

Time-dependent density functional theory of high-intensity short-pulse laser irradiation on insulators

S. A. Sato

Graduate School of Pure and Applied Sciences, University of Tsukuba, Tsukuba 305-8571, Japan

K. Yabana

*Center for Computational Sciences, University of Tsukuba, Tsukuba 305-8577, Japan
and Graduate School of Pure and Applied Sciences, University of Tsukuba, Tsukuba 305-8571, Japan*

Y. Shinohara

Max-Planck-Institut für Mikrostrukturphysik, Weinberg 2, D-06120 Halle, Germany

T. Otobe

Advanced Photon Research Center, JAEA, Kizugawa, Kyoto 619-0615, Japan

K.-M. Lee

Center for Relativistic Laser Science, Institute for Basic Science, Gwangju 500-712, South Korea

G. F. Bertsch

Department of Physics and Institute for Nuclear Theory, University of Washington, Seattle, Washington 98195, USA

(Received 28 November 2014; revised manuscript received 30 September 2015; published 12 November 2015)

We calculate the energy deposition by very short laser pulses in SiO₂ (α -quartz) with a view to establishing systematics for predicting damage and nanoparticle production. The theoretical framework is time-dependent density functional theory, implemented by the real-time method in a multiscale representation. For the most realistic simulations we employ a meta-GGA Kohn-Sham potential similar to that of Becke and Johnson. We find that the deposited energy in the medium can be accurately modeled as a function of the local electromagnetic pulse fluence. The energy-deposition function can in turn be quite well fitted to the strong-field Keldysh formula for a range of intensities from below the melting threshold to well beyond the ablation threshold. We find reasonable agreement between the damage threshold and the energy required to melt the substrate. Also, the depth of the ablated crater at higher energies is fairly well reproduced assuming that the material ablated with the energy exceeds that required to convert it to an atomic fluid. However, the calculated ablation threshold is higher than experiment, suggesting a nonthermal mechanism for the surface ablation.

DOI: [10.1103/PhysRevB.92.205413](https://doi.org/10.1103/PhysRevB.92.205413)

PACS number(s): 78.40.-q, 71.15.Mb, 78.66.Nk, 79.20.Eb

I. INTRODUCTION

Ablation of surfaces by intense femtosecond laser pulses is potentially a useful tool for material machining as well as preparation of nanosized particles [1–14]. It is important to have good models of the energy deposition and the ablation process to set up the pulse protocols for the purpose in mind. However, it is not easy to model the laser-target interaction because one has to deal with the quantum physics at the atomic scale together with the pulse propagation at a mesoscopic scale.

There is a large literature on the modeling of the laser-target interaction dynamics [2,11,15–21], as reviewed in Ref. [22] as well as Ref. [13]. The fundamental physics is the excitation of particle-hole pairs, often parametrized by Keldysh's approximate formulas [14,23]. The particle and hole carriers affect the electromagnetic response of the insulator, screening the field when their density becomes large. Here the effects are often parametrized by hybrid dielectric functions containing contributions intrinsic to the insulator and plasma contributions from the excited electrons. Both aspects of this electron dynamics are included in the time-dependent density functional theory (TDDFT), which is

fully quantum mechanical and does not require any specific assumptions about the dynamics. Employing a carefully chosen approximate functional, it gives a good compromise between *ab initio* theory and computational feasibility. In this work we shall apply the dynamic equations of TDDFT to calculate the propagation of short, intense electromagnetic pulses upon insulators and compute the energy transfer to the medium.

In recent work, TDDFT with strong fields has been applied to condensed media in several contexts: coherent phonon generation [24,25] and high-field interactions with diamond, silicon, and quartz [26–31]. In this work we treat the energy transfer to a crystalline SiO₂, α -quartz, a material of technological importance. From the transferred energy, we conduct a systematic investigation of laser-damage and laser-ablation phenomena in the first-principles level. The calculations require high-performance computers, so our goal is to also analyze the results in terms of simpler models that can be easily applied. We only discuss the deposited energy of the pulse, which is the most important determinant of the subsequent atomic dynamics. Since TDDFT employing practically usable functionals does not have any relaxation processes, it

is limited to short-time dynamics. The main limitations to consider are the electron-electron kinetic relaxation time τ_{ee} , the full electron thermalization time, and the electron-phonon equilibration time. The latter two processes have time scale much larger than 100 fs, which is well beyond the time domain considered here. Estimates of τ_{ee} range from 1 to 100 fs [11,12,32,33]. Fortunately for the modeling by TDDFT, the response of insulators to high fields is rather insensitive to the kinetic equilibration [34]. We note that on very long time scales another mechanism that is missing from TDDFT becomes important, namely an avalanche of electrons in the free carrier bands [18].

II. COMPUTATIONAL METHOD

The theory and its implementation used in the present calculation have been described elsewhere [28], so we describe it briefly. The laser pulse that enters from the vacuum and attenuates in the medium varies on a scale of micrometers, while the electron dynamics takes place in a subnanometer scale. To overcome these conflicting spatial scales, we have developed a multiscale implementation introducing two coordinate systems: macroscopic coordinate X for the laser pulse propagation and the microscopic coordinate \vec{r} for local electron dynamics. The laser pulse is described by the vector potential $\vec{A}_X(t)$ which satisfies

$$\frac{1}{c^2} \frac{\partial^2 \vec{A}_X(t)}{\partial t^2} - \frac{\partial^2 \vec{A}_X(t)}{\partial X^2} = -\frac{4\pi e}{c} \vec{J}_X(t). \quad (1)$$

At each point X we consider lattice-periodic electron dynamics driven by the electric field $E_X(t) = -(1/c)[dA_X(t)/dt]$. They are described by the electron orbitals $\psi_{i,X}(\vec{r},t)$ which satisfy the time-dependent Kohn-Sham equation,

$$i\hbar \frac{\partial}{\partial t} \psi_{i,X}(\vec{r},t) = \left\{ \frac{1}{2m} \left(-i\hbar \vec{\nabla}_r + \frac{e}{c} \vec{A}_X(t) \right)^2 - e\phi_X(\vec{r},t) + \mu_{xc,X}(\vec{r},t) \right\} \psi_{i,X}(\vec{r},t), \quad (2)$$

where the potential $\phi_X(\vec{r},t)$, which includes Hartree and ionic contributions, and the exchange-correlation potential $\mu_{xc,X}(\vec{r},t)$, are periodic in the lattice. The electric current $J_X(t)$ is provided from the electron orbitals as

$$J_X(t) = -\frac{e}{\Omega} \int_{\Omega} d\vec{r} \sum_i \frac{1}{2m} \left[\psi_{i,X}^* \left(\vec{p} + \frac{e}{c} A_X \right) \psi_{i,X} + \text{c.c.} \right] + J_{\text{PS}}, \quad (3)$$

where Ω is a volume of the unit cell and J_{PS} is a current contribution coming from the pseudopotential. We solve Eqs. (1)–(3) simultaneously as an initial value problem where the incident laser pulse is prepared in a vacuum region in front of the surface, while all Kohn-Sham orbitals are set to their ground state.

For a quantitative description of the laser-damage process, theoretical inputs should meet the following demands. First it is important that the band gap is described reasonably, since the number of photons required to excite electrons across the band gap is a crucial parameter for electronic excitations. It is also important that the dielectric function at around

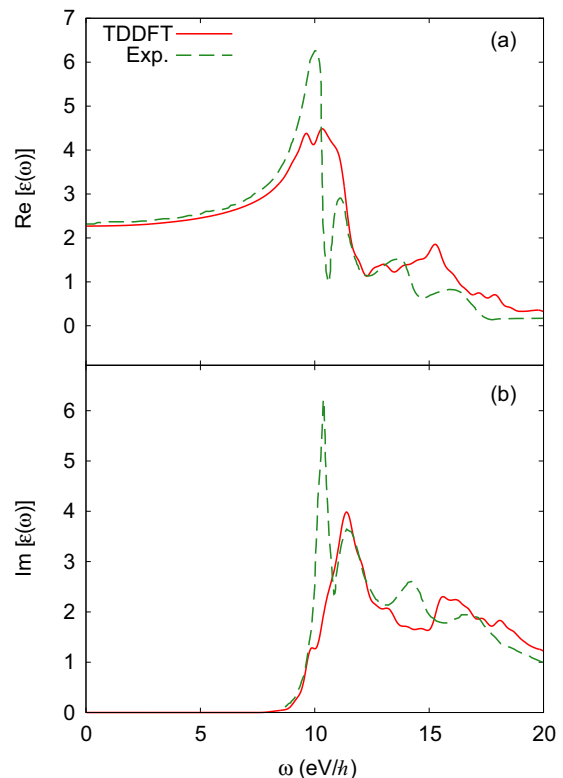


FIG. 1. (Color online) Real (a) and imaginary (b) parts of the dielectric function of SiO_2 in the direction parallel to the c axis.

the laser frequency 1.55 eV, in most measurements, should be described reasonably. In this work we use a modified Becke-Johnson exchange potential (mBJ) [35] as given by Ref. [36] (Eq. 2-4) with a LDA correlation potential [37] in the adiabatic approximation. We show in Fig. 1 real and imaginary parts of the dielectric function calculated by the real-time method [28], the same computational method as that will be used for nonlinear dynamics. The calculated indirect band gap with this potential is 1.3 eV lower than the experimental gap of 8.9 eV, but more relevant to electromagnetic interactions is the optical gap. This is seen to be 9 eV from the absorptive part of the dielectric function shown in Fig. 1, compared to the experimental value of 9–10 eV. The real part of the dielectric function at around 1.55 eV is also described reasonably. We note that there is no long-range exchange-correlation contribution included in the vector potential.

We compute the energy transfer to the medium from the electromagnetic side, since the calculation from the Kohn-Sham densities would require an explicit energy density functional for the mBJ potential. The energy transfer rate W is given by

$$W = -\vec{\mathcal{E}} \cdot \vec{J}, \quad (4)$$

where $\vec{\mathcal{E}}$ is the electric field associated with the pulse. In comparing different pulse lengths and intensities, we find the most convenient measure of the pulse strength is its fluence F given by $F_X = (c/4\pi) \int dt \hat{x} \cdot \vec{E} \times \vec{B}$, where X is the depth from the surface. With these definitions, the deposited energy density is given by $E_x(X) = -\int dt W_X(t) = -\frac{d}{dX} F_X$.

Our multiscale calculation uses a one-dimensional grid with spacing of 250 a.u. for propagation of laser electromagnetic fields. At each grid point, electron dynamics is calculated using an atomic-scale rectangular unit cell containing 6 silicon atoms and 12 oxygen atoms which are discretized into Cartesian grids of $20 \times 36 \times 50$. The dynamics of the 96 valence electrons is treated explicitly; the effects of the core electrons are taken into account by pseudopotentials [38]. Both electromagnetic fields and electrons are evolved with a common time step of 0.02 a.u.

The laser pulse in the vacuum is described by a gauge field $\vec{A}_X(t)$ of the form

$$\vec{A}_X(t) = \hat{z} A_0 \sin^2(\pi t_X / T_p) \cos(\omega t_X) \quad (5)$$

in the domain $0 < t_X < T_p$ and zero outside. Here ω is the photon's angular frequency, $t_X = t - X/c$ describes the space-time dependence of the field, and T_p controls the pulse length. It is related to the usual measure τ_p (full width at half-maximum intensity) by $\tau_p = 0.364 T_p$. Most of the results below were calculated for an average photon energy of $\hbar\omega = 1.55$ eV and the pulse length of $\tau_p = 7$ fs. We follow the pulse from the time its front reaches the surface ($\bar{2}10$) until it has propagated several micrometers into the material.

III. RESULTS

The main quantity we can calculate is the deposited energy E_x as a function of penetration depth x . The range of interest extends roughly from the energy required to melt the solid to the energy required to vaporize it. The first transition requires about 0.5 eV/atom in quartz, starting from room temperature. The second transition is not as well defined; we can estimate it as 6 eV/atom either as the heat of formation or from the ‘‘atomic-liquid’’ transition reported in Ref. [39].

A sampling of the results for the multiscale calculation is shown in Figs. 2–7. In Fig. 2 we show the deposited energy density at the surface for a range of laser fluences. The threshold for achieving melting is ~ 1.5 J/cm², while the

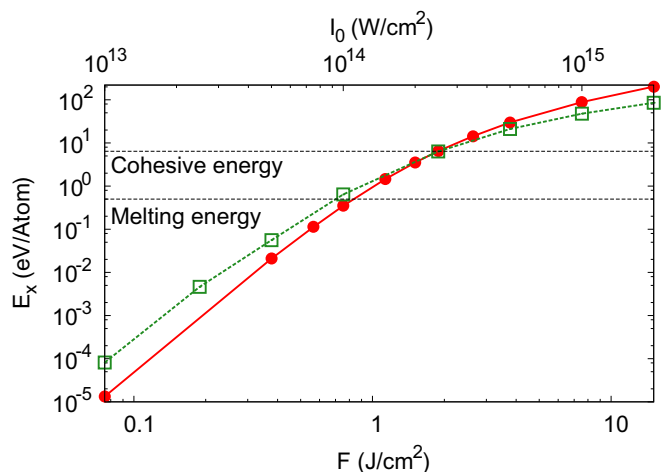


FIG. 2. (Color online) Deposited energy E_x at the surface of α -quartz is shown as a function of the fluence and the peak intensity of the pulse. Red circles show results using the mBJ potential, while green squares show results using the LDA functional [30].

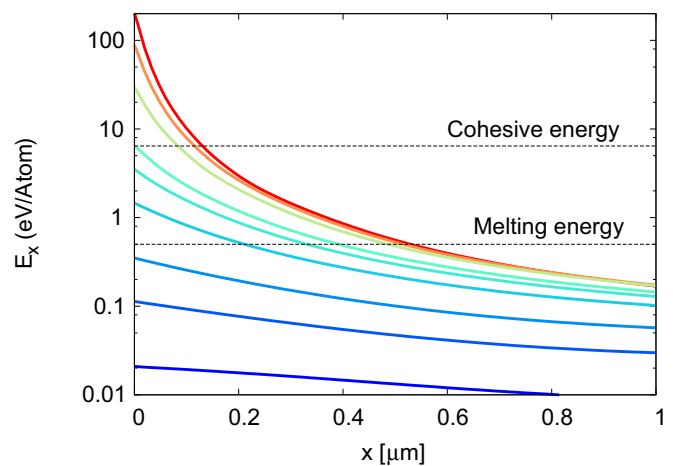


FIG. 3. (Color online) Deposited energy E_x in α -quartz as a function of distance below the surface. The curves show the results for intensities $I_0 = 0.5, 0.75, 1.0, 1.5, 2.0, 2.5, 5.0, 10.0, 20.0 \times 10^{14}$ W/cm² from lowest to highest graph. The pulse length is $\tau_p = 7$ fs for all intensities.

vaporization threshold as we have defined it is at ~ 2.5 J/cm². Thus, for applications that physically transform the material, we need to only consider fluences of the order 1.5 J/cm² and higher. Figure 2 shows the deposited energies of lower strength pulses as well, which may be of interest to analyze the parametric dependence of the energy deposition on the characteristics of the pulse. Figure 2 also shows the results for the LDA functional. One sees that lower-fluence pulses are more highly absorbed in LDA. This is to be expected due to the small band gap. The difference becomes small and even changes sign at high fluence. A possible explanation might be an increased screening for the LDA, as was discussed for the reflectivity.

The dependence of E_x on the depth in the medium is shown in Fig. 3 for a range of pulse intensities, all with pulse length of $\tau_p = 7$ fs. One sees that the melted region extends to a depth of 0.5–0.6 μ m for the stronger pulses. The depth permitting ablation only extends to 0.13 μ m for a pulse of 10 times the threshold intensity.

Figure 4 compares the pulse profile for the $I_0 = 10^{15}$ W/cm² pulse at two points, in the first cell and in the 80th cell at a depth of 1.06 μ m. At this depth, the intensity has decreased below the melting threshold. One sees that the shapes are quite similar. The main difference is that the attenuation is stronger in the later arriving cycles of the pulse train. This is to be expected; the early part of the pulse creates particle-hole pairs which can then modify the propagation of the rest of the pulse.

IV. APPROXIMATE DESCRIPTION

The mild changes in pulse shape suggest that the energy deposition might be modeled simply as a function of the strength of the pulse as it is attenuated in the medium. To see how well this works, we extract the local fluence of the pulses at the different cells in our simulation. The absorbed energy versus the local fluence for the range of pulses shown in Fig. 3 is plotted in Fig. 5. We see that they fall on a common

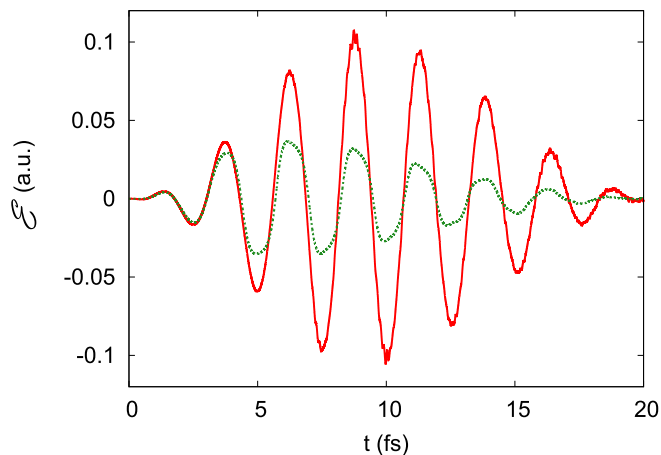


FIG. 4. (Color online) Pulse shapes at the first cell and at the 80th cell located at a depth of $1 \mu\text{m}$ are shown, for an incident pulse having intensity $I_0 = 10^{15} \text{ W/cm}^2$ and length $\tau_p = 7 \text{ fs}$.

line, extending down to a fluence of 1 J/cm^2 , well below the damage threshold. Thus, the change in pulse shapes can indeed be neglected, at least for $t_p = 7 \text{ fs}$ pulses. Remarkably, the dependence can be very well fitted following Keldysh's strong-field ionization rate equation [Ref. [14], Eq. (9)]. An approximate formula expressing the energy deposition in terms of the fluence is

$$E_x = AF^{5/4} \exp(-B/F^{1/2}). \quad (6)$$

The two-parameter fit [$A = 70 \text{ eV}(\text{J/cm}^2)^{-5/4}$, $B = 4.0 (\text{J/cm}^2)^{1/2}$] is shown as the solid black line in Fig. 5. One sees that the fit is valid from fluences from well below the thresholds to the highest calculated. The fit value $B = 4.0$ can be compared to the value obtained from a reduction of Keldysh's exponential factor,

$$B = \pi \tau_p^{1/2} m^{1/2} \varepsilon^{1/4} \Delta^{3/2} / 2, \quad (7)$$

in atomic units. Taking the reduced mass $m = 1/2$, the direct band gap $\Delta = 9 \text{ eV}$, and the dielectric constant $\varepsilon = 2.3$, Eq. (7) gives $B = 4.2$, a difference of only 5% from the fit value. The

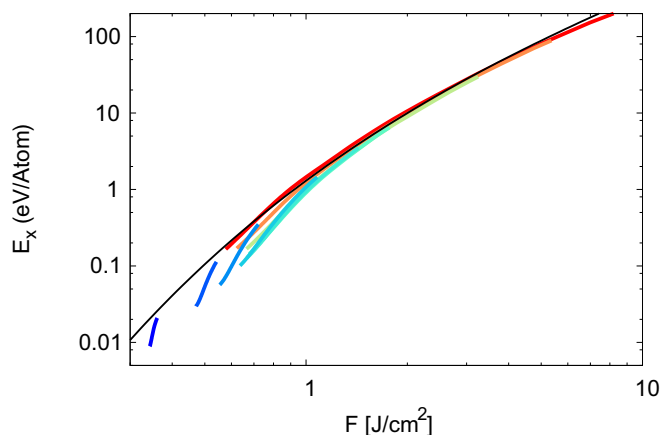


FIG. 5. (Color online) Absorbed energy is plotted as a function of local fluence of pulses. Black solid curve shows a fit by Keldysh's formula.

multiphoton process is only relevant at much lower fluences that are needed for structural changes.

V. EXPERIMENT

While it is not entirely clear how energy deposition profiles link to structural changes in the surface region, we can still compare the theory and experiment assuming that the melting and vaporization transitions control the surface damage and ablation. There are many measurements of thresholds for these quantities, but only a few for pulse as short as $\tau_p \sim 20 \text{ fs}$ or below [4,6,11,14]. Figure 6 shows a comparison with the data of Refs. [11,14] for fused silica. For the damage threshold shown by red symbols, we compare with calculated fluences to achieve $E_x = 0.5 \text{ eV/atom}$ at the surface. We see that the experimental threshold is in qualitative correspondence with that value.

The ablation threshold, shown by green symbols, is much lower than predicted by the $E_x = 6 \text{ eV/atom}$ criterion based on the formation of an atomic liquid [39]. This may indicate an importance of nonthermal effects in the ablation process by femtosecond laser pulses [40,41]. In fact, the reported thresholds for damage and ablation at $\tau_p = 7 \text{ fs}$ in Ref. [11] are nearly identical. This may be seen by the sharp edges of the ablation craters formed at the shortest pulse lengths. Perhaps one needs to consider a different mechanism for ablation at threshold, which may involve the electric fields produced when excited electrons are ejected from the surface. It should also be kept in mind that damage threshold depends on structures of the material; a lower threshold is reported for fused silica than crystalline SiO_2 using much longer pulses [42].

As a final theory-experiment comparison, we examine the depth of the ablated craters as a function of the fluence of the pulses. The available experimental data are shown in Fig. 7. For the theory we report the depth at which the deposited energy falls to $E_x = 6 \text{ eV/atom}$, as in Fig. 6. The agreement

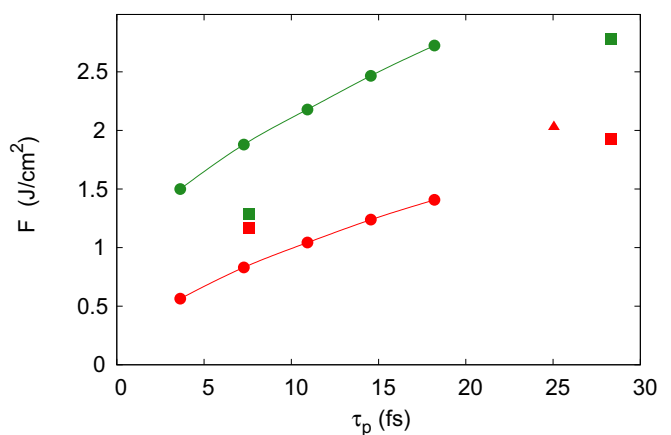


FIG. 6. (Color online) Threshold damage and threshold ablation fluences in SiO_2 are shown as a function of pulse width τ_p . Red and green circles are the calculated fluences to deposit an energy $E_x = 0.5 \text{ eV/atom}$ corresponding to a damage threshold and an energy $E_x = 6 \text{ eV/atom}$ corresponding to an ablation threshold in α -quartz, respectively. Experimental data from Ref. [11] for fused silica is shown with green and red squares; data from Ref. [14] is shown with a red triangle.

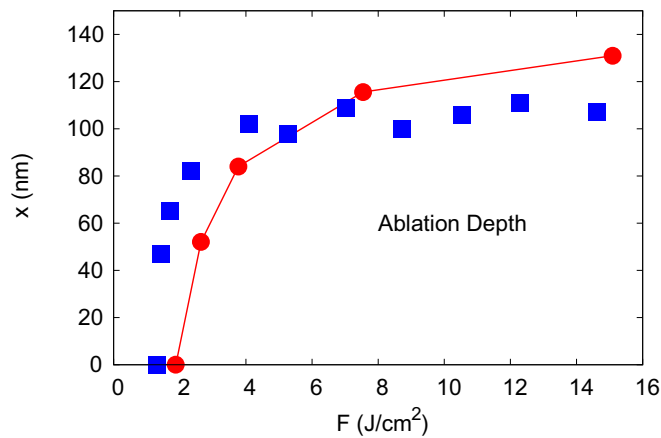


FIG. 7. (Color online) Depth of crater formed in SiO₂ by single laser pulses of length $\tau_p = 7$, as a function of the fluence of the original pulse. Experiment is shown in blue squares, from Ref. [12]. The red circles show the depth at which the calculated energy deposition falls below $E_x = 6$ eV/atom.

between theory and experiment is quite satisfactory. The theory reproduces the very sharp rise above threshold as well as the saturation at high fluences.

VI. CONCLUSION

We have shown that it is feasible to calculate the interaction of intense femtosecond laser pulses with insulating media by the TDDFT, avoiding the detailed modeling of plasma formation and dynamics required in earlier theoretical treatments.

The threshold for damage is accounted for by the calculated energy deposition needed to melt the quartz substrate. On the other hand, the calculated threshold for ablation via a transformation to an atomic liquid is 50% higher than the low values observed in two experiments. This may suggest the significance of a nonthermal mechanism in the ablation process. It may also indicate that another mechanism is responsible for the threshold behavior, such as an electric-field assisted ionic dissociation. However, we find good agreement with experiment on the depth of the ablation taking the energy deposition criterion to estimate the depth. It may well be that modeling energy deposition in wide-gap insulators could be greatly simplified once one has a suitable set of benchmark multiscale calculations based on the TDDFT. Since those calculations require much computer time, it would be useful to compare them to existing models [2,11,13,15–22] to validate assumptions in the models and to facilitate improved modeling of the phenomena.

ACKNOWLEDGMENTS

This work was supported by JSPS KAKENHI Grants No. 15H03674 and No. 26-1511, and was supported by Open Partnership Joint Projects of JSPS Bilateral Joint Research Projects. This work used computational resources of the K computer provided by the RIKEN Advanced Institute for Computational Science through the HPCI System Research project (Project ID: hp140103). G.F.B. acknowledges support by the US Department of Energy under Grant No. DE-FG02-00ER41132.

-
- [1] B. N. Chichkov, C. Momma, S. Nolte, V. von Alvensleben, and A. Tunnermann, *Appl. Phys. A* **63**, 109 (1996).
 - [2] B. C. Stuart, M. D. Feit, S. Herman, A. M. Rubenchik, B. W. Shore, and M. D. Perry, *Phys. Rev. B* **53**, 1749 (1996).
 - [3] X. Liu, D. Du, and G. Mourou, *IEEE J. Quantum Electron.* **33**, 1706 (1997).
 - [4] M. Lenzner, J. Krüger, S. Sartania, Z. Cheng, Ch. Spielmann, G. Mourou, W. Kautek, and F. Krausz, *Phys. Rev. Lett.* **80**, 4076 (1998).
 - [5] M. Geissler, G. Tempea, A. Scrinzi, M. Schnürer, F. Krausz, and T. Brabec, *Phys. Rev. Lett.* **83**, 2930 (1999).
 - [6] M. Lenzner, F. Krausz, J. Krüger, and W. Kautek, *Appl. Surf. Sci.* **154**, 11 (2000).
 - [7] L. Sudrie, A. Couairon, M. Franco, B. Lamouroux, B. Prade, S. Tzortzakis, and A. Mysyrowicz, *Phys. Rev. Lett.* **89**, 186601 (2002).
 - [8] G. Doumy, F. Quéré, O. Gobert, M. Perdrix, Ph. Martin, P. Audebert, J. C. Gauthier, J.-P. Geindre, and T. Wittmann, *Phys. Rev. E* **69**, 026402 (2004).
 - [9] S. Amoruso, G. Ausanio, R. Bruzzese, M. Vitiello, and X. Wang, *Phys. Rev. B* **71**, 033406 (2005).
 - [10] R. R. Gattass and E. Mazur, *Nat. Photon.* **2**, 219 (2008).
 - [11] B. Chimier, O. Utéza, N. Sanner, M. Sentis, T. Itina, P. Lassonde, F. Legare, F. Vidal, and J. C. Kieffer, *Phys. Rev. B* **84**, 094104 (2011).
 - [12] O. Utéza *et al.*, *Appl. Phys. A* **105**, 131 (2011).
 - [13] P. Balling and J. Schou, *Rep. Prog. Phys.* **76**, 036502 (2013).
 - [14] A.-C. Tien, S. Backus, H. Kapteyn, M. Murnane, and G. Mourou, *Phys. Rev. Lett.* **82**, 3883 (1999).
 - [15] A. Kaiser, B. Rethfeld, M. Vicanek, and G. Simon, *Phys. Rev. B* **61**, 11437 (2000).
 - [16] D. Perez and L. J. Lewis, *Phys. Rev. B* **67**, 184102 (2003).
 - [17] C. Rethfeld, K. Sokolowski-Tinten, D. von der Linde, and S. I. Anisimov, *Appl. Phys. A* **79**, 767 (2004).
 - [18] B. Rethfeld, *Phys. Rev. Lett.* **92**, 187401 (2004).
 - [19] J. R. Penano, P. Sprangle, B. Hafizi, W. Manheimer, and A. Zigler, *Phys. Rev. E* **72**, 036412 (2005).
 - [20] B. H. Christensen and P. Balling, *Phys. Rev. B* **79**, 155424 (2009).
 - [21] N. Brouwer and B. Rethfeld, *J. Opt. Soc. Am. B* **31**, C28 (2014).
 - [22] E. G. Gamaly, *Phys. Rep.* **508**, 91 (2011).
 - [23] L. V. Keldysh, *Sov. Phys. JETP* **20**, 1307 (1965).
 - [24] Y. Shinohara, K. Yabana, Y. Kawashita, J.-I. Iwata, T. Otobe, and G. F. Bertsch, *Phys. Rev. B* **82**, 155110 (2010).
 - [25] Y. Shinohara, S. A. Sato, K. Yabana, T. Otobe, J.-I. Iwata, and G. F. Bertsch, *J. Chem. Phys.* **137**, 22A527 (2012).
 - [26] T. Otobe, M. Yamagiwa, J.-I. Iwata, K. Yabana, T. Nakatsukasa, and G. F. Bertsch, *Phys. Rev. B* **77**, 165104 (2008).
 - [27] T. Otobe, K. Yabana, and J.-I. Iwata, *J. Phys. Condens. Matter* **21**, 064224 (2009).

- [28] K. Yabana, T. Sugiyama, Y. Shinohara, T. Otake, and G. F. Bertsch, *Phys. Rev. B* **85**, 045134 (2012).
- [29] S. A. Sato, K. Yabana, Y. Shinohara, T. Otake, and G. F. Bertsch, *Phys. Rev. B* **89**, 064304 (2014).
- [30] K.-M. Lee, C. M. Kim, S. A. Sato, T. Otake, Y. Shinohara, K. Yabana, and T. M. Jeong, *J. Appl. Phys.* **115**, 053519 (2014).
- [31] G. Wachter, C. Lemell, J. Burgdörfer, S. A. Sato, X.-M. Tong, and K. Yabana, *Phys. Rev. Lett.* **113**, 087401 (2014).
- [32] S. D. Brorson, J. G. Fujimoto, and E. P. Ippen, *Phys. Rev. Lett.* **59**, 1962 (1987).
- [33] W. S. Fann, R. Storz, H. W. K. Tom, and J. Bokor, *Phys. Rev. B* **46**, 13592 (1992).
- [34] S. A. Sato, Y. Shinohara, T. Otake, and K. Yabana, *Phys. Rev. B* **90**, 174303 (2014).
- [35] A. D. Becke and E. R. Johnson, *J. Chem Phys.* **124**, 221101 (2006).
- [36] F. Tran and P. Blaha, *Phys. Rev. Lett.* **102**, 226401 (2009).
- [37] J. P. Perdew and Y. Wang, *Phys. Rev. B* **45**, 13244 (1992).
- [38] L. Kleinman and D. M. Bylander, *Phys. Rev. Lett.* **48**, 1425 (1982).
- [39] D. G. Hicks, T. R. Boehly, J. H. Eggert, J. F. Miller, P. M. Celliers, and G. W. Collins, *Phys. Rev. Lett.* **97**, 025502 (2006).
- [40] P. Lorazo, L. J. Lewis, and M. Meunier, *Phys. Rev. Lett.* **91**, 225502 (2003).
- [41] T. Kumada, H. Akagi, R. Itakura, T. Otake, and A. Yokoyama, *J. Appl. Phys.* **115**, 103504 (2014).
- [42] S. Xu, J. Qiu, T. Jia, C. Li, H. Sun, and Z. Xu, *Opt. Commun.* **274**, 163 (2007).