

# Collapse of spin gap by Ru-site substitution in the antiferromagnetic Kondo semiconductor $\text{CeRu}_2\text{Al}_{10}$

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(Received 26 June 2014; revised manuscript received 29 September 2014; published 17 October 2014)

We investigated the Ce- and Ru-site substitution effects on the spin gap in  $\text{CeRu}_2\text{Al}_{10}$  by measuring the magnetic and thermal properties of  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ) and  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Re}, \text{Rh}$ ) system, respectively. The magnetic susceptibility shows that the itinerant and localized nature is enhanced by Re and Rh doping, respectively. In the latter, the orientation of the magnetic moment in the antiferromagnetic ordered phase suddenly changes from the  $c$  to  $a$  axis at  $x = 0.03$ . The orientation of the magnetic moment to the  $a$  axis is consistent with the large anisotropy of the magnetic susceptibility in the paramagnetic region. The specific heat shows that the exponential temperature dependence,  $e^{-\Delta/k_B T}$ , and the electronic specific coefficient  $\gamma$  is not changed in the Ce-site substituted systems at least up to  $y = 0.1$  but in the Ru-site substituted systems, the  $e^{-\Delta/k_B T}$  dependence disappears, and the  $\gamma$  value increases rapidly with  $x$ . These indicate that although the spin gap is robust against the Ce-site substitution by Ln ion at least up to  $y = 0.1$ , the spin gap is rapidly collapsed by the Ru-site substitution and in place, the conduction electron with heavy effective mass appears at the Fermi level. The spin gap which is formed under the subtle balance between the localized and itinerant nature is easily collapsed by a small amount of Re or Rh doping.

DOI: [10.1103/PhysRevB.90.165124](https://doi.org/10.1103/PhysRevB.90.165124)

PACS number(s): 75.30.Gw, 75.30.Mb, 71.27.+a

## I. INTRODUCTION

The Kondo insulator has continued to be one of the topics in the strongly correlated electron systems [1]. This system is characterized by the hybridization gap originating from the many-body effect between the conduction and  $f$  electrons. The ground state of the Kondo insulators known up to now is the spin singlet and the magnetic order does not take place, due to the stronger  $c$ - $f$  hybridization than the magnetic interaction. The Kondo semimetal with nonmagnetic ground state,  $\text{CeNiSn}$ , has been studied extensively as a typical compound which belongs to such a category and the experimental results have been discussed based on the existence of the V-shaped gap [2–5]. One of the big unresolved issues in this hybridization gap is the rapid collapse by doping, which should be associated with the strong correlation between the  $4f$  and conduction electron and also the coherence effect. Although several models have been proposed for the mechanism of the gap collapse by doping, it has not yet been clarified [1,6]. When the different kinds of interaction constructing the hybridization gap and magnetic order compete with each other, a new type of ground state and also an unusual doping effect are expected.

Recently discovered  $\text{CeRu}_2\text{Al}_{10}$  with the antiferromagnetic (AFM) ordering temperature  $T_0 = 27$  K is the very such a compound [7,8]. The anisotropic deviation of the lattice constants from the lanthanide contraction indicates the importance of the anisotropic  $c$ - $f$  hybridization in the AFM ordered phase [9]. There exist the following unusual properties in this compound [7–22]. (i) The AFM transition temperature is very high regardless of a large Ce-Ce distance [7,8]. (ii) The magnetic anisotropy in the AFM ordered phase is quite strange, where  $m_{\text{AF}} \parallel c$  is realized in spite of a large magnetic anisotropy,  $\chi_a \gg \chi_c \gg \chi_b$  in the paramagnetic region [10–12]. Here,  $m_{\text{AF}}$  is the AFM moment and  $\chi_a$  is the magnetic susceptibility along

the  $a$  axis, etc. Furthermore, the orientation of  $m_{\text{AF}}$  is easily changed from the  $c$  to  $b$  axis in the  $bc$  plane but is never oriented to the  $a$  axis by a small magnetic field or pressure and also by a small amount of La doping. When the magnetic field is applied to the  $c$  axis, a spin-flop transition from the  $c$  to  $b$  axis takes place at a relatively small magnetic field,  $H_{\text{sf}}$  in spite of  $\chi_a \gg \chi_c \gg \chi_b$  [17–19]. A small amount of La doping makes  $m_{\text{AF}} \parallel b$  more stable than  $m_{\text{AF}} \parallel c$  and the orientation of  $m_{\text{AF}}$  is quite easily changed from the  $b$  to  $c$  axis by a small pressure [21]. Thus, the magnetization easy axis below  $T_0$  is located in the  $bc$  plane in spite of  $\chi_a \gg \chi_c \gg \chi_b$  in the paramagnetic region, and the magnetic anisotropy in the  $bc$  plane is small. (iii) The pressure effect on  $T_0$  is very large and anisotropic, indicating the importance of the anisotropic  $c$ - $f$  hybridization in the AFM ordered phase [23]. (iv) A large spin and charge gap appear in the AFM ordered phase, whose origin has not yet been clarified, although it is inevitable to understand the unusual AFM order in  $\text{CeRu}_2\text{Al}_{10}$  [24–29].

Recently, in  $\text{Ce}(\text{Ru}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ , the drastic change of the magnetic property was reported in a small  $x$  region [30–32]. More recently, the similar doping effects were reported also in  $\text{Ce}(\text{Os}_{1-x}\text{Ir}_x)_2\text{Al}_{10}$  [33–35]. This drastic change is the rotation of  $m_{\text{AF}}$  from the  $c$  to  $a$  axis at  $x_c = 0.03$ , which is consistent with  $\chi_a \gg \chi_c \gg \chi_b$  above  $T_0$  but could never be achieved except by Rh doping. Its origin was ascribed to the suppression of the strong  $c$ - $f$  hybridization along the  $a$  axis by Rh doping [30]. Hoshino and Kuramoto discussed the possibility of the localized and itinerant transition in the Kondo AF magnet [36]. Thus, in the AFM Kondo semiconductor,  $\text{CeRu}_2\text{Al}_{10}$ , there exists a new type of doping effect, which has not been reported in the AFM heavy electron metallic compounds.

To understand the unusual AFM order in  $\text{CeRu}_2\text{Al}_{10}$ , we should clarify the origin of the unusual magnetic anisotropy and also spin gap in the AFM ordered phase. In the present paper, we performed the detailed investigation of the doping

effects on magnetic and thermal properties in  $\text{CeRu}_2\text{Al}_{10}$  to clarify the origin of the drastic change induced by doping.

## II. EXPERIMENTAL

Single crystals of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}: x = 0.02, 0.03, 0.04, 0.05$ , and  $\text{T} = \text{Re}: x = 0.05$ ) and  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}: y = 0.05$  and  $1$ ,  $\text{Ln} = \text{Pr}: y = 0.1$ ,  $\text{Ln} = \text{Y}: y = 0.1$ ) were prepared by the Al self-flux method. The magnetic susceptibility and specific heat were measured by using MPMS and PPMS (Quantum Design), respectively. Some of the results of the magnetic susceptibility and specific heat of  $\text{Ce}_{1-y}\text{La}_y\text{Ru}_2\text{Al}_{10}$  were already reported in Ref. [13].

Figure 1(a) shows the temperature ( $T$ ) dependence of the magnetic susceptibility ( $\chi$ ) of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}, \text{Re}$ ) and  $\text{Ce}_{0.9}\text{La}_{0.1}\text{Ru}_2\text{Al}_{10}$ . Figures 1(b) and 1(c) show  $\chi_a$  and  $\chi_c$  at low temperatures, respectively.  $\chi_b$  is not shown because of a small doping effect in all the cases. The inset of Fig. 1(a) shows the  $x$  dependence of the transition temperatures of  $\text{Ce}(\text{Ru}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$ , which shows a smooth variation up to  $x = 0.05$  without showing an anomaly at  $x = 0.03$ . In  $\text{Ce}_{0.9}\text{La}_{0.1}\text{Ru}_2\text{Al}_{10}$ , a doping effect on  $\chi_a$  is small, while a decrease of  $\chi_c$  below  $T_0$  disappears as a result of the reorientation of  $m_{\text{AF}}$  from the  $c$  to  $b$  axis [21]. On the other hand, in Rh doping, a big change appears in  $\chi_a$ . The downward deviation of  $\chi_a$  from the high temperature Curie-Weiss behavior below

$\sim 100$  K is suppressed and a normal Curie-Weiss behavior is observed. In the low temperature region, for  $x = 0.02$ ,  $\chi$  along three crystal axes exhibit the similar  $T$  dependencies to those in  $\text{CeRu}_2\text{Al}_{10}$ . Especially, a decrease of  $\chi_c$  below  $T_0$  is clear, indicating that the AFM order with  $m_{\text{AF}} \parallel c$  as in  $\text{CeRu}_2\text{Al}_{10}$ . A drastic change appears at  $x = 0.03$ .  $\chi_a$  shows a sharp peak at  $T_N$  and a rapid decrease below  $T_N$ . On the other hand, a sharp decrease of  $\chi_c$  below  $T_N$  disappears and is replaced by a weak  $T$  dependence. This indicates that the orientation of  $m_{\text{AF}}$  is changed from the  $c$  to  $a$  axis in this sample. Also for  $x = 0.05$ , the similar behaviors are seen in  $\chi_a$  and  $\chi_c$ . We note that for  $x = 0.03$ , there exist two transitions at  $T_N = 23.5$  K and  $T_0 = 25.5$  K. They are more clearly seen in specific heat, which will be shown later. This indicates that a drastic change takes place just at  $x_c = 0.03$  as is clearly seen in the inset of Fig. 1(a). We note that  $m_{\text{AF}} \parallel a$  is realized below  $T_N$  and  $m_{\text{AF}} \parallel c$  is realized between  $T_N$  and  $T_0$ . On the other hand, in Re doping,  $\chi_a$  is suppressed largely in a wide temperature range and a broad maximum is seen at  $\sim 27$  K.

Here, we comment the upturn of  $\chi$  seen below  $\sim 10$  K in the present results. In La doping, it is rather isotropic and could be ascribed to a free Ce ion which does not take part in the AFM order. In Rh doping with  $x = 0.02$ , the upturn in  $\chi_a$  is significant, although the effect on  $\chi_c$  is small. This might be because the  $c$ - $f$  hybridization along the  $a$  axis is suppressed, a singlet nature is suppressed, and a free magnetic ion character is dominant. For  $x > 0.03$ , the increase of  $\chi_a$  below  $\sim 10$  K which is seen for  $x = 0.02$  is rapidly suppressed and disappears completely for  $x = 0.05$ . This indicates that a very stable AFM order with  $m_{\text{AF}} \parallel a$  is realized for  $x = 0.05$ .

Figures 2(a) and 2(b) show the  $T$  dependencies of the specific heat,  $C$  of  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ) and those in the form of  $C_{4f}/T$ , respectively. Here, we note that the crystalline electric field ground state of  $\text{PrRu}_2\text{Al}_{10}$  is a singlet.  $C_{4f}$  is a magnetic part of  $C$  obtained by subtracting that of  $\text{LaRu}_2\text{Al}_{10}$  as a phonon contribution. In  $\text{CeRu}_2\text{Al}_{10}$ ,  $C_{4f}$  shows a mean-field-like  $T$  dependence, i.e., the  $e^{-\Delta/k_B T}$  dependence with  $\Delta \sim 100$  K at low temperatures and a sharp peak at  $T_0$ ,

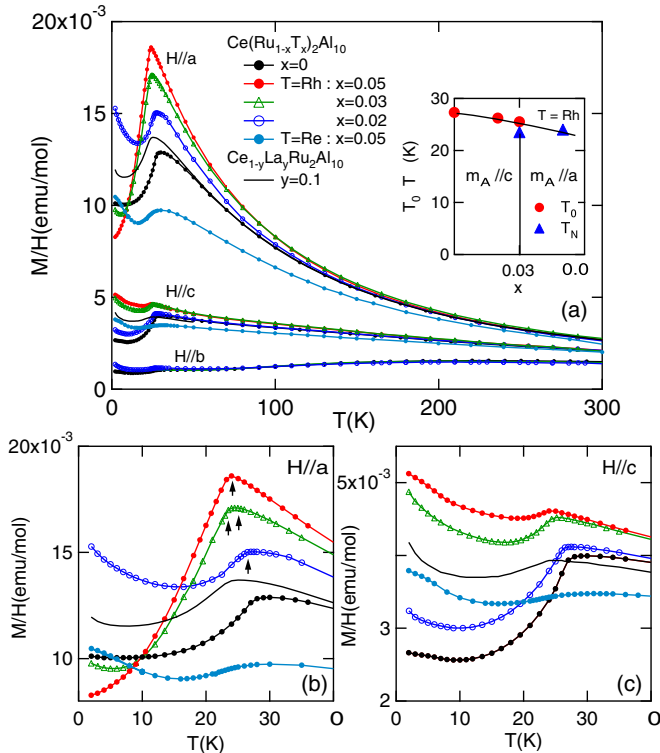


FIG. 1. (Color online) (a) Temperature dependence of  $\chi$  along the three crystal axes of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}, \text{Re}$ ) and  $\text{Ce}_{0.9}\text{La}_{0.1}\text{Ru}_2\text{Al}_{10}$  measured at  $H = 1$  T; (b)  $\chi_a$  and (c)  $\chi_c$  in an expanded scale at low temperatures. The arrows in Fig. 1(b) indicate the transition temperatures for  $\text{T} = \text{Rh}$ . The inset in Fig. 1(a) is the  $x$  dependence of the transition temperatures of  $\text{Ce}(\text{Ru}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$  at  $H = 0$ .

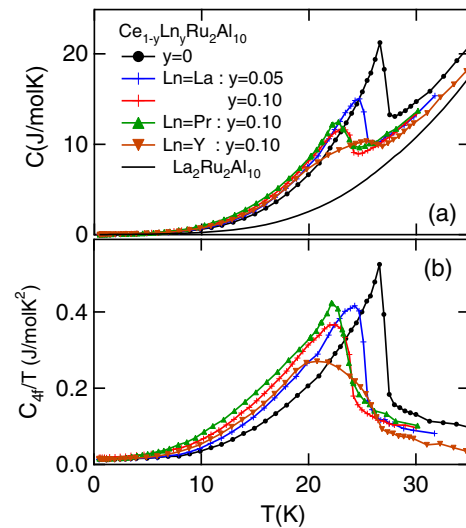


FIG. 2. (Color online) Temperature dependence of (a)  $C$  and (b)  $C_{4f}/T$  of  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ), where the result of  $\text{Ce}_{0.9}\text{La}_{0.1}\text{Ru}_2\text{Al}_{10}$  is cited from Ref. [13].

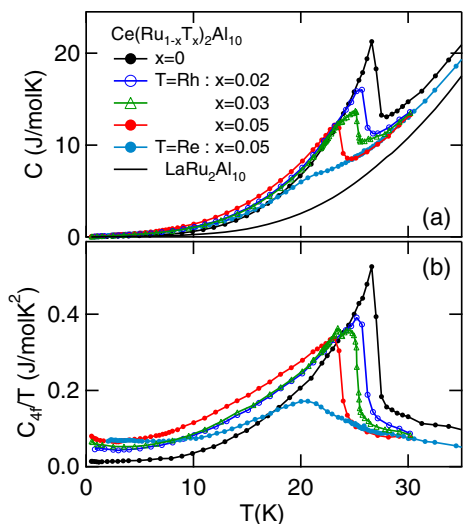


FIG. 3. (Color online) Temperature dependence of (a)  $C$  and (b)  $C_{4f}/T$  of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}: x = 0.02, 0.03, 0.05$ ,  $\text{T} = \text{Re}: x = 0.05$ ).

which indicates the existence of a large spin gap in magnetic excitation spectrum. A sharp peak at  $T_0$  is broadened by Ln doping, which is most pronounced in Y doping due to the smallest ionic radius of  $\text{Y}^{3+}$  ion. The doping effect at low temperatures below  $\sim 5$  K is small in all the doping cases at least up to  $y = 0.1$ . Namely, the  $e^{-\Delta/k_B T}$  dependence and the electronic specific heat coefficient,  $\gamma$  is not affected by nonmagnetic Ln doping up to  $y = 0.1$ . In La-doped samples, the specific heat was investigated in a wide range of  $y$  up to 0.9, where the  $e^{-\Delta/k_B T}$  dependence is not seen for  $y \geq 0.3$  and the  $\gamma$  value increases with increasing  $y$  [13].

Figures 3(a) and 3(b) show the  $T$  dependencies of  $C$  of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}, \text{Re}$ ) and those in the form of  $C_{4f}/T$ , respectively. In Rh doping, the effect is very large at low temperatures. By only a small amount of Rh doping, the  $e^{-\Delta/k_B T}$  dependence disappears and in place, the  $\gamma T$  term appears and increases rapidly with  $x$ . For  $x = 0.03$ , a sharp anomaly is seen at  $T_N = 23.5$  K but also a peak at  $T_0 = 25.5$  K. For  $x = 0.05$ , there exists only one magnetic transition at  $T_N$ . Although a drastic change appears at  $x_c = 0.03$  in  $\chi_a$ ,  $C$  does not show such a drastic change but a continuous one with  $x$  up to 0.05. In contrast to Rh doping, in Re doping, a peak of  $C$  at  $T_0$  is rapidly suppressed and only a broad maximum could be seen at  $T_0 \sim 20$  K. It is difficult to estimate  $T_0$  exactly from the present result. At low temperatures, a large increase of the  $\gamma$  value is seen as in Rh doping. The similar effect was recently reported in  $\text{Ce}(\text{Os}_{1-x}\text{Re}_x)_2\text{Al}_{10}$  [35].

Figures 4(a) and 4(b) show the  $T$  dependencies of the magnetic entropy,  $S_{\text{mag}}$  of  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ) and  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}, \text{Re}$ ), respectively. In La-doped samples, those with  $y = 0.1 \sim 0.9$  cited from Ref. [13] are also shown. We note that for  $y = 0.7$  and 0.9, due to the difficulty of the subtraction of phonon specific heat, the value of  $S_{\text{mag}}$  at high temperatures is not reliable. In all the doping cases, the slope of  $S_{\text{mag}}$  vs  $T$  below 5 K is small and is not changed up to  $y = 0.1$ . In La-doped samples, the slope increases with increasing  $y$  above 0.3, which corresponds to the increase of the  $\gamma$  value [13] and at the same time,  $S_{\text{mag}}$  at  $T_0$  is reduced

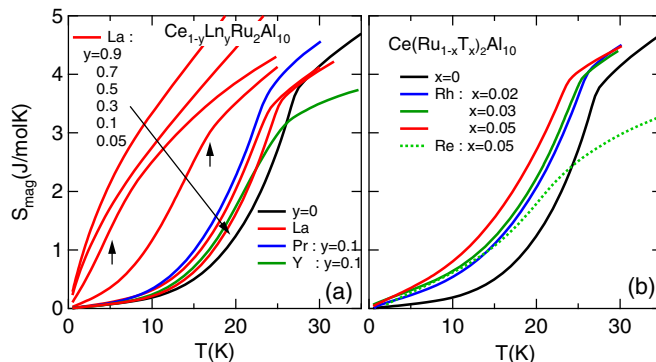


FIG. 4. (Color online) Temperature dependence of the magnetic entropy,  $S_{\text{mag}}$  of (a)  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ) and (b)  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}: x = 0.02, 0.03, 0.05$ ,  $\text{T} = \text{Re}: x = 0.05$ ). In Fig. 4(a), the results of La ( $y = 0.1 \sim 0.9$ ) are obtained from the specific heat data in Ref. [13] and the arrows for  $y = 0.5$  and 0.7 indicate the transition temperature  $T_0$  [13].

with increasing  $y$ . In the Pr-doped case,  $S_{\text{mag}}$  at  $T_0$  is slightly reduced but is largely reduced in the Y-doped one. A rather large suppression of  $S_{\text{mag}}$  even above  $T_0$  in the latter might be due to a modification of a phonon specific heat coming from a large difference of the ionic radius between Y and Ce.

Figure 5 shows the  $x$  and  $y$  dependence of the  $\gamma$  value of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Re}, \text{Rh}$ ) and  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ).  $S_{\text{mag}}$  at  $T_0$  in  $\text{CeRu}_2\text{Al}_{10}$  is  $\sim 0.65 \times R \ln 2$ .  $S_{\text{mag}}$  at the transition temperature ( $T_0$  and  $T_N$ ) is not affected by Rh doping, i.e., almost constant up to  $x = 0.05$ . This is the most important point in the present paper, which will be discussed later. We note that although a big change appears in  $\chi_a$  at  $x_c = 0.03$ , no anomalous variation is seen in the transition temperature ( $T_0$  or  $T_N$ ), a peak shape of  $C_{4f}$  and  $S_{\text{mag}}$  at  $T_0$  or  $T_N$ . In contrast to Rh doping, in Re doping with  $x = 0.05$ ,  $S_{\text{mag}}$  at  $T_0$  is very much reduced. As for the doping effect on

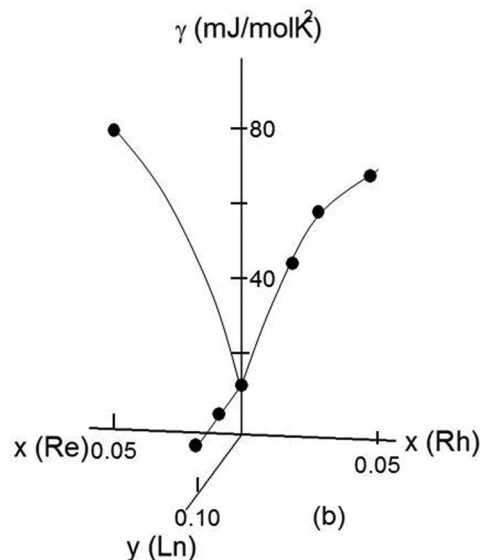


FIG. 5.  $x$  and  $y$  dependence of the  $\gamma$  value of  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Rh}, \text{Re}$ ) and  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ) obtained by subtracting that of  $\text{LaRu}_2\text{Al}_{10}$ .

the  $\gamma$  value, although it is not changed by Ln doping up to  $y = 0.1$ , it is rapidly enhanced with  $x$  by both Rh and Re doping. The similar doping effects were reported in Re- and Ir-doped CeOs<sub>2</sub>Al<sub>10</sub> [35].

### III. DISCUSSION

First, we discuss the doping effect on the ground-state properties in CeRu<sub>2</sub>Al<sub>10</sub>. By the nonmagnetic Ln doping, the  $\gamma$  value in CeRu<sub>2</sub>Al<sub>10</sub> is not changed and the  $e^{-\Delta/k_B T}$  dependence of  $C_{4f}$  at low temperatures exists at least up to  $y = 0.1$ . This indicates that the spin gap is not affected by the nonmagnetic Ln doping at least up to  $y = 0.1$ . In La-doped samples, with further increase of  $y$ , the anomaly at  $T_0$  broadens due to the randomness induced by a large amount of doping, the  $\gamma$  value increases [13], and  $S_{\text{mag}}$  at  $T_0$  is suppressed. The suppression of  $S_{\text{mag}}$  at  $T_0$  by La doping is a result of the competition between the Kondo effect and magnetic interaction. The former enhances the itinerant character and forms heavy electron, and the latter enhances the localized character. With the increase of  $y$ , the latter is suppressed and the former becomes dominant, and the system continuously changes into the dilute Kondo regime [13]. The magnetic susceptibility shows the following  $y$  dependence [13]. The decrease of  $\chi_a$  below  $T_0$  is suppressed and the anomaly at  $T_0$  is broadened. Although the decrease of  $\chi_a$  below  $T_0$  is scarcely observed for  $y = 0.3$ , only a Curie-like increase is seen with decreasing temperature for  $y \geq 0.5$ . We note that  $T_0$  is recognized for  $y = 0.5$  in the specific heat [13]. Considering that the existence of the spin gap was reported for  $y = 0.3$  [37], a decrease of  $\chi_a$  below  $T_0$  might be a sign of the existence of a spin gap. On the other hand, the large  $\gamma$  value of 60 mJ/molK<sup>2</sup> for  $y = 0.3$  indicates that the magnetic scattering intensity might be largely suppressed. Although the nature of the spin gap is changed in a large  $y$  region, almost the full gap is expected to exist at least up to  $y = 0.1$ . Thus, in Fig. 5, the  $\gamma$  value is plotted only below  $y = 0.1$ . We note that the small La-doping effect with a small doping concentration are different from the large La-doping effects on CeNiSn [3], which will be discussed later.

In contrast to the nonmagnetic Ln-doping case, Rh doping modifies the ground state largely. Apart from the drastic change in  $\chi_a$  at  $x_c = 0.03$ , which will be discussed later, the pronounced changes are observed in  $\chi_a$  above  $T_0$  and also in the low temperature specific heat. The downward deviation of  $\chi_a$  from the high temperature Curie-Weiss behavior below  $\sim 100$  K disappears rapidly and  $\chi_a$  starts to show a Curie-Weiss behavior by Rh doping. This indicates the enhancement of the localized nature of the  $4f$  electron by Rh doping. The  $\gamma$  value also shows a rapid increase with  $x$ . On the other hand, in Re doping, the itinerant nature is found to be enhanced from the results of  $\chi$  and  $C_{4f}$ .

The  $e^{-\Delta/k_B T}$  dependence of  $C_{4f}$  means the existence of the spin gap in the magnetic excitation spectrum as mentioned above. Kondo *et al.* discussed that the AFM ordered phase in CeRu<sub>2</sub>Al<sub>10</sub> has a singlet nature from the pronounced concave  $H$  dependence of the magnetization curve along the  $a$  axis and this originates from the strong  $c$ - $f$  hybridization along the  $a$  axis [16,30]. The present results show that by Rh doping, although the  $e^{-\Delta/k_B T}$  dependence disappears, and in

place, the  $\gamma T$  dependence appears. The  $\gamma T$  term means the existence of the density of states at the Fermi level. The most important result in the present study is that *the magnitude of  $S_{\text{mag}}$  at  $T_0$  or  $T_N$  is almost constant up to  $x = 0.05$* . This clearly demonstrates that the origin of the  $\gamma T$  term is fully magnetic. Namely, the spin degrees of freedom at the excited magnetic state induced by the spin gap formation is transferred to the low energy region by Rh doping and the  $\gamma$  value increases with  $x$ . This  $\gamma T$  term is considered as a Kondo resonance state at the Fermi level. This important conclusion could be obtained precisely because CeRu<sub>2</sub>Al<sub>10</sub> is the AFM compound and  $S_{\text{mag}}$  below  $T_0$  could be estimated exactly. In CeNiSn with a nonmagnetic ground state, it is difficult to discuss the origin of the  $\gamma T$  term induced by doping because the estimation of  $S_{\text{mag}}$  originating from the V-shape gap is difficult due to a lack of the magnetic transition temperature. We comment about the almost constant  $S_{\text{mag}}$  at  $T_0$  or  $T_N$  with an Rh-doping concentration. In CeRu<sub>2</sub>Al<sub>10</sub>,  $S_{\text{mag}}$  is  $\sim 0.65 R \ln 2$  whose reduction from  $R \ln 2$  is ascribed to the Kondo effect. When Rh is doped, there exist, at least, three kinds of effects. One is the enhancement of conduction electron mass as a result of the heavy electron formation, leading to the enhancement of  $S_{\text{mag}}$ . The second is the enhancement of localized character of the magnetic moment along the  $a$  axis, leading to the enhancement of  $S_{\text{mag}}$ . The third is the Kondo screening effect, reducing  $S_{\text{mag}}$ .  $S_{\text{mag}}$  at  $T_0$  or  $T_N$  is determined by the coexistence and competition among these three effects. Although it is difficult to estimate which effect is dominant in  $S_{\text{mag}}$  at  $T_0$  or  $T_N$  in Rh-doped CeRu<sub>2</sub>Al<sub>10</sub>, we consider that the rapid increase of the  $\gamma$  value by Rh doping originates from the collapse of the spin gap.

Here, we discuss the increase of the  $\gamma$  value by Re doping. Although the  $\gamma$  value increases rapidly as in the Rh-doping case, its origin should be different. The large suppression of  $\chi_a$  is seen in a wide range of temperature below 300 K in spite of a small Re-doping concentration of  $x = 0.05$  as is shown in Fig. 1. This indicates that the itinerant nature is largely enhanced in a wide range of temperatures, different from the Rh-doping case. Then, it is considered that the localized nature is suppressed and the spin gap is smeared out by Re doping. The existence of the spin gap is indicated by the suppression of  $\chi_a$  below  $T_0$ , which is also seen in Ce(Os<sub>1-x</sub>Re<sub>x</sub>)<sub>2</sub>Al<sub>10</sub> up to  $x = 0.05$  [35]. These are indicated by the recently reported results of the inelastic neutron scattering in Ce(Os<sub>1-x</sub>Re<sub>x</sub>)<sub>2</sub>Al<sub>10</sub> [38] and also in Ce(Ru<sub>0.97</sub>Re<sub>0.03</sub>)<sub>2</sub>Al<sub>10</sub> [39], where the magnitude of the spin gap is not changed but the magnetic scattering intensity is reduced. The similar doping effect on the spin gap was observed also in Ce(Ru<sub>1-x</sub>Fe<sub>x</sub>)<sub>2</sub>Al<sub>10</sub> [29]. The Re and Fe dopings seem to have the common feature that the itinerant nature is enhanced. Its origin should be investigated from the standpoint that the meaning of the Re doping is simply a hole doping or not as will be discussed later. Here, we note that very high  $T_0$  could be never explained by a small ordered moment of the order of  $0.1 \mu_B/\text{Ce}$  as in the Re- or Fe-doping case but the large  $c$ - $f$  hybridization should be associated with high  $T_0$ , which is suggested by the large enhancement of  $T_0$  by a small pressure [8,23]. Then, the AFM exchange interaction seems to play a role as merely a trigger to induce the AFM transition.

We comment about the Re-doping effect on the orientation of  $m_{\text{AF}}$  below  $T_0$  in CeRu<sub>2</sub>Al<sub>10</sub> and CeOs<sub>2</sub>Al<sub>10</sub>. The AFM order

of  $m_{\text{AF}} \parallel c$  with a reduced moment of  $0.18\mu_{\text{B}}/\text{Ce}$  is reported in  $\text{Ce}(\text{Os}_{0.97}\text{Re}_{0.03})_2\text{Al}_{10}$  [34]. On the other hand, very recent neutron diffraction experiment showed that  $m_{\text{AF}} \parallel b$  is realized in  $\text{Ce}(\text{Ru}_{0.97}\text{Re}_{0.03})_2\text{Al}_{10}$  [39]. This indicates that at least in  $\text{Ce}(\text{Ru}_{1-x}\text{Re}_x)_2\text{Al}_{10}$ , there exists a critical concentration where the orientation of  $m_{\text{AF}}$  is changed from the  $c$  to  $b$  axis between  $x = 0$  and  $0.03$ . This also suggests that the magnetic anisotropy in the  $bc$  plane is small, as was discussed in Ref. [21]. As mentioned in the Introduction, the magnetic anisotropy below  $T_0$  is quite strange. Although the change of the anisotropic  $c$ - $f$  hybridization is considered to be associated with the reorientation of  $m_{\text{AF}}$ , the mechanism is not known at present. Further investigations are necessary.

Next, we discuss the drastic change in  $\chi_a$  in  $\text{Ce}(\text{Ru}_{1-x}\text{Rh}_x)_2\text{Al}_{10}$  at  $x_c = 0.03$  above which the AFM order with  $m_{\text{AF}} \parallel a$  of  $\sim 1\mu_{\text{B}}/\text{Ce}$  consistent with  $\chi_a \gg \chi_c \gg \chi_b$  in the paramagnetic region is realized, which is ascribed to the suppression of the  $c$ - $f$  hybridization along the  $a$  axis by Rh doping. Although a drastic change is observed in  $\chi_a$  at  $x_c = 0.03$ , an anomaly is not seen in the  $x$  dependence of the transition temperatures ( $T_0$  or  $T_{\text{N}}$ ),  $S_{\text{mag}}$  at  $T_{\text{N}}$  or  $T_0$ , and also the  $\gamma$  value show a smooth variation with  $x$  up to  $x = 0.05$ . Since  $S_{\text{mag}}$  at the transition temperature is not changed with  $x$ , the Kondo effect still should play an important role even above  $x_c = 0.03$ . The results indicate that a drastic change induced by Rh doping is the anisotropic phenomenon and there exists a critical Rh-doping concentration above which the localized nature along the  $a$  axis is dominant. The drastic change of the anisotropic  $c$ - $f$  hybridization gives rise to the destruction of the spin gap as mentioned above and looks like the anisotropic itinerant-localized transition at first glance, which should be investigated more in detail in the future. This could be a new phenomenon which appears in the Kondo semiconductor with the AFM order, which is unexpected in the AFM heavy electron compounds. We note that the smooth variation of  $T_0$  or  $T_{\text{N}}$  and the  $\gamma$  value with the Rh doping suggests that the full spin gap is not necessarily indispensable to produce the very high transition temperature in the present system.

Finally, we discuss the different doping effects between  $\text{CeRu}_2\text{Al}_{10}$  and  $\text{CeNiSn}$ . In  $\text{CeNiSn}$ , a small amount of doping could destroy the gap easily because of the V-shaped gap [2–5]. In  $\text{CeRu}_2\text{Al}_{10}$ , since a full gap is opened, it might be difficult to destroy the gap by such a small amount of doping. However, this contradicts the experimental results. The most important effect by Rh and Re doping in  $\text{CeRu}_2\text{Al}_{10}$  is the destruction of spin gap and the appearance of the Kondo resonance state as discussed above. Another big difference is the La-doping effect. Although the La-doping effect in  $\text{CeRu}_2\text{Al}_{10}$  is very small, it is large in  $\text{CeNiSn}$  [2–5], which was discussed from the standpoint of the disturbance of the coherence effect, the Kondo hole, and the impurity band, etc. [1,6]. The gap in  $\text{CeRu}_2\text{Al}_{10}$  is robust against the Ce-site substitution by nonmagnetic Ln ion. This could be due to the Kondo semiconductor accompanied by the AFM order. On the other hand, the Re- and Rh-doping effects in  $\text{CeRu}_2\text{Al}_{10}$  are large as in the Co- and Cu-doping cases in  $\text{CeNiSn}$ . These could be considered as a hole and electron doping, respectively, if we take the deviation of the  $d$  electron number of the doped transition metal element from the mother one. Experimental results indicate that the itinerant nature is enhanced by hole

doping and the localized one by electron doping and could be understood as a result of the shift of the Fermi level against the  $4f$  level as was discussed in the doped  $\text{CeOs}_2\text{Al}_{10}$  by Kawabata *et al.* [35]. However, the meaning of a hole and electron doping is not clear. There exists no difference in the hole- or electron-doping effect on the collapse of the V-shaped gap or Hall effect in  $\text{CeNiSn}$ , etc. [2–5]. Since all of  $s$ ,  $p$ ,  $d$ , and  $f$  electrons in Ce, Ru, Al contribute to the electronic states at the Fermi level, it is difficult to consider the  $d$  electron of the doped transition metal element, specifically. Experimentally, the electron- or hole-doping effect is pronounced inside the gap in both systems of  $\text{CeNiSn}$  and  $\text{CeT}_2\text{Al}_{10}$  [2–5,31]. The  $d$  electron of the transition metal element should play an important role in the formation or destruction of the hybridization gap in  $\text{CeRu}_2\text{Al}_{10}$ , although the microscopic mechanism is not known at present. We do not know the reason why the different  $d$  electron number of the doped transition metal element so sensitively affects the ground-state properties in the Kondo semiconductor. However, both itinerant and localized natures of the  $4f$  electron are necessary to construct the spin gap and its existence or nonexistence stands under the subtle balance between the above two contradictory natures. The spin gap is easily collapsed by a small deviation from the subtle balance induced by Rh and Re doping.

#### IV. CONCLUSION

To conclude, the Ce- and Ru-site substitution effects on the spin gap in  $\text{CeRu}_2\text{Al}_{10}$  were investigated by measuring the magnetic and thermal properties of  $\text{Ce}_{1-y}\text{Ln}_y\text{Ru}_2\text{Al}_{10}$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Y}$ ) and  $\text{Ce}(\text{Ru}_{1-x}\text{T}_x)_2\text{Al}_{10}$  ( $\text{T} = \text{Re}, \text{Rh}$ ) system, respectively. The magnetic susceptibility measurement shows that the itinerant and localized nature is enhanced by Re and Rh doping, respectively. In the latter, although no anomaly is seen in the  $x$  dependence of  $T_0$  or  $T_{\text{N}}$ , the orientation of the magnetic moment in the AFM ordered phase suddenly changes from the  $c$  to  $a$  axis at  $x_c = 0.03$ . The magnetic moment parallel to the  $a$  axis is consistent with  $\chi_a \gg \chi_c \gg \chi_b$  in the paramagnetic region. The specific heat measurement shows that the  $e^{-\Delta/k_{\text{B}}T}$  dependence and the  $\gamma$  value are not changed in the Ce-site substituted systems up to  $y = 0.1$  but in the Ru-site substituted systems, the  $e^{-\Delta/k_{\text{B}}T}$  dependence disappears and the  $\gamma$  value increases rapidly with  $x$ . These indicate that the spin gap is robust against the Ce-site substitution by Ln ion at least up to  $y = 0.1$ , different from the nonmagnetic Kondo semimetal  $\text{CeNiSn}$  where the spin gap is rapidly collapsed by La doping. On the other hand, the spin gap is rapidly collapsed by the Ru-site substitution and in place, the conduction electron with heavy effective mass appears at the Fermi level. The spin gap which is formed under the subtle balance between the localized and itinerant nature is easily collapsed by a small amount of Re or Rh doping. The smooth variation of  $T_0$  or  $T_{\text{N}}$  and the  $\gamma$  value with  $x$  through  $x_c = 0.03$  in the Rh doping suggests that the full spin gap is not necessarily indispensable for producing the very high transition temperature in the present system.

#### ACKNOWLEDGMENT

The authors would like to thank Professor T. Takabatake and Professor S. Kimura for valuable discussions.

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