was 50 and 660 mW, respectively. Not all of the observed signal reduction can be attributed to a change of Mn²⁺ concentration alone. The dominant mechanism of the EPR intensity quenching shown in Fig. 1 comes from the skin effect, i.e., absorption by photogenerated free carriers, which reduces the microwave penetration depth and hence the effective volume of the sample. The skin effect manifests itself in a change of the resonance line shape from Gaussian to Dysonian, as shown in Fig. 1(b). In addition, we observe a small shift of the resonance line positions towards higher magnetic fields under illumination. This shift is due to exchange interaction between localized magnetic moments of Mn^{2+} and free carrier spins [28], an analog of the Knight shift in nuclear magnetic resonance. Both the change of the EPR lineshape and the shift of the resonance fields directly prove that illumination with light in the whole wavelength range (445–980 nm) studied leads to generation of free carriers.

To eliminate the skin effect the sample was thinned down to 100 μ m. This thickness was found to be sufficient to ensure microwave penetration of the entire sample. We no longer observed changes of the line shape accompanying the reduction of the Mn²⁺ EPR signal intensity upon illumination, as shown in Figs. 1(c) and 1(d). We can also exclude another possible source of intensity decrease in our experiment, i.e., sample heating due to incident laser power. Since the fine structure $-5/2 \rightarrow -3/2$ [high field resonances in Fig. 1(a)] and $3/2 \rightarrow 5/2$ transitions (low field resonances) have the same probability, the difference in the intensities of the high field and low field resonance lines reflects the difference in the thermal population of the -5/2 and 3/2 levels. At low temperatures [see Fig. 1(a)] the intensity of high field resonances is more than twice higher than that of the low field ones. With increasing sample temperature the intensity ratio decreases, and at 300 K both EPR resonances are almost equally intense. Even under illumination with 2.4 W at the lowest applied wavelength of 980 nm we observed no measurable change in the EPR signal intensity ratio between the $-5/2 \rightarrow -3/2$ and $3/2 \rightarrow 5/2$ resonances. Thus, any light induced changes of the EPR signal intensity measured in the so prepared sample reflect solely the change in the occupancy of the manganese 2+ charge state. Unless explicitly specified, all further data reported here refer to measurements performed on the thin sample.

The spectral dependence of the Mn²⁺ EPR signal photoquenching is presented in Fig. 2(a). Depicted is the relative reduction of the EPR signal intensity, ΔI_{EPR} , under illumination at a constant power of 50 mW. ΔI_{EPR} is defined as the difference between the signal intensities in the dark, $I_{EPR}(dark)$, and under illumination, $I_{EPR}(ilumin)$, divided by the dark intensity:

$$\Delta I_{EPR} = \frac{I_{EPR}(dark) - I_{EPR}(ilumin)}{I_{EPR}(dark)}.$$
 (1)

For comparison, the room temperature absorption spectra of ZnO:Mn 0.5% and undoped ZnO are shown [Fig. 2(b)]. As can be seen in Fig. 2(b), the onset of the Mn-related absorption is close to 620 nm (2 eV), which is consistent with the optical ($E_{opt} = 2.6 \pm 0.1$ eV) and thermal ($E_{th} = 2.1 \pm 0.1$ eV) ionization energies determined in Ref. [29] for the postulated Mn 2+ to 3+ photoionization transition. The agreement between the spectral dependence of the Mn²⁺ EPR signal photoquenching below 600 nm in Fig. 2(a) and the absorption band is indeed due to photoionization of Mn²⁺.

We note that the spectral dependence in Fig. 2 can not reproduce exactly the photoionization band measured in absorption. This is mainly due to the fact that the observed quenching of the Mn^{2+} EPR signal is reduced by the photoneutralization process, i.e., transition of an electron from the valence band to Mn³⁺. The onset of this transition should occur at 1.2 eV (1033 nm), however, we observe no increase of the Mn²⁺ EPR signal intensity under illumination with energies below 2.1 eV. Instead, above 600 nm there is a nonvanishing photoquenching tail in ΔI_{EPR} , which we attribute to an indirect quenching mechanism, i.e., capture of holes generated in the photoneutralization processes of other defects present in the sample. Although the tail seems to be weak at the excitation power of 50 mW, at high incident powers ΔI_{EPR} due to the indirect mechanism is comparable to that observed for direct photoionization of Mn²⁺. This means that the concentration of the defects involved is not negligible.

The fact that the photoneutralization process is not directly observed experimentally is surprising, since transitions from the valence band of p-type symmetry to the d orbital are allowed by the selection rules, whereas transitions from the d orbital to s-type conduction band are forbidden. Typically, for



FIG. 3. Shift of the Mn²⁺ g factor under excitation with 532 nm light (left axis, solid squares) and Mn²⁺ EPR signal photoquenching, ΔI_{EPR} , (right axis, circles) vs excitation power (*I*). The measurements were performed at 3.3 K with the magnetic field directed perpendicular to the ZnO c axis. The error bar shows the difference between the power value measured before and after recording of the EPR spectra.

transition metals the former process is much more efficient than the latter. The lack of the photoneutralization band for Mn implies that the hole recapture rate by Mn²⁺ may be faster than the electron recapture rate by Mn^{3+} . We have indirect experimental evidence for the existence of the photoneutralization process, stemming from the analysis of the Mn^{2+} g-factor shift under illumination. Shown in Fig. 3 is the difference between the perpendicular g factor under excitation with 532 nm light, g(I), and in the dark, g(0), depending on the excitation power (I). For comparison, the excitation power dependence of the Mn^{2+} EPR signal photoquenching, ΔI_{EPR} , is presented in the same figure. Since at higher laser diode currents the light intensity was slightly unstable, the power was measured twice, immediately before and after recording of the EPR spectra. The data for the g-factor shift are shown depending on the initially measured power, whereas ΔI_{EPR} is plotted vs the mean value. The error bar shows the difference between the initial and final power value.

Interaction of the local magnetic moment of the manganese ion with the spins of conducting carriers can lead to the Knight shift of the Mn^{2+} resonance field positions, which can be interpreted as a change of the g factor:

$$\Delta g = J_{s-d}\rho_{CB}(E_F)g_e + J_{p-d}\rho_{VB}(E_F)g_h, \qquad (2)$$

where $J_{s(p)-d}$ are the exchange integrals between the local moment and the conducting electron (s) or hole (p), $\rho_{CB}(E_F)$ and $\rho_{VB}(E_F)$ are the densities of states at the quasi-Fermi level in the conduction and valence band, respectively, and $g_{e(h)}$ is the conducting electron (hole) g factor. Despite the controversy about the actual values of exchange integrals for ZnO:Mn [30] it is established that J_{s-d} (also referred to as $N\alpha$) is of the order of 0.2–0.4 eV, whereas J_{p-d} (N β) is about an order of magnitude larger and of opposite sign. This means that interaction with conducting electrons should lead to an increase of the Mn^{2+} g factor. Instead, as can be seen in Fig. 3, the g factor changes with increasing excitation power in a manner similar to ΔI_{EPR} , but the shift is negative, as expected for interaction with conducting holes. This can be explained only under assumption that both types of carriers are generated with the 532 nm light. Even if the steady-state concentration of photogenerated holes is smaller than that of electrons and the perpendicular hole g factor for the Γ_7 valence band is much smaller than 2, the Knight shift can be negative owing to the larger p-d exchange integral and the higher density of states in the valence than in the conduction band. It should be stressed that the determined g-factor shift is over an order of magnitude smaller than that measured in Mn doped IV-VI semiconductors, where the exchange integrals are considerably lower than in ZnO [28]. Recently the electron gfactor in ZnO of $g_e = 1.98$ was determined by time-resolved Faraday rotation spectroscopy and found to increase upon doping with 0.21% Co by a factor of two for $N\alpha = +0.25 \text{ eV}$, [31] comparable with that of ZnO:Mn. The hole g factor and $N\beta$ could not be determined due to the short lifetime of photogenerated holes (of the order of picoseconds) in comparison with the nanosecond lifetime of photogenerated electrons. Unfortunately, the lack of reliable experimental data for the exchange integrals in ZnO:Mn makes even an estimation of the electron to hole concentration ratio impossible.

As already mentioned, in the thick ZnO:Mn sample we observe an additional reduction of the Mn^{2+} signal intensity under illumination, related to microwave absorption by free carriers. This reduction increases with the concentration of



FIG. 4. (a) Ratio ΔI_{EPR} (thick)/ ΔI_{EPR} (thin) in thick and thin samples vs excitation wavelength. (b) Spectral dependence of absorbance at T = 16 K. Note the different wavelength window in (a) and (b).



FIG. 5. Temperature dependencies of Mn^{2+} EPR signal photoquenching (ΔI_{EPR}) in the as-grown thin sample (squares) and in the same sample after hydrogenation (triangles) illuminated with 532 nm light at 50 mW. The dashed lines are illustrations of an $(1 - \exp(-E/kT))$ dependence with, E = 0.6 and 1.25 meV for the as-grown and hydrogenated sample, respectively.

photogenerated carriers as the effective volume penetrated by microwaves decreases. Thus, comparison of photoquenching in the thick and thinned sample can give additional insight into the possible carrier generation channels. If the free carriers would originate solely from transitions to and from the Mn²⁺ level, the spectral dependencies measured in thin and thick samples should be similar but for a scaling factor. In Fig. 4(a) we show the spectrally dependent quenching of the EPR signal intensity of Mn²⁺ measured in the thick sample divided by the quenching measured after the sample was thinned down to 100 μ m, ΔI_{EPR} (thick)/ ΔI_{EPR} (thin). The measurements were performed at a constant temperature of 3.8 K. As can be seen, the photoquenching ratio increases with increasing wavelength, in contrast to the behavior expected if Mn²⁺ photoionization and photoneutralization processes would be the only mechanisms of free carrier generation. This result demonstrates that there is at least a second channel of carrier photogeneration, dominant for wavelengths longer than 500 nm. Absorption extending to even longer wavelengths than applied in the photoquenching experiment is also observed in the optical spectrum of ZnO with 0.2% of Mn measured at low temperatures (16 K), and shown in Fig. 4(b). The nature and concentration of the defects responsible for carrier generation cannot be determined in our experiment as they give no paramagnetic signal. In the studied samples no EPR signal other than that of Mn²⁺ was detected. Unfortunately, we cannot even estimate the carrier concentration. The penetration depth (for an infinite sheet of a finite thickness) depends inversely proportional on the square root of the conductivity, which typically is orders of magnitude larger at GHz frequencies than the dc conductivity.

Shown in Fig. 5 are the temperature dependencies of ΔI_{EPR} in the as-grown sample (squares) and the same sample after hydrogenation (triangles) illuminated with 532 nm light at 50 mW. It is visible that Mn²⁺ photoquenching is much more efficient in the hydrogenated sample than in the as-grown one.

As already mentioned, the concentration of Mn^{2+} increased after hydrogenation by a factor of 5. This agrees with the fact that H acts as a shallow donor in ZnO [32]. However, the



FIG. 6. Dots: kinetics of Mn^{2+} photoquenching under 445 nm excitation at a power of 190 (upper trace) and 20 mW (lower trace) at 3 K. Red lines are calculated for an exponential rise and decay with the same rise/decay time of $\tau = 63$ ms.

decrease of the EPR intensity under illumination is larger by a factor of 12. Evidently, the photoneutalization transition is less efficient in the case of the hydrogenated sample due to simultaneous increase of Mn^{2+} concentration and corresponding decrease of Mn^{3+} concentration, which increases the ratio of the photoionization to photoneutralization rates.

As can be seen in Fig. 5, the temperature decrease of Mn²⁺ photoquenching resembles closely a thermally activated dependence of the type $a(1 - \exp(-E/kT))$. The dashed lines illustrate such a dependence with E = 0.6 and 1.25 meV for the as-grown and hydrogenated sample, respectively. Photoquenching under illumination with a 445 nm laser diode vields similar temperature dependencies, with identical, sample dependent E values as in the case of 532-nm illumination. The apparent activation energies are more than an order of magnitude lower than those of typical donors in ZnO [33], which suggests that the electrons photoionized from Mn²⁺ are not captured on ZnO donors. This is confirmed also by the measured abrupt photoquenching kinetics shown in Fig. 6. At liquid helium temperature electrons transferred from Mn^{2+} should be frozen on the ZnO donors. This would result in photoquenching persisting after the light is turned off, which is not the case here. Thermally deactivated photoquenching can be also obtained assuming that capture rates are thermally activated. In principle, it should be possible to extract the activation energy from experimental data by solving appropriate rate equations.

The rate equations describing the charge transfer processes under illumination at steady state conditions are given below. On the grounds mentioned above we have omitted terms relating to ionization and capture of electrons by ZnO donors. Also, the electron-hole recombination rate is not included. The assumption that carrier recombination proceeds predominantly via the Mn state is plausible since no near band-edge photoluminescence is detected in our samples.

$$\frac{dn_{Mn}}{dt} = -I\sigma_{OC}^{Mn}n_{Mn} + I\sigma_{OV}^{Mn}(N_{Mn} - n_{Mn}) + C_n^{Mn}n(N_{Mn} - n_{Mn}) - C_p^{Mn}pn_{Mn} = 0, \quad (3)$$

$$\frac{dn_X}{dt} = -I\sigma_{OV}^X n_X + C_p^X p(N_X - n_X) = 0, \qquad (4)$$

$$\frac{dn}{dt} = I\sigma_{OC}^{Mn}n_{Mn} - C_n^{Mn}n(N_{Mn} - n_{Mn}) = 0, \qquad (5)$$

$$\frac{dp}{dt} = I\sigma_{OV}^{Mn}(N_{Mn} - n_{Mn}) - C_p^{Mn}pn_{Mn}
+ I\sigma_{OV}^X n_X - C_p^X p(N_X - n_X)
= 0.$$
(6)

The charge neutrality condition gives:

$$n_{Mn}(0) - n_{Mn} = n - p + n_X(0) - n_X.$$
 (7)

Here, *n* and *p* are the electron and hole concentrations in the conduction and valence bands, respectively, and N_{Mn} and N_X represent the total concentration of Mn ions and the unknown acceptor centers *X*, whereas n_{Mn} and n_X are the concentrations of Mn²⁺ and neutral acceptors $[n_{Mn}(0)$ and $n_x(0)$ denote the respective concentrations without illumination]. Further, *I* denotes the illumination fluence, $\sigma_{OC}^{Mn}(\sigma_{OV}^{Mn})$ is the optical cross section for transitions between the Mn²⁺/Mn³⁺ ionization level and the conduction (valence) band, σ_{ov}^X is the cross section from the valence band to the defect level, whereas $C_p^{Mn}(C_n^{Mn})$ and C_p^X are the capture rates per unit volume of holes (electrons) on the Mn²⁺/Mn³⁺ and X^-/X^0 ionization levels, respectively. In the above rate equations, we neglect electron transitions between Mn and the acceptor *X* (since, as revealed by EPR, they are distant), as well as between *X* and the conduction band [we assume that the energy level of X^0/X^- is considerably below that of Mn³⁺/Mn²⁺, consequently *X* is not ionized with 532 nm light].

Unfortunately, the parameters in Eqs. (3)–(6) are not known, which makes finding an analytical solution in a form applicable for fitting of the experimental data impossible, even in a simplified case when we neglect the presence of the unknown acceptor.

Additional information concerning optical cross sections can be usually obtained from the initial decay of the photoquenching transients. However, the kinetics of Mn²⁺ photoionization turns out to be shorter than the response time of our apparatus, as demonstrated in Fig. 6. The kinetics presented in Fig. 6 was measured at 3 K at a constant field value, corresponding to a maximum intensity of one of the resonance lines. The upper and lower traces (dots) show the change of the signal intensity under 445 nm excitation at a power of 190 and 20 mW, respectively. The lines are calculated assuming an exponential rise and decay, with the same time of 63 ms. This time is, moreover, independent of excitation power. A decay constant below 63 ms is much too short to account for the kinetics of a process involving charge transfer between Mn and distant trap centers, which is usually of the order of minutes [34]. It is, of course, feasible in the case of close complexes but, as already mentioned, the observed Mn²⁺ centers have no defects in their immediate vicinity. Such defects would result in Mn site symmetry lower than the observed C_{3V} symmetry appropriate for isolated ions.

The photo-EPR experiments have confirmed that the Mn^{3+}/Mn^{2+} level is located at 2.1 eV below the conduction band minimum of ZnO. In addition, it was shown that in

as-grown ZnO:Mn crystals the manganese impurity occurs predominantly in the 3+ charge state. To account for the partial occupancy of the Mn²⁺ state, there have to be other acceptor centers in the sample which push the Fermi level below the impurity level. One of the candidates is the complex of manganese with interstitial oxygen, Mn-O_i, postulated by Gluba and Nickel [27], but the presence of such an acceptor center is not confirmed in our experiment. In EPR we observe only isolated Mn ions. It should be also noted that in our crystals, apart from Mn²⁺, we detect no other EPR signals, whether of acceptors or donors. The g factors of such defects are close to 2 and should give rise, if present at non-negligible concentration, to absorption lines in the magnetic field range of 3400-3600 G. Thus, there is no relevant experimental evidence regarding the identity of acceptors, since they are not seen either in EPR or in optical measurements (as already mentioned, Mn acts as a very efficient luminescence killer). In principle, those acceptors can be either native defects, or chemical contaminations related to the growth process. In the former case, both experimental [35] and theoretical [36– 38] studies agree that the dominant compensating acceptors (actually, double acceptors) in ZnO are the Zn vacancies. Their equilibrium concentration should be largely determined by that of the Mn²⁺ donor thanks to the self-compensation effect (i.e., to the dependence of formation energy on the Fermi energy) [31,35]. We point out that we have no experimental evidence in support of this assignment, but on the other hand the doubly ionized vacancy V_{Zn}^{2-} gives no EPR signal because of its vanishing spin.

In particular, the EPR signal of a residual donor with the *g* factor of 1.956, identified as hydrogen related shallow donor [39], is not observed even after hydrogenation of the sample. This signal does not appear also under illumination, which suggests that if this donor is present it is not effectively populated, i.e., the electron capture rate is much lower than that of Mn^{3+} ions.

Owing to limitations of our experimental setup, we cannot determine precisely the activation energies governing the temperature dependence of Mn²⁺ photoquenching but only give a rough estimate. Still, the experimental findings point out to energies of the order of meVs rather than tens of meVs typical for ZnO donors, which range from 35 to about 70 meV [33]. The temperature dependent change of the Mn^{2+} occupancy under illumination must have, therefore, a different origin than charge transfer to electron traps. Apparently there must be a large difference between the capture rates of photogenerated electrons and holes on the Mn^{2+}/Mn^{3+} level. There are two possible reasons for a lower (and thermally activated) electron capture rate. One is related to potential fluctuations in the ZnO conduction band. This could also explain the apparent increase of the activation energy in hydrogenated samples. The other possibility is a small energy barrier for electron capture resulting from lattice relaxation accompanying the change of the Mn charge state. In the second case, different energy barriers in as-grown and hydrogenated samples could be due to a change of the energy gap induced by hydrogen doping. Based on the experimental results the two possibilities cannot be distinguished. However, theoretical calculations presented in the next section favor the latter explanation.

III. THEORY

A. Calculation details

The calculations are performed within the density functional theory in the generalized gradient approximation (GGA) of the exchange-correlation potential [40-42]. The +U corrections are included. [22–24] We use the pseudopotential method implemented in the QUANTUM ESPRESSO code [43], with the valence atomic configuration $3d^{10}4s^2$ for Zn, $2s^2p^4$ for O, and $3s^2p^64s^2p^03d^5$ for Mn, respectively. The plane-waves kinetic energy cutoffs of 30 Ry for wave functions and 180 Ry for charge density are employed. The electronic structure of the wurtzite ZnO is examined with a $8 \times 8 \times 8$ k-point grid. Analysis of a single Mn impurity in ZnO is performed using $3 \times 3 \times 2$ supercells with 72 atoms (2.8 atomic percent of Mn). *k*-space summations are performed with a $3 \times 3 \times 3$ *k*point grid for density of states (DOS) calculations, while calculations with fixed occupation matrices are performed using the Γ point only. The U terms for 3d(Zn), 2p(O), and 3d(Mn) orbitals are treated as free parameters, whose values are discussed below. Ionic positions are optimized until the forces acting on ions became smaller than $0.02 \text{ eV}/\text{\AA}$.

B. Pure ZnO

It was previously shown that both the local density approximation (LDA) and GGA fail to give correct band characteristics of ZnO. In particular, the band gap E_{gap} of ZnO calculated within LDA/GGA [44-46] is about 1 eV. This is due to the universal "band gap problem," i.e., the underestimation of the gap within LDA/GGA on one hand but also to the too high calculated energies of the d(Zn)-derived bands [47] on the other hand. The inclusion of the U(Zn) term [46,48,49] solves this problem only partially, since the band gap is still underestimated by about 2 eV. For example, we find that when U(Zn) = 10 eV is employed the d(Zn) band is at about 8 eV below the valence band maximum (VBM), in agreement with experiment [46,49–51], but $E_{gap} \approx 1.2 \text{ eV}$ is still wrong. This is because the coupling between d(Zn) and VBM is weak due to the large energy difference between those states, and thus E_{gap} is not sensitive to the energy of the d(Zn) band. To obtain a correct value of E_{gap} one should observe that the upper valence band is derived from p(O) orbitals. Indeed, the inclusion of the U(O) term for the p(O) orbitals, in addition to U(Zn), gives a correct band structure [46,52,53]. We find that U(Zn) = 12.5 eV and U(O) = 6.25 eV reproduce both the experimental E_{gap} of 3.3 eV [49] and the energy of the d(Zn) band, centered about 8 eV below the VBM, in excellent agreement with Ref. [53]. These values also lead to the correct width of ~6 eV of the upper valence band of mostly 2p(O)character, and the lower conduction band of 4s(Zn) character. The relaxed crystal structure agrees well with experiment: The lattice parameters a = 3.23 Å and c = 5.19 Å, as well as the internal parameter u = 0.38 are underestimated by less than 1% in comparison with experimental values: a = 3.25 Å, c = 5.20 Å, and u = 0.38 [54]. One should finally observe that the electronic structure of ZnO represents a problem even for the GW approach: As is discussed in Refs. [46,55], different GW calculations, including quasiparticle self-consistent GW calculations, still place the d(Zn) band at an energy too high



FIG. 7. Energy bands (left panels) and DOS (right panels) of (a) $ZnO:Mn^{2+}$ and (b) $ZnO:Mn^{3+}$. Gray area and black lines (blue lines in the online version) in DOS display the total DOS and DOS projected on d(Mn) orbitals, respectively. Horizontal (red) lines denote the band gap of ZnO.

by about 1 eV, and an additional potential on Zn cations is needed to achieve the correct band structure.

C. Mn impurity in ZnO

Properties of the Mn ion in ZnO depend on its charge state. The band structure and DOS of ZnO doped with Mn^{2+} and Mn^{3+} are shown in Fig. 7 for U(Mn) = 0. Mn^{2+} introduces two levels into the gap, a $t_{2\uparrow}$ triplet at 2.64 eV above VBM and an $e_{2\uparrow}$ doublet at 1.90 eV. (Actually, $t_{2\uparrow}$ is split into a singlet and a doublet by the wurtzite crystal field with a small splitting of about 0.1 eV.) The spin-down states form resonances degenerate with the conduction band, and thus, in agreement with experiment, Mn cannot assume the 1+ charge state in n-type ZnO.

The $t_{2\uparrow}$ and $e_{2\uparrow}$ levels of Mn³⁺ are at about 1.45 and 0.28 eV above VBM, respectively, i.e., they are lower by \sim 1.5 eV than those of Mn²⁺. This large difference in the level energies of Mn²⁺ and Mn³⁺ stems from the strong intracenter Coulomb repulsion between d(Mn) electrons caused by the localization of their wave functions. Moreover, the localized character of d(Mn) is responsible for the relatively large 6% reduction of the Mn-O bond length, from 2.02 Å for Mn²⁺ to 1.90 Å for Mn³⁺, which is induced by the decrease in the Coulomb coupling between Mn and O anions. We also mention that the energies of the gap states of the isolated Mn³⁺ and those of Mn^{3+} with a photoelectron e_{CB} in the conduction band are the same to within 0.02 eV, and the Mn-O bond lengths are the same to within 0.01 Å. This is because of the delocalized character of the wave function from the bottom of the conduction band. The results for Mn^{3+} with e_{CB} are shown in Fig. 9(c).



FIG. 8. (a) Total energy change of Mn^{2+} and (Mn^{3+}, e_{CB}) as a function of configuration coordinate Q. Q_2 and Q_3 are equilibrium atomic configurations of Mn^{2+} and (Mn^{3+}, e_{CB}) charge states, respectively, and Q_B is the configuration coordinate of the barrier. (b) Single particle energy of the $t_{2\uparrow}$ level for both Mn^{2+} (red symbols) and (Mn^{3+}, e_{CB}) (blue symbols); note the strong dependence of the $t_{2\uparrow}$ energy on the charge state. U(Mn) = 0 is assumed.

D. Photoionization, recombination, and mechanism of metastability

Due to the strong dependence of gap levels on the Mn charge state, the energies of absorption and/or recombination cannot be deduced directly from single particle states of Mn^{2+} (or

 Mn^{3+}), as was indicated in, e.g., Refs. [56,57]. Consequently, energies of processes analyzed below are calculated from the total energy difference between final and initial states [58].

The absorption-recombination cycle of Mn^{2+} occurs in five steps. They are presented in Fig. 8, which shows both the total energy and the Mn energy levels for each step for U(Mn) = 0. Mn levels are shown in Fig. 9 in detail.

(i) In the first step [Fig. 8(a), $A \rightarrow B$] one electron from $t_{2\uparrow}$ of Mn^{2+} is excited to the conduction band, with the atomic positions kept fixed at the equilibrium configuration of Mn^{2+} , Q_2 . The excitation energy is $E_{abs} = 2.0$ eV. Photoionization induces a strong decrease of the $t_{2\uparrow}$ energy by about 2 eV, see Figs. 8(b) and 9(b), because the depopulation of the d(Mn) shell reduces the strength of the Coulomb repulsion.

(ii) In the second step (B \rightarrow C), atoms are allowed to relax towards the equilibrium configuration Q_3 of Mn³⁺ with the photoelectron e_{CB} in the conduction band. This case is denoted by (Mn³⁺, e_{CB}) in Figs. 8 and 9. During this step the Mn-O bonds are reduced by $\sim 6\%$, and the energy of $t_{2\uparrow}$ increases by about 1 eV [Figs. 8(b) and 9(c)], in agreement with its antibonding character. The corresponding energy gain $[E_{tot}(B) - E_{tot}(C)]$ is 0.69 eV.

This energy gain takes place in spite of the fact that the single particle gap level $t_{2\uparrow}$ increases in energy by more than 1 eV, see Figs. 8(b) and 9(c). This illustrates the fact that total energy differences cannot be deduced directly from single particle states of Mn²⁺ (or Mn³⁺), since other factors such as the Madelung ion-ion energy are dominant.

According to our results, the relaxed (Mn^{3+}, e_{CB}) state of Mn^{3+} with one electron in the conduction band is metastable, because its energy is higher than that of the relaxed Mn^{2+} by 1.32 eV [$(E_{tot}(C)-E_{tot}(A))$ in Fig. 8(a)], but a direct recombination of the photoelectron to the $t_{2\uparrow}$ level of Mn^{2+} is not possible. The instability stems from the fact that in the configuration Q_3 the energy of the $t_{2\uparrow}$ level of Mn^{2+} occupied with three electrons is above the conduction band bottom (CBB), see Fig. 8(b). Indeed, the calculated dependence of $t_{2\uparrow}$ of Mn^{2+} on the configuration coordinates, presented in Fig. 8(b), shows that $t_{2\uparrow}$ increases in energy with the decreasing Mn-O bond lengths and merges with the conduction band for the atomic configuration Q_B . For smaller bond lengths, in particular in the Q_3 configuration, it is a resonance



FIG. 9. Calculated diagrams of Mn levels for (a) Mn^{2+} at equilibrium configuration Q_2 , (b) Mn^{3+} with a photoelectron e_{CB} in the CB in the same atomic configuration Q_2 , (c) Mn^{3+} with e_{CB} in the relaxed configuration Q_3 , (d) Mn^{3+} with e_{CB} in the barrier configuration Q_B , (e) Mn^{2+} (when e_{CB} is captured by Mn) in the barrier configuration Q_B , and (f) Mn^{2+} relaxed to Q_2 ; this is the end step of the recombination process, the configuration is the same as in (a). U(Mn) = 0 is assumed.

degenerate with the conduction band. The extrapolated $t_{2\uparrow}$ energies are shown by dashed lines in Fig. 8(b), and the corresponding extrapolated total energy is shown by the dashed line in Fig. 8(a). We use extrapolated values because for the configuration coordinates in the range (Q_B, Q_3) we could not arrive at convergent results when fixing the occupation of the $t_{2\uparrow}$ level by three electrons. The occupancy of $t_{2\uparrow}$ by three electrons is unstable since there are empty conduction states lower in energy. In other words, Mn^{2+} is stable for configuration coordinates in the range from Q_2 to Q_B , when $t_{2\uparrow}$ is a gap state, while (Mn^{3+}, e_{CB}) is locally stabilized for configuration coordinates in the range (Q_3, Q_B) . At Q_B , the electron recombination is possible, with the corresponding energy gain E_{rec} . The difference in total energy of (Mn^{3+}, e_{CB}) between Q_3 and Q_B is the energy barrier E_B .

The difference between total energy of Mn^{2+} and (Mn^{3+}, e_{CB}) states in the Q_3 configuration is only estimated from single particle levels at the state halfway between, thanks to the Janak theorem [59]. It formally gives the lower energy of Mn^{2+} state by 0.59 eV. Actually, however, the Mn^{2+} state is unreachable in the Q_3 configuration and does not converge in our calculations. The Janak theorem can be applied in this case, since the ionic positions are kept fixed at Q_3 .

The recombination of e_{CB} requires three more steps shown in Figs. 8 and 9.

(iii) A thermally driven atomic transition from Q_3 to the barrier configuration Q_B (C \rightarrow D), which is described in detail below. According to our estimates, the upper limit for the barrier E_B is 60 meV.

(iv) The capture of the photoelectron by Mn^{3+} (D \rightarrow E), i.e., the transition to the Mn^{2+} state. This transition at the estimated Q_B configuration provides the energy gain of $E_{rec} = 0.98$ eV. (v) The relaxation of Mn^{2+} from Q_B to Q_2 (E \rightarrow A) with $E_{relax} = 0.41$ eV.

Finally, we notice that the metastable atomic configuration Q_3 of (Mn^{3+}, e_{CB}) is an excited state of the crystal as a whole, since the corresponding total energy is higher than that of ZnO:Mn²⁺ in the ground state configuration Q_2 . Importantly, however, in those particular atomic configurations electrons are in the respective ground states, which justifies the usage of GGA + U. Consequently, both the total crystal energies and the total energy difference between the metastable configuration Q_3 and the ground state Q_2 are well defined as well. Moreover, in the Q_3 configuration small displacements of anions around Mn increase the total energy of (Mn^{3+}, e_{CB}) , which proves that this is indeed a metastable state of the crystal, and the barrier for electron recombination is nonvanishing.

E. Estimation of the energy barrier

A detailed description of the metastability, in particular of the barrier height for return to the ground state, is difficult, because the atomic relaxations around Mn involve not only the nearest but also more distant neighbors. To make the problem tractable, we limit the parameter space to the four Mn-O bonds shown in Fig. 10(a). The local symmetry of Mn is C_{3v} in all the considered cases, and consequently there are three parameters that define the geometry, d_{1z} , d_{2y} , and d_{2z} , which are defined in the caption to Fig. 10. The three basal O atoms are equivalent. Mn is assumed to be at r = 0, and



FIG. 10. (a) Mn-O bonds. The atomic positions in cartesian coordinates are Mn(0,0,0), O1(0,0, d_{1z}), O2(0, d_{2y} , d_{2z}). (b) Two paths between Q_2 and Q_3 . For d_{2y}^B , Mn²⁺ becomes unstable, i.e., the $t_{2\uparrow}$ level of Mn²⁺ is above CBM. Q_B is the estimated barrier configuration.

the atoms beyond the first neighbors are allowed to relax. The calculated coordinates of the two nonequivalent oxygen ions for both Mn^{2+} and Mn^{3+} in the (Mn^{3+}, e_{CB}) configuration, together with the Zn-O bond lengths in ZnO for comparison, are given in Table I. Two possible paths between Q_2 and Q_3 are displayed in Fig. 10(b). In both cases we found that the $t_{2\uparrow}$ level of Mn^{2+} is much more sensitive to the changes of d_{2v} than of d_{1_7} or d_{2_7} . For both paths, the Mn²⁺ instability begins at almost the same d_{2y} , which is denoted by d_{2y}^B in Fig. 10(b). Therefore, the barrier configuration Q_B is taken as a point which is achieved from Q_3 by changing only the d_{2y} coordinate. With this assumption we find Q_B as the configuration at which the $t_{2\uparrow}$ level of Mn²⁺ is degenerate with CBM. This allows us to find the corresponding energy barrier, $E_B = E(Mn^{3+}, Q_3) - E(Mn^{3+}, Q_3)$ $E(Mn^{3+}, Q_B) = 60$ meV, which clearly represents the upper limit.

F. Dependence on U(Mn)

The analysis presented in the previous section was conducted assuming U(Mn) = 0. As was mentioned in Sec. III A, the value of U(Mn) is treated here as a free parameter, which can be adjusted to fit the experimental data. We have performed calculations for a few values of U(Mn), and the results are presented in Fig. 11. As follows from Fig. 11, the energies of gap levels of both Mn^{2+} and Mn^{3+} decrease with increasing U. In particular, assuming U(Mn) = 4 eV brings $t_{2\uparrow}$ about 0.9 eV

TABLE I. Equilibrium coordinates of O1 and O2 shown in Fig. 10(a), the respective Zn-O and Mn-O bond lengths d_1 and d_2 , and the average bond length $\langle d \rangle = (d_1 + 3d_2)/4$. All values are in Å.

	$d_1 = d_{1z}$	d_{2y}	d_{2z}	d_2	$\langle d \rangle$
ZnO:	1.98	1.87	-0.62	1.97	1.97
Mn^{2+} :	2.03	1.92	-0.63	2.02	2.02
Mn ³⁺ :	1.94	1.79	-0.59	1.88	1.90



FIG. 11. Dependence of the $t_{2\uparrow}$ energy level on U(Mn) for Mn^{2+} and (Mn^{3+}, e_{CB}) in the configurations Q_2 and Q_3 .

above the VBM and puts the $e_{2\uparrow}$ level below the VBM. We also note that for U(Mn) = 4 eV, in the equilibrium configuration Q_2 Mn-O bond lengths are 2.06 Å, while they are reduced to about 1.98 Å for Q_3 , which shows that the impact of U on bond lengths is moderate.

Comparing our results with previous theoretical investigations of Mn in ZnO we note that the LDA calculations including SIC corrections [60] were performed for high Mn content, for which a wide Mn-induced band in the band gap was found in qualitative agreement with our results. LDA supplemented with the +U term imposed on the d(Mn)orbitals was also used [27,30,61]. For U(Mn) = 3 eV, there is a reasonable agreement with Ref. [61], which uses U =3.9 eV and J = 1 eV (this corresponds to the effective U = 3.9 - 1.0 = 2.9 eV), and with the time dependent DFT [56]. The other applied U(Mn) values were 6 eV [30] obtained from the fit to the experimental magnetization data and 3.2 eV [27] estimated according to Ref. [62]. In these works, the $Mn^{2+} t_{2\uparrow}$ level is situated at about 0.7–1.0 eV above the VBM. The levels of Mn³⁺ were not investigated. Our results obtained with U(Mn) = 3-4 eV are reasonably close to those quoted above.

To obtain the optimal value of U(Mn) by fitting to our experimental results we note that the U-induced downward shifts of the Mn levels imply that the excitation energy [step $A \rightarrow B$ in Fig. 8(a)] increases from 2.0 to 2.84 eV when U changes from 0 to 4 eV. Moreover, the barrier E_B depends on the U(Mn) term: It decreases with the increasing U and it vanishes for U(Mn) higher than about 1.7 eV. The decrease of E_B is related with the U-induced decrease of the Mn levels. In particular, for U = 0 the $t_{2\uparrow}$ level is degenerate with the conduction band for the configuration Q_3 , while for U >1.7 eV it is below the CBM, and therefore a direct transition of the photoelectron from the conduction band to $t_{2\uparrow}$ is possible. This feature is illustrated in Fig. 12 for U(Mn) = 4 eV. Therefore, the best overall value of U(Mn) is about 1.5 eV, giving a barrier of about 1 meV, and the excitation energy of about 2.4 eV.



FIG. 12. The *Q* dependence of (a) the total energy and (b) single particle levels of Mn^{2+} and (Mn^{3+}, e_{CB}) for U(Mn) = 4 eV.

IV. SUMMARY

Photo-EPR experiments performed on ZnO:Mn single crystals have confirmed that the Mn^{3+}/Mn^{2+} level is located about 2.1 eV below the conduction band minimum of ZnO, as illumination of the crystal with photon energies higher than 2.1 eV leads to a partial, temperature dependent depopulation of the Mn^{2+} state at low temperatures, accompanied by photoconductivity. The unusually small thermal deactivation energy (of the order of 1 meV) together with the untypically fast kinetics of Mn^{2+} photoquenching point out to a process different from charge transfer from Mn^{2+} to other defect centers. We interpret the observed metastable change of Mn^{2+} occupancy under illumination as due to a small energy barrier for electron recapture from the conduction band by Mn^{3+} .

GGA+U approach was employed to study both the Mn²⁺-Mn³⁺ optical transitions and the stability of the (Mn³⁺, e_{CB}) photoexcited state. The excited state is found to be metastable, because in the relaxed configuration a direct recombination of the photoelectron is not possible, and recapture requires overcoming an energy barrier. The energy barrier E_B decreases with the increasing U(Mn) and vanishes for U > 1.7 eV. Comparing theory with experiment we find that U(Mn) of about 1.5 eV leads to photoionization energy, 2.4 eV, and the barrier E_B of the order 1 meV, in a reasonable agreement with the experimental data. Moreover, one should note that similar results hold for Mn and Fe ions in GaN [63,64], for which

the experimental intracenter transition energies are reproduced with very small U terms.

The metastability of (Mn^{3+}, e_{CB}) is related to the reduction of the Mn-O bonds after the Mn^{2+} ionization. This change of atomic configuration is coupled to electronic degrees of freedom, and it rises the energy of the d(Mn) donor level. More importantly, the Coulomb repulsion between the d(Mn)electrons is strong, and it rises the Mn level energy by ~ 1 eV when Mn changes its charge state to Mn^{2+} . In more detail, while the donor level of Mn^{3+} is situated below the bottom of the conduction band, after capturing the photoelectron the occupied donor level of Mn^{2+} would be above the empty conduction band, which is an unstable electronic configuration. This factor blocks the recombination of the

- K. Maeda, T. Takata, M. Hara, N. Saito, Y. Inoue, H. Kobayashi, and K. Domen, J. Am. Chem. Soc. **127**, 8286 (2005).
- [2] M. Law, L. E. Greene, J. C. Johnson, R. Saykally, and P. Yang, Nat. Mater. 4, 455 (2005).
- [3] U. Riaz, S. Ashraf, and J. Kashyap, Mater. Res. Bull. 71, 75 (2015).
- [4] C. A. Johnson, K. R. Kittilstved, T. C. Kaspar, T. C. Droubay, S. A. Chambers, G. M. Salley, and D. R. Gamelin, Phys. Rev. B 82, 115202 (2010).
- [5] A. Hausmann and H. Huppertz, J. Phys. Chem. Solids 29, 1369 (1968).
- [6] E. Chikoidze, H. J. von Bardeleben, Y. Dumont, P. Galtier, and J. L. Cantin, J. Appl. Phys. 97, 10D316 (2005).
- [7] M. Godlewski, A. Wąsiakowski, V. Yu. Ivanov, A. Wójcik-Głodowska, M. Łukasiewicz, E. Guziewicz, R. Jakieła, K. Kopalko, A. Zakrzewski, and Y. Dumont, Opt. Mater. 32, 680 (2010).
- [8] J. Dabrowski and M. Scheffler, Phys. Rev. B 40, 10391 (1989).
- [9] J. Dabrowski and M. Scheffler, Phys. Rev. Lett. **60**, 2183 (1988).
- [10] D. J. Chadi and K. J. Chang, Phys. Rev. Lett. **61**, 873 (1988).
- [11] L. Dobaczewski, P. Kaczor, M. Missous, A. R. Peaker, and Z. R. Żytkiewicz, Phys. Rev. Lett. 68, 2508 (1992).
- [12] P. Bogusławski and J. Bernholc, Phys. Rev. B 56, 9496 (1997).
- [13] C. Wetzel, T. Suski, J. W. Ager, III, E. R. Weber, E. E. Haller, S. Fischer, B. K. Meyer, R. J. Molnar, and P. Perlin, Phys. Rev. Lett. 78, 3923 (1997).
- [14] T. Thio, J. W. Bennett, D. J. Chadi, R. A. Linke, and M. C. Tamargo, J. Electron. Mater. 25, 229 (1996).
- [15] S. Lany and A. Zunger, Phys. Rev. Lett. 100, 016401 (2008).
- [16] R. Jones and S. Öberg, Phys. Rev. B 44, 3407 (1991).
- [17] T. M. Schmidt, A. Fazzio, and M. J. Caldas, Phys. Rev. B 53, 1315 (1996).
- [18] L. Shi and L.-W. Wang, Phys. Rev. Lett. 109, 245501 (2012).
- [19] L. Shi, K. Xu, and L.-W. Wang, Phys. Rev. B 91, 205315 (2015).
- [20] A. Alkauskas, Q. Yan, and C. G. Van de Walle, Phys. Rev. B 90, 075202 (2014).
- [21] A. Alkauskas, M. D. McCluskey, and C. G. Van de Walle, J. Appl. Phys. 119, 181101 (2016).
- [22] V. I. Anisimov, J. Zaanen, and O. K. Andersen, Phys. Rev. B 44, 943 (1991).

PHYSICAL REVIEW B 94, 165143 (2016)

photoelectron and drives the metastability of Mn^{3+} . While the role of the local lattice relaxations was recognized and extensively discussed for metastable centers in semiconductors [8–17], the role of the strong Coulomb coupling between *d* electrons is equally important in defining the Mn metastability.

ACKNOWLEDGMENTS

The authors acknowledge the support from the Projects No. 2012/05/B/ST3/03095 and No. 2011/01/D/ST7/02657, which are financed by Polish National Science Centre (NCN). Calculations were performed at the Interdisciplinary Centre for Mathematical and Computational Modelling, University of Warsaw (Grants No. G46-13 and No. G16-11).

- [23] V. I. Anisimov, I. V. Solovyev, M. A. Korotin, M. T. Czyżyk, and G. A. Sawatzky, Phys. Rev. B 48, 16929 (1993).
- [24] M. Cococcioni and S. de Gironcoli, Phys. Rev. B 71, 035105 (2005).
- [25] A. Mycielski, L. Kowalczyk, A. Szadkowski, B. Chwalisz, A. Wysmołek, R. Stępniewski, J. M. Baranowski, M. Potemski, A. Witowski, R. Jakieła, A. Barcz, B. Witkowska, W. Kaliszek, A. Jęrzejczak, A. Suchocki, E. Łusakowska, and E. Kamińska, J. Alloys Compd. **371**, 150 (2004).
- [26] See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.94.165143 for the angular dependence of the Mn²⁺ EPR spectra in as grown ZnO:Mn.
- [27] M. A. Gluba and N. H. Nickel, Phys. Rev. B 87, 085204 (2013).
- [28] T. Story, C. H. W. Swüste, P. J. T. Eggenkamp, H. J. M. Swagten, and W. J. M. de Jonge, Phys. Rev. Lett. 77, 2802 (1996).
- [29] M. Godlewski, A. Wójcik-Głodowska, E. Guziewicz, S. Yatsunenko, A. Zakrzewski, Y. Dumont, E. Chikoidze, and M. R. Phillips, Opt. Mater. **31**, 1768 (2009).
- [30] T. Chanier, F. Virot, and R. Hayn, Phys. Rev. B 79, 205204 (2009).
- [31] K. M. Whitaker, M. Raskin, G. Kiliani, K. Beha, S. T. Ochsenbein, N. Janssen, M. Fonin, U. Rüdiger, A. Leitenstorfer, D. R. Gamelin, and R. Bratschitsch, Nano Lett. 11, 3355 (2011).
- [32] C. G. Van de Walle, Phys. Rev. Lett. 85, 1012 (2000).
- [33] B. K. Meyer, J. Sann, D. M. Hofmann, C. Neumann, and A. Zeuner, Semicond. Sci. Technol. 20, S62 (2005).
- [34] M. Godlewski, Phys. Status Solidi A 90, 11 (1985).
- [35] D. C. Look, K. D. Leedy, L. Vines, B. G. Svensson, A. Zubiaga, F. Tuomisto, D. R. Doutt, and L. J. Brillson, Phys. Rev. B 84, 115202 (2011).
- [36] A. Janotti and C. G. Van de Walle, Phys. Rev. B 76, 165202 (2007).
- [37] S. Lany and A. Zunger, Phys. Rev. Lett. 98, 045501 (2007).
- [38] F. Oba, A. Togo, I. Tanaka, J. Paier, and G. Kresse, Phys. Rev. B 77, 245202 (2008).
- [39] D. M. Hofmann, A. Hofstaetter, F. Leiter, H. Zhou, F. Henecker, B. K. Meyer, S. B. Orlinskii, J. Schmidt, and P. G. Baranov, Phys. Rev. Lett. 88, 045504 (2002).
- [40] P. Hohenberg and W. Kohn, Phys. Rev. 136, B864 (1964).
- [41] W. Kohn and L. J. Sham, Phys. Rev. 140, A1133 (1965).

- [42] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996).
- [43] QUANTUM ESPRESSO, http://www.quantum-espresso.org.
- [44] P. Schröer, P. Krüger, and J. Pollmann, Phys. Rev. B 47, 6971 (1993).
- [45] J. E. Jaffe, J. A. Snyder, Z. Lin, and A. C. Hess, Phys. Rev. B 62, 1660 (2000).
- [46] L. Y. Lim, S. Lany, Y. J. Chang, E. Rotenberg, A. Zunger, and M. F. Toney, Phys. Rev. B 86, 235113 (2012).
- [47] S.-H. Wei and A. Zunger, Phys. Rev. B 37, 8958 (1988).
- [48] G. C. Zhou, L. Z. Sun, X. L. Zhong, X. Chen, L. Wei, and J. B. Wang, Phys. Lett. A 368, 112 (2007).
- [49] C. L. Dong, C. Persson, L. Vayssieres, A. Augustsson, T. Schmitt, M. Mattesini, R. Ahuja, C. L. Chang, and J. H. Guo, Phys. Rev. B 70, 195325 (2004).
- [50] L. Ley, R. A. Pollak, F. R. McFeely, S. P. Kowalczyk, and D. A. Shirley, Phys. Rev. B 9, 600 (1974).
- [51] C. J. Vesely and D. W. Langer, Phys. Rev. B 4, 451 (1971).
- [52] X. Ma, Y. Wu, Y. Lv, and Z. Y., J. Phys. Chem. C 117, 26029 (2013).
- [53] L. A. Agapito, S. Curtarolo, and M. Buongiorno Nardelli, Phys. Rev. X 5, 011006 (2015).
- [54] H. Karzel, W. Potzel, M. Kofferlein, W. Schiessl, M. Steiner, U. Hiller, G. M. Kalvius, D. W. Mitchell, T. P. Das, P. Blaha,

K. Schwarz, and M. P. Pasternak, Phys. Rev. B 53, 11425 (1996).

- [55] S. Lany, H. Raebiger, and A. Zunger, Phys. Rev. B 77, 241201 (2008).
- [56] E. Badaeva, C. M. Isborn, Y. Feng, S. T. Ochsenbein, D. R. Gamelin, and X. Li, J. Phys. Chem. C 113, 8710 (2009).
- [57] K. R. Kittilstved, W. K. Liu, and D. R. Gamelin, Nat. Mater. 5, 291 (2006).
- [58] We have also checked that the integration of Mn level energies over fractional occupancies in the range between 0 and 1 reproduces the exact results for absorption, in accordance with Janak's theorem [59], while the approximation by the midpoint value (occupancy 1/2) gives an error lower than 0.2 eV.
- [59] J. F. Janak, Phys. Rev. B 18, 7165 (1978).
- [60] M. Toyoda, H. Akai, K. Sato, and H. Katayama-Yoshida, Physica B: Condens. Matter 376-377, 647 (2006).
- [61] H. Raebiger, S. Lany, and A. Zunger, Phys. Rev. B 79, 165202 (2009).
- [62] A. Janotti, D. Segev, and C. G. Van de Walle, Phys. Rev. B 74, 045202 (2006).
- [63] O. Volnianska, T. Zakrzewski, and P. Boguslawski, J. Chem. Phys. 141, 114703 (2014).
- [64] T. Zakrzewski and P. Boguslawski, J. Alloys Compd. 664, 565 (2016).