Anomalous transport near the Lifshitz transition at the LaAlO₃/SrTiO₃ interface

S. Nandy,¹ N. Mohanta,² S. Acharya,¹ and A. Taraphder^{1,3}

¹Department of Physics, Indian Institute of Technology Kharagpur, West Bengal 721302, India

²Center for Electronic Correlations and Magnetism, Theoretical Physics III, Institute of Physics, University of Augsburg,

86135 Augsburg, Germany

³Centre for Theoretical Studies, Indian Institute of Technology Kharagpur, West Bengal 721302, India

(Received 8 July 2016; revised manuscript received 5 September 2016; published 3 October 2016)

The two-dimensional electron liquid, at the (001) interface between band insulators LaAlO₃ and SrTiO₃, undergoes Lifshitz transition as the interface is doped with carriers. At a critical carrier density, two additional orbitals populate at the Fermi level, with a concomitant change in the Fermi surface topology. Using dynamical mean-field theory, formulated within a realistic three-orbital model, we study the influence of the Lifshitz transition and local electron correlations on the transport properties. We look at the thermal conductivity, optical conductivity, Seebeck coefficient, and angle-resolved photoemission spectra and find that at a critical density, both the thermal and dc conductivities rise sharply to higher values while the Seebeck coefficient shows a cusp. The interorbital electron-electron interaction transfers spectral weight near the Γ point towards lower energy, thereby reducing the critical density. In the presence of external magnetic field, the critical density further reduces due to exchange splitting. Beyond a sufficiently large field, multiple cusps appear in the Seebeck coefficient revealing multiple Lifshitz transitions.

DOI: 10.1103/PhysRevB.94.155103

I. INTRODUCTION

The metallic interface between perovskite band insulators LaAlO₃ (LAO) and SrTiO₃ (STO) is a prototypical STO-based heterointerface [1–3] having a wide variety of intriguing properties such as superconductivity (below 200 mK) [4-7], ferromagnetism (below 200 K) [8-10], ferroelectricity [11], and strong spin-orbit coupling (SOC) [12,13]. The good tunability of these properties [14–18], with respect to external fields, makes this interface a potential candidate for novel device applications [19–21]. The electrons in the quasi-two-dimensional electron liquid (q2DEL) at the interface are supplied by an intrinsic electronic transfer process, known as the "polar catastrophe mechanism" [1,19,22], and also by the oxygen vacancies near the interface [23–25]. The superconductivity is mediated by interface phonons and is conventional in nature [26]. There are two possible sources of ferromagnetism: (i) as suggested previously [27,28], the electrons occupying the d_{xy} orbital of Ti ions at the TiO₂-terminated interface are localized due to the repulsive electron-electron interaction forming a quarter-filled charge-ordered insulating state and the ferromagnetism is a result of an exchange coupling between the localized moments and the conduction electrons residing below the interface layer; or (ii) density function theory (DFT) indicates that the oxygen vacancies near the interface lead to a spin splitting of the electrons in the occupied t_{2g} orbitals at the Fermi level giving rise to ferromagnetic order [29–33]. The ferromagnetism, which is tunable [29,34] and is of d_{xy} character [35], coexists with superconductivity [8,9,36–38] in spatially phase segregated regions due to the inhomogeneity at the interface [39–41]. The coexistence of these competing orders gives rise to unconventional phenomenon such as the field-induced transient superconductivity [42] and topological superconductivity due to the presence of the Rashba SOC [43,44]. Transport measurements reveal that another type of carrier, of higher mobility, appears as an additional conducting channel as the gate voltage is increased [10,45]. These carriers originate from the d_{yz} , d_{zx} orbitals, which are separated from the d_{xy} orbital due to confinement at the interface [46,47], and are believed to be responsible for participating in superconductivity [45,48–50]. The emergence of the high mobility carriers, with increasing the Fermi level, triggers a Lifshitz transition [51], in which the topology of the Fermi surface changes, and results in large off-diagonal Hall conductivity [52,53]. However, there are very few experiments so far that actually track the Lifshitz transition precisely. The impact of the Lifshitz transition on the transport properties, especially when the interaction between the electrons is not negligible, is not much explored either. Furthermore, the role of the electron correlation in the Lifshitz transition is an interesting aspect unaddressed so far.

In this paper we adopt a model Hamiltonian with six spin-orbit coupled t_{2g} orbitals, developed using DFT analysis [46], and employ dynamical mean-field theory (DMFT) with iterative perturbation theory (IPT) as the impurity solver to investigate the transport properties in the presence of interorbital electron-electron interaction. The change in topology in the interacting Fermi surface is investigated. We calculate the thermal conductivity, optical conductivity, and Seebeck coefficient (thermopower) which reveal anomalous behavior at a critical carrier density. As the carrier density is tuned, the thermal and optical conductivities sharply rise to higher values while the Seebeck coefficient exhibits a cusp. We compute the intensity of the angle-resolved photoemission spectroscopy (ARPES) which shows that the spectral weight, near the Γ point, is transferred towards lower energy. The electronelectron interaction, therefore, slowly decreases the critical density for the Lifshitz transition. We also study the situation in the presence of external magnetic field and find that the critical density further reduces with increasing field strength. However, beyond a large critical field, the spin degeneracy is removed in all the orbitals and multiple cusps appear in the Seebeck coefficient indicating multiple Lifshitz transitions. Unlike the low-field case, the critical densities for the other two Lifshitz transitions increase with increasing field strength. We compare our findings with existing experimental data and discuss the possibility to observe these anomalous phenomena in future experiments.

The rest of the paper is organized as follows. In Sec. II we introduce the effective Hamiltonian for the interface q2DEL and briefly describe the formulation of the multiorbital DMFT, employed to solve the interorbital electron-electron interaction. In Sec. III we discuss our numerical results establishing the anomalous features observed in the transport properties and the multiple Lifshitz transitions in the presence of external magnetic field. We also make comparisons of our results with existing experimental data. Finally, in Sec. IV we discuss the experimental aspects of the phenomena observed in our study and summarize our results.

II. MODEL AND METHOD

Electrons in q2DEL predominantly occupy the three t_{2g} orbitals of Ti ions at the terminating TiO₂ layer. These orbitals have parabolic dispersion near the Γ point with the d_{xy} orbital lying lower in energy than the d_{xz} , d_{yz} orbitals by 0.4 eV due to tetragonal distortion and quantum confinement at the interface [46,47]. A small Rashba-like splitting is observed near the Γ point while an atomic SOC splits the degenerate states near the crossing points of the orbitals resulting in an interorbital level mixing, as described in Fig. 2(a). Here we study the normal state transport properties in the presence of electron correlation and ignore, for simplicity, the competing ferromagnetic and superconducting orders. We also ignore the real-space inhomogeneity at the interface because the effect of nonmagnetic disorder is rather uninteresting in the context of the current study.

The noninteracting Hamiltonian, describing the interface electrons in the normal state, written in the basis of the three t_{2g} orbitals, is given by [46]

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{ASO} + \mathcal{H}_{RSO}, \tag{1}$$

where $\mathcal{H}_0 = \sum_{k,\alpha,\sigma} (\epsilon_{k\alpha} - \mu) c_{k\alpha\sigma}^{\dagger} c_{k\alpha\sigma}$ describes the band dispersion of the electrons in the three t_{2g} orbitals with $\epsilon_{ka} = -2t_1(\cos k_x + \cos k_y) - t_2 - 4t_3 \cos k_x \cos k_y$, $\epsilon_{kb} = -t_1(1 + 2\cos k_y) - 2t_2 \cos k_x - 2t_3 \cos k_y$, and $\epsilon_{kc} = -t_1(1 + 2\cos k_x) - 2t_2 \cos k_y - 2t_3 \cos k_x$, μ is the chemical potential and $t_1 = 0.277$ eV, $t_2 = 0.031$ eV, and $t_3 = 0.076$ eV are the tight-binding parameters.

The second term of the Hamiltonian is due to the atomic SOC $\mathcal{H}_{ASO} = \Delta_{so}\vec{l}\cdot\vec{s}$ which appears because of the crystal field splitting of the atomic orbitals. In terms of t_{2g} orbital basis $(c_{ka\uparrow}, c_{kb\uparrow}, c_{kc\uparrow}, c_{ka\downarrow}, c_{kb\downarrow}, c_{kc\downarrow})$ where $(a = d_{xy}, b = d_{yz}, c = d_{zx})$, \mathcal{H}_{ASO} can be written as

$$\mathcal{H}_{ASO} = \frac{\Delta_{so}}{2} \sum_{k} (c^{\dagger}_{ka\uparrow} \quad c^{\dagger}_{kb\uparrow} \quad c^{\dagger}_{kc\uparrow} \quad c^{\dagger}_{ka\downarrow} \quad c^{\dagger}_{kb\downarrow} \quad c^{\dagger}_{kc\downarrow}) \times \begin{pmatrix} 0 & 0 & 0 & 0 & 1 & -i \\ 0 & 0 & i & -1 & 0 & 0 \\ 0 & -i & 0 & i & 0 & 0 \\ 0 & -1 & -i & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & -i \\ i & 0 & 0 & 0 & i & 0 \end{pmatrix} \begin{pmatrix} c_{ka\uparrow} \\ c_{kb\uparrow} \\ c_{kc\uparrow} \\ c_{kb\downarrow} \\ c_{kb\downarrow} \\ c_{kc\downarrow} \end{pmatrix}, \quad (2)$$



FIG. 1. 3D band dispersion of the q2DEL at the interface obtained by diagonalizing the noninteracting part of the Hamiltonian.

where the strength of the atomic SOC is $\Delta_{so} = 19.3$ meV. The third term of the Hamiltonian is due to the Rashba SOC, appearing because of the broken inversion symmetry at the interface, and is expressed as

$$\mathcal{H}_{\rm RSO} = \gamma \sum_{k,\sigma} (c_{ka\sigma}^{\dagger} \quad c_{kb\sigma}^{\dagger} \quad c_{kc\sigma}^{\dagger}) \times \begin{pmatrix} 0 & -2i\sin k_x & -2i\sin k_y \\ 2i\sin k_x & 0 & 0 \\ 2i\sin k_y & 0 & 0 \end{pmatrix} \begin{pmatrix} c_{ka\sigma} \\ c_{kb\sigma} \\ c_{kc\sigma} \end{pmatrix},$$
(3)

where $\gamma = 20$ meV is the strength of the Rashba SOC. The 3D dispersion of all six bands of the q2DEL at the interface in the presence of the Rashba and atomic SOCs are shown in Fig. 1. To treat the electron correlation in the q2DEL, we use a multiorbital DMFT(IPT) method in which the information of the noninteracting orbital is fed through the density of states of each individual orbital. A proper treatment of SOC within QMC-based techniques is very much a live problem. When it comes to the solver for the DMFT there is no renormalization of the bare SOC strength but we have a Weiss field in the spin-orbital basis which is $N \times N$ (where N = 6 the number of orbitals here). A proper treatment of SOC within the DMFT should however be able to self-consistently renormalize the bare SOC scale and the implementation of the same within different solvers has not been accomplished here. The merits and shortcomings of the particular IPT solver in use has already been documented [54], particularly in a multiorbital system at and away from half-filling. The results were benchmarked against the CTQMC solver. Our main focus here is the Lifshitz transition at a critical density which has to do with the reconstruction of a multiband Fermi surface. The qualitative features of this should not change, though the critical densities could change slightly with different choices of the solver.

In the noninteracting three-orbital Hamiltonian in Eq. (1), the spin and orbital degrees of freedom are entangled due to the presence of the SOCs resulting in an effective six orbital system where electron spin is no longer a good quantum number. Therefore, we describe the electron-electron interaction using a six-orbital Hubbard Hamiltonian given by

$$\mathcal{H}_{U} = \sum_{\alpha,\alpha'} U_{\alpha\alpha'} n_{\alpha} n_{\alpha'} + \sum_{\alpha,\beta} U_{\alpha\beta} n_{\alpha} n_{\beta}, \qquad (4)$$

where $U_{\alpha\alpha'}$ is the repulsive interaction energies between electrons in the pairs of nearly degenerate orbitals with orbital indices { $\alpha = 1,3,5$, $\alpha' = \alpha + 1$ } while $U_{\alpha\beta}$ is the interaction energies between electrons in the widely separated orbitals, i.e., { $\alpha = 1,2$, $\beta = 3,4$ } and { $\alpha = 3,4$, $\beta = 5,6$ }. Since the interaction between electrons in the nearly degenerate orbitals is stronger than that between electrons in the widely separated orbitals, we take $U_{\alpha\beta} = \frac{U_{\alpha\alpha'}}{5}$. For notational convenience we shall therefore use $U = U_{\alpha\alpha'}$ in the rest of the paper. The total occupation number is computed using $n = \sum_{\alpha=1}^{6} \langle c_{\alpha}^{\dagger} c_{\alpha} \rangle$. We solve the effective Hamiltonian $\mathcal{H}_{\text{eff}} = \mathcal{H} + \mathcal{H}_U$ for different values of U ranging from 0 to 0.7 eV and for different carrier concentration across the Lifshitz transition.

There are, however, few reports of the values of these correlations U and $U_{\alpha\beta}$. There is so far no indication of strong correlation in this system from experimental observations [55]. Whereas a DFT calculation [56] puts the interface electrons in the strong coupling limit $U \simeq 3.6$ eV and $U_{\alpha\beta} = U/1.3$, others report a much lower value U < 1 eV [55]. In view of such disparities, it is useful to check the results at both intermediate and strong coupling limits which we report in the foregoing. We show that the qualitative features remain quite similar in both limits, while the critical electron density for Lifshitz transition changes with changing correlations. Since the electron density is very low here, the effect of correlation

is not expected to be dramatic as in a prototypical correlated electronic system. We work in the weak to intermediate interaction regime, with maximum U value up to 0.7 eV, where the typical bandwidth here is about 2 eV. As mentioned above, we also compare the results in the prescribed strong coupling limit of the DFT calculation [56].

III. RESULTS

A. Correlated Fermi surface

The Lifshitz transition refers to the change in topology of the Fermi surface (e.g., formation or disappearance of a pocket or an arc) by tuning of some parameter [51] which, in the present case, is the chemical potential or the carrier density. In the experimental setup, usually the gate voltage is varied to tune carrier density. From our data, it is quite easy to invert the carrier densities to the corresponding gate voltages [48]. The noninteracting band structure and the Fermi surfaces at three different carrier densities are shown in Figs. 2(a)-2(d). At low carrier densities the two lower orbitals are occupied resulting in a pair of elliptical Fermi surfaces. As the chemical potential is tuned up, additional electronlike pockets appear at a critical value $\mu_c = -1.067$ eV (corresponding carrier density $n_c = 0.1809$ el./u.c.), where the third and fourth orbitals start getting occupied. The orbitals first and second, third and fourth, fifth and sixth are pairwise nearly degenerate at the Γ point and there exists another critical density at which the fifth and sixth orbitals will appear at the Fermi level and additional pockets will form. The difference between these two critical densities is



FIG. 2. (a) The resultant band structure of the q2DEL along \bar{X} - Γ -X (in units of π) direction at the interface showing the t_{2g} orbitals in presence of the Rashba and atomic SOCs. (d), (c), and (b) The noninteracting (U = 0) Fermi surfaces below (n = 0.0945 el./u.c.), near (n = 0.1809 el./u.c.), and above (n = 0.8030 el./u.c.) the Lifshitz transition point ($\mu_c = -1.067$ eV) at which the third and fourth bands begin to get occupied. The dashed horizontal lines in (a), at the corresponding three chosen chemical potentials $\mu = -1.20$ eV, $\mu = -1.05$ eV, and $\mu = -0.90$ eV, respectively, are guide to the eyes. (e)–(p) Interacting Fermi surfaces at 60 K at the interface. Columns (e) to (g), (h) to (j), (k) to (m), and (n) to (p) show the evolution of the Fermi surface topology due to electron-electron interaction of strengths U = 0.3 eV, U = 0.5eV, U = 0.7 eV, and U = 3.0 eV, respectively, for suitable chemical potentials above, close, and below the corresponding n_c in the same color scheme for the six (renormalized) bands.

quite small in the present case to distinguish the first Lifshitz transition from the second. However, if such an interface is available where the atomic SOC is large this difference would be considerable and clearly delineable [57].

To get an impression of the effect of electron-electron interaction on the Fermi surface and hence on the Lifshitz transition, we calculate the correlated Fermi surfaces and compare with the noninteracting case. In the presence of electron correlations, the renormalized dispersion $E_{k\alpha}$ for orbital α is given by

$$E_{k\alpha} = E_{k\alpha}^0 - \mu + \operatorname{Re}\Sigma_{\alpha}(\mathbf{k}, E_{k\alpha}),$$

where $E_{k\alpha}^0$ is the noninteracting dispersion, obtained by diagonalizing the Hamiltonian (1) at each momentum point **k**, and $\Sigma_{\alpha}(\mathbf{k}, E_{k\alpha})$ is the self-energy. Figures 2(e)–2(p) show the correlated Fermi surfaces for various interaction strengths and carrier densities across the Lifshitz transition. With increasing U, the spectral weight near the Γ point is transferred towards lower energy and the nearly degenerate pairs of orbitals tend to split up. As shown in Fig. 2(1), at larger correlation strength, U = 0.7 eV, the fifth and sixth orbitals also appear as additional electronlike pockets in the Fermi surface, indicating the second Lifshitz transition driven by electron correlations. Similar progression of Fermi surface topology happens when the chemical potential is suitably tuned in the strong correlation limit [U = 3 eV, Figs. 2(n)-2(p)]. This essentially means that the critical densities for the transitions are reduced when interaction increases. If we look away from the critical point, we see that while there is no noticeable change due to increasing interaction in Figs. 2(g), 2(j), 2(m), and 2(p) for the lower two orbitals, Figs. 2(e), 2(h), 2(k), and 2(n) for the upper four orbitals show prominent changes.

B. Transport properties

To study the influence of the Lifshitz transition on the transport, various transport quantities are calculated. The transport coefficients that govern the electrical and thermal responses of the system are given in terms of current-current correlation functions which reduce to averages over the spectral density $\rho(\epsilon, \omega)$ in DMFT. The expressions for optical conductivity $[\sigma(\omega)]$, Seebeck coefficient (*S*), and thermal conductivity (*K*) are [58]

$$\sigma = \frac{e^2}{T}A_0, \quad S = \frac{-k_B}{e}\frac{A_1}{A_0}, \quad K = k_B^2 \left(A_2 - \frac{A_1^2}{A_0}\right),$$

where

$$A_n = \frac{\pi}{\hbar V} \sum_{k,\sigma} \int d\omega \rho_\sigma(k,\omega)^2 \left(\frac{\partial \epsilon_k}{\partial k_x}\right)^2 \left(-T \frac{\partial f(\omega)}{\partial \omega}\right) (\beta \omega)^n.$$

Here V is the volume and $f(\omega)$ is Fermi-Dirac distribution function. Figures 3(a) and 3(b) show the optical conductivity $\sigma(\omega)$ for different values of the electron-electron interaction strength U and the carrier concentration n, respectively, below and above the critical concentration n_c . At $n < n_c$, $\sigma(\omega)$ follows a hyperbolic dependence with energy ω showing insignificant effects of the interaction. On the other hand, at $n > n_c$, $\sigma(\omega)$ reveals, at lower U, a shoulderlike feature which transforms into a peak near $\omega_c \simeq 1.0$ eV with increasing U.



FIG. 3. The optical conductivity as a function of energy at 60 K for several values of interaction strength U with carrier concentration (a) n below Lifshitz transition (inset, for U = 3 eV) and (b) above Lifshitz transition [right inset, U = 3 eV; the corresponding DOS (in arb. units) in the left inset]. The (c) dc conductivity and (d) thermal conductivity as a function of the carrier concentration with U (in eV) same as in (a) and (b), showing the rapid rise beyond critical carrier concentration, marked by dashed line, n_c (U = 0).

Since the effective noninteracting bandwidth for the system is about 2 eV, a Hubbard correlation strength of 3 eV transfers the spectral weight to higher energies and an upper Hubbard band starts forming, as shown in the left inset of Fig. 3(b). The signature of the same appears in the optical conductivity where a strong subpeak at energies \sim 1.8–2.2 eV forms [right inset of Fig. 3(b)], suppressing the secondary small peak structures observed for the lower U values. The Drude peak gets suppressed significantly as well, consistent with the increment in resistivity (decrease in dc conductivity) at U = 3.0 eV. The increasing peak height of $\sigma(\omega_c)$ with increasing U indicates transfer of spectral weight toward higher energies. A closer look into $\sigma(\omega)$ reveals a two satellite structure of optical conductivity with satellites around 0.5 and 1.0 eV, respectively. This is again consistent with the features of correlated spectral weight transfer in the net density of states (DOS) for the system as shown in Fig. 4. The edge singularities of the



FIG. 4. Total density of states as a function of energy at 60 K for several values of U with carrier concentration (a) n = 0.0945 el./u.c. (below the Lifshitz transition) and (b) n = 1.4030 el./u.c. (above Lifshitz transition). The curves from U = 0.1 eV to U = 0.7 eV are progressively offset vertically by 0.4 for clarity of viewing, i.e., U = 0.1 eV is shifted up by 0.4 and U = 0.7 eV by 0.24.



FIG. 5. (a) The Seebeck coefficient *S* as a function of the electron concentration *n* at a temperature T = 60 K for various strengths *U* (in eV unit) of the electron-electron interaction showing the cusp at the critical carrier concentration n_c (inset, U = 3 eV). Variation of *S* with respect to temperature *T* below critical carrier concentration (red) and above critical carrier concentration (blue) for (b) U = 0.3 eV and (c) U = 0.7 eV, respectively (inset, U = 3 eV). The inset in (b) shows *S* with temperature across the critical carrier density.

DOS arise from the nearly nondispersive segments of the band structure. When correlation is cranked up, finite spectral weight transfers from the edge singularities lead to satellite features at $\omega \sim 0.5$ and 1.0 eV, respectively. As described in Figs. 3(c) and 3(d), the dc conductivity $[\sigma_{dc} = \sigma(\omega = 0)]$ and the thermal conductivity K rise rapidly to higher values with increasing carrier concentration n. This sharp change arises because a large number of accessible states appear at the Fermi level from the newly occupied orbitals and due to the nearly flat nature of the two lower orbitals above n_c . Evidently, at higher n, both the conductivities reduce with increasing U as a consequence of the piling up of the spectral weight at ω_c as discussed before in Fig. 3(b). The strong-coupling limit (inset, Fig. 3) is quite featureless, a considerable spectral weight is now transferred to the high energy region with a peak corresponding to the strong interaction. The thermopower or the Seebeck coefficient S, as depicted in Fig. 5(a), reveals a cusp at the critical carrier concentration n_c for the Lifshitz transition. With the enhancement in U, the cusp shifts largely towards lower *n* values, referred to above from the plots of the correlated Fermi surfaces; the depth of the cusp also increases. Figures 5(b) and 5(c) show the variation of S with respect to temperature T at carrier densities above and below the critical carrier density for U = 0.3 eV and U = 0.7 eV, respectively. The same variation is also observed for strong coupling case (inset, Fig. 5). The Seebeck coefficient varies almost linearly with temperature at $n > n_c$ However, at $n < n_c$, S decreases with temperature below 100 K and then becomes nearly flat. With increasing U, S can increase or decrease depending on the exact value of n as noticed in Fig. 5(a). Very similar temperature dependence of the Seebeck coefficient has been reported in the experiment [59].

As mentioned earlier, the Lifshitz transition here is induced by density (or chemical potential), not temperature. The Lifshitz transition does not connect two different thermodynamic phases on either side in the present case; it is purely topological in nature with no visible qualitative change across it, adding to the difficulties of its experimental determination. As shown below, it is possible to plot Seebeck coefficient with temperature while straddling the carrier density across the critical value. This would give a critical temperature for the Lifshitz transition. However, unlike in the cases where the Lifshitz transition is tuned by temperature, the critical temperature will depend on the gate voltage in use. The plot shown in the inset of Fig. 5(b) shows Seebeck coefficient for a range of the carrier densities from just below to above the critical carrier density as temperature varies from 12 to 760 K. A critical temperature of 244 K can be gleaned from this figure (for a chemical potential -1.10 eV at 8 K). This again underlines the need for a good diagnostic tool for locating the Lifshitz transition in the oxide interfaces.

C. Theoretical ARPES

To get more insight into the spectral weight transfer occurring in the presence of finite electron correlations, we study the ARPES intensity spectrum. The spectral intensity can be expressed as [60], where $\Sigma(\omega)$ is the momentum-independent self-energy from DMFT,

$$I(\mathbf{k},\omega) \propto \frac{\mathrm{Im}\Sigma(\omega)f(\omega)}{[\omega - \epsilon_k - \mathrm{Re}\Sigma(\omega)]^2 + [\mathrm{Im}\Sigma(\omega)]^2},$$

where $f(\omega)$ is the Fermi-Dirac distribution function. Figures 6(a)-6(c) show and compare the ARPES spectra at finite interaction strength U with that of the noninteracting case. The ARPES has the highest intensity and spectral weight around the high symmetry Γ point at the noninteracting level. In case of orbitals with predominantly d_{xz} and d_{yz} characters, the intense segments in the ARPES are due to the nearly nondispersive sections of the orbitals with heavy mass. At the noninteracting level, this heavy mass is a direct consequence of finite atomic spin-orbit coupling. With correlation the weight transfers over a finite energy window. For the d_{xy} orbital the spectral weight gets transferred over an energy range of ~ 0.15 and $\sim 0.3 \text{ eV}$ for U = 0.3 and 0.5 eV, respectively, around the Γ point. Around the same point for d_{xz} and d_{yz} orbitals the spectral weights get transferred over an energy scale of ~ 0.2 and ~ 0.4 eV for U = 0.3 and 0.5 eV, respectively. As the spectral weight transfers with finite correlation, the ARPES intensity profile around the Γ point becomes significantly weaker; for some orbitals intensity drops by a factor of 10 with $U = \frac{W}{4}$ (where W is the effective bandwidth of the dispersive bands). The spectral weight at the region near the Γ point is transferred towards lower energies while that at the regions away from the Γ point is transferred towards higher energies, thereby increasing the bandwidth of each orbital. Higher the U, the larger is the spectral weight transfer. The plots in Figs. 6(d)-6(1) describe the ARPES intensity along highsymmetry directions in the Brillouin zone. The interorbital finite interaction term at the local site within DMFT, pulls the bands of predominantly d_{xy} and $d_{xz,yz}$ characters towards each other (pulling the d_{xy} bands toward smaller energies and



FIG. 6. The ARPES intensity spectra along \bar{X} - Γ -X direction (in units of π) for (a) U = 0, (b) U = 0.3 eV, and (c) U = 0.5 eV, respectively at a carrier concentration n = 1.4030 el./u.c. and at a fixed temperature T = 60 K. (d)–(l) The momentum-resolved ARPES intensity along Γ -X, X-M, and M- Γ directions in the Brillouin zone (rows) and for U = 0, U = 0.3 eV, and (c) U = 0.5 eV (columns) at a fixed temperature T = 60 K.

driving the $d_{xz,yz}$ bands toward higher energies) allowing them to overlap and admix substantially.

D. Influence of magnetic field

Having explored the basic features of the Lifshitz transition and the role of the electron correlations in it, we study the effects with an external magnetic field. Figures 7(a)-7(c)show the band structure with an exchange field applied along the x direction in the absence of any electron correlations. With a finite field, the degeneracy is lifted at all momenta, except at the Γ point, creating a gap. However, the exchange split orbitals undergo band inversion at all the band crossing points due to the presence of the SOCs. Figures 7(d)-7(f)describe the corresponding Seebeck coefficients as a function of the carrier concentration. In addition to the cusp in the zero-field case, other cusps appear at larger fields indicating multiple Lifshitz transitions. The appearance of the multiple Lifshitz transition can be reconciled from the band structures directly. With the tuning of the Fermi level up from the two lower orbitals, additional electronlike pockets appear at all the carrier concentrations for which the Fermi level encounters additional orbital contribution at the Γ point. The degeneracy at the Γ point is maintained even at higher fields. For multiple transitions, the Seebeck coefficient at the higher (at larger *n*) cusps are larger in magnitude. For a quantitative description, the variation of the critical carrier densities for these Lifshitz transitions, given by the locations of the cusps in the Seebeck coefficient, with respect to the field strength h_x , is shown in Fig. 8. There are two clear regimes of field strength: the low



FIG. 7. The noninteracting band structure \bar{X} - Γ -X direction (in units of π) with in-plane magnetic field of strength (a) $h_x = 0$, (b) $h_x = 0.2$ eV, and (c) $h_x = 0.4$ eV. (d)–(f) The corresponding plots of the Seebeck coefficients as a function of the carrier concentration at temperature T = 60 K.



FIG. 8. The critical density for the first (n_{c1}) , second (n_{c2}) , and third (n_{c3}) Lifshitz transitions as a function of the strength h_x of the in-plane magnetic field. Left *y*-axis label is for n_{c1} and right *y*-axis label is for n_{c2} and n_{c3} . The numbers in both the *y* axes are in the unit of el./u.c.

field regime ($h_x < 0.2$ eV) has only one Lifshitz transition, whereas multiple transitions appear in higher fields ($h_x \ge 0.2$ eV). The critical density n_{c1} for the first transition decreases with increasing h_x , as observed in the experiment [52], and then becomes nearly constant with further increase in h_x in the second field regime. On the other hand, the second and third critical concentrations n_{c2} and n_{c3} , respectively, increase with increasing h_x . With the limited resolution, the data suggest that n_{c2} and n_{c3} originally coincide with n_{c1} at lower fields and get separated with increasing h_x due to the removed degeneracy at the Γ point. The third Lifshitz transition occurs at lower fields than the second transition, as evident from Fig. 7. The decrease/increase in the critical density/densities in the low/high field regime is a manifestation of the fact that the Zeeman field splits and pushes the bands away from each other. We also study the case with field applied perpendicular to the interface, and find similar qualitative features of the multiple Lifshitz transitions.

IV. DISCUSSION AND SUMMARY

An experimentally testable scenario involving the Lifshitz transition in the LAO/STO interface has been worked out. The transport properties of the q2DEL provide important signatures of the Lifshitz transition. The cusp in the Seebeck coefficient is a robust response of the change in the Fermi surface topology and can be used to examine Lifshitz transition in metallic systems. The electron-electron interaction may result in a Pomeranchuk instability in similar multiorbital materials. External magnetic field can lead to multiple Lifshitz transitions which shows up as multiple cusps in the Seebeck coefficient. However, detecting the multiple transitions in the experiment will require scanning over large exchange energies. Also, the carrier density in the LAO/STO heterointerface is small compared to other metallic interfaces and, therefore, difficult to tune to large values using the external gate voltage. Nevertheless, the phenomena of multiple Lifshitz transitions is possible in other similar multiorbital metallic systems and requires intensive effort to realize in the experiment.

To summarize, we have studied the Lifshitz transition in the LAO/STO interface and its influence on the transport properties using multiorbital DMFT, formulated within realistic bands at the interface. Though it is still not established if the q2DEL belongs in the intermediate or strong correlation class, the effects of correlation are visible in the dynamical spectral features of the electron density even in the intermediate regime. In particular, the location of the Lifshitz transition and therefore the transport bear signatures of it. The Lifshitz transition occurs when carriers from the d_{yz} and d_{zx} orbitals populate the Fermi level and additional electronlike pockets appear at the Fermi surface. The change in the Fermi surface topology appears as a sharp rise in the dc and thermal conductivities and as a cusp in the Seebeck coefficient. The repulsive electron-electron interaction transfers some of the spectral weights towards lower energies and effectively reduces the critical carrier concentration for the transition. The pronounced cusp features in the Seebeck coefficient can be a very handy tool for the identification of the Lifshitz transition, otherwise located by tracking the carrier concentration, not always very reliable in the oxide interfaces. In the presence of external magnetic field, the critical carrier concentration further reduces with increasing field strength and multiple transitions appear at sufficiently large fields.

ACKNOWLEDGMENTS

The authors thank Siddhartha Lal for discussions and acknowledge the use of the computing facility from DST-Fund for Improvement of S & T infrastructure (phase-II) Project installed in the Department of Physics, IIT Kharagpur, India. S.N. acknowledges MHRD, India for support. N.M. was supported by the Deutsche Forschungsgemeinschaft through TRR 80. S.A. acknowledges UGC, India for a research fellowship.

- [1] A. Ohtomo and H. Y. Hwang, Nature (London) 427, 423 (2004).
- [2] S. Thiel, G. Hammerl, A. Schmehl, C. W. Schneider, and J. Mannhart, Science 313, 1942 (2006).
- [3] M. Huijben, G. Rijnders, D. H. A. Blank, S. Bals, S. V. Aert, J. Verbeeck, G. V. Tendeloo, A. Brinkman, and H. Hilgenkamp, Nat. Mater. 5, 556 (2006).
- [4] N. Reyren, S. Thiel, A. D. Caviglia, L. F. Kourkoutis, G. Hammerl, C. Richter, C. W. Schneider, T. Kopp, A.-S. Retschi,

D. Jaccard, M. Gabay, D. A. Muller, J.-M. Triscone, and J. Mannhart, Science **317**, 1196 (2007).

- [5] S. Gariglio, N. Reyren, A. D. Caviglia, and J.-M. Triscone, J. Phys.: Condens. Matter 21, 164213 (2009).
- [6] C. Richter, H. Boschker, W. Dietsche, E. Fillis-Tsirakis, R. Jany, F. Loder, L. F. Kourkoutis, D. A. Muller, J. R. Kirtley, C. W. Schneider, and J. Mannhart, Nature (London) 502, 528 (2013).

- [7] S. N. Klimin, J. Tempere, J. T. Devreese, and D. van der Marel, Phys. Rev. B 89, 184514 (2014).
- [8] L. Li, C. Richter, J. Mannhart, and R. C. Ashoori, Nat. Phys. 7, 762 (2011).
- [9] D. A. Dikin, M. Mehta, C. W. Bark, C. M. Folkman, C. B. Eom, and V. Chandrasekhar, Phys. Rev. Lett. **107**, 056802 (2011).
- [10] A. Ron, E. Maniv, D. Graf, J.-H. Park, and Y. Dagan, Phys. Rev. Lett. 113, 216801 (2014).
- [11] V. T. Tra, J.-W. Chen, P.-C. Huang, B.-C. Huang, Y. Cao, C.-H. Yeh, H.-J. Liu, E. A. Eliseev, A. N. Morozovska, J.-Y. Lin, Y.-C. Chen, M.-W. Chu, P.-W. Chiu, Y.-P. Chiu, L.-Q. Chen, C.-L. Wu, and Y.-H. Chu, Adv. Mater. 25, 3357 (2013).
- [12] M. H. Fischer, S. Raghu, and E.-A. Kim, New J. Phys. 15, 023022 (2013).
- [13] A. Fête, S. Gariglio, A. D. Caviglia, J.-M. Triscone, and M. Gabay, Phys. Rev. B 86, 201105 (2012).
- [14] A. D. Caviglia, S. Gariglio, N. Reyren, D. Jaccard, T. Schneider, M. Gabay, S. Thiel, G. Hammerl, J. Mannhart, and J.-M. Triscone, Nature (London) 456, 624 (2008).
- [15] A. D. Caviglia, M. Gabay, S. Gariglio, N. Reyren, C. Cancellieri, and J.-M. Triscone, Phys. Rev. Lett. 104, 126803 (2010).
- [16] C. Cen, S. Thiel, G. Hammerl, C. W. Schneider, K. E. Andersen, C. S. Hellberg, J. Mannhart, and J. Levy, Nat. Mater. 7, 298 (2008).
- [17] J. T. Haraldsen, P. Wölfle, and A. V. Balatsky, Phys. Rev. B 85, 134501 (2012).
- [18] D. Bucheli, M. Grilli, F. Peronaci, G. Seibold, and S. Caprara, Phys. Rev. B 89, 195448 (2014).
- [19] N. Nakagawa, H. Y. Hwang, and D. A. Muller, Nat. Mater. 5, 204 (2006).
- [20] E. Dagotto, Science 318, 1076 (2007).
- [21] G. Rijnders and D. H. A. Blank, Nat. Mater. 7, 270 (2008).
- [22] Z. S. Popović, S. Satpathy, and R. M. Martin, Phys. Rev. Lett. 101, 256801 (2008).
- [23] Z. Q. Liu, C. J. Li, W. M. Lü, X. H. Huang, Z. Huang, S. W. Zeng, X. P. Qiu, L. S. Huang, A. Annadi, J. S. Chen, J. M. D. Coey, T. Venkatesan, and Ariando, Phys. Rev. X 3, 021010 (2013).
- [24] Y. Li, S. N. Phattalung, S. Limpijumnong, J. Kim, and J. Yu, Phys. Rev. B 84, 245307 (2011).
- [25] Z. Zhong, P. X. Xu, and P. J. Kelly, Phys. Rev. B 82, 165127 (2010).
- [26] H. Boschker, C. Richter, E. Fillis-Tsirakis, C. W. Schneider, and J. Mannhart, Sci. Rep. 5, 12309 (2015).
- [27] K. Michaeli, A. C. Potter, and P. A. Lee, Phys. Rev. Lett. 108, 117003 (2012).
- [28] S. Banerjee, O. Erten, and M. Randeria, Nat. Phys. 9, 626 (2013).
- [29] N. Ganguli and P. J. Kelly, Phys. Rev. Lett. 113, 127201 (2014).
- [30] N. Pavlenko, Phys. Rev. B 80, 075105 (2009).
- [31] M. Stengel and D. Vanderbilt, Phys. Rev. B 80, 241103 (2009).
- [32] J. Park, B.-G. Cho, K. D. Kim, J. Koo, H. Jang, K.-T. Ko, J.-H. Park, K.-B. Lee, J.-Y. Kim, D. R. Lee, C. A. Burns, S. S. A. Seo, and H. N. Lee, Phys. Rev. Lett. **110**, 017401 (2013).
- [33] N. Pavlenko, T. Kopp, and J. Mannhart, Phys. Rev. B 88, 201104 (2013).
- [34] P. Moetakef, J. R. Williams, D. G. Ouellette, A. P. Kajdos, D. Goldhaber-Gordon, S. J. Allen, and S. Stemmer, Phys. Rev. X 2, 021014 (2012).

- PHYSICAL REVIEW B **94**, 155103 (2016)
- [35] J.-S. Lee, Y. W. Xie, H. K. Sato, C. Bell, Y. Hikita, H. Y. Hwang, and C.-C. Kao, Nat. Mater. 12, 703 (2013).
- [36] J. A. Bert, B. Kalisky, C. Bell, M. Kim, Y. Hikita, H. Y. Hwang, and K. A. Moler, Nat. Phys. 7, 767 (2011).
- [37] L. Fidkowski, H.-C. Jiang, R. M. Lutchyn, and C. Nayak, Phys. Rev. B 87, 014436 (2013).
- [38] N. Pavlenko, T. Kopp, E. Y. Tsymbal, G. A. Sawatzky, and J. Mannhart, Phys. Rev. B 85, 020407 (2012).
- [39] N. Mohanta and A. Taraphder, J. Phys.: Condens. Matter 26, 025705 (2014).
- [40] N. Mohanta and A. Taraphder, J. Phys.: Condens. Matter 26, 215703 (2014).
- [41] Ariando, X. Wang, G. Baskaran, Z. Q. Liu, J. Huijben, J. B. Yi, A. Annadi, A. R. Barman, A. Rusydi, S. Dhar, Y. P. Feng, J. Ding, H. Hilgenkamp, and T. Venkatesan, Nat. Commun. 2, 188 (2011).
- [42] S. Kumar, G. Nath Daptary, P. Kumar, A. Dogra, N. Mohanta, A. Taraphder, R. C. Budhani, and A. Bid, arXiv:1411.3103.
- [43] N. Mohanta and A. Taraphder, Europhys. Lett. 108, 60001 (2014).
- [44] M. S. Scheurer and J. Schmalian, Nat. Commun. 6, 6005 (2015).
- [45] M. Ben Shalom, M. Sachs, D. Rakhmilevitch, A. Palevski, and Y. Dagan, Phys. Rev. Lett. 104, 126802 (2010).
- [46] Z. Zhong, A. Tóth, and K. Held, Phys. Rev. B 87, 161102 (2013).
- [47] G. Khalsa, B. Lee, and A. H. MacDonald, Phys. Rev. B 88, 041302 (2013).
- [48] N. Mohanta and A. Taraphder, Phys. Rev. B 92, 174531 (2015).
- [49] Y. Nakamura and Y. Yanase, J. Phys. Soc. Jpn. 82, 083705 (2013).
- [50] S. Caprara, J. Biscaras, N. Bergeal, D. Bucheli, S. Hurand, C. Feuillet-Palma, A. Rastogi, R. C. Budhani, J. Lesueur, and M. Grilli, Phys. Rev. B 88, 020504 (2013).
- [51] Y. Yamaji, T. Misawa, and M. Imada, J. Phys. Soc. Jpn. 75, 094719 (2006).
- [52] A. Joshua, J. Ruhman, S. Pecker, E. Altman, and S. Ilani, Proc. Natl. Acad. Sci. USA 110, 9633 (2013).
- [53] A. Joshua, S. Pecker, J. Ruhman, E. Altman, and S. Ilani, Nat. Commun. 3, 1129 (2012).
- [54] N. Dasari, W. Raja Mondal, P. Zhang, J. Moreno, M. Jarrell, and N. S. Vidhyadhiraja, arXiv:1504.04097.
- [55] C. Cancellieri, A. S. Mishchenko, U. Aschauer, A. Filippetti, C. Faber, O. S. Barisic, V. A. Rogalev, T. Schmitt, N. Nagaosa, and V. N. Strocov, Nat. Commun. 7, 10386 (2016).
- [56] M. Hirayama, T. Miyake, and M. Imada, J. Phys. Soc. Jpn. 81, 084708 (2012).
- [57] For example, in BaOsO₃/BaTiO₃, an atomic SOC ~440 meV leads to a gap of 570.4 meV, while the 19.3 meV SOC in the present case produces a 19 meV gap.
- [58] G. Pálsson and G. Kotliar, Phys. Rev. Lett. 80, 4775 (1998).
- [59] I. Pallecchi, M. Codda, E. Galleani d'Agliano, D. Marré, A. D. Caviglia, N. Reyren, S. Gariglio, and J.-M. Triscone, Phys. Rev. B 81, 085414 (2010).
- [60] T. Valla, A. V. Fedorov, P. D. Johnson, J. Xue, K. E. Smith, and F. J. DiSalvo, Phys. Rev. Lett. 85, 4759 (2000).