

Modified Schottky emission to explain thickness dependence and slow depolarization in BaTiO₃ nanowires

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We investigate the origin of the depolarization rates in ultrathin adsorbate-stabilized ferroelectric wires. By applying density functional theory calculations and analytic modeling, we demonstrate that the depolarization results from the leakage of charges stored at the surface adsorbates, which play an important role in the polarization stabilization. The depolarization speed varies with thickness and temperature, following several complex trends. A comprehensive physical model is presented, in which quantum tunneling, Schottky emission, and temperature-dependent electron mobility are taken into consideration. This model simulates experimental results, validating the physical mechanism. We also expect that this improved tunneling-Schottky emission model could be applied to predict the retention time of polarization and the leakage current for various ferroelectric materials with different thicknesses and temperatures.

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I. INTRODUCTION

Spontaneous electric polarization makes perovskite-based oxides of great interest for application to nonvolatile memory devices [1,2]. However, the polarization of ferroelectric materials may not be infinitely stable, and retention time is one of the key factors determining the performance of memory devices in nonvolatile technology. The proposed reasons for the polarization instability have included the depolarization field and the leakage current [3], whose effects become more significant as the oxide film gets thinner. Therefore, for successful technology application, the depolarization processes of nanoscale ferroelectric oxides must be better understood. Here, we report a combined experimental and theoretical investigation of the depolarization process of single-crystalline BaTiO₃ nanowires. We attribute the decay of polarization to the leakage of surface screening charge and propose an analytical model to explain the experimental decay rates.

A. Experimental background

The effects of the depolarization field on the stability of ferroelectricity in ultrathin materials was explored in BaTiO₃ nanowires by measuring the ferroelectric transition temperature as a function of the nanowire diameter in the range of 3–48 nm [4–7]. Positive ferroelectric domains were written perpendicular to the nanowire axis using a negative-bias voltage (–10 V) applied by a conductive scanning probe microscope cantilever tip (under ultrahigh vacuum conditions with a base pressure of 10^{–10} torr). The time evolution of the polarized domain was then monitored via time-resolved measurements of the local electric field, using noncontact electrostatic force microscopy (EFM). The writing and reading processes were done at various temperatures, starting from ≈393 K for thin nanowires (3–11 nm) and ≈418 K for the thicker ones (12–37 nm). The two sets of nanowires were

progressively cooled down and retested until ≈308 K and ≈383 K were reached, respectively. The Curie temperature T_C was defined as the highest temperature below which the polarization signal persists for a period longer than 200 h. Experiments showed that T_C is inversely proportional to the diameter of the BaTiO₃ nanowire, in accord with standard models of the depolarization field [8]. At several temperatures above T_C , the surface potential signals were measured during the process of polarization decay. The magnitude of surface potential was fitted with the expression:

$$S(t) = S(0)e^{-k_d t}, \quad (1)$$

where $S(t)$ is the potential at time t , which is proportional to the surface screening charge, and k_d is the decay rate, with the unit s^{–1} [9]. Here, we should note that experimentally it is found that the signals decay with time approximately (but not perfectly) exponentially. Despite the slight deviations, the decay rate k_d obtained from the data fitting is still an important physical parameter in describing the polarization decay speed. From the time evolution of the signal [4], we see that the bright circular signal faded without expansion, which means that the depolarization is a process of leakage or tunneling, rather than diffusion, of the surface screening charge. The observed decay rates k_d , which vary with nanowire thickness and temperature, are shown in Fig. 1 (please refer to the red circles). The raw data are also presented in the Supplemental Material (Tables S1 and S2) [10].

The experimental data show three general trends: (1) The depolarization process is slow (several hours); (2) for any thickness, the decay rate k_d increases with temperature; (3) for thin nanowires (5–9 nm), the decay rate k_d changes with thickness dramatically. However, for thicker wires, k_d stays nearly constant at different thicknesses (21, 25, 37, and 48 nm). Our study aims at illustrating the physical essence of these trends.

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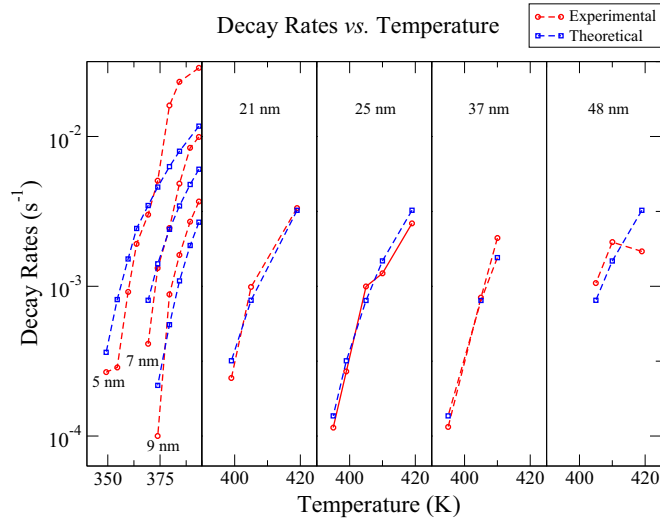


FIG. 1. (Color online) Depolarization rates measured from experiments (red circles) and calculated from our model (blue squares).

B. Polarization stabilization

In recent years, many studies have investigated the dependence of polarization stabilization and leakage current on chemical environment, temperature, electrode material, and thickness [11–29]. From these studies, several basic principles could be drawn.

(1) Surface polarization charge should be compensated by screening charge, in order to passivate the depolarization field and stabilize the ferroelectric distortion, or else the polarization would become unstable. The screening charge could be stored in surface electrodes or adsorbates [8,11–19].

(2) The polarization state of the material may lead to preferential adsorption of certain molecules on the surface [20–26].

(3) The response of polarization with electric field or temperature is fast, but the time scale for dissipation of the surface screening charge is slow (hours or days) [27–29].

Based on the evidence above and the observations in our experiments, we propose that the physical process of depolarization in the BaTiO₃ nanowire experiment is as follows: After the polarization is written, surface adsorbates on the nanowire act as an electrode that stores screening charge and stabilizes the polarization [4]. For the case without external applied voltage and above T_C , the polarized state is not stable. But due to the stabilization of the screening charge in the surface adsorbates, polarization in the nanowire still persists for some time. Screening charge leaks from the top electrode (surface adsorbate) to the other side of the BaTiO₃ nanowire (gold substrate). At the same time, polarization reduces along with the screening charge. This process is slow and takes hours.

In the following parts of this paper, support, analysis, and modeling of the physical processes described above are shown. In Sec. II, we use density functional theory to demonstrate the role of surface adsorption in surface charge screening. In Sec. III, analytical expressions describing leakage current leading to depolarization are developed. Finally, in Sec. IV, we present the results and discussion.

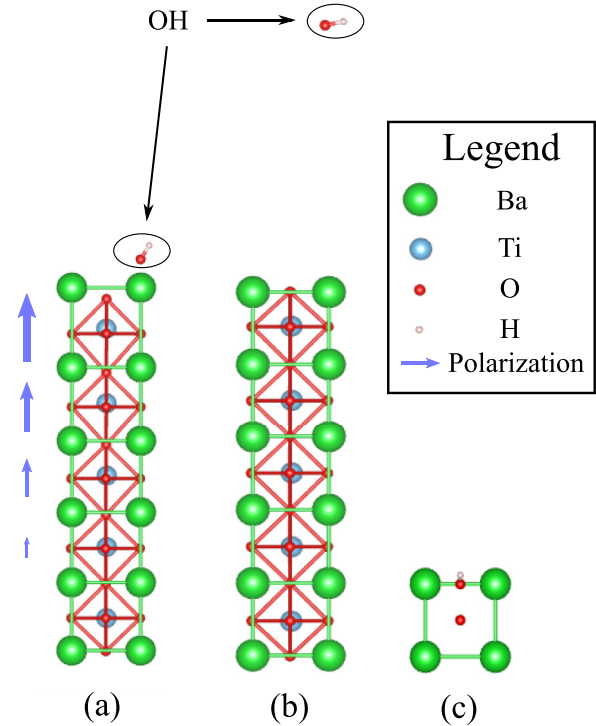


FIG. 2. (Color online) Relaxed structures for the BaTiO₃/OH systems acquired from DFT calculation. Green, blue, red, and gray spheres represent barium, titanium, oxygen, and hydrogen atoms, respectively. (a) Polar system, OH is adsorbed on the surface. The dimension of the arrow is proportional to the layer rumpling (cation-oxygen displacement in the z direction). (b) Nonpolar structure, OH is far away from the surface of the BaTiO₃ surface. (c) Top view of the OH adsorbate and the first atomic layer of BaTiO₃, corresponding to the structure in (a).

II. DENSITY FUNCTIONAL THEORY CALCULATION

In order to construct a theory of the depolarization process, density functional theory calculations (DFT) are carried out to assess the role of surface molecular and atomic adsorbates. We investigate the OH molecule on BaO-terminated BaTiO₃ slabs, as OH is the predominant species found on oxide surfaces, as demonstrated by both infrared spectra and *ab initio* calculations [30,31].

Density functional theory calculations with periodic boundary conditions were carried out using the QUANTUM-ESPRESSO plane-wave DFT code [32]. The exchange-correlation functional was approximated with the Perdew-Burke-Ernzerhof form of the generalized gradient scheme. Plane-wave cutoff energy of 50 Ry was used in all calculations. The pseudopotentials were generated using the OPIUM code following the norm-conserving designed nonlocal recipe [33,34]. (1×1) five-unit-cell-thick BaTiO₃ slabs, separated by more than 20 Å of vacuum normal to the surface, were used to simulate the thin films. Additional dipole correction was added in the middle of the vacuum to further correct the spurious electric field interaction between periodic images. A k -point mesh of $6 \times 6 \times 1$ was used following the Monkhorst-pack sampling scheme [35]. Atomic forces were converged until a maximum threshold of 0.05 eV/Å per atom is reached.

TABLE I. Löwdin population of the orbitals of the OH on the BaO-terminated BaTiO₃.

	Polar	Nonpolar
H 1s orbital	0.6121	0.5601
O 2s orbital	1.7315	1.8138
O 2p orbital	5.0719	4.5980
Net charge	-0.4155	0.0289

As shown in Fig. 2, from the relaxed structure, we see that the presence of the OH adsorbates enhances ferroelectricity at the positively polarized surface and maintains a characteristic ferroelectric displacement pattern throughout the film, which is consistent with the results in Ref. [4].

The density of states projected onto atomic orbitals (PDOS) was calculated to characterize the charge distribution on each atom. Results are shown in Table I, from which we see that if the BaTiO₃ nanowire is positively polarized, the hydroxyl oxygen 2p orbital possesses more electrons and OH is overall negatively charged. This is a robust evidence demonstrating that surface adsorbates stabilize the polarization by holding screening charges, which has an effect similar to an electrode. The leakage of charge mainly from the 2p orbital of oxygen results in the decay of polarization.

III. FORMALISM OF LEAKAGE CURRENT CALCULATION

There have been previous reports calculating the magnitude of leakage through ferroelectric films with tunneling models, Schottky emission, and the modified Schottky equation [36–38]. However, all these models come across difficulties in explaining all three depolarization rate trends mentioned in Sec. IB. A tunneling model alone cannot explain that for thick nanowires, decay rates are nearly thickness independent and for any thickness, the decay rates are strongly temperature dependent. On the other hand, a Schottky emission model cannot account for the thin nanowire thickness dependent rates. Here, we build a comprehensive model from the “effective velocity” point of view, which both accounts for the experimental results and illustrates their physical mechanisms.

The general expression for the time (t)-dependent leakage current J can be written as

$$-\frac{\partial Q(t)}{\partial t} = J(t) = \int Q(t)n(\mathbf{k})v_{\text{eff}}(\mathbf{k})d^3\mathbf{k}, \quad (2)$$

where $n(\mathbf{k})$ is the probability that an electron possesses a wave vector between \mathbf{k} and $\mathbf{k} + d\mathbf{k}$. $v_{\text{eff}}(\mathbf{k})$ is the effective velocity along the z direction, which is normal to the surface of the BaTiO₃ nanowire, for the electrons with wave vector \mathbf{k} . Q is the amount of extra charge (compared with neutral OH) stored in the adsorbate. In the following subsections, we define the parametrization of Eq. (2).

A. Wave-vector distribution of electrons in adsorbate

Unlike in traditional metal electrodes, electrons occupying orbitals localized on the OH adsorbates cannot be treated as a free electron gas, and the wave vector distribution does not follow Fermi-Dirac statistics. Instead, the wave vector

spectrum can be estimated from Bessel-Fourier transformation of the 2p orbital of oxygen, since screening charge is mainly associated with this atomic orbital. Here, the radial part of the 2p orbital of the oxygen is represented by a double-zeta function [39].

$$\begin{aligned} \phi_{2p}(\mathbf{r}) &= R(r)Y_{10}(\theta_r, \phi_r) \\ &= \left(c_1 \sqrt{\frac{(2z_1)^5}{4!}} r e^{-z_1 r} + c_2 \sqrt{\frac{(2z_2)^5}{4!}} r e^{-z_2 r} \right) Y_{10}(\theta_r, \phi_r) \\ &= (c'_1 r e^{-z_1 r} + c'_2 r e^{-z_2 r}) Y_{10}(\theta_r, \phi_r), \end{aligned} \quad (3)$$

$$\begin{aligned} \phi_{2p}(\mathbf{k}) &= \frac{1}{(2\pi)^{3/2}} \int e^{-i\mathbf{k}\cdot\mathbf{r}} \phi_{2p}(\mathbf{r}) d^3\mathbf{r} \\ &= -\sqrt{\frac{8}{\pi}} 4i Y_{10}(\theta_k, \phi_k) \left[\frac{c'_1 z_1 k}{(z_1^2 + k^2)^3} + \frac{c'_2 z_2 k}{(z_2^2 + k^2)^3} \right], \end{aligned} \quad (4)$$

$$\begin{aligned} n(\mathbf{k}) &= |\phi_{2p}(\mathbf{k})|^2 \\ &= \frac{128}{\pi} |Y_{10}(\theta_k, \phi_k)|^2 \left[\frac{c'_1 z_1 k}{(z_1^2 + k^2)^3} + \frac{c'_2 z_2 k}{(z_2^2 + k^2)^3} \right]^2, \end{aligned} \quad (5)$$

where Y_{10} is the spherical harmonic for $l = 1$ and $m = 0$. $c_{1,2}$ and $z_{1,2}$ are the parameters in the double-zeta function, acquired from Ref. [39]. c'_1 and c'_2 are reduced coefficients taking the normalization factors $\sqrt{\frac{(2z_1)^5}{4!}}$ and $\sqrt{\frac{(2z_2)^5}{4!}}$ into consideration. $\theta_{r,k}$ and $\phi_{r,k}$ are the angles between the directions of \mathbf{r} , \mathbf{k} and the axes in spherical coordinates. $\phi_{2p}(\mathbf{r})$ and $\phi_{2p}(\mathbf{k})$ are expressions for the oxygen 2p wave function in coordinate and wave vector representations. In this way, we obtain an analytical expression for $n(\mathbf{k})$. Here, we should note that in part II, we used pseudo-wave-functions in the DFT calculations; compared with all-electron wave functions, pseudo-wave-functions have lower high- k components on purpose to limit the number of plane waves used [40]. This does not affect the accuracy of the charge leakage rate calculation. This is because the DFT calculation is used only to illustrate the role of the screening charge and the mechanism of the depolarization process. The wave-vector distribution in this model is derived from the double-zeta function as described above. Additionally, in the later discussion, we will also include the fact that high-speed electrons lose their initial momentum quickly and drift under the effect of the electric field. Therefore, an underestimation of the high- k components has little effect on the charge dissipation speed.

B. Effective velocity

Here, we present an effective velocity model of the charge dissipation. The band diagram of the OH/BaTiO₃/Au substrate system is shown in Fig. 3(a).

We only consider the effective velocities of the electrons with the wave vector pointing toward the nanowire $\mathbf{k} \cdot \hat{\mathbf{z}} > 0$. Otherwise, the electron does not contribute to the leakage

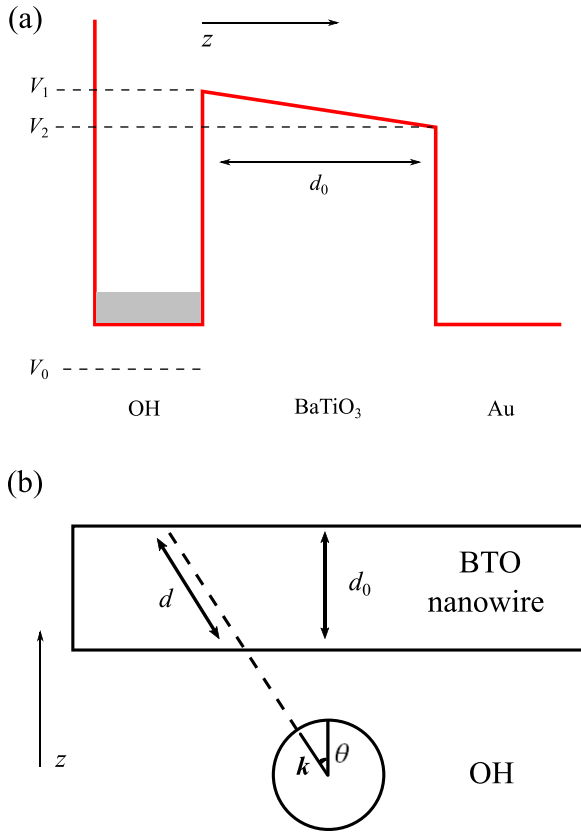


FIG. 3. (Color online) (a) Band diagram of the Au electrode/oxide insulator/adsorbate system. (b) Relationship of barrier thickness and direction of wave vector.

current J and its effective velocity $v_{\text{eff}} = 0$. For the electron moving toward the nanowire, the expression for effective velocity varies depending on whether the energy of the electron is higher than that of the BaTiO₃ conduction band edge. The potential energy of an electron affiliated with the hydroxyl molecule oxygen $2p$ orbital is set as V_0 . The total energy for this electron can be written as the sum of its kinetic energy $T(\mathbf{k})$ and V_0 :

$$E(\mathbf{k}) = T(\mathbf{k}) + V_0 = \frac{\hbar^2 |\mathbf{k}|^2}{2m_0} + V_0. \quad (6)$$

As shown in Fig. 3(a), the conduction band for the BaTiO₃ nanowire is not flat, and the slope equals the electronic charge e times the electric field E_{fe} inside the ferroelectric nanowire. Therefore,

$$V_2 = V_1 - eE_{\text{fe}}d_0. \quad (7)$$

For the case $E(\mathbf{k}) < V_2$, the mechanism that governs the electron movement is quantum tunneling. The electron tunnels from the surface adsorbate hydroxyl to the gold electrode at the other side, through the BaTiO₃ nanowire as an energy barrier. Around T_C , the dielectric constant of BaTiO₃ is large and E_{fe} is small. Therefore, the conduction band is nearly flat and we use the approximation that the energy barrier is a cuboid with the height $V_b = \frac{1}{2}(V_1 + V_2)$. The transmission coefficient $P(\mathbf{k})$, which is also the probability of one electron with wave vector

\mathbf{k} penetrating the barrier, could be expressed [41]:

$$P(\mathbf{k}) = \frac{4}{4 + \frac{[m_0 E + m^*(V_b - E)]^2}{m_0 m^* E (V_b - E)}} \sinh^2 \left[\frac{2m^* d^2 (V_b - E)}{\hbar^2} \right]^{1/2}, \quad (8)$$

where d is the length of the barrier. m^* is the effective mass of electrons in BaTiO₃. Assuming that the angle between the incident direction of the electron and the normal direction of the BaTiO₃ nanowire is θ , as shown in Fig. 3(b), d could be expressed as

$$d = \frac{d_0}{\cos \theta}. \quad (9)$$

In this tunneling process, an electron with an initial velocity $v = \frac{\hbar \mathbf{k}}{m_0}$ has a probability $P(\mathbf{k})$ of passing the energy barrier with the thickness d . Thus, the effective velocity could be expressed as

$$v_{\text{eff}}(\mathbf{k}) = v P(\mathbf{k}) = \frac{\hbar \mathbf{k} \cdot \hat{\mathbf{z}}}{m_0} P(\mathbf{k}) = \frac{\hbar k \cos \theta}{m_0} P(\mathbf{k}). \quad (10)$$

When the hydroxyl electron energy is higher than that of the BaTiO₃ conduction band edge $E(\mathbf{k}) > V_1$, the electron is not classically forbidden to enter the BaTiO₃ nanowire. However, very high velocity electrons could have very short mean free paths. Moreover, in the BaTiO₃ crystal, which is an insulator and possesses a small mean free path [42], the electron loses its initial momentum quickly and drifts under the effect of electric field E_{fe} inside the ferroelectric nanowire:

$$v_{\text{eff}} = \mu E_{\text{fe}}, \quad (11)$$

where μ is the electronic mobility, which depends on temperature, intermediate energy levels, and lattice vibrations. Lattice vibrations have a significant influence on the drift mobility due to electron-phonon interactions [43–46], in which an electron may lose or gain energy in a collision. This effect will be discussed in the following subsection.

For the final case, $V_2 < E(\mathbf{k}) < V_1$, the electron first tunnels through an energy barrier and then drifts in the conduction band. The effective velocity is given by

$$v_{\text{eff}} = \mu E_{\text{fe}} P(\mathbf{k}). \quad (12)$$

For this case, the energy barrier goes to zero within the nanowire. At this condition, the Wentzel-Kramers-Brillouin (WKB) [47] approximation fails. Since $E(\mathbf{k})$ is close to V_1 , we approximate $P(\mathbf{k})$ to 1.

Even though this approximation overestimates the tunneling current, later we will point out that despite this, the tunneling current is still a negligible contribution to the overall current.

C. Electric properties of BaTiO₃ nanowire

The relationship of surface charge density Q , electric displacement D_{fe} , and electric field E_{fe} though the insulator is given by dielectric constant $\epsilon(T)$ [12]:

$$Q(t) = D_{\text{fe}} = \epsilon(T) \epsilon_0 E_{\text{fe}}. \quad (13)$$

According to the Lyddane-Sachs-Teller [48] relation, the temperature-dependent static dielectric constant is expressed

as

$$\frac{\epsilon(T)}{\epsilon_\infty} = \frac{\prod_i \omega_{L_i}^2(T)}{\prod_i \omega_{T_i}^2(T)}, \quad (14)$$

where ω is the frequency of lattice vibration and T_i and L_i represent transverse and longitudinal modes. Approaching T_C , a transverse optical mode ω_{TO} becomes ‘‘soft,’’ indicating the occurrence of the phase transition [49–51]:

$$\omega_{TO}^2 \approx A(T - T_C), \quad (15)$$

$$\epsilon(T)^{-1} \propto \omega_{TO}^2 = A'(T - T_C), \quad (16)$$

where A and A' are constants, and for BaTiO₃ bulk [52,53], $T_C \approx 393$ K. However, for a thin film or nanowire, if polarization exists, a depolarization field is induced due to the incomplete charge compensation of polarization charge [13,54,55]. The depolarization field, which is antiparallel to the polarization, becomes significant as the thickness decreases. It also applies an electric force on the ions, and as a consequence, the soft vibrational mode is hardened. With the depolarization field effect included, the temperature-dependent soft-mode frequency for thin films should be rewritten as

$$\omega_{TO}^2 \approx A(T - T'_C), \quad (17)$$

$$\epsilon(T)^{-1} = A'(T - T'_C), \quad (18)$$

and

$$T'_C < T_C. \quad (19)$$

The depolarization field effect hardens the soft mode, increases the vibrational frequency, suppresses the ferroelectricity, and lowers the T_C . The values of T'_C for different thicknesses were previously experimentally measured [4].

Previous studies illustrated that the electronic mobility in BaTiO₃ varies over a large range (10^{-3} – 10^{-1} cm²/V s) [46,56,57]. The variation of mobility could be attributed to the different trap levels, types, and concentrations from the fabrication process. Despite the uncertainty, there is a general rule that electron mobility is determined by the optical phonons [43–46].

Many studies in recent years pointed out that scattering by the soft transverse optical mode is the primary factor affecting electron drift [46,58,59]. In this case [59],

$$\mu = \frac{f(T)}{\epsilon(T)} \propto f(T) \omega_{TO}^2, \quad (20)$$

and $f(T)$ depends weakly on T for BaTiO₃ [58,59]. For $T > T'_C$,

$$\mu \approx B \omega_{TO}^2 = B'(T - T'_C), \quad (21)$$

where B and B' are constants. An explicit explanation about the soft-mode-dependent mobility was proposed in Ref. [46]. In brief, according to thermodynamics, the mean-squared polarization fluctuation δP is related to the dielectric constant as [60]

$$\langle \delta P^2 \rangle = k_B T \epsilon / V \propto 1 / \omega_{TO}^2, \quad (22)$$

where k_B is Boltzmann constant and V is the volume. For the case $T > T'_C$, a high soft-mode frequency means a small

dielectric constant, large mean-square TO phonon amplitude, and polarization fluctuation. Besides, in a small region with approximately uniform polarization fluctuations, shifts in the conduction band edge $\Delta \mathcal{E}_c$ is [61]

$$\Delta \mathcal{E}_c = \text{const} + \beta \delta P^2, \quad (23)$$

where β is the polarization-potential parameter, which has a typical value $\beta \approx 2$ eV m⁴/C². In the nanowire, the low soft-mode frequency leads to inhomogeneity in $\Delta \mathcal{E}_c$, which then results to locally different effective masses and electronic energies. Therefore, an electron traveling through the wire scatters more. This is similar to an electron traveling on a curved path and harder to accelerate. A lower soft-mode frequency means more scattering, a shorter relaxation time τ_e , and a smaller electron mobility, since electron mobility is given by [62]

$$\mu = \frac{e \tau_e}{m^*}. \quad (24)$$

Thus, in this simulation, we use the empirical expression of electron mobility as shown in Eq. (21).

IV. RESULTS AND DISCUSSIONS

With the expressions of effective velocity deduced in a different wave-vector range,

$$v_{\text{eff}}(\mathbf{k}) = \begin{cases} \frac{\hbar \mathbf{k} \cdot \hat{\mathbf{z}}}{m_o} P(\mathbf{k}) & \text{if } E(\mathbf{k}) < V_2, \mathbf{k} \cdot \hat{\mathbf{z}} > 0 \\ \mu E_{\text{fe}} P(\mathbf{k}) & \text{if } V_2 < E(\mathbf{k}) < V_1, \mathbf{k} \cdot \hat{\mathbf{z}} > 0 \\ \mu E_{\text{fe}} & \text{if } E(\mathbf{k}) > V_1, \mathbf{k} \cdot \hat{\mathbf{z}} > 0 \\ 0 & \text{if } \mathbf{k} \cdot \hat{\mathbf{z}} < 0, \end{cases} \quad (25)$$

we could calculate the time evolution of the surface charge with Eq. (2).

The expression of current density was shown in Eq. (1). In the calculation of charge density evolution with time, the initial charge density used in the simulation is $Q(0) = 0.26$ C/m² [33], which is the spontaneous polarization for the tetragonal phase of BaTiO₃. The time window is selected as 10^4 s, which is long enough to demonstrate the general trend of time evolution of the surface charge in adsorbate OH. Other parameters involved in the presented tunneling and modified Schottky model are listed in Table II. Most of the parameters are from previous literature. The difference of the potential energy of electrons in the adsorbate oxygen $2p$ orbital (V_0) and in the conduction band formed by titanium $3d$ orbitals (V_1) is estimated from the band gap of BaTiO₃ (3.20 eV) [63]. This is a good approximation because the adsorbate oxygen $2p$ orbital is approximately at the same level with the valence band formed by oxygen $2p$ orbitals of the nanowire.

$$V_1 - \overline{E(\mathbf{k})} \approx 3.20 \text{ eV}, \quad (26)$$

where $\overline{E(\mathbf{k})}$ is the average energy of electrons in the adsorbate oxygen $2p$ orbital, and

$$\overline{E(\mathbf{k})} = \overline{T(\mathbf{k})} + V_0, \quad (27)$$

$$\overline{T(\mathbf{k})} = \int_0^\infty n(\mathbf{k}) \frac{\hbar^2 \mathbf{k}^2}{2m_0} d^3 \mathbf{k} = 68.28 \text{ eV}, \quad (28)$$

$$V_1 - V_0 = V_1 - \overline{E(\mathbf{k})} + \overline{T(\mathbf{k})} = 71.48 \text{ eV}. \quad (29)$$

TABLE II. Parameters involved in the presented tunneling and modified Schottky model of nanowire depolarization.

Parameter	Description	Value
T'_C (5 nm)	T_C for 5 nm nanowire ^a	340.3 K
T'_C (7 nm)	T_C for 7 nm nanowire ^a	355.2 K
T'_C (9 nm)	T_C for 9 nm nanowire ^a	367.9 K
T_C	T_C for thick nanowires ^a	391 K
c_1	Parameter in Eq. (3) ^b	0.72540
c_2	Parameter in Eq. (3) ^b	0.35173
z_1	Parameter in Eq. (3) ^b	1.62807 bohr ⁻¹
z_2	Parameter in Eq. (3) ^b	3.57388 bohr ⁻¹
m^*	Effective electronic mass	6.5 m_0
$V_1 - V_0$	Energy barrier ^d	71.48 eV
A'	Defined in Eq. (18) ^e	$7.84 \times 10^{-6} \text{ K}^{-1}$
B'	Defined in Eq. (21) ^f	5.025×10^{-6}

^aReference [4].

^bReference [39].

^cReference [56].

^dFrom the band gap estimation.

^eEstimated from Ref. [53].

^fThe unit is cm^2/VsK .

In the modeling, the surface charge density Q decays with time t , but not exactly exponentially. We fit each Q vs t curve with an exponential function by the least squares fitting method. In this way, we obtain decay constants from this model that can be compared with experimental ones. B' of Eq. (21) is the only parameter calculated by fitting the data in experiments to the decay rates calculated by this analytical model, rather than from any references or *ab initio* calculation.

The decay rates calculated from this model and experimental data are shown in Fig. 1. Experimental data are marked with red circles and theoretically calculated ones are blue squares. Symbols for decay rates of a given thickness are connected with dashed lines, to demonstrate their temperature dependence. From the comparison, it could be seen that this model not only simulates the experimental results to a good extent, but also sheds light on the general rules of ferroelectric leakage current.

For nanowires with any thicknesses, calculations based on Eqs. (2) and (25) demonstrate that the tunneling current provides a negligible part of the total leakage current. Even for the thinnest nanowires (5 nm) with a surface charge density $Q(0) = 0.26 \text{ C/m}^2$, the tunneling current is around 10^{-6} A/m^2 or less, generally no more than 1% of the total leakage current. Emission of electrons with energies higher than the barrier contributes nearly all the current. The fact that tunneling, whose rate is thickness dependent, plays a minor role is consistent with the experimental finding that decay rates are thickness independent for thick nanowires [64].

For thin nanowires, at a certain temperature which is above T_C , the soft-mode frequency decreases with thickness due to the depolarization field effect. A thinner nanowire corresponds to a higher soft-mode frequency and a smaller dielectric constant, as shown in Eq. (17). Thus, the electric field through a thinner nanowire is larger and accelerates the electron emission. Meanwhile, a higher transverse optical mode frequency results in a faster electron drift mobility. This makes the

leakage current and polarization decay constant significantly thickness dependent for thin wires. For thick nanowires, the soft-mode frequency at a certain temperature approaches that of the bulk BaTiO₃ crystal. In this range, thickness affects the electric field, electron mobility, and leakage current little. It is worth mentioning that the conclusion, that leakage current depends on thicknesses only for thin nanowires or films, is consistent with previous studies [64–66].

In this study, the surface adsorbate OH plays the role of top electrode, which is the source of nonequilibrium charge carriers. This modified Schottky model, simulating leakage current in ferroelectric oxides, differs from the traditional Schottky emission model in many aspects. The electrons are localized in a $2p$ orbital, and their wave-vector distribution is now not based on Fermi-Dirac statistics. Different from the traditional Schottky emission model, in which the thermal population of electrons leads to the temperature dependence of leakage current, here, the temperature-dependent leakage current is attributed to change of electric field through the nanowire and electronic mobility accompanied with the hardening (or softening) of the transverse optical mode in this model.

V. CONCLUSION

In summary, the depolarization process of BaTiO₃ nanowires has been studied by both experiment and first-principles calculation. We investigated the mechanisms which govern the polarization decay and drew several principles. A new proposed theoretical model, which combines molecular orbital theory, quantum tunneling, and the modified Schottky equation, could explain successfully the general trends in the temperature and nanowire-thickness-dependent decay rates. Our study demonstrates that the surface adsorbate plays a significant role in stabilizing ferroelectricity and that depolarization is a process of charge leaking from the hydroxyl surface adsorbate to the gold substrate.

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APPENDIX A: DERIVATION OF EQ. (4)

$$\begin{aligned}
 \phi_{2p}(\mathbf{k}) &= \frac{1}{(2\pi)^{3/2}} \int e^{-i\mathbf{k}\cdot\mathbf{r}} \phi_{2p}(\mathbf{r}) d^3\mathbf{r} = \sqrt{\frac{1}{8\pi^3}} \int_0^\infty \int_0^\infty 4\pi \sum_{l=0}^\infty \sum_{m=-l}^l (-i)^l j_l(kr) \\
 & Y_{lm}^*(\theta_r, \phi_r) Y_{lm}(\theta_k, \phi_k) R(r) Y_{10}(\theta_r, \phi_r) r^2 dr d\Omega \\
 &= -\sqrt{\frac{1}{8\pi^3}} Y_{10}(\theta_k, \phi_k) \int_0^\infty 4\pi i j_1(kr) R(r) r^2 dr = -\sqrt{\frac{2}{\pi}} Y_{10}(\theta_k, \phi_k) \int_0^\infty i \left[\frac{\sin(kr)}{k^2 r^2} - \frac{\cos(kr)}{kr} \right] R(r) r^2 dr \\
 &= -\sqrt{\frac{2}{\pi}} Y_{10}(\theta_k, \phi_k) \int_0^\infty i \left[\frac{e^{ikr} - e^{-ikr}}{2k^2 i} - \frac{r(e^{ikr} + e^{-ikr})}{2k} \right] R(r) dr \\
 &= -\sqrt{\frac{2}{\pi}} \frac{c'_1}{2k^2} Y_{10}(\theta_k, \phi_k) \int_0^\infty r(e^{-z_1 r + ikr} - e^{-z_1 r - ikr}) dr - \sqrt{\frac{2}{\pi}} \frac{c'_2}{2k^2} Y_{10}(\theta_k, \phi_k) \int_0^\infty r(e^{-z_2 r + ikr} - e^{-z_2 r - ikr}) dr \\
 &\quad + \sqrt{\frac{2}{\pi}} \frac{c'_1 i}{2k} Y_{10}(\theta_k, \phi_k) \int_0^\infty r^2(e^{-z_1 r + ikr} + e^{-z_1 r - ikr}) dr + \sqrt{\frac{2}{\pi}} \frac{c'_2 i}{2k} Y_{10}(\theta_k, \phi_k) \int_0^\infty r^2(e^{-z_2 r + ikr} + e^{-z_2 r - ikr}) dr \\
 &= -\sqrt{\frac{2}{\pi}} \frac{c'_1}{2k^2} Y_{10}(\theta_k, \phi_k) \left[\frac{1}{(z_1 - ik)^2} - \frac{1}{(z_1 + ik)^2} \right] - \sqrt{\frac{2}{\pi}} \frac{c'_2}{2k^2} Y_{10}(\theta_k, \phi_k) \left[\frac{1}{(z_2 - ik)^2} - \frac{1}{(z_2 + ik)^2} \right] \\
 &\quad + \sqrt{\frac{2}{\pi}} \frac{c'_1 i}{2k} Y_{10}(\theta_k, \phi_k) \left[\frac{2}{(z_1 - ik)^3} + \frac{2}{(z_1 + ik)^3} \right] + \sqrt{\frac{2}{\pi}} \frac{c'_2 i}{2k} Y_{10}(\theta_k, \phi_k) \left[\frac{2}{(z_2 - ik)^3} + \frac{2}{(z_2 + ik)^3} \right] \\
 &= \sqrt{\frac{8}{\pi}} Y_{10}(\theta_k, \phi_k) \left[\frac{c'_1(z_1^3 - 3z_1 k^2)i}{k(z_1^2 + k^2)^3} + \frac{c'_2(z_2^3 - 3z_2 k^2)i}{k(z_2^2 + k^2)^3} - \frac{c'_1 z_1 i}{k(z_1^2 + k^2)^2} - \frac{c'_2 z_2 i}{k(z_2^2 + k^2)^2} \right] \\
 &= -\sqrt{\frac{8}{\pi}} 4i Y_{10}(\theta_k, \phi_k) \left[\frac{c'_1 z_1 k}{(z_1^2 + k^2)^3} + \frac{c'_2 z_2 k}{(z_2^2 + k^2)^3} \right].
 \end{aligned}$$

APPENDIX B: DERIVATION OF EQ. (8)

The derivation follows the idea in Ref. [41]. We consider the case that an electron with the wave vector k penetrates a BaTiO₃ (BTO) nanowire.

As shown in Fig. 4, the length of the penetration path is d . The energy of the electron is $E(\mathbf{k})$ and the energy of the BaTiO₃ conduction band is V_b . In the region of OH, the wave function is the plane wave including incident part and reflection part,

$$\varphi_1(x) = Ae^{ikx} + Be^{-ikx} \quad (x < 0), \quad (\text{B1})$$

$$k = \left(\frac{2m_0 E}{\hbar^2} \right)^{1/2}. \quad (\text{B2})$$

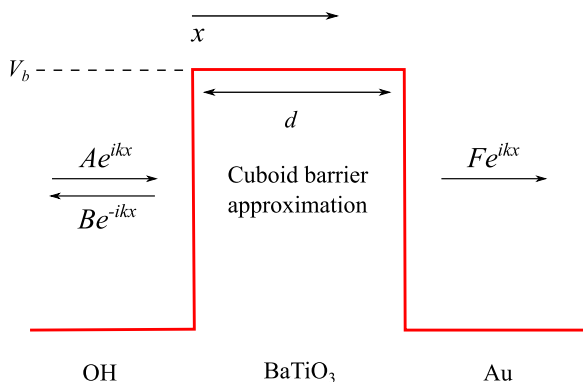


FIG. 4. (Color online) Energy barrier diagram.

In the BaTiO₃ region, the Schrödinger equation is

$$-\frac{\hbar^2}{2m_0} \frac{d^2\varphi(x)}{dx^2} + V(x) = E_{\text{BTO}}\varphi(x). \quad (\text{B3})$$

When we consider the electrons around the conduction band, we can write the potential energy term into effective mass,

$$-\frac{\hbar^2}{2m^*} \frac{d^2\varphi(x)}{dx^2} = E_{\text{BTO}}\varphi(x), \quad (\text{B4})$$

$$E_{\text{BTO}} = V_b - E(\mathbf{k}), \quad (\text{B5})$$

where m^* is the effective mass. The solution of the above Schrödinger equation is

$$\varphi_2(x) = Ce^{k'x} + De^{-k'x} \quad (0 < x < d), \quad (\text{B6})$$

$$k' = \left(\frac{2m^*(V_b - E)}{\hbar^2} \right)^{1/2}. \quad (\text{B7})$$

With the analysis above, the wave function in each region is summarized as

$$\begin{aligned}
 \varphi_1(x) &= Ae^{ikx} + Be^{-ikx} & x < 0 \\
 \varphi_2(x) &= Ce^{k'x} + De^{-k'x} & 0 < x < d \\
 \varphi_3(x) &= Fe^{ikx} & x > d.
 \end{aligned} \quad (\text{B8})$$

The tunneling probability is given by

$$P = \frac{|F|^2}{|A|^2}. \quad (\text{B9})$$

$\varphi(x)$ and $d\varphi(x)/dx$ must be continuous at the boundaries.

$$A + B = C + D, \quad (\text{B10})$$

$$ik(A - B) = k'(C - D), \quad (\text{B11})$$

$$Ce^{k'd} + De^{-k'd} = Fe^{ikd}, \quad (\text{B12})$$

$$k'Ce^{k'd} - k'De^{-k'd} = ikFe^{ikd}, \quad (\text{B13})$$

From Eqs. (B12) and (B13) we have

$$C = \frac{(k' + ik)Fe^{ikd}}{2k'e^{k'd}}, \quad (\text{B14})$$

$$D = \frac{(k' - ik)Fe^{ikd}}{2k'e^{-k'd}}. \quad (\text{B15})$$

From (B10) $\times ik +$ (B11), we have

$$A = \frac{(ik + k')C + (ik - k')D}{2ik}. \quad (\text{B16})$$

Substituting (B14) and (B15) into (B16) gives

$$A = \frac{Fe^{ikd}}{4ikk'} [(ik + k')^2 e^{-k'd} - (ik - k')^2 e^{k'd}], \quad (\text{B17})$$

$$\frac{F}{A} = \frac{4ikk'e^{-ikd}}{2(k^2 - k'^2) \sinh k'd + 4ikk' \cosh k'd}, \quad (\text{B18})$$

$$P = \frac{|F|^2}{|A|^2} = \frac{16k^2k'^2}{4(k'^2 - k^2)^2 \sinh^2 k'd + 16k^2k'^2 \cosh^2 k'd}. \quad (\text{B19})$$

Since $\cosh^2 k'd = 1 + \sinh^2 k'd$,

$$\begin{aligned} P &= \frac{16k^2k'^2}{4(k'^2k^2)^2 \sinh^2 k'd + 16k^2k'^2} \\ &= \frac{4}{4 + \frac{(k^2+k'^2)^2}{k^2k'^2} \sinh^2 k'd}. \end{aligned} \quad (\text{B20})$$

Therefore,

$$P = \frac{4}{4 + \frac{[m_0E + m^*(V_b - E)]^2}{m_0m^*E(V_b - E)} \sinh^2 \left[\frac{2m^*d^2(V_b - E)}{\hbar^2} \right]^{1/2}}. \quad (\text{B21})$$

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