

Lattice dynamics and vibrational spectra of the orthorhombic, tetragonal, and cubic phases of methylammonium lead iodide

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The hybrid halide perovskite $\text{CH}_3\text{NH}_3\text{PbI}_3$ exhibits a complex structural behavior, with successive transitions between orthorhombic, tetragonal, and cubic polymorphs around 165 and 327 K. Herein we report first-principles lattice dynamics (phonon spectrum) for each phase of $\text{CH}_3\text{NH}_3\text{PbI}_3$. The equilibrium structures compare well to solutions of temperature-dependent powder neutron diffraction. By following the normal modes, we calculate infrared and Raman intensities of the vibrations, and compare them to the measurement of a single crystal where the Raman laser is controlled to avoid degradation of the sample. Despite a clear separation in energy between low-frequency modes associated with the inorganic $(\text{PbI}_3^-)_n$ network and high-frequency modes of the organic CH_3NH_3^+ cation, significant coupling between them is found, which emphasizes the interplay between molecular orientation and the corner-sharing octahedral networks in the structural transformations. Soft modes are found at the boundary of the Brillouin zone of the cubic phase, consistent with displacive instabilities and anharmonicity involving tilting of the PbI_6 octahedra around room temperature.

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I. INTRODUCTION

Materials that adopt the perovskite crystal structure are known for their complex structural landscapes, with a large number of accessible polymorphs depending on the temperature, pressure, and/or applied electric field. For ternary ABX_3 perovskites, the A site cation is at the center of a cube formed of corner-sharing BX_6 octahedra. Displacement of the A cation is usually associated with a ferroelectric (Brillouin-zone center) instability, while tilting of the BX_6 octahedral network is usually linked to antiferroelectric (Brillouin-zone boundary) transitions [1,2].

Hybrid organic-inorganic perovskites are formed when one of the elemental perovskite building blocks is replaced by a molecular anion or cation [3,4]. There exists a large family of such compounds, including the widely studied formate perovskites, which contains both molecular anions and cations [5–7]. Hybrid *halide* perovskites are of current intense research effort due to their high-efficiency photovoltaic action [8–16].

Methylammonium lead iodide (MAPbI_3 , where MA represents the CH_3NH_3^+ cation) was first reported by Weber in 1978 [17]. It is the most relevant hybrid halide perovskite for photovoltaic application. The transition from orthorhombic to tetragonal to cubic perovskite structures as a function of temperature has been studied by techniques including

calorimetry and infrared spectroscopy [18], single-crystal x-ray diffraction [19], and dielectric spectroscopy [20]. Recently analysis of powder neutron-diffraction (PND) measurements has provided more quantitative insight into the temperature-dependent behavior of the MA cation within the anionic $(\text{PbI}_3^-)_n$ network [21]. There is now direct evidence for the degree of order of the MA cation in the different phases, and the average lattice parameters (and thus extent of octahedral tilting) as a function of temperature through the first- and second-order phase transitions. Quasielastic neutron scattering has provided further insight into the rotational dynamics of the MA cation with a room-temperature residence time of ~ 14 ps [22], while time-resolved vibrational spectroscopy has identified fast librations (300 fs) and slow rotations (3 ps) of the molecule [23].

In this study, we calculate the phonon dispersion in each phase of MAPbI_3 within the harmonic approximation, computing the force constants with density functional theory (DFT). We use the PBESol functional, which is a generalized-gradient approximation (GGA) to the exchange-correlation functional, numerically evaluated with Perdew's method, adjusted to give more accurate lattice constants and forces for solids [24]. The lattice dynamic calculations allow the atomic origin of each phonon mode to be identified. Changes in lattice polarization and polarizability for each eigenvector provide the infrared and Raman activity of each mode. Spectral features related to the inorganic and organic components (from 0 to 3000 cm^{-1}) are well reproduced in comparison to the Raman spectra of a single crystal of MAPbI_3 . Overlap is found between the vibrations of the CH_3NH_3^+ and PbI_3^- components up to 130 cm^{-1} , with the modes from 300 to 3000 cm^{-1} being associated with pure molecular vibrations. The phonon dispersion has implications for developing quantitative models for the generation,

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transport, and recombination of photogenerated electrons and holes in hybrid perovskite solar cells.

Structure models

The normal modes of a system are defined for an equilibrium configuration. Calculating the vibrations for a nonequilibrium structure will result in imaginary frequencies upon diagonalizing the dynamical matrix. Therefore, we have generated well-optimized structures of MAPbI₃. One challenge in calculating the phonons of hybrid perovskites is the soft nature and complicated potential-energy landscape of some of the restoring potentials, particularly those involving the organic cation.

The models for the crystal structures used in this study are discussed in detail below and a comparison with the measured diffraction patterns is provided as Supplemental Material [25].

1. Orthorhombic phase

The orthorhombic perovskite structure is the low-temperature ground state of MAPbI₃ and maintains its stability up to around 165 K [21,26,27]. A comparison of the enthalpy from DFT calculations confirms this ordering in stability. The difference in enthalpy is small, i.e., just 2 meV per MAPbI₃ unit, compared to the lowest energy tetragonal phase, yet 90 meV compared to the high-temperature cubic phase.

Initial diffraction pattern solutions are assigned to the $Pna2_1$ space group [18,26]. Recent analysis of higher-quality powder neutron-diffraction data reassigns it to $Pnma$ (a D_{2h} point group) [21]. The structure is a $\sqrt{2}a \times \sqrt{2}a \times 2a$ supercell expansion of the simple cubic perovskite lattice, i.e., following the lattice transformation matrix

$$\begin{pmatrix} 1 & -1 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 2 \end{pmatrix}. \quad (1)$$

In the $Pna2_1$ phase, the PbI₆ octahedra are distorted and tilt as $a^+b^-b^-$ in Glazer notation [1] with respect to the orientation of the conventional cubic cell. In this low-temperature phase, the four molecular cations in the unit cell are static on the diagonals of the ab planes pointing towards the undistorted facets of the cuboctahedral cavity. Correspondingly, molecules belonging to different planes are antialigned with a head-tail motif. Such an antiferroelectric alignment is expected from consideration of the molecular dipole-dipole interaction [28].

In the low-temperature orthorhombic phase, the CH₃NH₃⁺ sublattice is fully ordered (a low-entropy state). The ordering may be sensitive to the material preparation and/or cooling rate into this phase, i.e., the degree of quasithermal equilibrium. It is possible that different ordering might be frozen into the low-temperature phase by epitaxy or application of external force or electric fields.

2. Tetragonal phase

At 165 K, MAPbI₃ goes through a first-order phase transition from the orthorhombic to the tetragonal space group $I4/mcm$ (D_{4h} point group), which continuously undergoes a second-order phase transition to the cubic phase around 327 K [21,26,27]. As with the orthorhombic phase, this can

be considered a $\sqrt{2}a \times \sqrt{2}a \times 2a$ expansion of the cubic perovskite unit cell.

The molecular cations are no longer in a fixed position as in the orthorhombic phase. The molecules are disordered between two nonequivalent positions in each cage [27,30]. The tetragonal distortion parameter in the cubic basis is greater than unity ($\frac{c}{2a} \sim 1.01$ at 300 K), corresponding to an elongation of the PbI₆ octahedra along the c axis. The associated octahedral tilting pattern is $a^0a^0c^-$ in Glazer notation.

Atomistic simulations within periodic boundary conditions require an ordered configuration. The solved crystal structure shows that there are several possible configurations for the organic cations within the tetragonal unit cell. These configurations have similar enthalpies within DFT [31], which is consistent with the observed disorder. We choose to use the most energetically stable structure, which is also consistent with a previous DFT investigation [32].

In the model of the tetragonal structure, the MA cations are aligned as in the orthorhombic phase, towards the face of the perovskite cage, i.e., $\langle 100 \rangle$ in the cubic basis. The MA in different (001) planes are approximately orthogonal to one another. The orientational dynamics of the methylammonium ions, which exists above 165 K, is not taken into account in this equilibrium configuration study.

3. Cubic phase

With increasing temperature, the tetragonal lattice parameters become more isotropic (i.e., $\frac{c}{2a}$ moves closer to 1) and the molecular disorder increases, to the point where a transition to a cubic phase occurs around 327 K. The transition can be seen clearly from changes in the heat capacity [18] as well as in temperature-dependent neutron diffraction [21].

The cubic space group $Pm\bar{3}m$ (O_h symmetry) has been assigned to this high-temperature phase. Although the methylammonium ions possesses C_{3v} symmetry, the orientational disorder gives rise to the effective higher symmetry on average. The local structure will necessarily have a lower symmetry. Indeed, for the bromide and chloride analogues of MAPbI₃, pair-distribution function analysis of x-ray scattering data indicates a local structure with significant distortion of the lead halide framework at room temperature [33].

We previously considered alignment of the molecules along the principal $\langle 100 \rangle$ (face), $\langle 110 \rangle$ (edge), and $\langle 111 \rangle$ (diagonal) directions of the cubic unit cell, and showed that they are of similar DFT enthalpy, with a small barrier for rotation [34]. Further *ab initio* molecular dynamics showed an average preference for the $\langle 100 \rangle$ facial configuration at 300 K [28]. Therefore, we chose the $\langle 100 \rangle$ configuration as our reference structure for the lattice vibrations.

Representations of the crystal structure of each phase are shown in Fig. 1, the equilibrium structure parameters are listed in Table I, and the structures themselves are available in an online repository [29].

II. METHODS

A. Computations

The total energy and atomic forces were computed from first principles within density functional theory as implemented

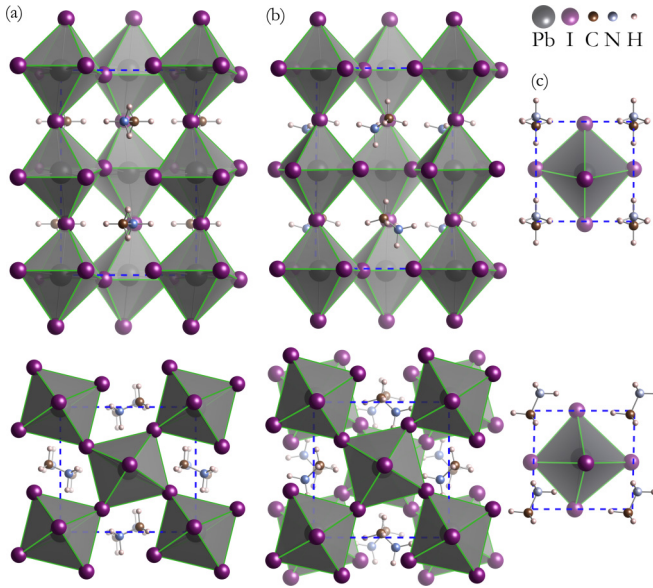


FIG. 1. (Color online) The crystal structures of the (a) orthorhombic, (b) tetragonal, and (c) cubic phases of $\text{CH}_3\text{NH}_3\text{PbI}_3$. The upper and lower panels are oriented through (100) and (001) , respectively. Lattice parameters and coordinates obtained from powder neutron diffraction were optimized using density functional theory (PBESol). The PbI_6 octahedra are shaded gray. All structures are available in an online repository [29].

in the code VASP [36,37]. Noise in the lattice vibrations was minimized by rigorous convergence of total Kohn-Sham energy with respect to the basis set (kinetic-energy cutoff for plane waves) and sampling of reciprocal space (density of the k -point mesh). The final computational setup is summarized in Table I.

We performed complete optimization of the cell volume, shape, and atomic positions, with the PBESol [24] semilocal exchange-correlation functional. The scalar-relativistic projector-augmented wave method [38] was employed, with a pseudopotential treating the Pb $5d$ orbitals as valence. Spin-orbit coupling was not considered as it mainly affects the Pb $6p$ conduction band, which does not influence the interatomic interactions at equilibrium. All atomic forces were reduced to below a threshold of $1 \text{ meV}/\text{\AA}$. Due to the presence

of the organic cations, which break the ideal lattice symmetry, deviations in the expected parameters can occur, e.g., in the high-temperature pseudocubic phase, the three equilibrium lattice parameters are not equal. The equilibrium structure parameters (at 0 K and excluding zero-point contributions) are reported in Table I.

The normal modes are calculated within the harmonic approximation, using the PHONOPY [39–41] package to construct and evaluate the dynamical matrix composed of DFT force constants. Both the finite displacement method (FDM or supercell approach) [42] and density functional perturbation theory (DFPT) [43] approaches to construct the force constants were tested. The results of both approaches produced similar vibrational spectra, with a variance in the mode energies of 6 cm^{-1} .

Within a primitive cell of N atoms, there are $6N$ possible displacements ($\pm x, \pm y, \pm z$), which can be reduced by the crystal symmetry. For the orthorhombic phase, the 288 possible displacements are reduced to 41, while the tetragonal and cubic phases required 288 and 72 displacements, respectively. The phonon dispersion (for \mathbf{q} points away from the Brillouin-zone center, the Γ point) in the cubic phase was probed in a $2 \times 2 \times 2$ supercell. Due to computational expense, we did not calculate this for the other (larger unit cell) phases, where the phonons are considered at the Γ point only.

Once the normal eigenmodes and eigenvalues are calculated, it is possible to model their associated Raman and infrared (IR) activity by mode following. The two spectroscopic techniques probe different physical responses of the material: the change in polarization for IR and the change in polarizability for Raman. The IR spectra are simulated with the analytic formula of Gianozzi and Baroni (using the Born effective charge tensor) [43]. Prediction of the Raman spectra required computing the change in macroscopic dielectric tensor with respect to each normal mode of the system, a significant DFT calculation in terms of computational expense [44].

B. Experiment

Methylammonium lead iodide single crystals were grown according to the method of Poglitsch and Weber [26]. 12.5 g of lead acetate trihydrate [$\text{Pb}(\text{CH}_3\text{CO}_2)_2 \cdot 3 \text{H}_2\text{O}$, Sigma] was

TABLE I. Equilibrium cell parameters from DFT/PBESol energy minimization, including the converged plane-wave cutoff, k -point mesh, and force threshold. Z represents the number of formula units of $\text{CH}_3\text{NH}_3\text{PbI}_3$ per cell. The calculated difference in enthalpy (ΔH) of each phase is given with respect to the ground-state orthorhombic configuration and per $\text{CH}_3\text{NH}_3\text{PbI}_3$ unit. Shown for comparison are the cell parameters and average Pb-I interatomic separations (d) from powder neutron diffraction (PND) [21].

Phase	a (\AA)	b (\AA)	c (\AA)	$d(\text{Pb-I})$ (\AA)	Z	Cutoff (eV)	k points	Forces ($\text{meV}/\text{\AA}$)	ΔH (meV)
Orthorhombic									
DFT/PBESol	9.04	12.66	8.35	3.18	4	700	$5 \times 4 \times 5$	1	0
PND (100 K)	8.87	12.63	8.58	3.19					
Tetragonal									
DFT/PBESol	8.70	8.72	12.83	3.19	4	800	$5 \times 5 \times 3$	1	2
PND (180 K)	8.81	8.81	12.71	3.17					
Cubic									
DFT/PBESol	6.29	6.23	6.37	3.17	1	700	$6 \times 6 \times 6$	1	90
PND (352 K)	6.32	6.32	6.32	3.16					

dissolved in 10 mL hydroiodic acid (HI_{aq} , 57 wt%, Sigma) in a 50 mL round bottom flask and heated to 100 °C in an oil bath. Separately, 0.597 g of CH_3NH_2 (aq, 40 wt%, Sigma) was added dropwise to a further 2 mL of HI_{aq} kept at 0 °C in an ice bath under stirring. The methylammonium iodide solution was then added to the lead acetate solution and the mixture was cooled over five days to a temperature of 46 °C, resulting in the formation of black crystals with largest face length around 8 mm. The content of the flasks was subsequently filtered and dried for 12 hours at 100 °C.

Raman spectra were collected in backscattering geometry with a high-resolution LabRam HR800 spectrometer using a grating with 600 lines per millimeter and equipped with a liquid-nitrogen-cooled charge coupled device (CCD) detector. The 785 nm line of a diode-pumped solid-state laser was used as excitation beam and focused onto the sample using a long-distance 20× microscope objective. Raman measurements were carried out at 100 K using a gas-flow-type cryostat with optical access that fits under the microscope of the Raman setup. The high spectral resolution and stray-light rejection of the LabRam spectrometer, particularly in combination with the 785 nm line, allowed us to measure the Raman spectrum of MAPI at very low Raman shifts down to 20 to 30 cm^{-1} . In this way, we were able to spectrally resolve several low-frequency modes associated with vibrations of the inorganic cage of the hybrid perovskite.

Heating by laser light directly absorbed by $\text{CH}_3\text{NH}_3\text{PbI}_3$ has been shown to lead to rapid degradation of the material, resulting in PbI_2 Raman signatures [45]. Since 785 nm light is only weakly absorbed, the heating effect of the laser was low enough to ensure the crystal structure was preserved. The power density incident on the sample was kept at 80 W/cm^2 . At such power level, it was checked that no appreciable spectral changes in peak width and/or position occurred, while still providing a good signal-to-noise ratio. Further, samples were kept under vacuum inside the cryostat during the measurements.

III. RESULTS

A. Harmonic phonons

The full phonon density of states (DOS) is shown for the three phases of $\text{CH}_3\text{NH}_3\text{PbI}_3$ in Fig. 2. Also plotted is the partial DOS, where assignment to CH_3NH_3^+ or PbI_3^- is performed based on the atomic contribution to each eigenvector. An animation of all 36 eigenmodes of the cubic phase is provided as Supplemental Material [25].

Qualitatively, each MAPbI_3 phase shows similar vibrational properties with three energetic regions of phonons: (i) a low-frequency band from 0–150 cm^{-1} , (ii) a midfrequency band from 280–1600 cm^{-1} , and (iii) a high-frequency band from 2900–3300 cm^{-1} . These ranges are consistent with previous computational reports [46,47].

Due to the large difference in atomic mass of the organic and inorganic components, and to the difference in bonding between the inorganic cage and the covalently bonded molecule, we anticipated that the low-frequency modes would be comprised entirely of motion by the PbI_6 octahedra, while the high-frequency modes would involve the CH_3NH_3^+ cation.

This is qualitatively the case, but there is also significant coupling between the two. Taking the example of the cubic phase with 36 modes, the highest-energy 18 modes [forming bands (ii) and (iii)] correspond to molecular vibrations, i.e., the $3N-6$ modes of the methylammonium ion. For an isolated nonlinear molecule, the 6 translational and rotational degrees of freedom do not contribute to the pure vibrational spectrum, but this is not the case for a molecule inside a cuboctahedral cavity.

The 6 additional molecular modes are strongly coupled to the 9 modes (i.e., $3N-3$ for PbI_3^-) associated with stretching of the Pb-I bonds and breathing of the PbI_6 octahedra, which results in the spectral overlap observed in the partial DOS of band (i). Particularly striking is the low-frequency pivoting motion associated with the libration of the molecular dipole, coupled with a breathing of the octahedral framework (e.g., modes 10 and 15 in the SI). The final three zero-frequency modes correspond to acoustic translations of the lattice.

B. Vibrational spectra

For MAPbI_3 , it is not possible for the relaxed (nonidealized) crystal structures to assign the spectral activity directly with group theoretic irreducible representation analysis of the phonon modes. The molecule breaks the average crystal symmetry. This symmetry lowering allows for simultaneous Raman and IR activity, even in the pseudocubic phase. The predicted spectra (the Γ -point phonon modes weighted by the computed spectral intensity, convolved with a Lorentzian for experimental comparison) are reported in Fig. 2 for each phase.

Raman and IR activity is observed across each of the three phonon bands previously discussed. A notable exception is the lowest-energy purely molecular vibration near 300 cm^{-1} , which is neither Raman nor IR active.

To understand the effect of embedding the methylammonium in MAPbI_3 , we calculate the normal-mode vibrations of an isolated methylammonium ion in vacuum with a similar density functional theory method to our periodic calculations Perdew-Burke-Ernzerhof (PBE) with an atom-centered augmented cc-pVQZ basis set. Thereby, we calculate the 18 molecular modes, directly accessing their symmetries and nature. The C_{3v} symmetry of the molecule separates the vibrational bands into one A symmetric mode and blueshifted twofold degenerate asymmetric E modes. The six bands we find are in ascending energy: twist around the C-N axis (282, 886 cm^{-1}), vibration along the C-N axis (923, 1239 cm^{-1}), bending of the C-H bonds (1418, 1451 cm^{-1}), bending of the N-H bonds (1478, 1622 cm^{-1}), stretching of the C-H bonds (3018, 3119 cm^{-1}), and stretching of the N-H bonds (3321, 3395 cm^{-1}).

As the cation charge density is centered towards the N, the motion of the protons associated with N have the strongest affect on the dipole moment and therefore strongest IR activity. Due to the stronger bonds, their frequencies are consistently blueshifted relative to the C end. Owing to the molecular dipole moment (2.2 D [28], which is rotation and position invariant, and corresponds to a polarization contribution of $\sim 3 \mu\text{C}/\text{cm}^2$), the two high-frequency asymmetric stretching modes of NH_3^+ [band (iii)] results in the strongest absolute IR intensity. The hydrogen stretching modes [band (iii)] are responsible for

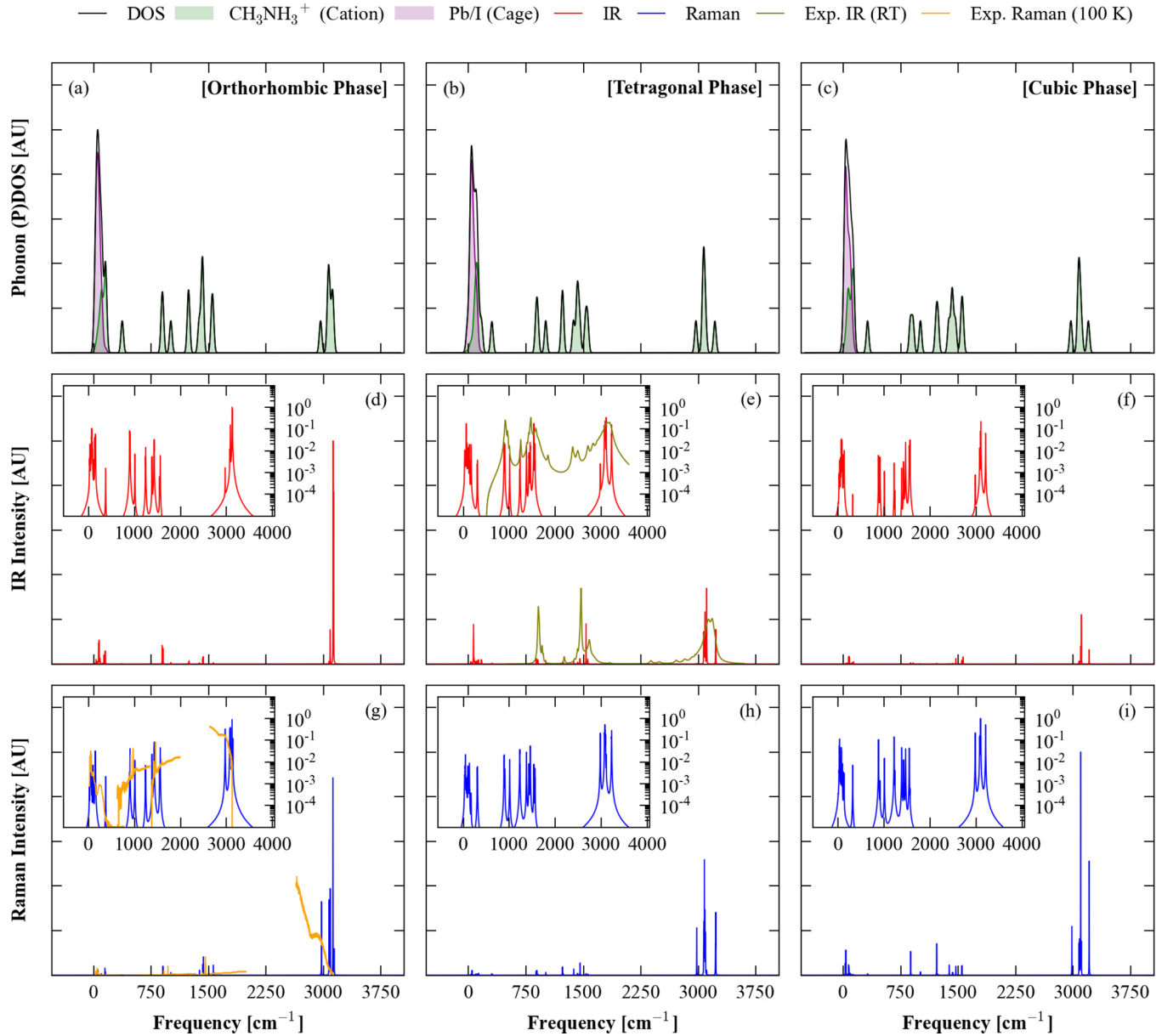


FIG. 2. (Color online) (a)–(c) Projected phonon density of states (PDOS) for the three phases of $\text{CH}_3\text{NH}_3\text{PbI}_3$ as calculated from DFT/PBESol, generated by convolution with a 16 cm^{-1} Lorentzian. Note that no imaginary (negative) modes are found in the orthorhombic or tetragonal phases. (d)–(f) Simulated infrared (IR) spectra. (e) The measured IR spectrum at 300 K from Ref. [35] is coplotted in green (light gray). (g)–(i) Simulated Raman spectrum. (g) The measured Raman spectrum of a single crystal in the orthorhombic phase at 100 K is coplotted in orange (light gray). Simulated spectra were broadened by convolution with a 2 cm^{-1} Lorentzian. Insets in the simulated spectra are the same data on a logarithmic scale to show the structure in the low-intensity modes.

significant Raman activity. The only mode involving C or N motion is the weakly IR and Raman active vibration at 923 cm^{-1} (vacuum), 1007 cm^{-1} (cubic perovskite).

The rotation of the CH_3 against the NH_3 unit, while being strongly populated in molecular dynamic simulations, and which forms the main source of quasi-inelastic neutron scattering, is entirely IR and Raman inactive in vacuum. This is the mode responsible for the 282 cm^{-1} (vacuum), 318 cm^{-1} (cubic), $300\text{--}310 \text{ cm}^{-1}$ (tetragonal), $370\text{--}372 \text{ cm}^{-1}$ (orthorhombic) vibration. Progressive confinement of MA from vacuum to the orthorhombic phase blueshifts the energy of the vibration.

In the solid state, the degeneracies in the molecular modes are typically split by local environment effects, peaks are both redshifted and blueshifted, and the IR and Raman activity varies. As such, it is evident that analysis of the Raman and IR spectra in the experimentally easily accessible molecular frequency range can enable statements to be made about the local structure and configuration of the hybrid perovskite. Our data is collected for a particular representation of the cubic and tetragonal phase; in reality, the location of the MA in these phases will be disordered. As such, a detailed comparison of theory to experiment will require sampling the thermodynamic ensemble of structures.

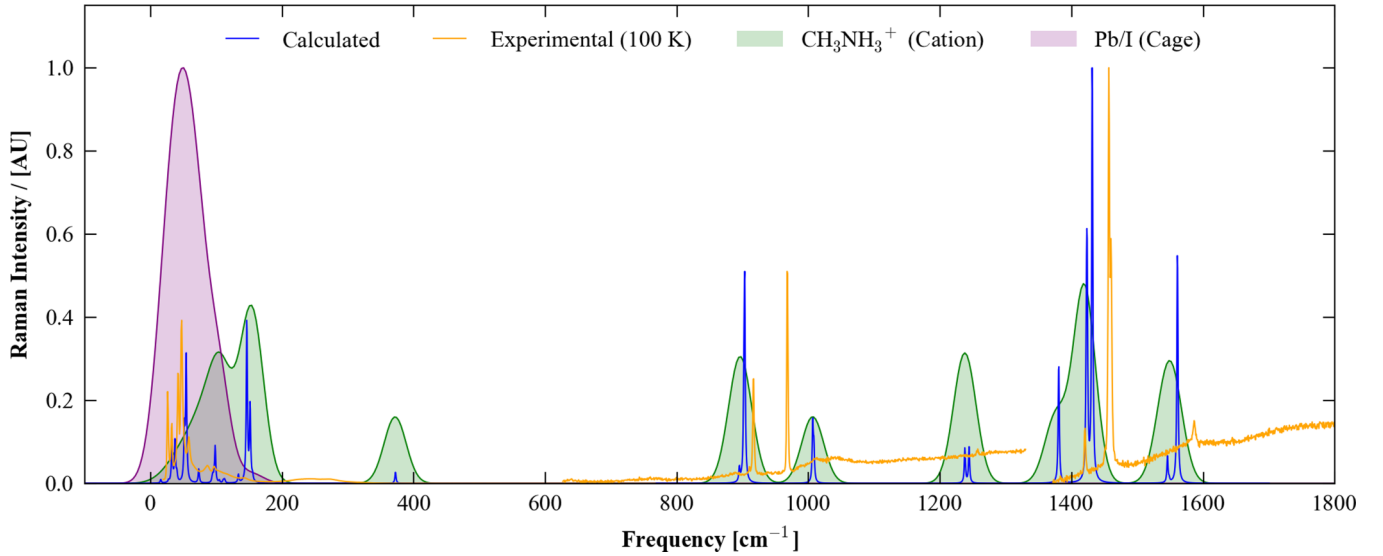


FIG. 3. (Color online) Comparison of the calculated and measured (100 K) Raman spectrum for the orthorhombic perovskite phase of $\text{CH}_3\text{NH}_3\text{PbI}_3$ in the range 0–1800 cm^{-1} , which includes phonon modes centered on the inorganic cage (lowest frequency), organic cage (highest frequency), and coupled modes (intermediate frequency). The simulated spectrum was broadened by convolution of a 2 cm^{-1} Lorentzian, while the underlying phonon density of states is shown for comparison with a broadening of 32 cm^{-1} .

Here, Raman spectra for the three phases is reported across the full frequency range. The spectrum up to 450 cm^{-1} was reported in Ref. [46]. Reliable measurements are a challenge due to chemical instability of the material. MAPbI_3 is strongly affected by environmental conditions, such as the presence of ambient moisture [27,48]. Isolated in vacuum, the material can still decompose and bleach due to heating, including by that imposed by the (typically high) Raman laser fluence [45]. Such degradation leads to the formation of PbI_2 , which overlaps in Raman spectra with MAPbI_3 , and so easily leads to misinterpretation.

The Raman spectra of a high-quality single crystal of MAPbI_3 is shown in Fig. 2, and compared in detail with the calculations in Fig. 3. Across the full spectral range, the agreement between the predicted and measured spectra is good, with the response across bands (i)–(iii) well reproduced. On closer inspection of Fig. 3, there are noticeable shifts in peak positions, which can be attributed to three potential sources of error: (a) the harmonic approximation (anharmonic renormalization may be large), (b) the limits of the exchange-correlation treatment (nonlocal interactions may be important), and (c) the assumption of a fully ordered structure (local inhomogeneity may be prevalent). There is also a notable case of an absence of measured Raman activity around 150 cm^{-1} , which we can tentatively attribute to a lifetime broadening effect. The same level of theory applied to the lead-based semiconductors PbS and PbTe results in quantitative agreement with measured phonon frequencies and dispersion [49], which highlights the complex nature of $\text{CH}_3\text{NH}_3\text{PbI}_3$.

We have also included in Fig. 2 a room-temperature IR spectrum reported by Glaser *et al.* [35], which again shows excellent agreement across the spectrum. A number of very weak absorption peaks below 3000 cm^{-1} are evident,

which could be related to molecular disorder and/or partial decomposition. The temperature-resolved (between 140 and 299 K) IR spectra for tetragonal and orthorhombic phases have been previously reported by Yamamuro [50]. We reproduce the position and the intensity of the peak observed at 900 cm^{-1} , reliably assigning it to the (also Raman-active) C-N bond stretch. High-quality IR measurements, in particular looking at the very low-energy transitions, would provide considerable information on the nature of the domains and local structure in a MAPbI_3 film.

C. Anharmonic effects

The lattice dynamic simulations discussed above were performed within the harmonic approximation. All eigenmodes at the center of the Brillouin zone were real (positive frequencies) for each phase, i.e., the structures are locally stable.

The phonon dispersion across the first Brillouin zone is shown for the cubic perovskite structure in Fig. 4. Here imaginary (negative frequency or “soft”) modes are found at the zone boundaries. Such instabilities are a common feature of the perovskite structure and represent antiferroelectric distortions linked to rotations and tilting of the octahedra in neighboring unit cells [2]. The soft modes are centered around the R and M points, which correspond to the $\langle 111 \rangle$ and $\langle 110 \rangle$ directions in the cubic lattice. This behavior is similar to the inorganic perovskite CsPbCl_3 , where neutron scattering was used to probe condensation of these modes, which leads to successive transitions from the cubic to tetragonal to orthorhombic phases [51]. The effect of these modes in MAPbI_3 , and the associated high levels of anharmonicity at room temperature, can be observed directly in molecular dynamics simulations, where temporal rotations of the CH_3NH_3^+ ions and distortions of the PbI_6 octahedra have been found in several studies [22,28,52].

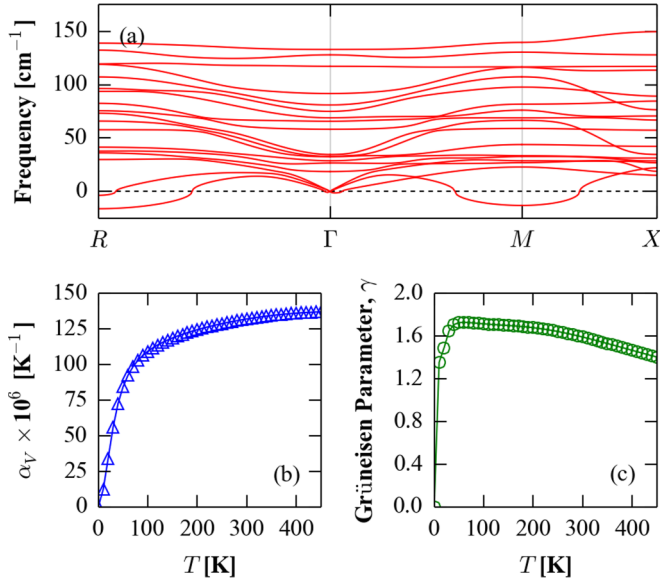


FIG. 4. (Color online) Vibrational properties of the cubic phase of MAPbI₃: (a) Phonon dispersion of the low-frequency (inorganic cage) modes within the harmonic approximation. Negative frequency (imaginary or “soft”) modes are found at the Brillouin-zone boundary points $M[\frac{2\pi}{a}(\frac{1}{2}, \frac{1}{2}, 0)]$ and $R[\frac{2\pi}{a}(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})]$. (b) Volumetric thermal expansion within the quasiharmonic approximation. (c) Average Grüneisen parameter within the quasiharmonic approximation.

An approach to include the effects of temperature (thermal expansion) and first-order anharmonicity in lattice dynamic calculations is the quasiharmonic approximation (QHA) [53,54]. The computational cost is one order of magnitude higher than the harmonic approximation and thus was considered for the cubic phase only. The volumetric thermal-expansion coefficient extracted from the PND data at 300 K is $1.32 \times 10^{-4}/\text{K}$, which compares very well to the value of $1.25 \times 10^{-4}/\text{K}$ computed within the QHA. The predicted thermal expansion for MAPbI₃ is similar to inorganic semiconductors (e.g., for PbTe, the value is $0.7 \times 10^{-4}/\text{K}$ at 300 K [40]) and positive over the full temperature range.

The temperature dependence of the phonon modes can be described by the Grüneisen parameter, which has an average of around 1.6 (see Fig. 4), slightly below the value of 1.7 found in PbI₂ [55]. The imaginary modes at R and M remain at all temperatures, consistent with the cubic lattice being a dynamic average of a locally distorted structure; the same phenomenon is observed in CsSnI₃ [56]. The high level of anharmonicity associated with the soft tilting modes is consistent with the “ultralow” ($<1 \text{ W m}^{-1} \text{ K}^{-1}$ at 300 K) lattice thermal conductivity reported for single crystals and polycrystalline MAPbI₃ [57]. Hybrid halide perovskites are thus also promising for application in thermoelectric devices if thermal-stability issues can be overcome [58].

IV. CONCLUSIONS

The vibrational frequencies of three crystallographic phases of the hybrid perovskite CH₃NH₃PbI₃ have been investigated. We identified three main phonon branches present in the three phases. Two high-frequency branches are associated with the vibration and bond stretching of the molecular cation with frequencies in the range 300 to 3300 cm⁻¹. The lowest-energy branch, below 150 cm⁻¹, arises predominately from the inorganic cage, but with half of the modes coupled to the motion of the molecule. The simulated Raman spectrum of the orthorhombic phase is in good agreement with measurements on a single crystal of MAPbI₃. Dynamic instabilities occur at the zone boundaries of the cubic phase, which requires methods beyond the harmonic approximation, such as self-consistent phonon theory, for an accurate treatment. These results suggest that the room-temperature structure of MAPbI₃ is fluctuational, owing to the persistent tilting and distortion of the octahedral networks and rotations of the molecular cations.

These factors may be important for developing a quantitative understanding and model of how hybrid perovskite solar cells operate. Upon excitation, the relative stability of free carriers and excitons depends intimately on the dielectric screening of the material, which includes vibrational and rotational components. The transport and recombination of photogenerated charge carriers will also be influenced by electron-phonon coupling, which can significantly reduce the effective size and distribution of electrons and holes within the perovskite layer.

Note added in proof. A neutron scattering investigation of MAPbBr₃ has very recently been reported [59], which identifies strong coupling between the vibrations of the molecule and the inorganic cage, analogous to the overlap identified in our study of the iodide material. A soft mode associated with octahedral tilting is also measured that is in support of our observations.

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