Perturbation on hyperfine-enhanced ¹⁴¹Pr nuclear spin dynamics associated with antiferroquadrupolar order in PrV₂Al₂₀

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The nature of multipolar order and hyperfine-enhanced (HE) 141 Pr nuclear spin dynamics in PrV_2AI_{20} was investigated using the muon spin relaxation technique. No explicit sign of time-reversal symmetry breaking was found below the multipolar order temperature $T_Q \sim 0.6$ K in a zero applied field as anticipated on the basis of the antiferroquadrupolar (AFQ) order picture proposed by Sakai and Nakatsuji [J. Phys. Soc. Jpn. 80, 063701 (2011)]. Further evidence of the nonmagnetic ground state was obtained from the observation of HE 141 Pr nuclear spin fluctuations in the MHz scale. A marked increase in the muon spin-lattice relaxation rate $(1/T_{1,\mu})$ was observed below 1 K with decreasing temperature, which was attributed to the perturbation on the HE 141 Pr nuclear spin dynamics associated with the development of AFQ correlations. The longitudinal field dependence of $1/T_{1,\mu}$ revealed that the enhanced 141 Pr nuclear spin accidentally has an effective gyromagnetic ratio close to that of the muon.

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I. INTRODUCTION

Recently, considerable attention has been paid to the quadrupolar degrees of freedom (DOF) of 4f electrons in Pr-based compounds with the non-Kramers Γ_3 crystalline-electric-field (CEF) ground doublet. Various novel phenomena related to Γ_{3g} quadrupoles, such as incommensurate quadrupolar order, multichannel Kondo effects, quadrupolar quantum criticality, and consequent heavy fermion superconductivity, have been intensively studied [1–7]. However, experimental techniques to probe quadrupolar properties are still quite limited. The development of new methodologies is critical for the further advancement of this research field.

The hyperfine enhancement of 141 Pr nuclear magnetism is a common phenomenon for Γ_1 and Γ_3 CEF ground multiplets without dipolar DOF [8–11]. This effect arises from the Van Vleck–like admixture of magnetic CEF excited multiplets into the nonmagnetic ground multiplets as a result of strong intra-atomic hyperfine coupling [8]. The 141 Pr nuclear spin-spin interaction is mediated by electronic exchange between hyperfine-induced 4f moments. Therefore, the 4f quadrupolar state in the Γ_3 ground doublet can potentially be probed via hyperfine-enhanced (HE) 141 Pr nuclear spin dynamics.

In this paper, we report an observation of quadrupole-induced perturbation on HE $^{141}{\rm Pr}$ nuclear spin dynamics in the Γ_3 ground doublet system ${\rm PrV_2Al_{20}}$ using the muon spin relaxation ($\mu{\rm SR}$) technique. ${\rm PrV_2Al_{20}}$ shows multipolar order at $T_Q\sim 0.6$ K, which is well below the temperature corresponding to the first excited CEF level at $\Delta_{\rm ex}/k_B\sim 40$ K [5]. The primary order parameter is supposed to be a Γ_{3g} quadrupole based on active multipolar DOF in the Γ_3 ground doublet, entropy release $<\!R\,{\rm ln2}$, and magnetization [5,12]. These are similar to those in isostructural ${\rm PrTi_2Al_{20}}$ ($T_Q\sim 2.0$ K [5], $\Delta_{\rm ex}/k_B\sim 65$ K [13]); however, the field

dependences of the specific-heat anomalies at T_O are totally different. The width of the specific-heat peak becomes broader with increasing field in PrTi₂Al₂₀, whereas it is almost field-independent in PrV₂Al₂₀ [5]. These responses to applied magnetic fields suggest ferro- and antiferro-quadrupolar (FQ and AFQ) order in Ti and V compounds, respectively. In PrTi₂Al₂₀, the FQ order has been definitely identified from microscopic points of view using μ SR, NMR, and neutron scattering techniques, and the primary order parameter has been determined to be an O_2^0 -type Γ_{3g} quadrupolar moment [13-15]. In contrast, no direct microscopic evidence of the putative AFQ order in PrV₂Al₂₀ has been provided to date. Herein, we first establish the nonmagnetic nature of the primary order parameter in PrV₂Al₂₀ from the µSR point of view using its high sensitivity to local magnetic fields. This provides a strong justification for the AFQ order and AFQ quantum criticality at ambient pressure [5,7,16]. Next, we show that the muon spin-lattice relaxation rate $(1/T_{1,\mu})$ exhibits a steplike change at around T_O , which can be attributed to the perturbation on the strength of electron-mediated ¹⁴¹Pr nuclear spin interactions. A comparison is made with the flat temperature dependence of $1/T_{1,\mu}$ reported for the FQ compound PrTi₂Al₂₀ [14].

II. EXPERIMENTAL

Single-crystalline samples of PrV_2Al_{20} were prepared by the Al self-flux method [5]. Pulsed μ SR measurements were performed under a zero applied field (ZF) and longitudinal magnetic fields (B_0) at the D1 area of the J-PARC muon facility, Tokai, Japan, using the D Ω 1 spectrometer. μ SR spectra were recorded over the temperature ranges of 0.045–3 and 3–40 K with a 3 He- 4 He dilution refrigerator and a conventional 4 He flow cryostat, respectively. The PrV_2Al_{20} single crystals were randomly aligned and glued on silver sample holders with commercial Apiezon N grease. Spin-polarized single-bunch muon pulses were incident on the samples with initial muon

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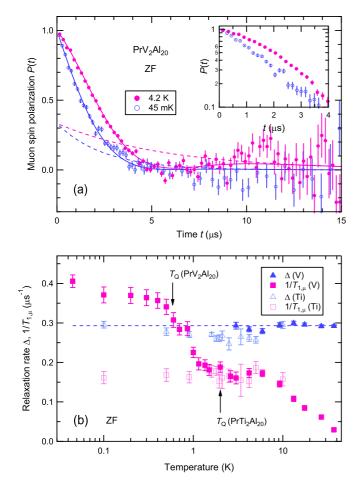


FIG. 1. (Color online) (a) ZF- μ SR spectra of PrV₂Al₂₀ at 4.2 K (closed circles) and 45 mK (open circles). The solid curves represent the best fits to Eq. (1). The broken curves designate the 1/3 component. The inset shows the same data with P(t) plotted on a log scale. (b) Δ (triangles) and $1/T_{1,\mu}$ (squares) under ZF in PrV₂Al₂₀ (closed symbols) and PrTi₂Al₂₀ (open symbols, data from Ref. [14]) as functions of temperature. The broken line represents the average value of Δ for PrV₂Al₂₀.

spin polarization P(t=0) antiparallel to the beam incident direction. μ -decay positrons were detected by forward and backward positron counters. Because our samples do not show any sign of superconductivity down to 0.045 K, a possibility of time-reversal symmetry breaking associated with superconductivity can be ignored.

III. RESULTS AND DISCUSSION

Figure 1(a) shows the ZF- μ SR spectra of PrV₂Al₂₀ at 4.2 and 0.045 K. P(t) is the projection of P(t) onto the beam incident axis, and it has been normalized after subtracting the background signal from the silver sample holders. P(t) at 4.2 K above T_Q exhibits a Gaussian-like damping in the early-time region and a slight recovery after 6 μ s. These features can be modeled well with the function

$$P(t) = e^{-t/T_{1,\mu}} G_{KT}(t; \Delta, B_0 = 0)$$

= $\frac{1}{3} e^{-t/T_{1,\mu}} + \frac{2}{3} (1 - \Delta^2 t^2) e^{-\frac{1}{2} \Delta^2 t^2 - t/T_{1,\mu}},$ (1)

where the exponential function describes T_1 relaxation caused by magnetic fluctuations, and the static Gaussian Kubo-Toyabe function $G_{\rm KT}(t;\Delta,B_0)$ with the relaxation rate Δ expresses loss of muon spin coherence under static local fields with an isotropic Gaussian probability distribution [17]. This model was also adopted in Ref. [14] to describe ZF- μ SR in PrTi₂Al₂₀, where the primary origins of the fluctuating and static local fields were determined to be HE ¹⁴¹Pr and bare ²⁷Al nuclear spins, respectively. These imply that a similar mechanism is also in effect in PrV₂Al₂₀.

The damping of the spectrum at 0.045 K is obviously faster than that at 4.2 K. Supposing that the additional damping were entirely due to the development of static local fields below T_Q , the extra field spread would be roughly estimated to be $(\tau_{0.045\,\mathrm{K}}^{-2} - \tau_{4.2\,\mathrm{K}}^{-2})^{1/2}/\gamma_{\mu} \sim 4 \times 10^{-4}\,\mathrm{T}$, where τ is the 1/e width, and γ_{μ} (= $2\pi \times 135.53\,\mathrm{MHz/T}$) is the muon gyromagnetic ratio. On the other hand, muons in SmTi₂Al₂₀ with a $0.51-\mu_B/\mathrm{Sm}$ ordered moment feel a local field of $\sim 5 \times 10^{-2}$ T [18,19]. From a simple scaling, the magnitude of the hypothetical ordered moment in PrV₂Al₂₀ is estimated to be $4 \times 10^{-3} \mu_B/\text{Pr}$. This is too small to be associated with the entropy release $\sim 0.5R \ln 2$ at T_Q [5]. Therefore, the possibility of magnetic order and consequent development of static local fields is ruled out in PrV₂Al₂₀. The ZF spectrum at 0.045 K is more exponential-like in shape, as shown in the inset of Fig. 1(a). This suggests that the additional damping is primarily due to an increase in $1/T_{1,\mu}$. Further evidence can be obtained by carefully investigating the 1/3 component as the first term in Eq. (1). The relaxation of this component is caused by the T_1 process under effective longitudinal fields associated with the longitudinal component of the static nuclear dipolar fields along P(t = 0) [17]. Therefore, the loss of the recovery after 6 μ s at 0.045 K manifests the increase in $1/T_{1.\mu}$. From our ZF- μ SR measurements, no explicit proof of time-reversal symmetry breaking was found below T_Q . This strongly suggests that the order parameter is a time-reversaleven multipole, supporting the AFQ order scenario from a microscopic point of view. Note that a T_{xyz} -type magnetic octupole is also active in the Γ_3 subspace [7]. Our results suggest that T_{xyz} octupolar order is unlikely in our samples.

ZF- μ SR spectra were fit to Eq. (1) to extract the temperature dependences of Δ and $1/T_{1,\mu}$. First, fits were performed in the entire temperature range with Δ and $1/T_{1,\mu}$ being free. The values of Δ obtained from the fits were almost constant above 3 K. This is reasonable because Δ resulting from the 27 Al and 51 V nuclear dipolar moments is expected to be independent of temperature in the temperature range where muons are immobile. The uncertainty in Δ steeply increases below 3 K as T_1 relaxation becomes dominant. This hinders the precise estimation of $1/T_{1,\mu}$ at low temperatures; therefore, we fixed Δ to the average value above 3 K and fit the spectra below 3 K with only $1/T_{1,\mu}$ being free. Satisfactory fits were obtained, as shown by the solid curves in Fig. 1(a).

The values of Δ and $1/T_{1,\mu}$ for PrV_2Al_{20} are shown by the solid triangles and squares, respectively, in Fig. 1(b). Those for $PrTi_2Al_{20}$ from Ref. [14] are also plotted with corresponding open symbols. The Δ values of both compounds are in good agreement, further demonstrating the validity of our model and fitting procedure for PrV_2Al_{20} . The root-mean-square (rms) width of the Gaussian local field distribution

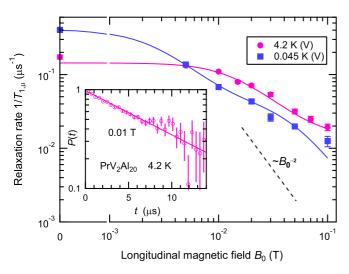


FIG. 2. (Color online) B_0 dependences of $1/T_{1,\mu}$ at 4.2 K (circles) and 0.045 K (squares) in PrV_2Al_{20} . The horizontal axis is on a linear scale for $B_0 < 10^{-3}$ T and on a log scale for $B_0 \geqslant 10^{-3}$ T. The solid curves represent the best fits to Eq. (2). The broken line illustrates the slope of functions that follow a B_0^{-2} dependence. The inset shows the μ SR spectrum at 4.2 K in $B_0 = 0.01$ T.

 $\Delta/\gamma_{\mu} \sim 3.5 \times 10^{-4}$ T is reasonable for abundant ²⁷Al and ⁵¹V nuclei [19]. The $1/T_{1,\mu}$ of PrV_2Al_{20} exhibits a double-plateau structure, as shown in Fig. 1(b). An increase in $1/T_{1,\mu}$ with decreasing temperature in the temperature range of 6-40 K is ascribed to the development of HE ¹⁴¹Pr nuclear moments associated with the increased Van Vleck contribution in magnetic susceptibility. The first plateau in the temperature range of 1-6 K suggests that exchange-mediated ¹⁴¹Pr spinspin interactions are fully developed and the ¹⁴¹Pr nuclear spin fluctuation rate ν is consequently temperature-independent. In PrTi₂Al₂₀, this plateau extends down to 0.1 K without any significant anomaly at $T_Q \sim 2.0$ K. By contrast, the $1/T_{1,\mu}$ of PrV₂Al₂₀ clearly increases with decreasing temperature below 1 K, and a second plateau forms below $T_O \sim 0.6$ K. This behavior suggests that the exchange-mediated ¹⁴¹Pr nuclear spin interactions are effectively weakened as AFQ correlations develop below 1 K. The significant difference between the FQ and AFQ compounds implies that the antiferrotype correlation might be essential for this perturbation.

Note that low-energy magnetic excitations in a magnetically ordered state can also contribute to the T_1 relaxation. When this process is dominant, however, $1/T_{1,\mu}$ should steeply decrease with decreasing temperature as the low-energy excitations are suppressed. This is clearly not the case in PrV_2Al_{20} , and therefore this possibility is excluded.

One may associate the difference between T_Q and the onset temperature of the increase in $1/T_{1,\mu}$ with a possibility of muon-charge-induced nucleation of a quadrupolar cluster slightly above T_Q . Unfortunately, it is difficult to completely rule out such a possibility from our data. However, even if that is the case, the sharp contrast between the FQ and AFQ compounds still suggests the importance of AFQ correlations for understanding the behavior of $1/T_{1,\mu}$ in PrV_2AI_{20} .

Figure 2 shows the B_0 dependences of $1/T_{1,\mu}$ in $\Pr{V_2Al_{20}}$ at 4.2 and 0.045 K. The $1/T_{1,\mu}$ value for $B_0 > 0$ was obtained from fits to $P(t) = e^{-t/T_{1,\mu}} G_{KT}(t; \Delta, B_0)$, with Δ being fixed to

TABLE I. ν , σ_B , and K for PrV₂Al₂₀ at 4.2 and 0.045 K.

<i>T</i> (K)	ν (MHz)	$\sigma_B \ (10^{-4} \ { m T})$	K
4.2 0.045	$22.7^{+1.4}_{-1.3}\ 4.0\pm0.2$	14.9 ± 0.4 10.5 ± 0.2	$9.8^{+0.6}_{-0.7} \\ 10.4 \pm 0.1$

the average value in ZF. The validity of our single- T_1 model can be visually checked in $B_0 \geqslant 0.01$ T, where $G_{\rm KT}(t;\Delta,B_0) \sim 1$ holds. All spectra above 0.01 T follow a single-exponential function well, as the example shown in the inset of Fig. 2 illustrates. The influence of avoided level crossing resonance [20] with ²⁷Al seems negligible since the $1/T_{1,\mu}$ - B_0 curves show smooth changes without any significant anomaly.

The $1/T_{1,\mu}$ due to the dipolar coupling between HE ¹⁴¹Pr nuclear and muon spins in B_0 is described by

$$\frac{1}{T_{1,\mu}} = \frac{\sigma_B^2 \gamma_\mu^2}{5} \left\{ \frac{3\nu}{\nu^2 + \gamma_\mu^2 B_0^2} + \frac{\nu}{\nu^2 + [\gamma_\mu - \gamma_I^*]^2 B_0^2} + \frac{6\nu}{\nu^2 + [\gamma_\mu + \gamma_I^*]^2 B_0^2} \right\},$$
(2)

where σ_B and γ_I^* are the rms width of the local field distribution and the effective gyromagnetic ratio for the HE ¹⁴¹Pr nuclear spin, respectively [17,21]. γ_I^* is enhanced by a factor of (1 + K) compared to the bare ¹⁴¹Pr gyromagnetic ratio $[\gamma_I = 2\pi \times$ 13.054(2) MHz/T [22]], where K is the ¹⁴¹Pr Knight shift. As an approximation, we use an orientation-averaged K in the AFQ ordered state, where anisotropy in K is expected to arise because of the splitting of the Γ_3 doublet. A simpler form of Eq. (2) with $\gamma_I^* = 0$ is frequently used, as was adopted in Ref. [14] for fitting $1/T_{1,\mu}(B_0)$ of $PrTi_2Al_{20}$. When γ_I^* is comparable with γ_{μ} (namely, $K \sim 9.4$), the second term in Eq. (2) results in a high-field tail in the plot of $1/T_{1,\mu}$ versus B_0 . This should be the case in PrV_2Al_{20} because K is roughly estimated to be 12 by the relationship $K = a_{hf} \chi_{4f}$, where a_{hf} (=187.7 mol/emu [23]) is the hyperfine coupling constant for Pr^{3+} , and χ_{4f} (=0.067 emu/mol at 2 K [5]) is the molar 4fsusceptibility. Fits to Eq. (2) were performed without restraints on σ_R , ν , and K. Satisfactory fits were obtained, as shown by the solid curves in Fig. 2.

The fitting parameters for 4.2 and 0.045 K are listed in Table I. The MHz-scale ν is typical of exchange-mediated ¹⁴¹Pr nuclear spin-spin interactions in nonmagnetic CEF ground states [10,14,21,24–26], further justifying our model. A marked reduction in ν at 0.045 K clarifies that the steplike increase in $1/T_{1,\mu}$ below 1 K in ZF is mainly due to the slowing down of 141 Pr nuclear spin fluctuations. Taking ν at 0.045 K as a measure of the effective nuclear exchange constant $|J_{\rm nucl}|/\hbar$ in the ground state, we can estimate the 141Pr nuclear order temperature T_{NO} using the following relationship: $T_{\text{NO}} =$ $|J_{\text{nucl}}|I(I+1)/3k_B$, where I=5/2 is the ¹⁴¹Pr nuclear spin. Accordingly, T_{NO} for PrV_2Al_{20} is estimated to be 89(5) μ K, slightly lower than that estimated for PrTi₂Al₂₀ [14]. The value of σ_B is significantly larger than $\Delta/\gamma_{\mu} \sim 3.5 \times 10^{-4} \text{ T}$ associated with ²⁷Al and ⁵¹V nuclei. Together with the large K, this is consistent with the hyperfine enhancement picture. Such an effect occurs only when the Pr³⁺ ground state does not involve active dipolar DOF [24]. Therefore, our observation of the HE ^{141}Pr nuclear spin dynamics provides further microscopic evidence of the nonmagnetic Γ_3 ground doublet and AFQ order in $\text{PrV}_2\text{Al}_{20}$. A slight decrease in σ_B at the lower temperature can likely be ascribed to a change in the shape of the local field distribution because of the anisotropy in *K* expected in the AFQ ordered state. The *K* values at 0.045 and 4.2 K agree within the error. This is reasonable because the splitting of the Γ_3 doublet does not change the orientation-averaged value of single-ion Van Vleck susceptibility when the Γ_3 splitting is negligibly small compared to Δ_{ex} . The fit to the data at 0.045 K deviates slightly at 0.1 T, as shown in Fig. 2. This might be due to the anisotropy in *K* below T_Q , which is not explicitly taken into account in Eq. (2).

The temperature dependence of $1/T_{1,\mu}$ for PrV_2Al_{20} shown in Fig. 1(b) indicates that ν ($\propto |J_{\text{nucl}}|$) begins to decrease below 1 K and levels off at around T_Q . This behavior suggests that the strength of the ¹⁴¹Pr nuclear spin coupling is effectively weakened as AFQ correlations develop. One possible origin for this reduction is intra-atomic electric quadrupolar coupling between 4f and 141 Pr quadrupolar moments. Here we assume that the 4f ground state is one of the eigenstates for the O_2^0 quadrupolar operator. Sixfold-degenerate ¹⁴¹Pr spin wave functions split into $|I_z = \pm 1/2\rangle$, $|\pm 3/2\rangle$, and $|\pm 5/2\rangle$ under the electric field gradient arising from the on-site O_2^0 moment. These levels are separated by $h\nu_O$ ($\pm 1/2 \leftrightarrow \pm 3/2$) and $2h\nu_O$ $(\pm 3/2 \leftrightarrow \pm 5/2)$. Following the treatment in Ref. [27], we estimated v_Q to be 1.6 MHz using the radial $\langle r^{-3} \rangle_{4f} =$ $5.369a_0^{-3}$, the Sternheimer factor $R_{4f} = 0.1308$ [28], and the ¹⁴¹Pr quadrupolar moment Q = -0.059 barn [22]. The estimated v_O is not negligible compared with the unperturbed v at 4.2 K; thus, the intra-atomic quadrupolar coupling can significantly reduce the transition probabilities between the separated levels.

Other possible origins for the effective reduction in $|J_{\text{nucl}}|$ come from the path of the ¹⁴¹Pr nuclear spin exchange. Considering that this is mediated by the Ruderman-Kittel-Kasuya-Yoshida interactions between 4f dipolar moments induced by the intra-atomic hyperfine interaction, the orientation-averaged $|J_{\text{nucl}}|$ can be approximately expressed as

$$|J_{\text{nucl}}| = \left(\frac{\gamma_I \hbar}{g_J \mu_B}\right)^2 |J_{ff}| \text{Tr}[K_+ K_-]/3, \tag{3}$$

where g_J (=4/5) is the Landé g-factor for \Pr^{3+} , $|J_{ff}|$ is the 4f exchange constant, and K_\pm are $^{141}\Pr$ Knight shift

tensors for the two closest Pr ions. This relation suggests that perturbation of ${\rm Tr}[K_+K_-]/3$ and/or $|J_{ff}|$ can be responsible for the reduction in $|J_{\rm nucl}|$. Here we focus on the contribution from the Knight shift factor because any change in $|J_{ff}|$ is expected to be relatively small. Calculating the single-ion Van Vleck susceptibility for the O_2^0 eigenstates yields the diagonal K_\pm with a set of principal values expressed as $(K \mp K_a, K \mp K_a, K \pm 2K_a)$, where K_a is an anisotropic part. Consequently, ${\rm Tr}[K_+K_-]/3$ is evaluated to be $K^2-2K_a^2$, which is smaller than K^2 for the paraquadrupolar state and thus is consistent with the reduced $|J_{\rm nucl}|$. A similar conclusion is also reached for O_2^2 eigenstates.

The intra-atomic quadrupolar coupling should also be in effect in the FQ compound $\Pr{Ti_2Al_{20}}$, which can decrease ν . The flat temperature dependence of $1/T_{1,\mu}$ in $\Pr{Ti_2Al_{20}}$ suggests that other contributions compensate for this "decoupling" effect. In the case of the O_2^0 -type FQ order, the Knight shift factor in Eq. (3) is replaced with $\Pr{K_{\pm}^2/3} = K^2 + 2K_a^2$. The enhancement in $|J_{\text{nucl}}|$ because of this factor may be a source of the compensation.

IV. CONCLUSION

 μSR is sensitive to slow spin fluctuations in the MHz scale and thus is appropriate for probing HE ^{141}Pr nuclear spin dynamics. In this study, we used μSR to demonstrate that the AFQ correlations of 4f electrons can significantly perturb the strength of the HE ^{141}Pr nuclear spin-spin interaction in PrV_2AI_{20} . This paves the way for an alternative approach to investigate quadrupolar correlations in Pr-based compounds using local spin probes via the observation of HE ^{141}Pr nuclear spin dynamics.

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