Sharp magnetization jump at the first-order superconducting transition in Sr₂RuO₄

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The magnetization and magnetic torque of a high-quality single crystal of $Sr₂RuO₄$ have been measured down to 0.1 K under precise control of the magnetic-field orientation. When the magnetic field is applied exactly parallel to the *ab* plane, a sharp magnetization jump $4\pi \delta M$ of (0.74 ± 0.15) G at the upper critical field $H_{c2,ab} \sim 15$ kOe with a field hysteresis of 100 Oe is observed at low temperatures, evidencing a first-order superconducting-normal transition. A strong magnetic torque appearing when *H* is slightly tilted away from the *ab* plane confirms an intrinsic anisotropy $\Gamma = \xi_a/\xi_c$ of as large as 60 even at 100 mK, in contrast with the observed H_{c2} anisotropy of ∼20. The present results raise fundamental issues in both the existing spin-triplet and spin-singlet scenarios, providing, in turn, crucial hints toward the resolution of the superconducting nature of $Sr₂RuO₄$.

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Spin-triplet superconductors have recently become increasingly familiar, because several promising candidates have been discovered, including ferromagnetic and noncentrosymmetric superconductors (SCs). In general, crucial evidence for spin-triplet pairing is provided by an invariance of the spin susceptibility across the superconducting-normal (S-N) transition on cooling; spins of the triplet Cooper pairs can be easily polarized along the field direction perpendicular to the *d* vector, because equal-spin pairs can be formed under Zeeman-split Fermi surfaces. If such a configuration is available, the Pauli-paramagnetic effect (PPE) is absent. This feature of triplet SCs admits a high upper critical field H_{c2} that is determined solely by the orbital effect.

In $Sr₂RuO₄$, nuclear-magnetic-resonance (NMR) Knightshift [\[1\]](#page-3-0) and polarized-neutron scattering [\[2\]](#page-3-0) experiments have provided accumulating experimental evidence for a spin-triplet pairing with a chiral-*p*-wave state $d = \Delta \hat{z}(k_x + i k_y)$ [\[3,4\]](#page-3-0). In addition, an unusual *increase* of the NMR Knight shift has been recently found in the superconducting state [\[5\]](#page-3-0), which has been understood in the framework of equal-spin pairing states including the proposed chiral-*p*-wave state [\[6\]](#page-3-0). Despite compelling evidence for equal-spin pairing, the upper critical field H_{c2} of $Sr₂RuO₄$ is strongly suppressed at low temperatures for $H \parallel ab$ [\[4,7\]](#page-3-0), in a fashion very similar to the PPE in spin-singlet SCs. Accordingly, the H_{c2} anisotropy $\Gamma_H = H_{c2,ab}/H_{c2,c}$, which has a large value of ~60 near T_c , considerably reduces to ∼20 at 0.1 K [\[7,8\]](#page-3-0). The origin of the strongly *T*-dependent Γ_H has remained unresolved. A similar H_{c2} limiting has also been observed for UPt₃ in $H \parallel c$ [\[9,10\]](#page-3-0), another long-standing candidate for a spin-triplet superconductor; this limiting appears to be incompatible with an invariant Knight shift [\[11,12\]](#page-3-0). Quite recently, an even more mysterious phenomenon has been found in $Sr₂RuO₄$ by the magnetocaloric effect [\[13\]](#page-3-0) and specific-heat measurements [\[14\]](#page-3-0); the S-N transition at H_{c2} becomes of first order below about 0.8 K when the magnetic field is applied closely parallel to the *ab* plane. The first-order transition (FOT) has been reported to be accompanied by an entropy release of $(10 \pm 3)\%$ of the normal-state value at 0.2 K.

To our knowledge, the FOT in the presence of a strong suppression of H_{c2} has only been predicted for spin-singlet SCs exhibiting a strong PPE [\[15\]](#page-3-0), as is the case of a *d*wave superconductor $CeCoIn₅$ [\[16–18\]](#page-3-0), in which a distinct jump in the magnetization has been observed [\[19\]](#page-3-0). Plausibly, $Ba_xK_{1-x}Fe₂As₂$ [\[20,21\]](#page-3-0) may also exhibit this type of FOT, although the specific-heat and magnetization jumps have not yet been clearly observed [\[22,23\]](#page-3-0). In sharp contrast, the origin of FOT in $Sr₂RuO₄$ has remained unidentified because no PPE is expected in the basal plane for the anticipated chiral-*p*wave order parameter. Further experimental investigations are clearly needed to uncover its mechanism.

To this end, quantitative evaluation of the magnetization jump at FOT is of primary interest. Magnetization of $Sr₂RuO₄$ in the superconducting state was previously measured with a crystal of dimensions of $3 \times 3 \times 0.5$ mm³ ($T_c = 1.42$ K) [\[24\]](#page-3-0). The result shows a two-step change of slope below H_{c2} at 0.14 K, which was interpreted as the occurrence of a different superconducting phase; no clear evidence of FOT was obtained. In the present Rapid Communication, we succeed in detecting a sharp magnetization jump of as large as 0.74 G at the FOT at 0.1 K using an ultraclean sample. Moreover, we estimate the intrinsic anisotropy parameter $\Gamma = \xi_a/\xi_c$ from the analysis of the magnetization torque that appears when *H* is slightly tilted away from the basal plane, and obtain a significantly large value $\Gamma \sim 60$ even at 0.1 K, confirming the anisotropy reported in Ref. $[25]$, but this time on a thermodynamical basis. This result implies a large in-plane orbital limiting field of 45 kOe at $T = 0$, three times as large as the observed $H_{c2,ab}$.

Magnetization *M* was measured down to 0.1 K in a dilution refrigerator by using a high-resolution capacitively detected Faraday magnetometer [\[26\]](#page-4-0). A magnetic field as well as a field gradient of 500 Oe*/*cm were applied parallel to the vertical (*z* axis) direction. A high-quality single crystal of $Sr₂RuO₄$ ($T_c = 1.50$ K) used in the present study was grown by a floating-zone method [\[27\]](#page-4-0). To avoid possible crystal inhomogeneity as well as a field distribution in the sample caused by the field gradient, a tiny crystal with dimensions

FIG. 1. (Color online) Field dependence of the magnetization $M_{SC} = M - \chi_n H$ at 0.1 K for *H* || *ab*, where $\chi_n H$ is the normal-state contribution. The solid line represents the M_{av} data obtained by averaging the increasing- and decreasing-field data (M_{SC}^{u} and M_{SC}^{d}). The upper inset is an enlarged view near H_{c2} . The lower inset shows dM_{av}/dH , compared with the previous results [\[24\]](#page-3-0) (crosses).

of roughly $1 \times 0.4 \times 0.3$ mm³ (0.72 mg mass) was selected. It was fixed on a stage of the capacitor transducer so that the crystal [110] axis, the longest dimension of the sample shape, is positioned at $z = 0$ nearly parallel to the horizontal $(x \text{ axis})$ direction. The capacitor transducer was mounted on a stage that can be tilted around the *x* axis, whose tilting angle was precisely controlled from the top of the refrigerator insert [see the Supplemental Material [\[28\]](#page-4-0) (I) for details]. The fine tuning of the angle *θ* between a magnetic field and the crystal *ab* plane was accomplished with an accuracy of better than ±0*.*05◦.

The field dependence of the superconducting magnetization $M_{\text{SC}} = M - \chi_n H$ measured at 0.1 K is shown in Fig. 1. Here, χ_n is the paramagnetic susceptibility in the normal state. As clearly seen in the enlarged plot near H_{c2} (upper inset), M_{SC} exhibits a sharp jump with a hysteresis of the onset field of about 100 Oe, clearly evidencing FOT. Note that this hysteresis in the *onset* field is totally different from the ordinary magnetization hysteresis caused by vortex pinning. This magnetization jump grows below about 0.6 K [see the Supplemental material $[28]$ (II)]. The solid line in Fig. 1 is the average of M_{SC} in the increasing- and decreasing-field sweeps, labeled as *M*av. The lower inset of Fig. 1 shows a field derivative dM_{av}/dH of the present data (solid line), indicating a sharp peak associated with the FOT at *H*c2. For comparison, dM_{av}/dH of the previous report [\[24\]](#page-3-0) obtained with a field gradient of 800 Oe*/*cm is also shown (crosses). The much narrower (larger) peak width (height) of the present result clearly demonstrates the higher quality of the present sample and a smaller field inhomogeneity.

The data in Fig. 1 show that the M_{av} jump at the first-order S-N transition δM is (0.01 \pm 0.002) emu/g, i.e., $4\pi \delta M =$ (0.74 ± 0.15) G using a density of 5.9 g/cm³. According to the Clausius-Clapeyron equation $dH_{c2}/dT = -\delta S/\delta M$, δM is estimated to be (0.011 ± 0.006) emu/g by using the previously reported entropy jump $\delta S/T = (3.5 \pm 1) \text{ mJ}/(\text{K}^2 \text{ mol})$ and $dH_{c2}/dT \sim (-2 \pm 0.5) \text{ kOe/K}$ [\[13\]](#page-3-0) at 0.2 K. Thus, the δM value determined in the present experiment is consistent with the results of the thermal measurements [\[13,14\]](#page-3-0).

FIG. 2. Field dependence of (a) a raw-capacitance data measured in 0 Oe/cm, ΔC_0 , where the normal-state value has been subtracted, and (b) $d(\Delta C_0)/dH$ at 0.1 K. Numbers labeling the curves represent the field angle *θ* measured from the *ab* plane in degrees. Each data in (a) and (b) is vertically shifted by $\pm 2 \times 10^{-4}$ pF and $\pm 1 \times 10^{-7}$ pF/Oe, respectively, for clarity. (c) Angle *θ* dependence of the intensity of a peak in $d(\Delta C_0)/dH(H)$ appearing near H_{c2} .

Figures $2(a)$ and $2(b)$ represent the field dependence of the raw-capacitance data ΔC_0 and $d(\Delta C_0)/dH$, respectively, measured at 0.1 K in various field orientations under a gradient field of 0 Oe*/*cm. Here, the normal-state value has been subtracted for each curve. Note that the main contribution of ΔC_0 comes from the magnetic torque $\tau = M \times H$. In a magnetic field exactly parallel to the *ab* plane ($\theta = 0$), $\Delta C_0(H)$ is almost invariant with changing field. By tilting the field orientation slightly away from the *ab* plane, ΔC_0 and $d(\Delta C_0)/dH$ become significantly large in the superconducting state. A steep change in ΔC_0 and a very sharp peak $\lim_{\epsilon \to 0} |d(\Delta C_0)/dH|$ are seen near H_{c2} only when $0.2 \lesssim |\theta| \lesssim 2^{\circ}$ [Fig. 2(c)]. This fact, combined with the M_{av} jump at $\theta = 0$, confirms that the S-N transition is of first order in a very narrow *θ* range of $|\theta| \lesssim 2^\circ$.

In Figs. [3\(a\)](#page-2-0) and [3\(b\),](#page-2-0) the $\Delta C_0(H,\theta)$ data at 0.1 K are plotted as a function of *θ* for several fixed magnetic fields. At any fields presented here, $\Delta C_0(\theta)$ develops at low θ close to 0°. In the high-field regime, e.g., 11 kOe $\leq H \leq 13$ kOe, ΔC_0 suddenly becomes zero around $|\theta| \sim 2^{\circ}$ due to the first-order S-N transition. By contrast, in the intermediate-field region, e.g., 5 kOe $\leq H \leq 7$ kOe, ΔC_0 remains finite and decreases gradually toward zero for $|\theta| \gtrsim 2^\circ$.

The behavior in $\Delta C_0(H,\theta)$ can be understood as the occurrence of the transverse magnetic flux perpendicular to the applied field in a quasi-two-dimensional superconductor, irrespective of the superconducting symmetry; the transverse field is induced so that the magnetic-flux orientation is tilted toward the crystal *ab*-plane direction because the magnetic vortex disfavors to penetrate from one to another layer of the *ab* plane for a small *θ*. The transverse flux can be detected by *τ* (*θ,H*) as well as the vortex-lattice form factor (*F*), which reflects the spatial distribution of the transverse flux. As represented in Fig. [3\(d\)](#page-2-0) by crosses, a peak in $|\Delta C_0(\theta)|$ always stays at $|\theta| \sim 1.5^{\circ}$ in the intermediate-field regime.

FIG. 3. (Color online) (a), (b) Field-angle *θ* dependence of the raw-capacitance data ΔC_0 at various fields for $T = 0.1$ K. Each data is vertically shifted by -4×10^{-4} pF for clarity. Numbers labeling the curves show the applied field in kG. The dashed lines are the calculated results using Eq. (1). (c) Angle θ dependence of $|\Delta C_0|$ normalized by its value at 1.5[°], $|\Delta C_0^*|$, at 0.1 K (circles) and the vortex-lattice form factor $F^2(\theta)$ at 40 mK (squares) in 7 kOe [\[25\]](#page-4-0). Triangles are the calculated data of the magnetic torque normalized by its maximum value $|\tau_c^*|$ on the basis of the microscopic theory for a spin-singlet superconductor [\[30\]](#page-4-0). The behavior for a spin-triplet superconductor with conventional orbital limiting is expected to be essentially the same. (d) Angle θ dependence of H_{c2} (circles) plotted with a contour map of $\Delta C_0(H,\theta)$. The open (solid) circles represent the first- (second-) order S-N transition. The peak position in $|\Delta C_0(H,\theta)|$ at 0.1 K (cross) and that in $F^2(H,\theta)$ detected from SANS experiments at 40 mK (squares [\[25\]](#page-4-0)) are also shown.

This peak angle is in good agreement with that of $F^2(\theta)$ [squares in Fig. $3(d)$] determined from the recent small-angle neutron scattering (SANS) experiment [\[25\]](#page-4-0). Indeed, $\Delta C_0(\theta)$ and $F^2(\theta)$ data at 7 kOe coincide sufficiently, as displayed in Fig. $3(c)$. These facts support that both are attributed to the same origin, namely, the induced transverse flux.

The *θ* dependence of *τ* for a quasi-two-dimensional superconductor with a conventional orbital-limited H_{c2} can be written as [\[29\]](#page-4-0)

$$
\tau(\theta) \propto \frac{\sin(2\theta)}{\sqrt{\cos^2 \theta + \Gamma^2 \sin^2 \theta}} \ln \frac{\eta \Gamma H_{c2,c}}{B \sqrt{\cos^2 \theta + \Gamma^2 \sin^2 \theta}}, \quad (1)
$$

where $\Gamma = \xi_a/\xi_c$ is the anisotropy ratio of the coherence length, and *η* is a coefficient (*η* ∼ 1). The peak of *τ* (*θ*) occurring at $\theta \sim 1.3^\circ$ can be explained with $\eta = 1.5$ and $\Gamma = 60$ [dashed lines in Figs. 3(a) and 3(b)], the Γ_H value of Sr_2RuO_4 near T_c [\[8\]](#page-3-0). If we adopt $\Gamma = 20$, the Γ_H value at low temperatures [\[7,8\]](#page-3-0), the $\tau(\theta)$ peak moves to $\theta \sim 3^{\circ}$, in disagreement with the experiment. The angular variation of $\tau(\theta)$ calculated on the basis of the microscopic theory using $\Gamma = 60$ [\[30\]](#page-4-0) is also in good agreement with the experiment, as indicated by triangles in Fig. $3(c)$. We should note here that, although the calculation of $\tau(\theta)$ in Fig. 3(c) was made based on a model of spin-singlet superconductivity, it is expected

FIG. 4. (Color online) (a) Field dependence of the total magnetization M_t , the spin magnetization M_s , and the orbital diamagnetism M_{dia} at $T = 0.1T_c$ and $\theta = 0$, obtained from the microscopic calculation for a Pauli-limited spin-singlet superconductor [\[30\]](#page-4-0) with the same parameters for the calculation of $|\tau_c^*|$. Here, the calculated magnetizations are normalized by M_0 , defined as $\chi_n H_{c2}$ in (a). (b) M_{dia} calculated for a chiral-p-wave superconductor [\[34\]](#page-4-0) with $\Gamma = 60$, $\kappa = 162$, $T = 0.1T_c$, and $\theta = 0$, normalized by M_0 , the same parameter in (a). For (b), M_s shall follow $\chi_n H$ in (a).

that models of spin-triplet superconductivity provide nearly the same results. These analyses suggest that the intrinsic anisotropy Γ of Sr₂RuO₄ is large (Γ ~ 60) and independent of *T* . This fact implies that the conventional in-plane orbital limiting field $H_{c2,ab}^{orb}$ reaches ~45 kOe at $T = 0$.

To briefly summarize the experimental results, FOT in Sr2RuO4 is characterized by an entropy jump *δS* of ∼10% of the normal-state value $\gamma_n T$ [\[13\]](#page-3-0), a magnetization jump δM of ∼25% of *χ*n*H*c2*,ab* (≈3 G), and a strongly suppressed*H*c2*,ab*(0) $(\approx 1/3$ of $H_{c2,ab}^{orb})$.

Note that these are similar to the characteristic features of FOT in spin-singlet SCs driven by a strong PPE. We calculate the field dependence of the magnetization of a strongly Pauli-limited spin-singlet (s -wave) SC at $T = 0.1T_c$ by numerically solving the microscopic Eilenberger equation using a three-dimensional cylindrical Fermi surface and $\Gamma =$ 60. The details of the calculation method have been reported in Refs. [\[31,32\]](#page-4-0). The Maki parameter μ is chosen to be 2.4 for *H* \parallel *ab* and 0.04 for *H* \parallel *c*, so that $H_{c2,ab}(0)/H_{c2,ab}^{orb} \approx 1/3$ and $H_{c2,c}(0)/H_{c2,c}^{orb} \approx 1$. The Ginzburg-Landau parameter $\kappa = 2.7$ for $H \parallel c$ [\[4\]](#page-3-0) is adopted and κ for $H \parallel ab$ is set to be 162. From this calculation, a clear FOT is reproducible, as shown in Fig. $4(a)$, where M_s and M_{dia} indicate the spin and the orbital contributions to the total magnetization M_t , respectively. The jump in M_t is predominantly due to a change in M_s . The diamagnetic contribution M_{dia} to the jump is small, roughly 10% of that of M_s . Note that the calculated magnetizations in Fig. $4(a)$ are normalized by the value $M_0 = \chi_n H_{c2}$. If we adopt $4\pi M_0 = 3$ G [\[4\]](#page-3-0), the calculated M_t jump is equal to 1.1 G. Instead, if M_t is normalized by the equality $-\int_0^{H_{c2}} (M_t - \chi_n H) dH = H_c^2 / 8\pi$ ($H_c = 194$ Oe [\[33\]](#page-4-0)), the magnetization jump becomes about 0.9 G. In any case, the calculated discontinuity in M_t is in reasonably good agreement with the observed value of (0.74 ± 0.15) G, in spite of the highly simplified model. The slight difference between the experimental observation and the calculated M_t jump can be solved by considering the multiband effect.

However, the present results raise a fundamental quantitative issue against the PPE scenario as well. Within the PPE scenario for spin-singlet superconductivity, a jump in M_s as well as a jump in S/T can be ascribed to a discontinuous increase in the zero-energy quasiparticle density of states. Because of this fact, it is expected that the jump heights relative to the normal-state values in magnetization and entropy should be nearly equal to each other, i.e., $\delta M_s / \chi_n H_{c2,ab} \simeq \delta S / \gamma_n T$. Indeed, a microscopic calculation supports this idea [\[32\]](#page-4-0). On the other hand, in the experiment, a substantial discrepancy between *δM/χ*n*H*c2*,ab* (∼25%) and *δS/γ*n*T* (∼10%) [13] has been observed. Hence, the observed ratio between *δM* and *δS* quantitatively contradicts the PPE scenario, although the Clausius-Clapeyron relation manifests the accuracy of the ratio *δM/δS*, as we described above. In other words, *δM* should contain a large fraction of nonspin contribution, and the observed H_{c2} slope is flatter than the expectation for the PPE scenario by a factor of 2.5. In addition, as already mentioned, this scenario results in a sizable suppression of the spin susceptibility below H_{c2} , which contradicts the NMR [1] and neutron-scattering [2] results.

Another question is whether the observed magnetization jump can be explained by the anticipated chiral-*p*-wave order parameter. Microscopic calculations of the magnetization of the chiral- p -wave state $[34]$ have been done by using the parameters $\Gamma = 60$ and $\kappa = 162$, and an example of the results for *H* \parallel *ab* at *T* = 0.1*T*_c is given in Fig. [4\(b\).](#page-2-0) Because *H* \perp *d* in this configuration, the spin part M_s is irrelevant, and only

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the diamagnetic contribution M_{dia} is shown. M_{dia} is suppressed smoothly toward H_{c2} ($=$ H_{c2}^{orb}) with increasing field, and no FOT occurs, as expected. The M_{dia} value at $H = H_{c2}^{\text{orb}}/3$, the actual upper critical field for $Sr₂RuO₄$, is only 0.2 G, much smaller than the observed M_{av} jump of (0.74 \pm 0.15) G. This discrepancy can be resolved by considering the constraint $-\int_0^{H_{c2}} M_{\text{dia}} dH = H_c^2/8\pi = \text{const; if } H_{c2}$ is suppressed below the orbital limiting field by any mechanism, M_{dia} should be augmented so as to conserve the condensation energy. However, at this stage, we are not aware of theoretical models to explain a strong H_{c2} suppression in the spin-triplet state with invariant spin susceptibility. Alternatively, a "hidden" depairing mechanism not considered in the framework of the two-dimensional chiral-*p*-wave scenario, such as those related to the internal angular moment of the Cooper pair, might be important. Unless such a depairing mechanism is introduced, it seems difficult to reconcile the present results with the NMR and neutron Knight-shift results [1,2,5].

In summary, a sharp magnetization jump of (0.74 ± 0.15) G, evidencing a first-order S-N transition, is clearly observed. This result provides information toward an understanding of the superconducting nature of $Sr₂RuO₄$.

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