

## Exciton valley dynamics probed by Kerr rotation in WSe<sub>2</sub> monolayers

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We have experimentally studied the pump-probe Kerr rotation dynamics in WSe<sub>2</sub> monolayers. This yields a direct measurement of the exciton valley depolarization time  $\tau_v$ . At  $T = 4$  K, we find  $\tau_v \approx 6$  ps, a fast relaxation time resulting from the strong electron-hole Coulomb exchange interaction in bright excitons. The exciton valley depolarization time decreases significantly when the lattice temperature increases, with  $\tau_v$  being as short as 1.5 ps at 125 K. The temperature dependence is well explained by the developed theory, taking into account the exchange interaction and fast exciton scattering time on the short-range potential.

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Monolayers of transition metal dichalcogenides (TMDCs), such as MoS<sub>2</sub> and WSe<sub>2</sub>, are two-dimensional (2D) semiconductors with strong light absorption and emission associated with direct optical transitions [1–3]. The optical properties of these 2D crystals are strongly influenced by excitons, Coulomb bound electron-hole pairs, with experimentally determined binding energies of up to 0.6 eV ( $\sim 1/3$  of the optical band gap  $\sim 1.7$  eV) [4–10]. Due to the combined effect of inversion symmetry breaking and a strong spin-orbit interaction, the interband transitions are governed by chiral selection rules which allow efficient optical initialization of an electron-hole pair in a specific  $K$  valley in momentum space [11–15]. The circular polarization ( $\sigma^+$  or  $\sigma^-$ ) of the absorbed or emitted photon can be directly associated with selective carrier excitation in one of the two nonequivalent valleys,  $K_+$  or  $K_-$ , respectively, formed at the edges of the Brillouin zone. Hence, the spin state of an exciton  $S_z = \pm 1$  is correlated with its valley state  $K_{\pm}$ . Recent time-resolved studies demonstrate photoluminescence (PL) lifetimes in the picosecond range, indicating high exciton oscillator strengths [16–18]. Pump-probe absorption and reflectivity measurements in monolayer (ML) MoS<sub>2</sub> have also shown polarization decay times in the picosecond range [19–21] corresponding to fast relaxation of the valley polarization, which is surprising as the valley degree of freedom is expected to be protected by the considerable single particle spin splittings in the valence and conduction bands [22].

In this Rapid Communication we use a powerful technique, namely, time-resolved Kerr rotation (TRKR) [23], to investigate the exciton dynamics in ML WSe<sub>2</sub>. In contrast to time-resolved PL spectroscopy, TRKR allows one to address the spin states of both photocreated and resident carriers polarized by a  $\sigma^+$  or  $\sigma^-$  polarized pump laser. We detect a spin-Kerr signal for the neutral exciton, well separated from the charged exciton signal, and uncover a valley relaxation time of  $\tau_v = 6$  ps at  $T = 4$  K, which we attribute to the strong Coulomb exchange interaction between the electron

and the hole. The strongly bound excitons in ML WSe<sub>2</sub> [18] give access in TRKR to a temperature-dependent regime of exciton spin dynamics: In standard quasi-2D semiconductor systems such as GaAs quantum wells, excitons are ionized as the temperature increases since their binding energy is small ( $\sim 10$  meV) [24–26]. The temperature dependence of the exciton spin dynamics is therefore inaccessible. This is in contrast to very robust excitons in ML WSe<sub>2</sub>, where we can investigate this evolution. We measure a temperature induced decrease of  $\tau_v$  that we interpret in terms of the temperature dependence of the exchange interaction induced exciton spin relaxation. Our theory describes very satisfactorily the experimental data. Moreover, we found no evidence of transfer of spin/valley polarization to resident carriers in WSe<sub>2</sub> MLs, contrary to similar time-resolved Kerr experiments performed in III-V or II-VI semiconductors [27,28].

The investigated monolayer WSe<sub>2</sub> flakes are obtained by micromechanical cleavage of a bulk WSe<sub>2</sub> crystal (from SPI Supplies, USA) on 90 nm SiO<sub>2</sub> on a Si substrate. The 1 ML region is identified by optical contrast [Fig. 1(a)] and very clearly in PL spectroscopy [2]. The sample is excited near normal incidence with degenerate pump and delayed probe pulses from a mode-locked Ti:sapphire laser ( $\sim 120$  fs pulse duration, 76 MHz repetition frequency). The laser beams are focused to a spot size of  $\sim 5$   $\mu\text{m}$ , and the pump and probe beams have an average power of 300 and 30  $\mu\text{W}$ , respectively. This corresponds to a typical pump-generated exciton density of about  $10^{12}$   $\text{cm}^{-2}$ . The circularly polarized pump pulse incident normal to the sample creates spin-polarized electronic excitations with the spin vector perpendicular to the flake plane. The temporal evolution of the carrier spins is recorded by measuring the Kerr rotation angle  $\theta(\Delta t)$  of the reflected linearly polarized probe pulse while sweeping the delay time  $\Delta t$ , which corresponds to the net spin component normal to the sample plane [23,28,29]. Continuous-wave (cw) micro-PL is performed with a laser excitation energy  $E_l = 1.96$  eV with a standard monochromator coupled to a CCD detection system. Figure 1(b) displays the temperature dependence of the PL spectra from  $T = 4$  to 300 K. Similarly to previous studies, three features can be identified at  $T = 4$  K [18,30]: The emission peaks at  $E = 1.742$  and 1.714 eV correspond

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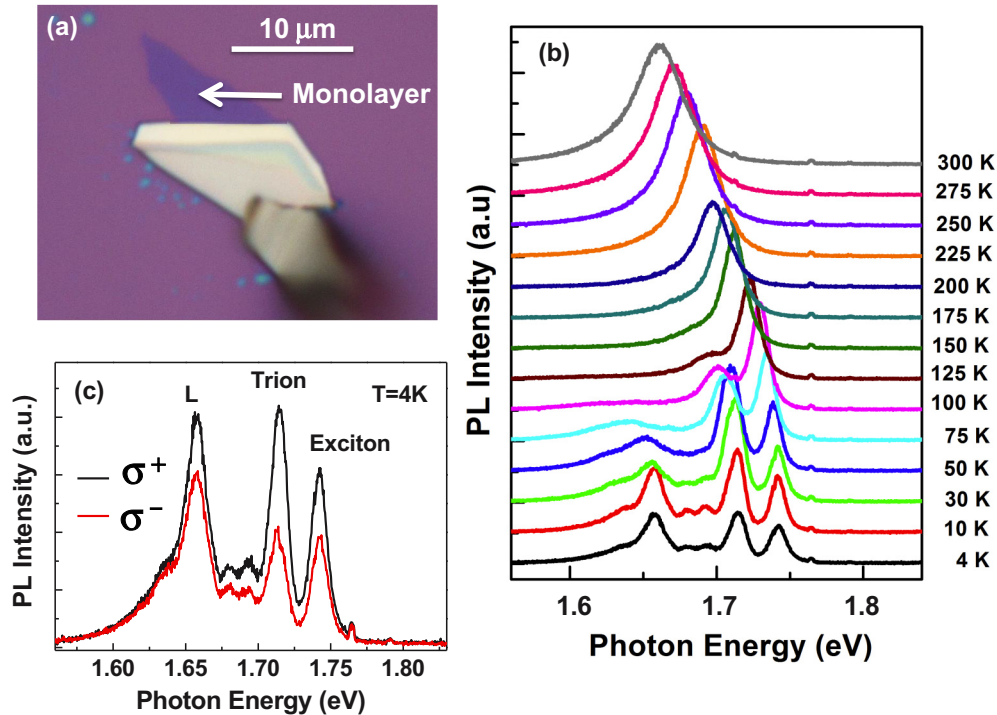


FIG. 1. (Color online) (a) Optical reflection image of the sample indicating the investigated WSe<sub>2</sub> ML flake (the white zone corresponds to multiple layers). (b) Temperature dependence of the WSe<sub>2</sub> ML PL spectra. (c) Right ( $\sigma^+$ ) and left ( $\sigma^-$ ) circularly polarized PL components at  $T = 4$  K under cw  $\sigma^+$  polarized He-Ne laser excitation ( $E_l = 1.96$  eV).

to the recombination of neutral excitons and charged excitons (trions), respectively [Fig. 1(c)]. Considering the commonly observed residual  $n$ -type doping [18,31], the trion charge is assumed to be negative, but this assumption is not critical for the present study and the discussion below. The identification of these transitions is based on the emission polarization analysis [18,30]. Under  $\sigma^+$  polarized excitation light, the exciton and trion PL peaks are characterized by a significant circular polarization degree (typically 33% and 23%, respectively, at  $T = 4$  K); note the different intensities of the  $\sigma^+$  and  $\sigma^-$  PL components in Fig. 1(c), which demonstrate the optical initialization of valley polarization [11–15]. In contrast, only the exciton line exhibits a linear polarization degree following a linearly polarized light excitation (not shown) as a consequence of the creation of a coherent superposition of valley states [30]. The clear separation by 30 meV of the trion and the neutral exciton in WSe<sub>2</sub> MLs is a major advantage compared to state-of-the-art MoS<sub>2</sub> ML samples where the two lines cannot be resolved [32]. Below the trion emission several emission peaks are observed at low temperature [labeled L in Fig. 1(c)]; these peaks, already observed in MoS<sub>2</sub> or WSe<sub>2</sub> MLs [11–13,18], have been assigned to localized exciton complexes. In this work we focus on the temperature dependence of the neutral exciton dynamics. As shown in Fig. 1(b), the exciton emission remains strong as the temperature increases (we observe clearly the redshift of the line) whereas both the trion and localized state emissions vanish for  $T \gtrsim 100$  K.

Figure 2 shows the Kerr rotation dynamics  $\theta(\Delta t)$  measured at 4 K for both  $\sigma^+$  and  $\sigma^-$  polarized pump pulses. The pump energy  $E_l = 1.735$  eV is set to the maximum of the Kerr signal, which is very close to the neutral exciton transition identified

in the PL spectra [Fig. 1(c)]. The observed sign reversal of the Kerr signal in Fig. 2 at the reversal of pump helicity is a consequence of the optical initialization of the  $K_+$  and  $K_-$  valleys, respectively. We have measured in the same conditions the transient reflectivity using linearly cross-polarized pump and probe pulses. As shown in Fig. 3(b), the reflectivity decay time is about ten times longer than the one observed in TRKR. Thus the monoexponential decay time  $\tau_v = (6 \pm 0.1)$  ps of the Kerr rotation dynamics at  $T = 4$  K in Fig. 2 probes directly the fast exciton valley depolarization. In agreement with recent estimations, it results from the strong long-range

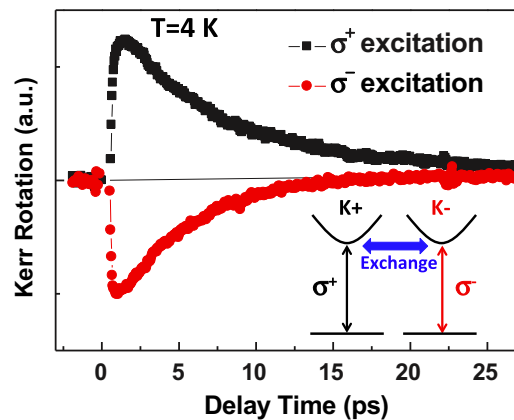


FIG. 2. (Color online) Kerr rotation dynamics at  $T = 4$  K for a  $\sigma^+$  and  $\sigma^-$  pump beam. The laser excitation energy is  $E_l = 1.735$  eV. Inset: Schematics of the optical selection rules of the excitons in  $K_{\pm}$  valleys and their coupling induced by the long-range exchange interaction.

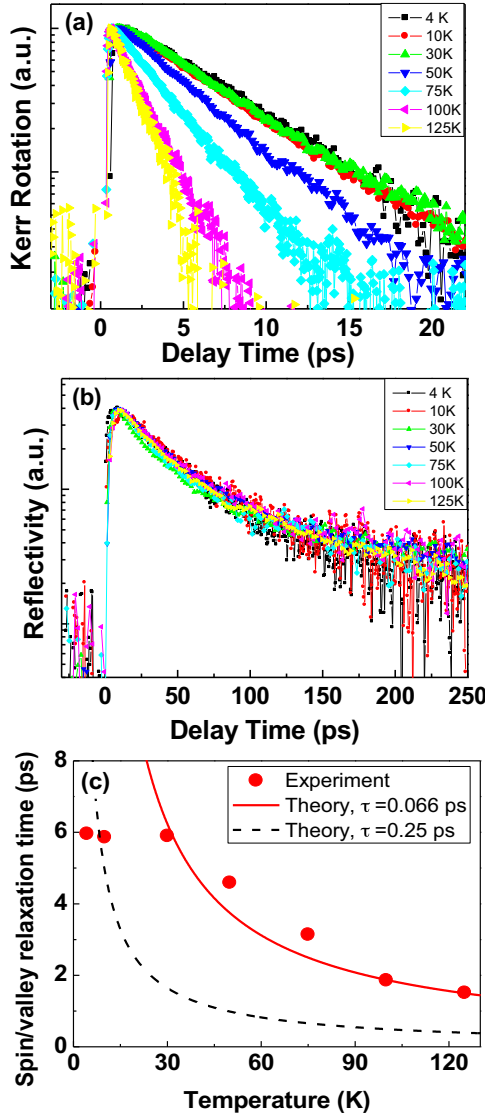


FIG. 3. (Color online) (a) Kerr rotation dynamics after a  $\sigma^+$  polarized pump pulse for different lattice temperatures. (b) Transient reflectivity dynamics for different temperatures. The laser excitation energies are identical to the ones used in (a) (see text). (c) Temperature dependence of the measured (symbol) and calculated after Eq. (1) (solid and dashed lines) exciton valley polarization relaxation time (see text for details).

exchange interaction [33,34]. Due to a limited time resolution, previous investigations by time-resolved PL spectroscopy could not yield the measurement of the exciton valley depolarization time [17,18]. The Kerr rotation dynamics used here is characterized by a higher time resolution ( $\sim 100$  fs) and allows us a strictly resonant excitation of the exciton.

Figure 3(a) displays the variation of the TRKR dynamics as a function of the temperature. For each temperature, the laser excitation energy is set at the maximum Kerr rotation signal, which follows well the energy of the neutral exciton PL shown in Fig. 1(b). For  $T \gtrsim 30$  K, we observe a clear decrease of the exciton valley polarization decay time  $\tau_v$  down to 1.5 ps at  $T = 125$  K; for higher temperatures the signal-to-noise ratio is too small to get reliable data. We stress

that the transient reflectivity measurements performed in the same temperature range exhibit much longer decay times with a very weak temperature dependence [Fig. 3(b)] [19]. We have also investigated the excitation power dependences of the exciton dynamics. In the studied power range corresponding to a variation of exciton density from  $\sim 1.5 \times 10^{11}$  to  $10^{12}$   $\text{cm}^{-2}$ , both the TRKR and reflectivity dynamics do not depend on the exciton photogenerated density within experimental accuracy (not shown). This demonstrates that the exciton-exciton interactions play a minor role in the exciton valley dynamics presented in Figs. 2 and 3.

In order to describe quantitatively the experimental findings we note that the Kerr rotation angle  $\theta$  is proportional to the total spin of the exciton ensemble  $S = \sum_{\mathbf{K}} S_{\mathbf{K}}$  (the mechanisms of Kerr rotation by exciton spins in  $\text{WSe}_2$  MLs are similar to those in quasi-2D semiconductors and can be described as in Ref. [28]);  $S_{\mathbf{K}}$  is the spin distribution function (with  $S_z = \pm 1$  corresponding to  $K_{\pm}$  valleys) and  $\mathbf{K}$  is the wave vector of exciton. The spin/valley dynamics of excitons is governed by the long-range exchange interaction between an electron and a hole [33,34] which acts as an effective magnetic field  $\mathbf{\Omega}_{\mathbf{K}} = \alpha \mathbf{K} (\cos 2\vartheta, \sin 2\vartheta)$  on the exciton spin. Here  $\vartheta$  is the polar angle of  $\mathbf{K}$  and the constant  $\alpha$  depends on the oscillator strength of the exciton transition and system geometry. Following Ref. [33] for the system “vacuum-1 ML of  $\text{WSe}_2$ -substrate” we obtain, assuming the same background refractive index  $n$  of the ML and the substrate,  $\alpha = c\Gamma_0(n+1)/[(n^2+1)\omega_0]$ , where  $\omega_0$  is the exciton resonance frequency, and  $\Gamma_0$  is its radiative lifetime [35]. This effective field causes spin precession of excitons which is randomized by the scattering and described by the kinetic equation [26,33]  $\partial S_{\mathbf{K}}/\partial t + S_{\mathbf{K}} \times \mathbf{\Omega}_{\mathbf{K}} = Q\{S_{\mathbf{K}}\}$ , where  $Q\{S_{\mathbf{K}}\}$  is the collision integral. Assuming that the excitons are thermalized and the scattering is caused by a short-range potential, we obtain for the spin/valley relaxation rate  $\tau_{zz}^{-1}$ ,

$$\frac{1}{\tau_{zz}} = \frac{2\alpha^2\tau M k_B T}{\hbar^2}, \quad (1)$$

where  $M = 0.67m_0$  is the exciton mass [18], and  $\tau$  is the scattering time. Equation (1) is valid provided that the radiative lifetime of excitons exceeds  $\tau_{zz}$ ,  $k_B T \tau / \hbar \gg 1$  and  $\alpha^2 M k_B T \tau^2 / \hbar^2 \ll 1$ . The second condition means that the average kinetic energy must be larger than the homogeneous broadening and the latter that the spin relaxation occurs in the spin diffusive regime. Figure 3(c) shows the experimentally measured exciton polarization decay times [points are extracted from the monoexponential decay presented in Fig. 3(a)] and theoretical calculations carried out for  $\Gamma_0 = 0.16$   $\text{ps}^{-1}$  [corresponding to the radiative lifetime of the states in the light cone  $1/(2\Gamma_0) = 3$  ps, a value consistent with measurements [18]] and  $n = \sqrt{10}$ . Qualitatively, the drop of the exciton spin/valley relaxation time when  $T$  increases can be well explained by the increase with temperature of the effective magnetic field  $\mathbf{\Omega}_{\mathbf{K}}$ , which makes spin precession and decoherence faster [Eq. (1)]. The solid and dashed lines in Fig. 3(c) correspond to the calculated exciton spin/valley relaxation time for two different scattering times  $\tau = 0.066$  and  $0.25$  ps, respectively. The latter value of  $\tau$  corresponds to an exciton energy uncertainty equivalent to 30 K corresponding to an

Ioffe-Regel criterion of delocalization where the product of the thermal wave vector  $k_T = (2Mk_B T)^{1/2}/\hbar$  and the mean free path  $l = \tau \hbar k_T / M$  is on the order of 1. Remarkably, we observe a nice agreement between the calculated and measured exciton relaxation times in Fig. 3(c) for  $T > 30$  K with the scattering time  $\tau = 0.066$  ps, but a formal criterion of the kinetic equation is fulfilled only for  $T \gtrsim 100$  K [36].

For  $4 < T < 30$  K, the measured exciton spin relaxation time is temperature independent (the sample temperature was carefully checked). In this temperature range, the PL spectra in Fig. 1(b) are also identical whereas shifts of the peaks energies and relative changes of intensities are clearly observed for larger temperatures. We believe that this behavior could be either due to (i) a regime where  $K_B T$  is smaller than the collision broadening, leading to a temperature-independent spin relaxation time [33] or (ii) a localized character of the exciton below 30 K.

Finally, we emphasize that the Kerr rotation signal for delay times longer than  $\sim 25$  ps vanishes within our experimental accuracy, regardless of the temperature. This means that we get no evidence of the transfer of spin polarization to the resident carriers, though they are clearly present, as shown by the detection of the trion line in Fig. 1. This behavior is

probably due to the very robust spin/valley polarization of single particles, electrons, and holes in TMDC 2D layers [11], because the polarization transfer from photogenerated carriers to resident ones, *n*-doped III-V or II-VI semiconductors, usually requires a single particle spin flip [28].

In conclusion, we have demonstrated that the exciton valley dynamics in WSe<sub>2</sub> monolayers can be directly probed by time-resolved Kerr rotation dynamics performed in resonant excitation conditions. The temperature dependence of the exciton depolarization time is well described by Coulomb exchange interaction induced exciton spin/valley dephasing assuming efficient scattering on a short-range potential.

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