

Defects in AlN as candidates for solid-state qubits

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We investigate point defects and defect complexes in AlN for potential applicability as single-spin centers and solid-state qubits analogous to those observed in diamond and SiC. We find that isolated anion vacancies (V_N) meet many of the criteria for an individually addressable quantum system, but their states are too close to the conduction-band edge. We therefore investigate how the properties can be tuned by complexing of the vacancy with substitutional impurities on neighboring lattice sites. Based on our comprehensive investigation, the transition-metal dopants Ti and Zr emerge as the best candidates: They favorably substitute on the Al site and form complexes with V_N that possess the desired array of electronic and optical properties. Favorable charge and spin states, binding energies, and optical excitation energies are reported. Our results indicate that implantation of Ti or Zr into single-crystal AlN substrates can lead to the formation of individually addressable solid-state qubits in this material.

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The rapidly growing interest in quantum-information technologies has created a need for identifying optically addressable single-spin centers that may serve as qubits. The NV^- center in diamond, which consists of a carbon vacancy (V_C) next to a substitutional nitrogen atom (N_C), has emerged as the prototypical deep-level solid-state qubit because of its ability to be initialized, manipulated, and measured at room temperature [1,2]. Different polytypes of silicon carbide (SiC) have subsequently been found to also exhibit point defects that may be manipulated as room-temperature qubits [3–9], demonstrating that materials other than diamond can act as suitable hosts. It is still highly desirable to identify centers with similar characteristics in additional semiconductors or insulators for which high-quality crystal growth and processing are available.

In this Rapid Communication we investigate AlN as a candidate host material. AlN meets the requirements [4] to act as a host for qubit centers: It has a very large band gap (6.12 eV [10]), which suppresses coupling between defect levels in the band gap and bulk states, and a very small spin-orbit splitting (19 meV [11]), which enhances qubit-state lifetime. High-quality crystal growth [12–14] and doping techniques [15] have been developed. A slight drawback is that its host elements have nonzero nuclear spin [4]; however, spin-bath effects can be brought under control with appropriate pulsing and polarization techniques [16]. AlN is thus an attractive host material, and our aim is to identify suitable single-spin centers.

We will show that defect theory points to complexes between nitrogen vacancies (V_N) and donor defects as attractive qubit candidates. The quantitative details are addressed with cutting-edge first-principles calculations based on density functional theory (DFT) with a hybrid functional. In particular, we conduct a comprehensive investigation of group-IV impurities and their complexes with V_N . Transition-metal impurities such as Ti or Zr emerge as excellent candidates to form complexes with V_N that show outstanding promise as qubits.

Point defects induce levels within the band gap of a semiconductor that, when appropriately occupied with electrons,

can give rise to controllable quantum states. Vacancies, in particular, provide suitable states that are “atomiclike” due to the concentration of their wave function within a small spatial volume. The electronic structure of a tetrahedrally bonded material such as AlN can be understood within molecular orbital (or tight-binding) theory in terms of interactions between sp^3 hybrid orbitals, with bonding (antibonding) combinations giving rise to the valence (conduction) bands. The removal of a host atom leads to “dangling bonds” (DBs) (hybrid orbitals on the neighboring atoms) that interact and split into a symmetric a_1 state and three t_2 states. A suitable arrangement of electrons in these states can give rise to spin configurations suitable for use as a solid-state qubit [4]. The electron occupation (which determines the charge state of the defect) is determined by the Fermi level in the material, which in turn can be controlled by doping. The energetic position and ordering of the states, which determines the spin, can also be manipulated, for instance, by positioning suitable impurities near the vacancy. In analogy with the prototype NV^- center in diamond and the ($V_{Si}-V_C$)⁰ center in 4H-SiC [3,7], a triplet ($S = 1$) ground state is desirable, although recent experiments have identified that a quadruplet ($S = 3/2$) state (as in V_{Si}^- in SiC) can also be suitable [9].

Vacancies in AlN can form on the cation or anion sites. In a cation vacancy, the DBs are anion derived and hence lie within the lower half of the band gap [17]. Ensuring that the resulting defect levels are not too close to the valence-band maximum (VBM) and sufficiently isolated from the bulk states [4] may require additional engineering, as recently explored for a $V_{Al}-O_N$ complex [18]. However, manipulating the charge and spin states in such cation-vacancy-related centers would require the Fermi level to lie below mid gap, which is challenging in AlN. Indeed, p -type conductivity in AlN has not been demonstrated [19].

The natural tendency of AlN towards Fermi-level positions in the upper part of the gap (as evidenced by the feasibility of n -type doping [15,20,21]) renders defect centers based on anion vacancies more promising. Here, cation DBs interact to form the defect states. Cation DBs lie in the upper part

of the gap [17], and hence the t_2 states may be too close to the conduction-band minimum (CBM). As with the cation vacancy, defect engineering can push the t_2 levels deeper into the gap, for instance, by applying strain, by alloying the host with a larger band gap material (such as BN), or by complexing with an adjacent impurity. We will focus on the latter, in particular, on donor dopants that stabilize defect levels in a complex. Complex formation is actually facilitated by the Coulomb attraction between positively charged donors and the V_N^- (which is negatively charged when the Fermi level is in the upper part of the gap, a natural consequence of donor doping).

We will investigate the quantitative details of this scheme by performing advanced first-principles calculations based on the HSE06 screened hybrid functional [22,23]. This methodology was previously very successful in describing the properties of analogous deep-center qubit candidates such as the NV^- center in diamond and the divacancy in SiC [3–9]. In particular, we investigate a number of group-IV impurities and their complexes with V_N , finding that most of them do not have any significant effect on the positions of the t_2 -derived defect levels within the band gap. The exceptions are transition metals such as Ti or Zr, which strongly affect the position and nature of the vacancy levels and lead to favorably positioned localized states within the band gap. Specifically, we will find the neutral $(Ti_{Al}V_N)^0$ and $(Zr_{Al}V_N)^0$ complexes to be stable for a wide range of conditions and to exhibit $S = 1$ spin configurations well suited for application in solid-state qubits. The results for Ti in SiC in Ref. [24] support the notion that our hybrid functional approach yields reliable results for Ti- and Zr-related defects in AlN.

Defect formation energies (E^f) are key quantities from which we can derive impurity and defect concentrations, the stability of different charge states, and the related electronic transition levels [25]. Since the spin states depend on the charge state, E^f also determines whether a given defect will occur in a desired spin configuration. The formation energy of the V_N in AlN is given by

$$E^f[V_N^q] = E_{\text{tot}}[V_N^q] - E_{\text{tot}}[\text{AlN}] + \frac{1}{2}E_{\text{tot}}[N_2] + \mu_N + q\epsilon_F + \Delta_q, \quad (1)$$

where $E_{\text{tot}}[V_N^q]$ and $E_{\text{tot}}[\text{AlN}]$ represent the total energy of the supercell containing a vacancy in charge state q , and that of a perfect crystal in the same supercell. The Fermi level ϵ_F represents the chemical potential for electrons, which is referenced to the VBM and ranges over the band gap up to the CBM. The chemical potential (μ_N) represents the energy of the reservoir with which N atoms are exchanged and reflects the experimental conditions; it varies between N-rich (Al-poor) and N-poor (Al-rich) extremes, with bounds set by the calculated formation enthalpy of AlN ($\mu_{Al} + \mu_N = \Delta H[\text{AlN}] = -3.18$ eV). Lastly, the Δ_q term represents the charge-dependent finite-size correction [26]. Similar expressions apply to impurities or dopants, whose chemical potentials may be coupled to those of the host elements, as detailed in the Supplemental Material [23].

Formation energies such as Eq. (1) can be used to determine defect concentrations when conditions are sufficiently close to equilibrium; nonequilibrium processes such as ion implan-

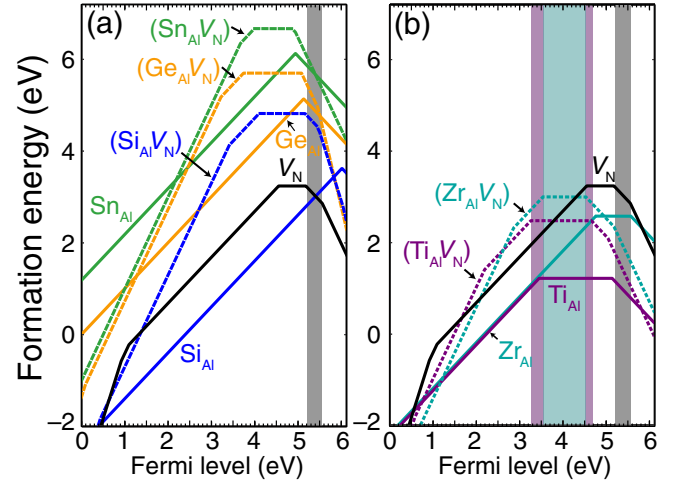


FIG. 1. Formation energies of the isolated V_N , various dopant impurities substituting on the Al site, and complexes in AlN, for Al-rich conditions. (a) Group-IVA impurities (Si, Ge, Sn); (b) group-IVB impurities (Ti and Zr). Only the lowest-energy configurations of the complexes are included, as described in the text. Shaded regions indicate the Fermi-level values for which an $S = 1$ state is favored for the isolated V_N (gray), for the $(Ti_{Al}V_N)^0$ complex (purple), and for the $(Zr_{Al}V_N)^0$ complex (teal).

tation can result in higher concentrations. Even in the latter case, formation energies can provide useful information about the relative stability of various configurations, about binding energies for complexes, about what charge and spin states a given defect will adopt for a given Fermi-level position, and about the position of its defect levels in the band gap.

Formation energies of the V_N and various dopants are shown in Fig. 1 for Al-rich conditions [23]. The vacancy can assume many different charge states, ranging from +3 for ϵ_F at the VBM to -2 for ϵ_F at the CBM. The desired high-spin states ($S = 1$ or $S = 3/2$) occur only for charge states (-1 and -2) that have high formation energies (even under the most favorable Al-rich conditions), making it unlikely that vacancies would form spontaneously. This is not an obstacle, however, since vacancies can be readily produced by irradiation or ion implantation, as is common practice for the NV^- center in diamond.

We find that the low-spin configurations of V_N ($S = 0$ or $1/2$) are only ~ 0.1 eV higher in energy than the $S = 1$ or $3/2$ configurations, indicating a potential sensitivity to spin flips from external perturbations. Another drawback is that the states associated with the excited configuration of the isolated V_N^- and V_N^{-2} centers are very close to the CBM, as illustrated in the defect level diagram (DLD) of Fig. 2(a). The DLD for the V_N^{-2} is nearly identical, but with the spin-majority $a_1(2)$ state occupied to give the $S = 3/2$ state. Along with the small energy difference between the high- and low-spin states, this proximity could be an additional source of decoherence due to coupling with the bulk conduction-band states that could limit the effectiveness of the isolated V_N in AlN as a viable qubit candidate. We therefore explore how the properties of the spin center can be engineered through complexing with impurities.

Si, Ge, and Sn prefer the substitutional Al site in AlN, and act as donors. In particular, Si is a successful n -type dopant

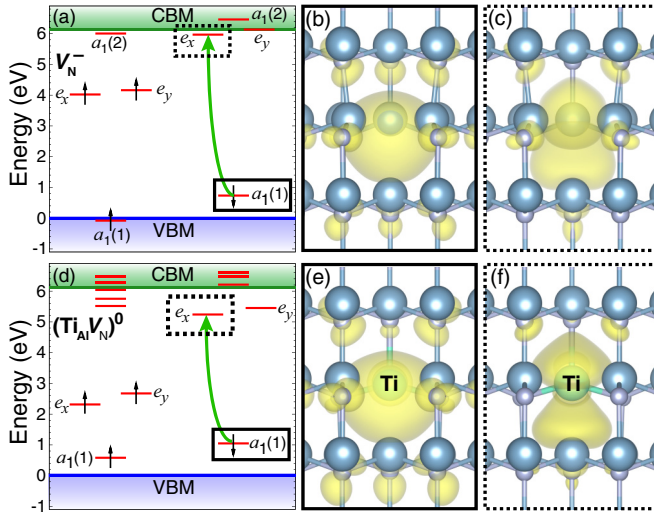


FIG. 2. Defect-level diagrams (DLDs) for (a) an isolated negatively charged nitrogen vacancy V_N^{-1} and (b) a $(\text{Ti}_{\text{Al}}V_N)^0$ complex in AlN, showing the location and occupancy of the single-particle defect states within the band gap. The arrows indicate the spin-conserving internal transition from the occupied $a_1(1)$ state (solid box) to the unoccupied e state (dashed box) in the spin-minority channel. To the right are charge-density isosurfaces depicting wave functions for the single-particle states involved in these transitions: (b) $a_1(1)$ state of V_N^{-1} ; (c) e_x state of V_N^{-1} ; (e) $a_1(1)$ state of $(\text{Ti}_{\text{Al}}V_N)^0$; (f) e_x state of $(\text{Ti}_{\text{Al}}V_N)^0$. The isosurfaces are displayed at 10% of their maximum value.

in AlN [15,20]. The formation energies of Si, Ge, and Sn are plotted in Fig. 1(a). All three of these impurities exhibit DX -like behavior; i.e., for Fermi levels high in the band gap they become more stable in a negative charge state (and thus act as acceptors), accompanied by a large lattice relaxation. If these dopants are incorporated in high concentrations (exceeding the concentration of any other defect or impurity), charge neutrality will pin the Fermi level at the $\epsilon(+/-)$ transition level, which occurs at 0.12 eV below the CBM for Si, 0.99 eV for Ge, and 1.18 eV below for Sn. These transition levels are in good agreement with experimental and theoretical data where available [20,27].

We now examine the complexes formed between the group-IVA impurities and V_N , whose formation energies are also included in Fig. 1(a). The formation energy of the complexes is quite high for Fermi-level positions that lead to desirable

spin states. However, as already noted, V_N are likely to be introduced by implantation or irradiation; based on reported migration barriers for V_N in GaN (~ 2.6 – 4.3 eV) [28–30] we estimate a temperature in excess of 500°C is needed to drive the formation of complexes via V_N diffusion. The complexes are stable in charge states ranging from $+2$ to -3 . Unfortunately, the process of complex formation turns out to destabilize the desired $S = 1$ and $S = 3/2$ states. The local lattice relaxations favor low-spin ground states, and therefore these complexes between V_N and group-IVA donors do not serve as suitable NV-center analogs.

We therefore turn to an exploration of group-IVB dopants, in particular, the transition metals Ti and Zr. As seen in Fig. 1(b), these impurities can assume $+1$, 0 , and -1 charge states and have very modest formation energies when incorporated on the Al site for both Al-rich and N-rich conditions [23]. Incorporation on the N site is highly energetically unfavorable. Ti_{Al} and Zr_{Al} can therefore easily be incorporated during growth, and if they are present in concentrations higher than those of other impurities or native defects, they will also determine the location of the Fermi level: If additional impurities/defects are predominantly donorlike, ϵ_F will be pinned at the $\epsilon(0/-)$ level of the transition-metal impurity (2.67 eV below the CBM for Ti_{Al} and 1.37 eV below the CBM for Zr_{Al}); if additional impurities are predominantly acceptorlike, ϵ_F will be pinned at the $\epsilon(+/0)$ level of the transition-metal impurity (0.99 eV below the CBM for Ti_{Al} and 0.53 eV below the CBM for Zr_{Al}).

Complexes between Ti and Zr and the V_N are also included in Fig. 1(b). The neutral complexes are stable in the $S = 1$ state, highlighted by the shaded regions in Fig. 1(b): from 2.87 to 1.46 eV below the CBM for $(\text{Ti}_{\text{Al}}V_N)^0$ and from 2.58 to 1.59 eV below the CBM for $(\text{Zr}_{\text{Al}}V_N)^0$. The -1 charge state of the complexes favors a low-spin $S = 1/2$ configuration, making it uninteresting as a qubit candidate. These numbers actually indicate a very favorable situation in the case of Ti: As noted above, in the presence of additional donorlike impurities/defects, a high concentration of Ti_{Al} will pin ϵ_F at 2.67 eV below the CBM, within the stability window of neutral $(\text{Ti}_{\text{Al}}V_N)^0$ ($S = 1$). With Zr the situation is not as advantageous: Stabilizing the $(\text{Zr}_{\text{Al}}V_N)^0$ complex would require additional doping measures to fix the Fermi level.

In terms of their spin configurations, we find that the level structure of the complexes is advantageously distanced from the CBM, as seen from the DLD of the $(\text{Ti}_{\text{Al}}V_N)^0$ in Fig. 2(b). We find that the symmetry of the localized defect states of the

TABLE I. Calculated optical excitation energies [absorption, emission, and zero-phonon line (ZPL)] associated with the spin-conserving excitations [see Figs. 3(a) and 3(d)] of isolated V_N and $(\text{Ti}_{\text{Al}}V_N)$ and $(\text{Zr}_{\text{Al}}V_N)$ complexes in AlN. Competing channels that ionize the centers by excitation to the conduction band are also described. All values are in eV.

Center	$D^q + \hbar\omega \rightarrow D^q$			$D^q + \hbar\omega \rightarrow D^{q+1} + e^- _{\text{CBM}}$					
	Spin-conserving excitation: $S \rightarrow S$			Spin-minority excitation: $S \rightarrow S+1/2$			Spin-majority excitation: $S \rightarrow S-1/2$		
	Absorption	ZPL	Emission	Absorption	ZPL	Emission	Absorption	ZPL	Emission
V_N^-	4.13	3.82	3.52	4.84	4.13	3.49	1.62	0.95	0.31
V_N^{-2}	4.17	3.83	3.52	4.36	3.70	3.12	1.20	0.62	0.04
$(\text{Ti}_{\text{Al}}V_N)^0$	3.19	2.86	2.44	5.16	4.43	3.92	3.34	2.76	2.25
$(\text{Zr}_{\text{Al}}V_N)^0$	2.83	2.36	1.91	4.97	4.29	3.78	3.07	2.62	2.11

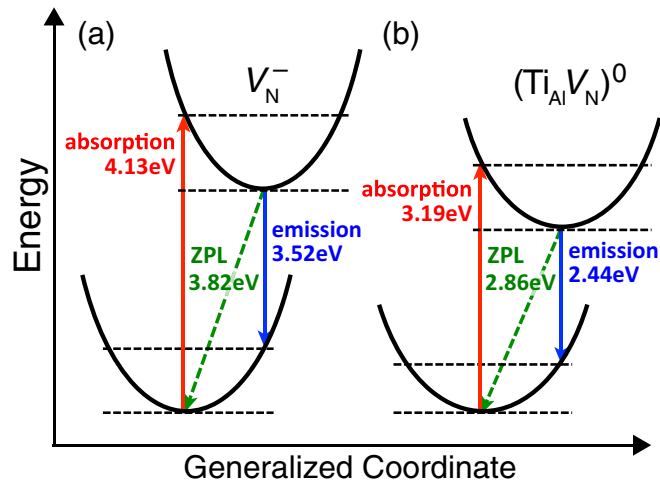


FIG. 3. Configuration coordinate diagram of the spin-conserving triplet excitations for (a) the V_N^- and (b) the $(\text{Ti}_{\text{Al}}V_N)^0$ complex in AlN. The absorption, emission, and zero-phonon line (ZPL) energies are for excitations in the spin-minority channel, as shown in Figs. 2(a) and 2(d). Axes are not to scale.

complexes is preserved while the position of the higher-lying e states is lowered relative to the analogous levels for the isolated V_N . This suggests the $(\text{Ti}_{\text{Al}}V_N)^0$ and $(\text{Zr}_{\text{Al}}V_N)^0$ complexes could support quantum states that are less prone to unwanted coupling with the delocalized conduction band states.

It is also important to assess how stable the complexes are with respect to dissociation. The binding energy of the $(\text{Ti}_{\text{Al}}V_N)^0$ complex can be estimated relative to constituents that obey charge neutrality. With respect to Ti_{Al}^- and V_N^+ , the binding energy is 2.6 eV; with respect to Ti_{Al}^+ and V_N^- , 3.7 eV; and with respect to Ti_{Al}^0 and the V_N^0 , 2.0 eV. These numbers indicate that, once formed, the complexes will be stable. For the Zr-containing complexes, we find similarly large binding energies in excess of 2 eV.

Having addressed the formation, stability, and spin state of the complexes, we now examine the optical excitation energies. Results are summarized in Table I, which also contains values for the isolated V_N . We obtain the optical energies using a configuration-coordinate diagram analysis as illustrated in Fig. 3 and schematically included in Fig. 2 for the intradefect transitions of the V_N^- and $(\text{Ti}_{\text{Al}}V_N)^0$. The calculated absorption energies range from 2.8 eV to 4.2 eV and have zero-phonon lines (ZPLs) from 2.4 to 3.8 eV. These values are much larger than those for other deep-center qubits such as the NV^- center in diamond (ZPL \sim 2 eV) or complexes in SiC (ZPL \sim 1 eV) [6,7,9]. This distinction indicates that qubits in AlN may provide functionality in the blue or UV region of the spectrum, compared to red or infrared excitations for qubits in diamond and SiC.

Lastly, we evaluate the isolation of the excited quantum states by combining the charge-state transition levels with the calculated optical excitation energies. For the example of the isolated V_N^- , we can estimate the position of the optically excited state by adding the ZPL (3.8 eV) to the $\epsilon(0/-)$ level (\sim 1.0 eV below the CBM), finding that an electron would be excited to a state \sim 2.8 eV above the CBM. Such an excitation could occur in an Auger-like process where the electron escapes to the conduction band, as was shown for the NV^- -to- NV^0 transition in diamond [31]. For the $(\text{Ti}_{\text{Al}}V_N)^0$, this same analysis leads to an excited state at \sim 0.9 eV below the CBM, indicating this state would be less prone to decoherence.

Table I also lists the energies required to ionize the defects by promoting an electron to the CBM rather than forming an intradefect photoexcited state of the deep center. These energies provide an additional measure of the optical isolation of the defect centers, representing the energy necessary to couple the defect to the bulk states by promoting an electron to the CBM. As seen in the DLDs of Fig. 2, the lowest-energy excitation of this type would correspond to promoting the highest-lying electron in the spin-majority channel [e.g., from the occupied e_y state for the case of the V_N^- in Fig. 2(a)]. Another transition corresponds to the excitation of the highest-occupied spin-minority electron to the CBM. The difference in energy between this transition and the intradefect transition is a good metric of how isolated the defect states are from the CBM. These differences are gratifyingly large in the case of the $(\text{Ti}_{\text{Al}}V_N)$ and $(\text{Zr}_{\text{Al}}V_N)$ complexes.

In summary, we have found that V_N -related centers in AlN can lead to viable deep-center qubits that exhibit properties similar to the NV^- center in diamond. Based on a comprehensive study of group-IV impurities, Ti and Zr were found to be the most promising dopants that can be stabilized in $(\text{Ti}_{\text{Al}}V_N)^0$ and $(\text{Zr}_{\text{Al}}V_N)^0$ complexes with V_N that possess a high-spin ($S = 1$) ground state. The optical signatures associated with these complexes confirm that they could provide robust solid-state qubit candidates in the blue or UV.

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