

Dirac metal to topological metal transition at a structural phase change in Au_2Pb and prediction of \mathbb{Z}_2 topology for the superconductor

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Three-dimensional Dirac semimetals (DSMs) are materials that have massless Dirac electrons and exhibit exotic physical properties. It has been suggested that structurally distorting a DSM can create a topological insulator but this has not yet been experimentally verified. Furthermore, Majorana fermions have been theoretically proposed to exist in materials that exhibit both superconductivity and topological surface states. Here we show that the cubic Laves phase Au_2Pb has a bulk Dirac cone that is predicted to gap on cooling through a structural phase transition at 100 K. The low temperature phase can be assigned a $Z_2 = -1$ topological index, and this phase becomes superconducting below 1.2 K. These characteristics make Au_2Pb a unique platform for studying the transition between bulk Dirac electrons and topological surface states as well as studying the interaction of superconductivity with topological surface states, combining many different properties of emergent materials—superconductivity, bulk Dirac electrons, and a topologically nontrivial Z_2 invariant.

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I. INTRODUCTION

Dirac semimetals (DSMs) have recently emerged as a new type of electronic material with relativistic, massless electrons in the bulk [1–5]. Cd_3As_2 and Na_3Bi , for example, display Dirac points protected by crystalline symmetry, and transport experiments have shown properties such as ultrahigh mobility and large linear magnetoresistance [2,4–6]. The effects of structural and electronic instabilities on the three-dimensional (3D) Dirac spectrum are not well known to date, however. Breaking crystalline symmetry, for example, can gap out the Dirac spectrum, adding a finite mass term and creating a topological insulator [1,3]. Furthermore, the behavior of Dirac electrons in 3D materials under the influence of electronic or magnetic instabilities such as ferromagnetism and superconductivity is not yet well explored.

To date, cubic Laves phases, which are based on the pyrochlore lattice [7], have not been investigated as potential 3D DSMs although they display a range of other interesting electronic properties [8,9]. Here we report the properties and electronic structure of Au_2Pb , a cubic Laves phase [10] that has been reported to superconduct below 1.2 K [11]. Our electronic structure calculations predict that cubic Au_2Pb has a bulk Dirac cone at room temperature. The band inversion energy of this cone is much larger than in the other known 3D DSMs. We find, however, through high resolution x-ray diffraction experiments, that Au_2Pb on cooling undergoes a previously unreported symmetry breaking phase transition near 50 K,

which our calculations show to gap out the Dirac spectrum in the high temperature phase. The result is a low temperature nontrivial massive 3D Dirac phase with $Z_2 = -1$ topology. Upon further cooling, Au_2Pb becomes superconducting. This implies that Au_2Pb is a bulk superconductor with spin polarized topological surface states whose existence is guaranteed by the nontrivial Z_2 topology of the low temperature phase. The surfaces of single crystals of Au_2Pb are therefore a natural platform for realizing Majorana fermions [12] and for probing other consequences of the interaction of topological surface states with superconductivity.

II. EXPERIMENT AND CALCULATION

Single crystals of Au_2Pb were grown out of Pb flux. Synchrotron x-ray diffraction studies were performed on Au_2Pb at the Advanced Photon Source at Argonne National Laboratory on beamline 11-BM. The patterns were collected from 7 to 154 K in 2.5 K increments, with a wavelength of 0.413841 Å and a 2θ range of 0.5 to 26 deg. Structural solution was performed by utilizing distortion mode analysis by utilizing a combination of ISODISTORT and TOPAS [13,14]. The powder data were refined with the Rietveld method, using the FULLPROF program [15]. Resistivity and heat capacity measurements were performed with a Physical Property Measurement System (PPMS) from Quantum Design, equipped with a ^3He cryostat.

Electronic structure calculations were performed in the framework of density functional theory (DFT) using the WIEN2K [16] code with a full-potential linearized augmented

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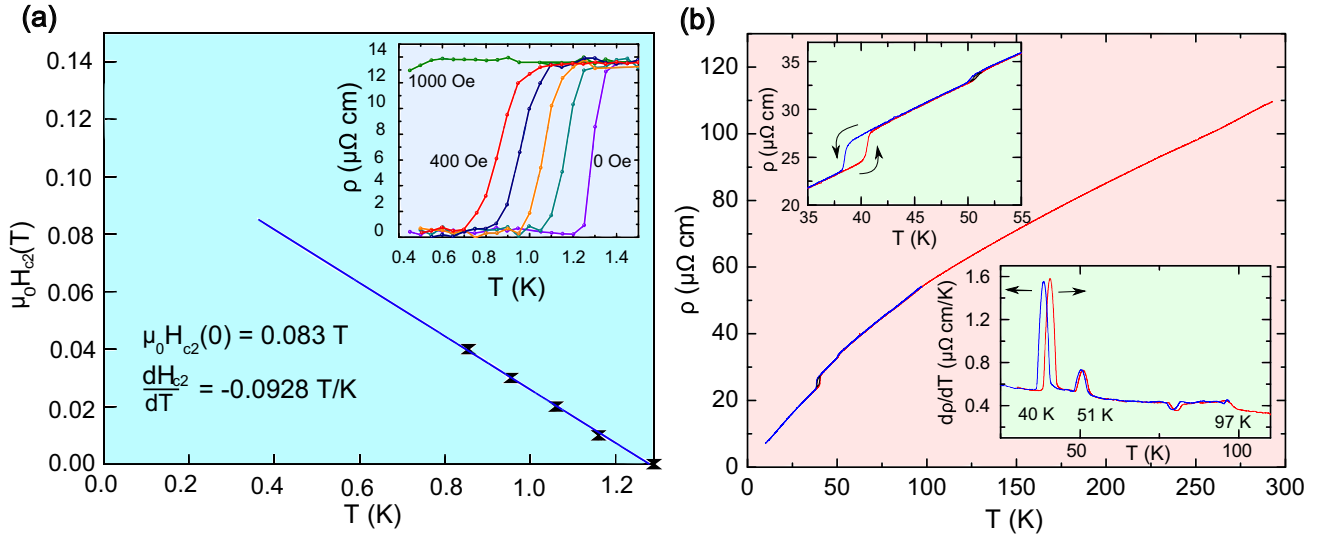


FIG. 1. (Color online) Characterization of the superconductivity and normal state resistivity in Au_2Pb . (a) Critical field determination of Au_2Pb , the blue line shows the linear fit to determine the slope $dH_{c2}/dT = -0.0928$ T/K. The inset shows the resistivity close to T_c for different fields. (b) $\rho(T)$ between 300 and 25 K. Three discontinuities can be seen, at 97, 51, and 40 K. The lower inset shows the derivative which shows the discontinuities more clearly. Blue lines represent data measured on cooling while red lines represent data measured on heating.

plane-wave and local orbitals [FP-LAPW + l_0] basis [17] together with the Perdew-Becke-Ernzerhof (PBE) parametrization [18] of the generalized gradient approximation (GGA) as the exchange-correlation functional. The plane wave cut-off parameter $R_{\text{MT}}K_{\text{MAX}}$ was set to 8 and the irreducible Brillouin zone was sampled by 560 k points (cubic) and 216 k points (orthorhombic). Experimental lattice parameters from the Rietveld refinements were used in calculations. Spin-orbit coupling (SOC) was included.

III. RESULTS

The superconducting transition for Au_2Pb was confirmed with resistivity and specific heat measurements. The resistivity shows a sharp drop at $T_c = 1.3$ K. In Fig. 1(a) the T_c determined resistively is plotted versus the applied field. A clear linear dependence of $\mu_0 H_{c2}(T)$ is seen; a linear fit to the data reveals $dH_{c2}/dT_c = -0.0928$ T/K. By using the Werthamer-Helfand-Hohenberg (WHH) relationship [19] $\mu_0 H_{c2}(0) = -0.7T_c dH_{c2}/dT_c$, we estimate the zero-temperature upper critical field to be 83 mT. The coherence length can be calculated by using the Ginzburg-Landau formula $\xi_{\text{GL}}(0) = [\phi_0/2\pi H_{c2}(0)]^{1/2}$, where $\phi_0 = h/2e$ and is found to be $\xi_{\text{GL}}(0) = 629$ Å.

Figure 2(a) presents the electronic part of the specific heat of Au_2Pb . A sharp anomaly is observed at the superconducting transition temperature (1.19 K) indicating bulk superconductivity. The behavior above T_c follows the expected $C_V = \gamma T + \beta T^3$ relation, where γT describes the electronic contribution and βT^3 the phonon contribution, related to the Debye temperature Θ_D . γ is the Sommerfeld parameter. Fitting from 1.3 to 2.5 K we obtain $\gamma = 2.2$ mJ/mol K^2 and $\Theta_D = 139.6$ K. Estimating the magnitude of the specific heat jump $\Delta C/\gamma T_c = 1.95$, higher than the BCS value of 1.43, but lower than that of elemental Pb [20]. Assuming $\mu^* = 0.13$, the electron-phonon coupling constant (λ_{ep}) can

then be calculated from the inverted McMillan's formula [21]: $\lambda_{\text{ep}} = \frac{1.04 + \mu^* \ln(\frac{\Theta_D}{1.45T_c})}{(1 - 0.62)\mu^* \ln(\frac{\Theta_D}{1.45T_c}) - 1.04}$ and is 0.58, which suggests weak coupling. The noninteracting density of states at the Fermi energy is given by $N(E_F) = \frac{3\gamma}{\pi^2 k_B^2 (1 + \lambda_{\text{ep}})}$. The value obtained for Au_2Pb , $N(E_F) = 0.6$ states eV^{-1} per formula unit, agrees well with the ≈ 0.5 states eV^{-1} per formula unit predicted by band structure calculation (see below). Table I summarizes

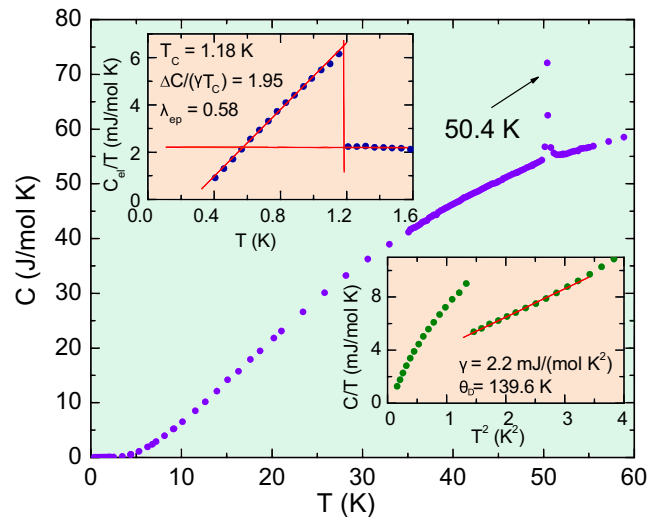


FIG. 2. (Color online) Specific heat of Au_2Pb , confirming the bulk superconductivity and a phase transition at 50.4 K. The upper inset shows the electronic specific heat vs temperature of Au_2Pb . The sharp jump indicates bulk superconductivity. The value of $\Delta C/(\gamma T_c) = 1.95$ is higher than the expected BCS value. The lower inset shows the linear fit above T_c that was used to determine the Sommerfeld coefficient γ and the coefficient for the phononic contribution to the heat capacity β .

TABLE I. Superconducting properties of Au₂Pb.

Parameter	Au ₂ Pb
T_c	1.18 K
dH_{c2}/dT	-0.0928 T/K
$\mu_0 H_{c2}$	83 mT
$\xi(0)$	629 Å
γ	2.2 mJ/mol K ²
$\frac{\Delta C}{\gamma T_c}$	1.95
Θ_D	139.6 K
λ_{ep}	0.58
$N(E_F)_{\text{measured}}$	0.6 states eV ⁻¹ /f.u.
$N(E_F)_{\text{calculated}}$	0.5 states eV ⁻¹ /f.u.

the superconducting properties. We conclude that Au₂Pb is a robust weakly coupled BCS superconductor.

The full temperature range of the resistivity is shown in Fig. 1(b). The data reveal several discontinuities, which we determined are related to structural phase transitions; one of them (at 50.4 K) is also seen in the heat capacity data (Fig. 2). In agreement with these observations, our low temperature synchrotron powder diffraction data shows that Au₂Pb undergoes two structural phase transitions on cooling. It is cubic above 100 K, below that temperature an unknown intermediate structure appears for a short range of temperature. Then on cooling to 55 K and below, a third structure appears. This is the structure of the low temperature superconducting phase. It is primitive orthorhombic and below 40 K it is the only phase remaining. We were able to fully solve the structure (R_{Bragg} value of 5.73%) in the space group $Pbcn$ with the lattice constants $a = 7.9040(7)$ Å, $b = 5.5786(10)$ Å, and $c = 11.1905(2)$ Å. Table II summarizes the atom positions. This low temperature structure is a slightly distorted version of the cubic Laves phase structure, with the pyrochlore planes being buckled (Fig. 3). Note that temperature dependent structural phase transitions of the cubic Laves phase are common [7].

The calculated electronic structures of the high temperature cubic and low temperature orthorhombic phases for Au₂Pb are shown in Figs. 4 and 5. Counting all the parity eigenvalues for the time-reversal-invariant momenta (TRIM) points of the bulk Brillouin zone (BZ) [22], gives a Z_2 invariant of -1 for both structures. [We counted 11 electrons for each Au and 4 for Pb (see Tables S1 and S2 in the Supplemental Material [23] for a listing of the parities and Fig. S1 for the influence of spin-orbit coupling to the band structure)]. In both cases the parity at Γ is opposite from the parity at all other TRIM

TABLE II. Structural information for low temperature ($T = 6.76$ K) orthorhombic Au₂Pb. Space group $Pbnc$, $a = 7.9040(7)$ Å, $b = 5.5786(10)$ Å, and $c = 11.1905(2)$ Å.

Atom	Wyckoff	x	y	z
Pb	8d	0.3696(2)	-0.0062(2)	0.1274(2)
Au 1	4c	0.0000	0.0120(4)	0.25000
Au 2	8d	0.2741(1)	0.2148(2)	0.3742(2)
Au 3	4a	0.00000	0.00000	0.00000

leading to $Z_2 = -1$. In the cubic high temperature phase there is an allowed crossing along the Γ -X line that is protected by C_4 rotation symmetry. (The point group along this line is C_{4v} , allowing for two different irreducible representations, Γ_6 and Γ_7). Since the irreducible representation of the two bands crossing at the Γ -X line is different, the crossing is protected by crystalline symmetry. In contrast, the potential cones along Γ -K are gapped out because the symmetry along this line is C_{2v} , which allows only one irreducible representation in the presence of SOC. Thus, around the Fermi level, there are massless Dirac electrons present in high temperature Au₂Pb [Figs. 4(a) and 4(b)], there are also electron and hole pockets at different places within the BZ. This of course raises the question of whether these other, non-Dirac bands at E_F will be problematic for detecting the Dirac electrons. To address this, in Fig. 4(b) we show the calculated 3D band structure of cubic Au₂Pb, which clearly indicates that the Dirac cone is in fact isolated and therefore will be detectable by ARPES studies on a cubic surface such as (0,0,1). Furthermore, a 2D energy projection of the 3D k space along a (0,0,1) surface normal that includes the nearest other Fermi pockets [Fig. 4(c)] indicates that the Dirac point is well separated from the Fermi pockets in such a 2D projection. Thus Au₂Pb, along with PtBi₂, which has a 3D Dirac cone 300 meV below the Fermi energy [24], is one of the very few cubic materials predicted to have a 3D Dirac cone. Due to the cubic symmetry there are six different Dirac cones in the BZ, in contrast to Cd₃As₂ and Na₃Bi where there are two cones in the BZ. The cones in Au₂Pb are also further apart in momentum space than the ones on Cd₃As₂ and Na₃Bi; the distance is 0.203 Å⁻¹ in Au₂Pb and 0.152 Å⁻¹ in Na₃Bi. Furthermore, the Lifshitz transition in Au₂Pb is much higher in energy than in the other two materials (roughly 400 meV), which allows the Dirac states to be probed for larger variations of the Fermi level. (In Na₃Bi it is around 130 meV and in Cd₃As₂ it is 20 meV.)

IV. DISCUSSION AND CONCLUSIONS

Upon cooling into the low temperature structure, the Dirac electrons in Au₂Pb become massive because the symmetry reduction allows the bands along Γ -X to mix. Nonetheless the superconducting low temperature phase is topologically nontrivial. The $Z_2 = -1$ invariant indicates that it must have topological surface states, which should project to the $\bar{\Gamma}$ point of the surface BZ, for all surfaces. Note that low temperature Au₂Pb is not strictly speaking a TI since the Fermi surface has electron and hole pockets. Due to the continuous gap present in the electronic structure, however, it can be viewed as an insulator with bent bands. The same is observed in elemental Sb which is a topological nontrivial metal [25]. It is important to realize that the bands crossing the Fermi level are required in order to observe superconductivity in the low temperature state; a true TI does not have a Fermi surface and therefore cannot be superconducting. In addition, surface states have been detected by APRES on other topological materials with pockets from other than Dirac electrons, such as Sb [25] or Bi₄Se₃ [26], and hence they will also be detectable in Au₂Pb. With single crystal diffraction we identified the (110), (100), and (111) surfaces of the cubic structure to be exposed in the as-grown material. Spectroscopy studies on the (100) surface,

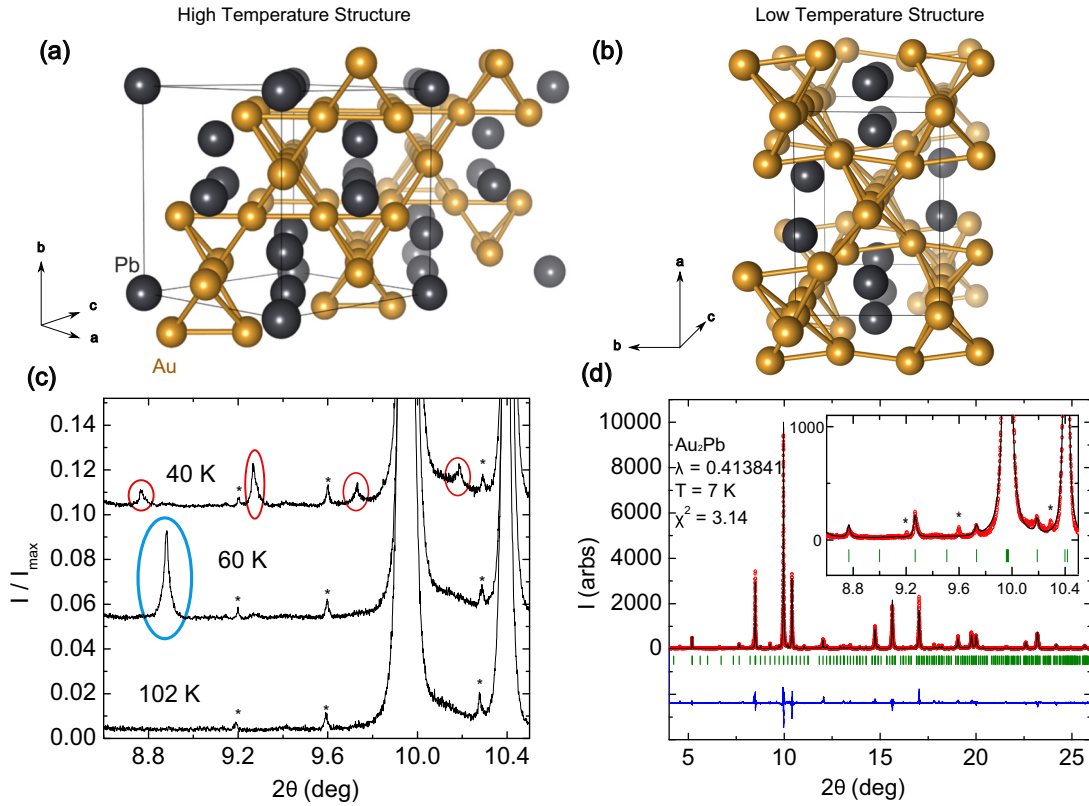


FIG. 3. (Color online) Structural information on Au_2Pb . (a) Crystal structure of the high temperature cubic Laves phase Au_2Pb . (b) Crystal structure of the low temperature orthorhombic, distorted phase of Au_2Pb . (c) Synchrotron diffraction patterns at different temperatures showing the presence of three different phases in Au_2Pb . Newly appearing peaks are circled, peaks associated with the orthorhombic phase are circled in red. Blue circled peaks belong to the intermediate phase. Impurity phases are marked with asterisks; those peaks remain present across the whole temperature regime measured. Patterns are displaced for clarity. (d) Rietveld refinement of orthorhombic Au_2Pb at 7 K, the insert shows the region shown in (c); all the newly appearing peaks are captured by the structural model.

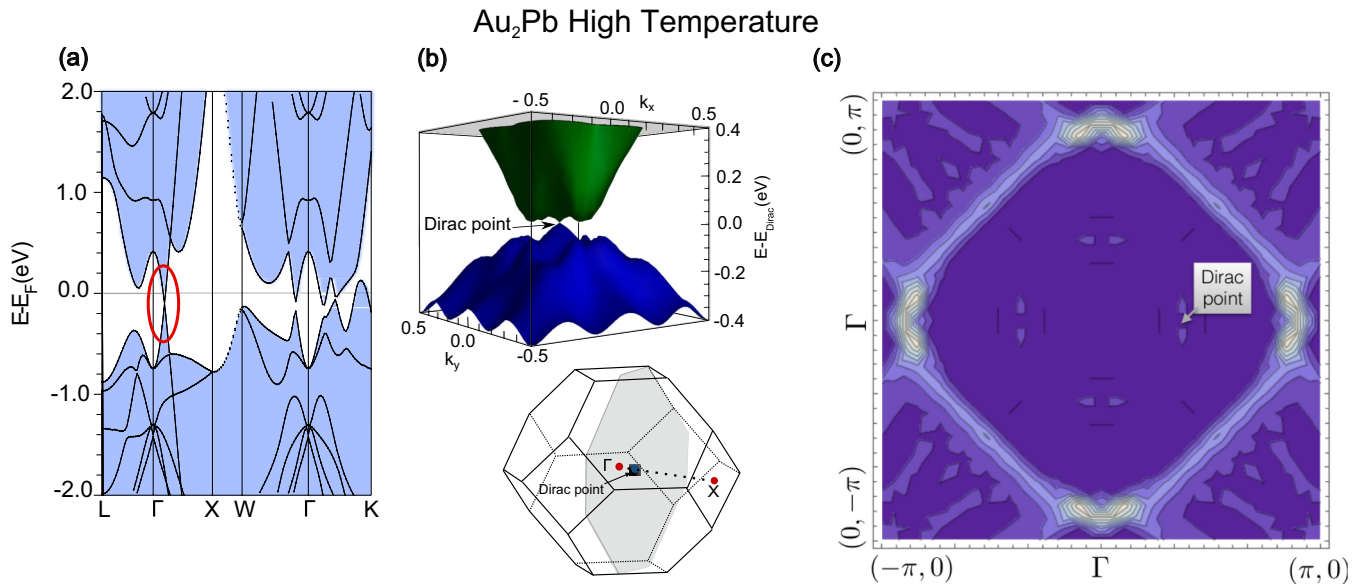


FIG. 4. (Color online) (a) Electronic structure of high temperature cubic Au_2Pb . (b) A view of the electronic structure of the high temperature phase along the (100) direction. The cubic electronic structure has a 3D Dirac cone along Γ -X (circled), which gets gapped out when the compound becomes distorted at low temperatures (Fig. 5). Despite the metallic pockets the Dirac point should be visible in APRES measured on the (100) surface. (c) 2D projection of the 3D band structure of cubic Au_2Pb , along a cubic axis such as (0,0,1). Color brightness shows the intensity of the signal that would be observed (e.g., in ARPES) by probing the bulk along this cubic axis, at energies near the energy of the Dirac cone, below the Fermi energy. The features associated with the Dirac cone are well separated, even in this 2D projection, from the Fermi surfaces of other band crossings.

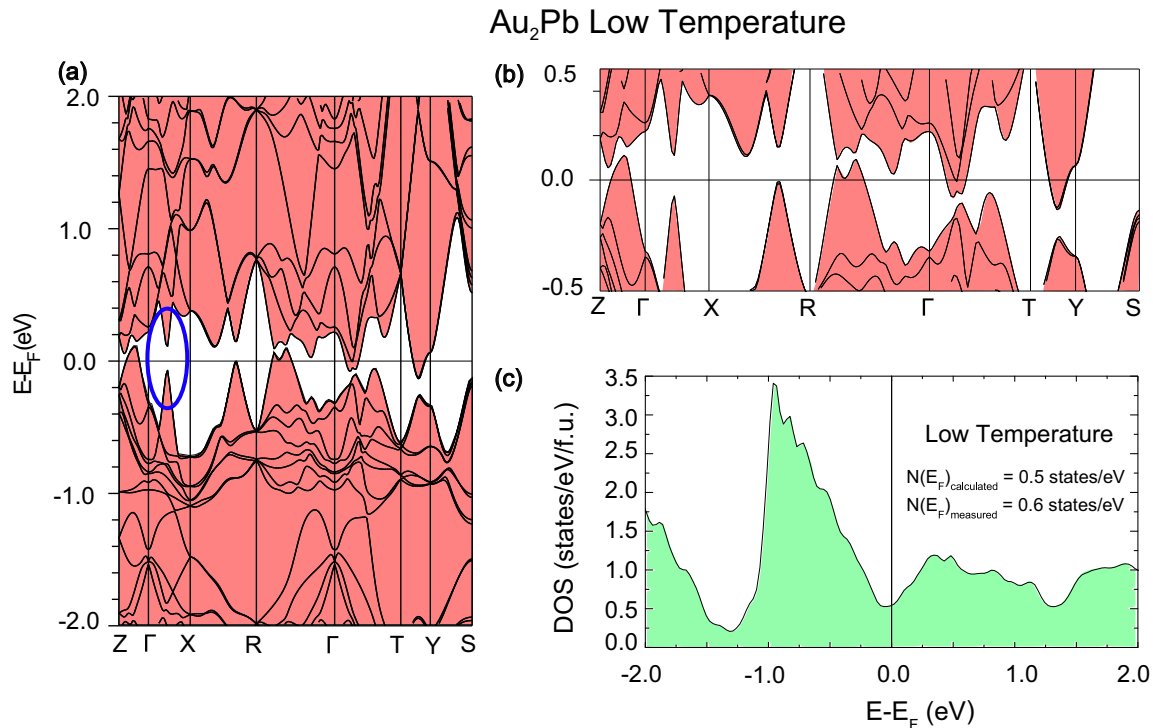


FIG. 5. (Color online) (a) Electronic structures of low temperature orthorhombic Au₂Pb. (b) Emphasizes the continuous gap in the electronic structure of orthorhombic Au₂Pb. An energy dependent density of states (DOS) plot is shown for orthorhombic Au₂Pb in (c). Orthorhombic Au₂Pb has a continuous gap and can be viewed as a semiconductor with bent bands. The calculated DOS at E_F matches well with the measured value.

which contains the projection of the Γ -X line should therefore be feasible. The fact that many surfaces are naturally exposed allows for probing many different surfaces as well. In addition, magnetotransport measurement could be undertaken with an applied field along the (100) plane, which theoretically breaks the Dirac point into two Weyl nodes.

We have presented an example of a real material where a naturally occurring symmetry change at a structural transition is predicted to gap out a 3D Dirac cone. In addition to therefore undergoing a massless to massive quasiparticle transition upon cooling, the low temperature phase of Au₂Pb is topologically nontrivial. This phase becomes superconducting. A few other materials with topological band structures have been shown to be superconducting. These are Cu_xBi₂Se₃ [27], Sn_{1-x}In_xTe [28], TlBiTe₂ [29], Tl₅Te₃ [30], and the half-Heusler alloys YPtBi [31], ErPdBi [32], LuPdBi [33], and LuPtBi [34]. Each of these has disadvantages. In Cu_xBi₂Se₃ and Sn_{1-x}In_xTe the superconductivity emerges from a parent TI material but requires doping to induce metallicity. The half-Heusler compounds do not have a continuous gap, and, in order to display surface states, strain would be needed. TlBiTe₂ also requires doping to be superconducting and has a very low T_c (0.14 K). In the case of Tl₅Te₃, the Fermi level does not lie within the continuous gap. Au₂Pb in contrast has a continuous gap throughout the BZ, with the Fermi level inside this gap and in the superconducting regime is both superconducting and topological at its native composition. Thus for Au₂Pb there is a natural interface between a spin polarized topological surface state and a superconductor in a bulk material.

Topological superconductivity is associated with quasiparticle excitations that are Majorana fermions [35]. Relevant to the case of Au₂Pb, Majorana fermions are predicted to occur at the surface of topological insulators (TIs) when the proximity effect is used to induce superconductivity [12]. The strong spin splitting of the TI allows for p -wave Cooper pairing on the surface in spite of the s -wave superconductivity in the bulk. The Fermi energy must be in the band inverted regime of the electronic structure, which is the case for Au₂Pb. Thus we argue that because the T_c of Au₂Pb is high enough for STM studies, this compound is a uniquely promising candidate for studying the interaction between superconductivity and topological surface states.

In addition, the phase transition observed in Au₂Pb allows for studies of the breakdown of the 3D Dirac cone on symmetry breaking. It has been proposed that the known 3D Dirac semimetals Cd₂As₃ and Na₃Bi should transition into a TI state if they are distorted [1,3], but this will be difficult to achieve experimentally as such distortions are not naturally occurring in these materials. Au₂Pb, in contrast, distorts naturally upon cooling. The 3D Dirac properties of cubic Au₂Pb are advantageous to other known 3D DSMs in additional ways. The cubic symmetry causes the presence of six cones rather than only two. The cones are farther apart in momentum space than the cones of other 3D DSMs. These characteristics, together with the very high band inversion energy, make Au₂Pb a unique 3D Dirac material.

Finally, we note that the electronic structure of cubic Au₂Pb does not only have the 3D Dirac cone at the Fermi level but also other bands crossing on the Γ -K line. The low temperature

electronic structure is topologically nontrivial but has a Fermi surface composed of electron and hole pockets. These pockets allow the compound to become superconducting. This is in contrast to a true TI which cannot become superconducting without doping. As such, our work on Au₂Pb indicates that 3D Dirac materials that have other pockets that are well separated away in the BZ should be an interesting focus for future research, as more instabilities and symmetry breaking transitions are possible. Au₂Pb is therefore a new type of material that combines many physical properties of interest including the transition from massless to massive electrons, topological surface states, and superconductivity. It will therefore be of significant interest for further study; ARPES study of the high temperature and low temperature phases will be of particular near-term interest.

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