# **Distinctive orbital anisotropy observed in the nematic state of a FeSe thin film**

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The nematic state, where a system is translationally invariant but breaks rotational symmetry, has drawn great attention recently due to the experimental observations of such a state in both cuprates and iron-based superconductors. The origin of nematicity and its possible tie to the pairing mechanism of high- $T_c$ , however, still remain controversial. Here, we study the electronic structure of a multilayer FeSe film using angle-resolved photoemission spectroscopy. The band reconstruction in the nematic state is clearly delineated. We find that the energy splitting between *dxz* and *dyz* bands shows a nonmonotonic distribution in momentum space. From the Brillouin zone center to the Brillouin zone corner, the magnitude of splitting first decreases, then increases, and finally reaches the maximum value of ∼70 meV. Moreover, besides the *dxz* and *dyz* bands, band splitting was also observed on the *dxy* bands with a comparable energy scale around 45 meV. Our results suggest that the electronic anisotropy in the nematic state cannot be explained by a simple on-site ferro-orbital order. Instead, strong anisotropy exists in the hopping of all  $d_{xz}$ ,  $d_{yz}$ , and  $d_{xy}$  orbitals, the origin of which holds the key to a microscopic understanding of the nematicity in iron-based superconductors.

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### **I. INTRODUCTION**

High- $T_c$  superconductivity often occurs in proximity to symmetry-breaking states, whose origins are intimately related to the pairing mechanism of superconductivity. Among all these symmetry-breaking states, the nematic state, in which electrons break the rotational symmetry without breaking the translational symmetry, has recently drawn great attention  $[1,2]$ . It was observed in proximity to high- $T_c$  superconductivity in both cuprates and iron-based superconductors [\[3–9\]](#page-6-0), and the quantum fluctuation near a nematic quantum critical point was proposed to be critical for high- $T_c$  supercon-ductivity [\[10,11\]](#page-6-0).

In iron-based superconductors, the nematic state develops simultaneously with a structural transition from tetragonal to orthorhombic structure [\[2\]](#page-6-0). A magnetic transition into a collinear antiferromagnetic (CAF) order follows simultaneously or at a lower temperature [\[12\]](#page-6-0). In order to explain the nematic state, most theories emphasize the importance of orbital/spin fluctuations or their strong coupling, in connection with the multiorbital and correlated nature of iron-based superconductors [\[13](#page-6-0)[–19\]](#page-7-0). The key debates among these theories lie in which fluctuation dominates at high temperature and what relationship the nematic and magnetic states have. Under the spin-nematic scenario [\[18,](#page-6-0)[19\]](#page-7-0), both the nematic and magnetic states share the same origin, namely, the spin fluctuation. It has been proposed that the spin fluctuation could break the *C*4 rotational symmetry spontaneously by peaking either at  $(0, \pi)$  or  $(\pi, 0)$ , resulting in a spin-nematic state. Such a state occurs prior to the magnetic ordered state and is responsible for the structural transition through magnetic-elastic coupling. On the other hand, in the orbital-ordering scenario, the nematic and magnetic states are considered to be separate [\[13–15\]](#page-6-0). The orbital fluctuation dominates at high temperature and breaks the *C*4 rotational symmetry by triggering a  $d_{xz}/d_{yz}$ ferro-orbital ordering. Subsequently, at a lower temperature, the orbital ordering further enhances the spin fluctuation and its anisotropy, which results in a magnetic transition under sufficiently strong coupling between the spin and orbital/lattice degrees of freedom.

The origin of nematicity is crucial for understanding the nature of competing phases in high- $T_c$  superconductors and needs to be examined experimentally. However, clear experimental delineation of the nematic state has always been challenging. In most iron pnictide compounds, the nematic and magnetic states are strongly intertwined with each other, preventing us from probing the intrinsic properties of the nematic state. FeSe is an ideal system. Bulk FeSe shows a structural transition at ∼90 K, where the lattice breaks the *C*4 rotational symmetry. However, no long-range magnetic order has been observed down to the lowest experimental temperature [\[20–22\]](#page-7-0). Its electronic structure has been studied by several angle-resolved photoemission spectroscopy (ARPES) groups [\[23–27\]](#page-7-0). The energy splitting between the  $d_{xz}$  and  $d_{yz}$  bands has been observed in the nematic state, and the importance of  $d_{xz}$  and  $d_{yz}$ orbital ordering has been discussed. In this paper, we present

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<span id="page-1-0"></span>our ARPES studies on the 35-monolayer (35-ML) FeSe film grown on SrTiO<sub>3</sub>. The nematic transition temperature  $T_{\text{nem}}$  is around 125 K, and the band reconstruction in the nematic state is clearly delineated. We find that the energy splitting between the  $d_{xz}$  and  $d_{yz}$  bands shows nontrivial momentum dependence. Specifically, from the Brillouin zone (BZ) center  $\Gamma$  to the BZ corner *M*, the energy splitting of bands first decreases, then increases, and finally achieves the maximum value of ∼70 meV at *M*. Moreover, three electron bands were clearly resolved near  $M$ , demonstrating that the  $d_{xy}$  bands are also reconstructed in the nematic state with an energy scale around 45 meV. Our results have strong implications for theories aiming to understand the nature of the nematic state. The momentum dependence of the  $d_{xz}$  and  $d_{yz}$  energy splitting and the reconstruction of  $d_{xy}$  exclude the simple on-site ferro-orbital ordering as a driving force of nematicity. Instead, the hopping anisotropy of all the  $d_{xz}$ ,  $d_{yz}$ , and  $d_{xy}$ orbitals should play a more important role.

## **II. EXPERIMENT**

FeSe films were grown on high-quality Nb-doped (0*.*05% wt) SrTiO<sub>3</sub> (100) substrates. A TiO<sub>2</sub>-terminated atomic flat surface was prepared by degassing at 450◦ C for several hours and subsequently annealing at 900° C for 20 min. The growth was carried out under Se-rich conditions with a Se/Fe flux ratio of 3–4. Substrate temperatures were kept at 380◦ C during the growth. The films were subsequently annealed at 450◦ C for 4 h immediately after growth. ARPES measurements were performed at beamline 5-4 of the Stanford

Synchrotron Radiation Lightsource (SSRL) and beamline 10.0.1 of the Advanced Light Source (ALS). All data were taken with Scienta R4000 electron analyzers. The overall energy resolution was 5–10 meV, depending on the photon energy, and the angular resolution was 0*.*3◦. For the ARPES measurements at SSRL, the films were transferred from the growth chamber to the ARPES chamber via a vacuum suitcase with a pressure better than  $1 \times 10^{-9}$  Torr. For the ARPES measurements at ALS, each film was capped with a Se layer 25 nm thick to protect the thin film during sample transfer. The film was then heated up to  $400^\circ$ C to decap the Se capping layer in the ARPES chamber. All the samples were measured in ultrahigh vacuum with a base pressure better than  $3 \times 10^{-11}$  Torr.

#### **III. RESULTS**

The CAF order of iron-based superconductors breaks the translational symmetry [\[12\]](#page-6-0). As a result, the unit cell rotates 45◦ and doubles in size. The electronic manifestation for such a translational symmetry breaking is the band folding in momentum space. We take NaFeAs as an example; the structural transition temperature  $T_s$  and magnetic transition temperature  $T_N$  of NaFeAs are around 56 and 46 K, respectively [\[28\]](#page-7-0). As shown in Fig.  $1(a)$ , the Fermi surface of NaFeAs at 70 K consists of hole pockets around  $\Gamma$  and electron pockets around  $M$  [\[29,30\]](#page-7-0). In a CAF ordered state, the bands around  $\Gamma$  and  $M$ fold onto each other [Fig.  $1(b)$ ], and the Fermi surface sheets are reconstructed so that they are symmetric with respect to the magnetic BZ boundary [Fig.  $1(a)$ ]. We note that, without



FIG. 1. Absence of magnetic order in the FeSe thin film. (a) The Fermi surface mapping taken at 70 and 20 K in NaFeAs. The Brillouin zone (BZ) boundary in the magnetic state is shown by the green solid line. The structural transition temperature and magnetic transition temperature are abbreviated as  $T_s$  and  $T_N$ , respectively. (b) The second derivative photoemission intensity distribution taken along the  $\Gamma$ -*M* direction. The main (solid line) and folded (dashed line) bands are illustrated in the top panels. (c) and (d) The corresponding data taken on a 35-ML FeSe film at 160 and 20 K, respectively. The data were taken with 38 eV photons with  $k_z$  near the  $\Gamma$  point. The nematic transition temperature is abbreviated as  $T_{\text{nem}}$ .

<span id="page-2-0"></span>translational symmetry breaking, the size of the unit cell remains the same and the bands do not fold. Therefore, the band folding observed here is spectroscopic evidence of long-range magnetic order in NaFeAs, indicting translational symmetry breaking.

For the 35-ML FeSe film, such band-folding behavior is clearly absent. Figure  $1(c)$  shows the Fermi surface mappings taken on the 35-ML FeSe film. The Fermi surface at 160 K consists of small hole and electron pockets, which is similar to that of NaFeAs. At 20 K, the Fermi surface of the FeSe thin film is only reconstructed around the *M* point and forms four intense propellerlike pockets. The strong discrepancy of the Fermi surface between  $\Gamma$  and  $M$  indicates the absence of band-folding behavior. Figure  $1(d)$  shows the measured dispersion taken along the  $\Gamma$ -*M* direction. None of the bands observed at 20 K could be attributed to band folding. Further evidence comes from the absence of a spin-density wave (SDW) gap. In contrast to NaFeAs, where the band dispersions break into segments in the SDW state due to the SDW gap opening [Fig.  $1(b)$ ], the bands disperse continuously in FeSe, and no SDW gap is observed [Fig.  $1(d)$ ]. All these results unambiguously demonstrate the absence of magnetic order in the 35-ML FeSe film, which is also consistent with the data taken from the FeSe single crystal showing no static magnetic order down to the lowest temperature [\[20–27\]](#page-7-0). Note that no surface reconstruction has been observed in the FeSe thin film and the bands show moderate  $k_z$  dispersion in ARPES studies [\[31,32\]](#page-7-0). Therefore, the ARPES spectra reflect the intrinsic properties of the FeSe thin film.

The sample in the nematic state consists of two perpendicular domains due to the breaking of *C*4 rotational symmetry. As shown in previous ARPES studies on detwinned Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> and NaFeAs [\[5](#page-6-0)[,29,30\]](#page-7-0), the  $d_{xz}$  and  $d_{yz}$ bands shift oppositely along two perpendicular Fe-Fe directions in a single domain. Such a band shift manifests itself as an energy splitting between the  $d_{xz}$  and  $d_{yz}$  bands in the twinned sample due to the superposition of photoemission signals from two perpendicular domains. In the FeSe thin film, the most pronounced band reconstruction is the energy splitting between the  $d_{xz}$  and  $d_{yz}$  bands [Fig. [1\(d\)\]](#page-1-0), which is similar to what has been observed in iron pnictide compounds [\[5](#page-6-0)[,29,30\]](#page-7-0). However, without the interference of long-range magnetic order, the band reconstruction is much simpler and more distinguishable in FeSe. For example, the whole  $d_{yz}$  holelike band is observed shifting up to above  $E_F$  in FeSe, while in NaFeAs, only a small section of this band can be observed due to the SDW gap opening associated with the CAF order. Therefore, FeSe is an ideal system for us to quantitatively study the band reconstruction in the nematic state.

We overlaid the high-temperature band dispersion extracted from Fig.  $2(a)$  (the red dashed lines) on top of the lowtemperature spectra image, as shown in Fig. 2(b). The band



FIG. 2. Nontrivial momentum dependence of the band reconstruction. (a) The second derivative photoemission intensity distribution taken on a 35-ML FeSe film along the  $\Gamma$ -*M* direction at 140 K. (b) The same as (a), but taken at 70 K. The red dashed lines show the high-temperature band dispersion extracted from (a). The data were taken with 25 eV photons. The hole bands show moderate  $k_z$  dispersion and cross  $E_F$  when the 25 eV photon energy selects  $k_z$  between  $\Gamma$  and Z. (c) The temperature dependence of the energy distribution curves (EDCs) taken at five different momenta after the division of Fermi-Dirac function. The peak positions are determined via a combination of the spectral weight maximum and second-derivative-curve minimum. The top red and blue bars illustrate the energy scale of the band shift. We note that there is constant finite-energy splitting between the inner and outer hole bands at  $\Gamma$  above  $T_{\text{nem}}$ , which could be due to spin-orbit coupling. (d) The temperature dependence of the band positions extracted from the data in (c).

reconstruction at *M* is much more pronounced than that at  $\Gamma$ . Figure  $2(c)$  shows the detailed temperature evolution of the energy distribution curves (EDCs) taken at five different momenta, as indicated in Fig. [2\(b\).](#page-2-0) The band positions at each temperature were determined through peak fittings and plotted in Fig. [2\(d\).](#page-2-0) All bands start to shift at  $\sim$ 125 K, which we interpret as *T*nem for the 35-ML FeSe film, as this is the temperature at which symmetry breaking between the *dxz* and  $d_{yz}$  orbitals begins.  $T_{\text{nem}}$  of the 35-ML FeSe film is higher than that of the FeSe single crystal. The enhancement of *T*nem may originate from the lattice strain in the FeSe thin film  $[33]$ . When the thickness of the film decreases, the SrTiO<sub>3</sub> substrate induces tensile strain to the FeSe thin film. As a result, the general electronic correlation and orbital and spin fluctuations all change due to the changes in bond angle and bond length. We note that spin-orbital coupling induces a finite band splitting at  $\Gamma$  even above  $T_{\text{nem}}$ . To characterize the C4 rotational symmetry breaking between  $d_{xz}$  and  $d_{yz}$ , only the additional band splitting below  $T_{\text{nem}}$  is considered. We then determine the magnitude of band splitting between *dxz* and *dyz* bands at different momenta. We found that the magnitude of band splitting is strongly momentum dependent and changes nonmonotonically from  $\Gamma$  to M. More specifically, it is around 20 meV at  $\Gamma$  and decreases to its minimum value at the momentum slightly away from  $\Gamma$ , then increases towards  $M$ , and finally reaches its maximum value of 70 meV at *M* [Fig. 3(a)].

The energy splitting between  $d_{xz}$  and  $d_{yz}$  has been taken as evidence of the existence of ferro-orbital ordering in the nematic state. However, the  $d_{xz}$  and  $d_{yz}$  ferro-orbital ordering is normally considered an on-site occupation difference between the  $d_{xz}$  and  $d_{yz}$  orbitals. Such an occupation difference would result in a  $d_{xz}$  and  $d_{yz}$  band splitting that is momentum independent [Fig.  $3(b)$ ], which is inconsistent with our observation. Alternatively, the middle parts of the  $d_{xz}$  and  $d_{yz}$  bands remain unchanged through the nematic transition [Fig.  $3(a)$ ], indicating that the band shift might change sign when going from  $\Gamma$  to *M*. As shown in Fig. 3(c), such a band shift could well explain the observed nonmonotonic momentum dependence of the energy splitting. Consistently, the sign reversal of the band shift at  $\Gamma$  and *M* has been confirmed recently by the ARPES study on a detwinned FeSe single crystal [\[27\]](#page-7-0).

Because the band reconstruction occurs primarily near the *M* point, Fig. [4](#page-4-0) focuses on the temperature dependence of photoemission spectra taken around the *M* point in the 35-ML FeSe film. The Fermi surface is ellipselike at 160 K. The *C*2 symmetry of the Fermi surface above  $T_{\text{nem}}$  originates from the matrix element effect and the glide-mirror symmetry of the FeSe plane [\[34\]](#page-7-0). Upon entering the nematic state, the Fermi surface shrinks along the  $k_x$  direction and finally evolves into two small Fermi pockets [Fig.  $4(a)$ ]. The band reconstruction could be tracked by the energy positions of the holelike band tops and the electronlike band bottoms [Fig.  $4(b)$ ]. The band tops and bottoms are degenerate at 160 K, respecting the *C*4 symmetry of the tetragonal lattice. Upon lowering the temperature, the hole and electron bands shift consistently and split into three separate branches: one branch  $(E_{up})$  shifts upwards above the Fermi energy  $E_F$ , and another branch  $(E_{down})$  shifts downwards to higher binding energy. In the middle, a shallow electron band, whose band bottom *E*<sup>0</sup>



FIG. 3. Momentum dependence of the band splitting along the -*M* direction in the nematic state. (a) Momentum dependence of the band splitting between  $d_{xz}$  and  $d_{yz}$  bands along the  $\Gamma$ -*M* direction. The shaded area is illustrated to guide the eye. (b) Illustration of the  $d_{xz}$  and  $d_{yz}$  band splitting in the nematic state considering the on-site occupation difference between  $d_{xz}$  and  $d_{yz}$  bands. (c) Illustration of the  $d_{xz}$  and  $d_{yz}$  band splitting in the nematic state considering the band shift reversion from  $\Gamma$  to *M*.

is nearly unchanged with temperature, was observed at low temperature.

We then determine how the bands are reconstructed near the *M* point. The  $d_{xz}$ ,  $d_{yz}$ , and  $d_{xy}$  orbitals construct two pairs of holelike and electron bands near the *M* point [Figs. [4\(c1\)](#page-4-0) and  $4(d1)$ ]. The holelike band top and electron band bottom are degenerate at the *M* point. Such degeneracy can only be lifted by a breaking of glide-mirror symmetry or spin-orbital coupling. For the FeSe thin film, there is no experimental evidence for glide-mirror symmetry breaking, and the effect of spin-orbital coupling is weak near the *M* point. Therefore, the degeneracy between the holelike band top and electron band bottom should remain unchanged when entering the nematic state. However, for the middle electron band, there is no holelike band associated with it. In the nematic state, the  $d_{yz}$  and  $d_{xz}$  holelike bands shift upwards and downwards, respectively (Figs. [2](#page-2-0) and 3). According to the band symmetry, once the  $d_{xz}$  electron band shifts below the  $d_{xy}$  holelike band,

<span id="page-4-0"></span>

FIG. 4. Band structure reconstruction near the *M* point in the nematic state. (a) Temperature dependence of the Fermi surface mapping near the *M* point. (b) Temperature dependence of the second derivative of photoemission intensity distribution taken along the  $\Gamma$ -*M* direction. The cut direction is shown by the cyan solid line in (a). The solid lines mark the energy positions of either the band tops of holelike bands or bottoms of electronlike bands. The dashed lines are a guide to the eyes for the band dispersion and Fermi surface. (c) Schematic of the band shift and hybridization of the  $d_{xz}$  and  $d_{xy}$  bands near the  $M_y$  point. (d) Schematic of the band shift of the  $d_{yz}$  and  $d_{xy}$  bands near the  $M_x$  point. The data were taken with 38 eV photons.

a hybridization gap will open between them, resulting in an energy separation between the electron band bottom and holelike band top  $[35,36]$  [Fig.  $4(c2)$ ]. This is the only possible schematic in which an electron band bottom is observed and there is no associated holelike band top. Moreover, the band dispersion of the middle electron band flattens in the nematic state, which can be well explained by the hybridization gap opening between the *dxz* electron band and the *dyz* hole band [Fig.  $4(c2)$ ]. Therefore, the middle electron band most likely originates from the hybridized  $d_{xz}$  and  $d_{xy}$  bands. Contrary to the  $d_{xz}$  electron band, when the  $d_{yz}$  electron band shifts up, there is no band hybridization, and the electron band bottom remains degenerate with the holelike band top [Fig.  $4(d2)$ ]. The upper electron band can be then attributed to the  $d_{yz}$  electron band. For the deeper electron band, previous ARPES studies attribute it to the  $d_{xz}$  band [\[23–25\]](#page-7-0). However, as shown here in the FeSe thin film, the  $d_{xz}$  and  $d_{yz}$  orbitals contribute the middle and upper electron bands, suggesting that the deeper electron band has to originate from the  $d_{xy}$  orbital. Its band bottom shifts downwards in the nematic state [Fig.  $4(d2)$ ]. We note that the middle flat electron band has not been observed in the FeSe single crystal [\[23–27\]](#page-7-0). Recently, it was shown that the middle electron band is above  $E_F$  in the FeSe single crystal and hence cannot be observed [\[37\]](#page-7-0). By doping electrons, the middle electron band shifts downwards and emerges at certain doping level. The observation of three electron bands in the FeSe thin film complements the previous ARPES studies on FeSe and is crucial for understanding the complex band reconstruction in the nematic state.

We now illustrate the band reconstruction near the *M* point in Figs.  $5(a)$ – $5(d)$ . We first consider the band structure in a one-Fe BZ for simplicity. The *dyz* and *dxz* bands hybridize with the  $d_{xy}$  bands near  $M_X$  and  $M_Y$ , respectively, forming two pairs of electron and holelike bands [\[38\]](#page-7-0). In the nematic state, the *dyz* band shifts up around the  $M_X$  point. As a result, the electron pocket shrinks along one direction and eventually evolves into two small Fermi pockets. On the contrary, around the *MY* point, the *dxz* band shifts downwards and opens a hybridization gap with the  $d_{xy}$  band, which enlarges the electron pocket at the *MY* point. This enlargement could also be considered a volume compensation for the shrink of the electron pocket at the *MY* point. We then folded these bands back into the two-Fe BZ and obtained the reconstructed Fermi surface and band structure in Fig.  $5(d)$ . Moreover, due to the sample twinning effect, the experimental band structure is a superposition of bands from two perpendicular domains [\[4\]](#page-6-0). Taking this effect into

<span id="page-5-0"></span>

FIG. 5. Schematics of band reconstruction near the *M* point through the nematic transition. Illustration of (a) the reconstruction of the Fermi surface and (b) and (c) band structure around the *M* point in a one-Fe BZ. For simplicity, we neglect the hole bands and associated hole pockets near the  $\Gamma$  point. The bands are stretched in three-dimensional plots for a better view of the band reconstruction. (d) Illustration of the low-temperature electronic structure in two-Fe BZ by folding the corresponding bands between  $M_X$  and  $M_Y$  (left panel) and in the twinned sample by overlapping the bands in two perpendicular domains (right panel). (e) Temperature dependence of the energy splitting extracted from the band tops and bottoms at the *M* point.

consideration, Fig.  $5(d)$  reproduces the observed propellerlike Fermi pockets and the band splitting at the *M* point very well. We note that part of the circular electron pocket is constructed by the  $d_{xy}$  orbital [Fig.  $5(d)$ ], whose photoemission matrix elements are much weaker than the  $d_{xz}$  and  $d_{yz}$  orbitals [\[5\]](#page-6-0). Therefore, the circular electron pocket appears to be missing in the Fermi surface mapping in Fig. [4\(a\).](#page-4-0)

One intriguing feature in Fig.  $5(a)$  is that the  $d_{xy}$  electron band shifts towards higher binding energy near the  $M_X$  point, resulting in a finite-energy splitting between the *dxy* bands at the  $M_X$  and  $M_Y$  points ( $\Delta_{xy} = E_{xy} - E_{xy'}$ ). Such an energy splitting is around 45 meV, which is comparable to the 70 meV energy splitting between the  $d_{xz}$  and  $d_{yz}$  bands ( $\Delta_{yz-xz}$  =  $E_{yz} - E_{xz}$ ). This result suggests that the  $d_{xy}$  orbital also plays an important role in driving nematicity. Figure  $5(e)$  shows the temperature dependence of  $\Delta_{yz-xz}$  and  $\Delta_{xy}$ . The orderparameter-like behavior suggests that both  $d_{xz}/d_{yz}$  and  $d_{xy}$ energy splittings could be viewed as a pivotal characteristic property of the nematic state. Their origin holds the key to understanding the mechanism of the nematicity.

# **IV. DISCUSSION**

The observed band reconstruction and its distinctive distribution in the momentum space put strong constraints on theories. Our results do not favor the spin-nematic scenario because no signature of long-range magnetic ordering, i.e., band folding, was observed in FeSe down to the lowest measurement temperature (20 K), even though  $T_{\text{nem}}$  is as high as 125 K and the band-splitting energy around *M* is as large as 70 meV. This is consistent with the results for the FeSe single crystal, where *T*nem is ∼90 K and no band folding was observed down to 5 K  $[20-27]$ . One may argue that the FeSe system might have a strong spin fluctuation without long-range magnetic order due to the fine balance of the exchange interaction [\[39\]](#page-7-0) or spin/charge fluctuations [\[40\]](#page-7-0). However, this seems highly unlikely considering the existence of nematicity without long-range magnetic order in the large parameter space of the layer dependence of the FeSe thin film, where  $T_{\text{nem}}$  changes from 170 to 125 K when the thickness of the film increases from 2 to 35 ML [\[33\]](#page-7-0). Based on all these facts, the electronic nematicity here is unlikely of spin-nematic origin. This is further supported by the NMR and thermodynamic studies on the FeSe single crystal, which also point out the nonmagnetic origin of the nematic state [\[21,22\]](#page-7-0).

Ruling out the spin-nematicity scenario, let us consider the possibility of orbital ordering. Such a scenario could naturally explain the absence of magnetic ordering in FeSe by assuming a weak coupling between the spin and orbital/lattice. However, the on-site energy difference between the  $d_{xz}$  and  $d_{yz}$  orbitals

<span id="page-6-0"></span>would only lead to a band shift that is momentum independent. Therefore, the on-site ferro-orbital ordering alone cannot account for the nontrivial momentum dependence of the band reconstruction observed here.

The nontrivial momentum-dependent band reconstruction requires further theoretical understanding. One possible explanation is the orbital-dependent band renormalization. When entering the nematic state, the *C*4 rotational symmetry breaking does not occur in the orbital occupation. Instead, the anisotropy occurs in the hopping of  $d_{xz}$ ,  $d_{xy}$ , and  $d_{xy}$ orbitals. The hopping anisotropy between the  $\Gamma$ - $M_X$  and  $\Gamma$ - $M_Y$ directions renormalizes the bands of  $d_{yz}$ ,  $d_{yz}$ , and  $d_{xy}$  orbitals differently, resulting in the nontrivial shift of bands at  $\Gamma$  and *M*. The huge hopping anisotropy cannot originate purely from the lattice distortion because the change in the lattice constant is too small to account for such a large energy scale [5]. The itinerant orbital ordering, the coupling between the spin and orbital degree of freedoms, and the role of the selenium anion may need to be considered [16[,41\]](#page-7-0).

Finally, the fact that such a huge anisotropy persists down to the lowest measurement temperature raises an important question of how such a nematic order coexists and interacts with superconductivity. In comparison with the FeSe single crystal, *T*nem is enhanced to 125 K, and no superconductivity has been observed in the 35-ML FeSe thin film, indicating a competition between the nematic order and superconductivity. On the other hand, we note that the observed nematic order is robust in all multilayer FeSe thin films down to 2 ML, with *T*nem as high as 170 K in the 2-ML film [\[33\]](#page-7-0). In contrast, no signature of nematic order, i.e., the orbital anisotropy, has been detected in the 1-ML FeSe that holds the record  $T_c$  in all ironbased superconductors [\[31,33\]](#page-7-0). The natural question is how such a strong nematic order in multilayer FeSe is completely suppressed in 1-ML FeSe. Is it due to strong coupling between the substrate and FeSe that prevents the 1-ML FeSe from going

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through the nematic/structural transition or due to the heavy electron doping that suppresses the nematic order and thereby promotes the superconductivity? The more important question may be whether strong nematic fluctuations exist in 1-ML FeSe with the complete suppression of nematic order. The answer to this question is intimately related to the pairing mechanism in 1-ML FeSe, which is an intensely debated topic in the field. Further investigations are required to elucidate these issues.

# **V. CONCLUSION**

In conclusion, we reported the temperature evolution of the electronic band structure in the FeSe thin film. The system enters the nematic state at 125 K, but the signature of magnetic order was not observed at the lowest measurement temperature. All the  $d_{xz}$ ,  $d_{yz}$ ,  $d_{xy}$  orbitals participate in the band reconstruction in the nematic state. The energy splitting of the  $d_{xz}/d_{yz}$  bands shows nontrivial momentum dependence, and the  $d_{xy}$  bands split at the *M* point with a comparable energy scale. Our result excludes the on-site ferro-orbital ordering as the driving force for the nematicity. Instead, anisotropy occurs in the hopping of all  $d_{xz}$ ,  $d_{yz}$ ,  $d_{xy}$  orbitals. Its origin holds the key to understanding the nematicity and calls for further theoretical and experimental studies.

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