# Structural instability and the Mott-Peierls transition in a half-metallic hollandite : K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>

Sooran Kim, Kyoo Kim,<sup>\*</sup> and B. I. Min<sup>†</sup>

Department of Physics, PCTP, Pohang University of Science and Technology, Pohang 790-784, Korea (Received 25 March 2014; revised manuscript received 3 July 2014; published 18 July 2014)

In order to explore the driving mechanism of the concomitant metal-insulator and structural transitions in quasi-one-dimensional hollandite  $K_2Cr_8O_{16}$ , electronic structures and phonon properties are investigated by employing the *ab initio* density functional theory (DFT) calculations. We have found that the imaginary phonon frequency reflecting the structural instability appears only in the DFT + U (U: Coulomb correlation) calculation, which indicates that the Coulomb correlation plays an essential role in the structural transition. The lattice displacements of the softened phonon at X explain the observed lattice distortions in  $K_2Cr_8O_{16}$  perfectly well, suggesting the Peierls distortion vector  $\mathbf{Q}$  of X (0, 0, 1/2). The combined study of electronic and phonon properties reveals that half-metallic  $K_2Cr_8O_{16}$ , upon cooling, undergoes the correlation-assisted Peierls transition to become a Mott-Peierls ferromagnetic insulator at low temperature.

DOI: 10.1103/PhysRevB.90.045124

PACS number(s): 71.30.+h, 63.20.D-, 71.10.Fd, 75.50.-y

#### I. INTRODUCTION

Strongly correlated transition-metal (TM) oxides have been studied for the last decade because of their diverse intriguing properties according to pressure, doping, temperature, and so on [1]. Among those, hollandite-type TM oxides  $A_2M_8O_{16}$ (A=alkali metal, M=TM element) have drawn recent attention due to their quasi-one-dimensional column structure made of four double MO chains (see Fig. 1). Despite the similarity in the crystal structures, these materials have different physical properties depending on the TM element. K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub> and  $K_2V_8O_{16}$  exhibit the metal-insulator transition (MIT) and the structural transition concomitantly upon cooling [2,3]. In contrast, K<sub>2</sub>Mo<sub>8</sub>O<sub>16</sub> is an insulator for the entire temperature range [4].  $K_2Cr_8O_{16}$  and  $K_xTi_8O_{16}$  show magnetic transition from paramagnetic to ferromagnetic (FM) phase with varying the temperature and the carrier concentration, respectively [5–7]. On the other hand,  $K_2V_8O_{16}$  has a complex ground state containing the charge ordering and the spin-singlet structure [3,8]. The possibility of Tomonaga-Luttinger liquid property has also been suggested in  $K_2Ru_8O_{16}$  [9].

 $K_2Cr_8O_{16}$  of present concern exhibits an interesting phase diagram depending on the temperature (T). It would have a nominal mixed-valence state with the average electrons per Cr being 2.25 (Cr<sup>4+</sup>:Cr<sup>3+</sup> = 3:1). At high T, K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub> is a paramagnetic metal with the body-centered tetragonal crystal structure (I4/m) [5,10]. Figure 1 presents the crystal structure and the corresponding Brillouin zone (BZ). Along the c axis, the double chain of edge-shared CrO<sub>6</sub> octahedra exists. Upon cooling, two phase transitions take place. At first, the magnetic transition occurs at 180 K from paramagnetic to FM phase. The observed magnetic moment of the system is close to  $18\mu_B$  [5,11]. This magnetic transition is not accompanied with the structural transition, and so this phase is still metallic. Interestingly, the FM phase has a half-metallic nature [5,12]. This feature was explained by the double exchange mechanism arising from the Hund coupling between the fully occupied  $d_{xy}$ 

orbital and the partially occupied  $d_{zx}$  and  $d_{yz}$  of Cr [12], as in CrO<sub>2</sub> [13].

The second transition is the MIT at 95 K. At this transition, the ferromagnetic property is preserved [5]. An insulator version of the double exchange ferromagnetism was proposed to explain this property [14]. When the MIT was first observed, the structural transition was not detected [5], and so the charge ordering [15] and the charge-density wave [12] were suggested as the mechanism of the MIT. Later, however, the structural transition coexisting with the MIT was observed [2], from the body-centered tetragonal to the monoclinic structure (P112<sub>1</sub>/*a*) that has an increased unit cell of  $\sqrt{2} \times \sqrt{2} \times 1$ . Based on this newly discovered structure, it was suggested that the MIT is caused by a Peierls instability in the quasione-dimensional column structure made of four coupled Cr-O chains running along the *c* direction [2].

There have been a few electronic band structure studies on  $K_2Cr_8O_{16}$  [2,12,15]. By contrast, there has been no phonon study, which can provide a direct clue to the structural transition. Since the electronic structure of  $K_2Cr_8O_{16}$  is similar to that of  $CrO_2$ , it is expected that the Coulomb correlation effect plays an important role in determining physical properties. However, the roles of the Coulomb correlation in the MIT and in stabilizing the ferromagnetic insulator (FI) ground state have not been explored yet.

In this paper, we have investigated electronic structures and the phonon dispersion properties of  $K_2Cr_8O_{16}$  to explore the driving mechanism of the MIT and the structural transition. To analyze the effect of on-site Coulomb correlation U we studied the phonon properties both without and with U in the density functional theory (DFT) calculations. We have found that the structural instability occurs only in the DFT + U, which indicates that the Coulomb correlation plays an essential role in the structural transition. The displacements of normal mode of softened phonon at X(0, 0, 1/2) are quite consistent with the observed structural distortions occurring at the MIT, which leads to the formation of Cr tetramers in the four coupled Cr-O chains and their stripe-type arrangement. Noteworthy is that this  $\mathbf{Q} = X$  (0, 0, 1/2) is different from the previously suggested Peierls nesting vector of  $\mathbf{Q} = (1/2, 1/2, -1/2)$  [2]. We have demonstrated that the FI phase of K2Cr8O16 belongs to a Mott-Peierls insulator, for which both the lattice

<sup>\*</sup>kyoo@postech.ac.kr

<sup>&</sup>lt;sup>†</sup>bimin@postech.ac.kr

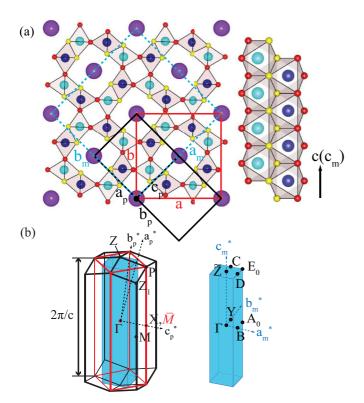


FIG. 1. (Color online) (a) Crystal structure of  $K_2Cr_8O_{16}$ . Black and red lines represent the primitive and the conventional unit cell of the FM phase, respectively, while blue dotted line represents the unit cell of the FI phase. Purple, blue, sky-blue, yellow, and red balls represent K, Cr(z = 0), Cr(z = 0.5) O(1), and O(2), respectively. Right is the double chain of edge-shared  $CrO_6$  octahedra along the *c* axis. In the FM phase, there are two types of O sites: edge-shared O(1)and corner-shared O(2). (b) The BZ of  $K_2Cr_8O_{16}$ . Black and red lines represent the BZs of the primitive and the conventional cell of the FM phase, respectively, and the blue filled box represents the BZ of the FI phase.  $(a_p^*, b_p^*, c_p^*)$  and  $(a_m^*, b_m^*, c_m^*)$  are reciprocal lattice vectors of the primitive body-centered tetragonal unit cell of the FM phase and the monoclinic unit cell of the FI phase, respectively. Note that, in the FM phase,  $\overline{M}$  of the BZ of the conventional cell is equivalent to X of the BZ of the primitive cell.

displacements and the Coulomb correlation are essential in opening the gap.

#### **II. COMPUTATIONAL DETAILS**

For the DFT calculations, we employed the pseudopotential band method implemented in VASP [16], and for the phonon calculations, we employed the PHONOPY code [17]. The force constants for the phonon calculation were obtained from the supercell calculation with finite displacements by the Hellmann-Feynman theorem [18]. We used the pseudopotential band method with projected augmented-wave potentials [19,20]. The generalized gradient approximation (GGA-PBE) was used for the exchange-correlation functional [21]. Before carrying out the phonon calculations, we performed the full relaxation, which adjusts the lattice constant and atomic positions under the symmetry constraint of the original structure. The initial structural data before the full relaxation were taken from the experiment [22]. For the GGA + U calculations, we have checked several U values, and presented the results for U = 3.0 eV below [2]. The energy cut-off of 520 eV was used for the number of plane wave bases. The **k**-point samplings are  $(6 \times 6 \times 20)$  for the conventional tetragonal unit cell of the FM metallic phase, and  $(4 \times 4 \times 20)$  for the monoclinic unit cell of the FI phase in the Monkhorst-Pack grid. The  $(2 \times 2 \times 2)$  supercell of the conventional tetragonal structure is selected for the phonon calculation of the FM metallic phase.

## **III. RESULTS AND DISCUSSIONS**

We first carried out the band structure calculations for the FM phase of  $K_2Cr_8O_{16}$  both in the GGA and the GGA + U schemes. Both schemes produce the metallic phase, more precisely, the half-metallic phase, as is consistent with existing reports [5,12]. In both cases, total magnetic moments per formula unit are obtained to be  $18.00\mu_B$  [23], which is close to the experimental value [5,11].

Figure 2 presents the phonon dispersion curve and the phonon partial density of states (DOS) of  $K_2Cr_8O_{16}$  in its FM phase. Figures 2(a) and 2(b) were calculated without and with U, respectively. In both cases, flat bands are observed at  $\sim 10$  meV, which correspond to the localized phonon bands from K. The significant difference between phonon bands of the GGA and the GGA + U is the existence of the imaginary phonon frequency in the latter [Fig. 2(b)], which indicates

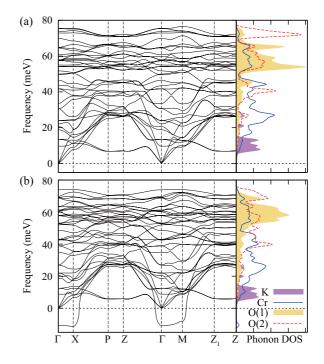


FIG. 2. (Color online) Phonon dispersion and the corresponding partial DOS of  $K_2Cr_8O_{16}$  in its FM phase: (a) result from the GGA, and (b) result from the GGA + U (U = 3.0 eV). The *k*-point symmetry lines are along the BZ boundaries of the primitive unit cell of the FM phase. The negative phonon frequencies (imaginary frequencies) reflect the structural instability. It is seen from the DOS in (b) that the softened phonons are related mostly to the lattice vibrations of Cr ions.

the structural instability of the FM phase of  $K_2Cr_8O_{16}$  in agreement with the experiment. The fact that the structural instability is obtained in the GGA + U but not in the GGA reflects that the GGA + U phonon calculation describes the experimental structural transition properly, while the GGA phonon calculation does not. It is seen that the structural instabilities are prominent at M, X, and  $\Gamma$ , which correspond to mostly Cr displacements as shown in phonon DOS. We also checked the structural instability with varying U value. It occurs only when  $U > \sim 2.5$  eV. This means that large enough U is necessary to induce the structural instability, which corroborates that the structural transition is really driven by the Coulomb correlation effect. We will discuss below that the softened phonon responsible for the transition in  $K_2Cr_8O_{16}$ is that at X.

To investigate the structural instability signaled by phonons in more detail, let us examine the low temperature structure of the FI phase of K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>. The main difference between the FM phase and the FI phase is the increased unit cell size by  $\sqrt{2} \times$  $\sqrt{2} \times 1$  with respect to the conventional cell of the FM phase due to the distortions of Cr and O. Toriyama et al. [2] observed that, in the *ab* plane, there is a stripe-type arrangement of the Cr tetramers formed in the four-chain columns. To explain the modulation of the tetragonal cell in the *a* and *b* directions, there should be a structural instability at  $\overline{M}$  in the conventional tetragonal cell, which actually corresponds to the X point in the primitive cell of the FM phase [see Fig. 1(b)]. It is because the softened phonon mode at  $\overline{M}$  in the tetragonal unit cell exhibits the opposite atomic displacements alternating in every other unit cell along the a and b directions and increases the unit cell in the *ab* plane. Note that this  $\mathbf{Q}(=X)$  vector is different from the previously suggested Peierls nesting vector  $Q_z = 2\pi/c$  [2], which actually corresponds to the M point (1/2, 1/2, -1/2)in the primitive cell or the  $\Gamma$  point in the conventional cell.

Figure 3 shows the lattice displacements of the softened phonon modes at *X* and *M*. In both cases, the formation of Cr tetramers, which is the main lattice distortion from FM to FI phase, appears, as depicted by the gray boxes in (1), (2), (3), and (4) in Figs. 3(b) and 3(d). The softened phonon at *X* in Figs. 3(a) and 3(b) produces not only the formation of Cr tetramer in the four-chain column along the *c* direction but also the stripe-type arrangement of Cr tetramers in the *ab* plane, as shown in Fig. 4(a). The formation of Cr tetramers shown in Fig. 3(b) is perfectly consistent with that reported by Toriyama *et al.* [2]. The stripe-type arrangement of Cr tetramers explains the unit cell increasing in the *ab* plane after the MIT. Namely, the normal mode of softened phonon at *X* is exactly consistent with the experimental lattice distortions.

Figures 3(c) and 3(d) present the lattice displacements by the softened phonon at M, which is the previously suggested Peierls nesting vector,  $Q_z = 2\pi/c$  [2]. The formation of Cr tetramers is also obtained in this case, as shown in Fig. 3(d). However, the arrangement of Cr tetramers in the *ab* plane is different from the experimentally observed stripe type. In this case, the arrangement is of uniform type, as shown in Fig. 4(b), which cannot explain the increasing unit cell from the FM phase to the FI phase. This result is somehow expected because the M point in the primitive cell of the FM phase is in the same position as the  $\Gamma$  point in the conventional tetragonal cell of the FM phase. That is why the structural instability at M

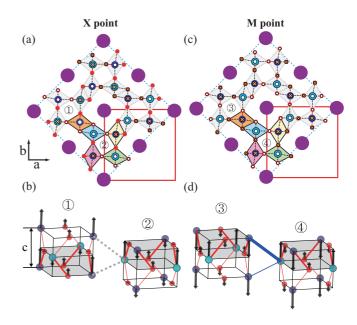


FIG. 3. (Color online) (a),(b) Lattice displacements of the softened phonon mode at *X*, and (c),(d) those at *M*. Purple, blue, sky-blue, and red circles are K, Cr(z = 0), Cr(z = 0.5), and O, respectively. White circles and orange crosses at Cr and O in (a) and (c) denote the outward and inward arrows, respectively. (b) and (d) show the main atomic displacements of Cr and O(2), which lead to the formation of Cr tetramers in the four-chain column, as depicted by the gray boxes in ①, ②, ③, and ④. Thick and thin red lines represent shorter and longer bonds between Cr and O ions, respectively. Dotted gray lines connecting Cr ions in-between the double chain of (b) stand for the uniform distance between Cr-Cr, whereas thick and thin blue lines in (d) stand for the shorter and longer distances between Cr-Cr, respectively.

produces the uniform-type arrangement of Cr tetramers, which does not increase the unit cell of the conventional tetragonal structure in the *ab* plane. We thus suggest that the Peierls distortion vector **Q** that yields the Peierls instability is X (0, 0, 1/2) in the primitive cell of the body-centered tetragonal structure, not M (1/2, 1/2, -1/2).

This result is indeed consistent with that from total energy calculations. We checked the total energies of modulated structures corresponding to the softened phonon modes at X, M, and  $\Gamma$  with varying associated displacements. At each mode, the total energy has the minimum at the equilibrium displacement. It is found that the total energy of the modulated structure due to the X phonon mode is the lowest, while that due to the M phonon mode is the highest. This result is in agreement with the above phonon mode analysis.

The main difference between the lattice displacements of the softened phonons at X and M lies in the linking of Cr-Cr in the double chains of the edge-shared  $CrO_6$  octahedra. If Cr atoms in each chain move oppositely, the Cr-Cr dimerization of zigzag type is formed in the double chain, as shown in Fig. 3(d). Otherwise, there is no Cr-Cr dimerization [Fig. 3(b)]. Due to these two possibilities of Cr-Cr linkings in the double chains, there occur three types of arrangements of Cr tetramers [22], as shown in Fig. 4. The stripe type in Fig. 4(a) contains the half of double chains with Cr dimers, while the uniform type

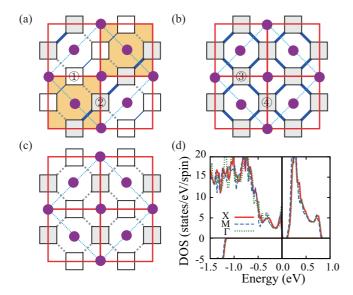


FIG. 4. (Color online) The arrangements of Cr tetramers in the *ab* plane obtained from the softened phonon modes. Dotted gray, thick and thin blue lines connecting Cr ions in the double chains are the same as in Fig. 3. Solid purple circles represent K atoms. (a) The stripe-type arrangement by the softened phonon at X. Yellow shadow indicates the modulation of the tetragonal structure in the *ab* plane, as observed in the experiment [2]. (b) The uniform-type arrangement by the softened phonon at  $\Pi$ . (c) The checkerboard-type arrangement by the softened phonon at  $\Gamma$ . (d) Total DOS of each tetramer arrangement obtained in the GGA + U (U = 3.0 eV). Positive and negative DOSs represent those of spin-majority and spin-minority electrons, respectively.

in Fig. 4(b) and the checkerboard type in Fig. 4(c) have all and none of the double chains with Cr dimers, respectively. Noteworthy is that these three types of arrangements match exactly with the normal mode displacements of the softened phonons at X, M, and  $\Gamma$ .

To check the role of the Cr-Cr dimers in the double chains, we compared the DOSs of the above three modulated structures in Fig. 4(d). Intriguingly, the insulating phases are obtained for all three cases, regardless of existence or nonexistence of the Cr-Cr dimers in the double chain. The sizes of energy gaps of three cases are 0.1-0.13 eV, which are similar to that of the FI phase [2]. This result indicates that the insulating nature of the full phase originates from the formation of Cr tetramers in the four-chain columns, not from the Cr-Cr dimers in the double chains. This feature is quite different from the case in K<sub>2</sub>Mo<sub>8</sub>O<sub>16</sub>, for which the insulating gap was reported to arise from the distortions in the double chain of the edge-shared MoO<sub>6</sub> octahedra [24].

We also checked the roles of the Coulomb correlation Uand the Peierls dimerization in the MIT and the structural transition. To investigate the U effect in the FM phase, the charge-density difference (CDD) between the GGA + Uand GGA calculations is plotted in Fig. 5(a). It is seen that Cr  $d_{yz+zx}$  and O(2)  $p_z$  electrons are more occupied in the GGA + U than in the GGA, while Cr  $d_{yz-zx}$  electrons are less occupied. This result suggests that the hybridization  $\pi$ bonding between the Cr  $d_{yz+zx}$  and O  $p_z$  orbitals increases with U. In fact, the Cr  $d_{yz+zx}$ -O  $p_z$  spin transfer path in the

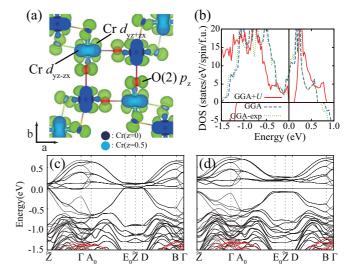


FIG. 5. (Color online) (a) The CDD between the GGA + U(U = 3.0 eV) and the GGA for the FM phase of K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>. Green and blue represent the positive and negative parts, respectively. The Cr tetramer, indicated by the red line, is seen to be connected by the  $\pi$  bonding. (b) Comparison of total DOSs of the GGA and the GGA + U(U = 3.0 eV) for the FI phase of K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>. The DOS of GGA-exp is obtained for the experimental structure in the GGA. (c) The GGA + U(U = 3.0 eV) band structure of the FM phase of K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>, and (d) that of the FI phase. Band splitting is evident in the BZ boundary including  $\tilde{Z}$ . Spin-majority and spin-minority bands are plotted by black and red lines, respectively. The structures of FM and FI phases were optimized before the calculations except the case of GGA-exp in (b).

FI phase is emphasized in the recent NMR paper [25]. This hybridization is important for the formation of Cr tetramer, because Cr ions in tetramer are linked with O(2). Therefore, U effect facilitates the transition from the FM phase to the FI phase by increasing the hybridization between Cr  $d_{yz+zx}$  and O(2)  $p_z$ . Thus, this increased hybridization is expected to cause the structural instability in the phonon dispersion of the FM phase, so as to produce the stabilized Cr tetramers. Phonon data and the CDD result are reminiscent of the correlation-assisted Peierls transition or Mott-Peierls transition in VO<sub>2</sub>[26–28]. But the unique feature of K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub> is that the Mott-Peierls transition occurs in the fully spin-polarized band.

Figure 5(b) shows the role of U in the FI phase in the band-gap opening. The band gap opens only when both the distortion and the Coulomb correlation are taken into account. We found that the Cr-tetramer distortion is stabilized only with the Coulomb correlation. In the GGA calculation, a Cr tetramer given for an initial structure disappears after the structural optimization, and there is no band-gap opening. The GGA calculation for the experimental structure of the FI phase containing Cr tetramers also does not produce the band gap [see the DOS of GGA-exp in Fig. 5(b)]. Namely, the GGA calculation does not open the band gap, even in the presence of the Peierls dimerization. This implies that K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub> belongs to a Mott insulator possessing the Peierls-type instability. The band gap in the GGA + U is 0.125 eV, which is in agreement with the previous calculation [2].

Figures 5(c) and 5(d) show GGA + U band structures of the FM and FI phases of  $K_2Cr_8O_{16}$ , calculated in the FI phase symmetry. In the band structure of the FM phase in Fig. 5(c), there is no band-gap opening because of the absence of the Peierls distortion. That is, the band gap opens in the presence of the Peierls distortion [Fig. 5(d)]. Through the lattice distortion, the energy gain is obtained mainly from bands at  $\tilde{Z}$ ,  $E_0$ , and D, which are in the BZ boundary along the  $c^*$  direction [see Fig. 1(b)]. The energy gain from the lattice distortion in this case is ~19 meV/f.u.

### **IV. CONCLUSION**

Based on the systematic studies of electronic and phonon properties, we have found that  $K_2Cr_8O_{16}$  is a strongly correlated system having the Coulomb correlation effect both in the FM and the FI phases. We demonstrated that the structural instability that occurs at X only in the GGA + U scheme describes perfectly well the experimentally observed lattice PHYSICAL REVIEW B 90, 045124 (2014)

distortions, such as the formation of Cr tetramers along the *c* direction and the stripe-type arrangement of Cr tetramers in the *ab* plane. Thus we proposed the Mott-Peierls transition as the driving mechanism of the concomitant MIT and the structure transition in K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>. Our finding of the Peierls distortion vector  $\mathbf{Q} = X$  rules out the previously suggested nesting vector of  $Q_z = 2\pi/c$  for the Peierls transition in K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub>. We also showed that the Cr tetramers and the insulating gap of the FI phase are stable only with Coulomb correlation, which corroborates that the FI phase of K<sub>2</sub>Cr<sub>8</sub>O<sub>16</sub> is a Mott-Peierls insulator.

### ACKNOWLEDGMENTS

This work was supported by the NRF (Grants No. 2009-0079947 and No. 2011-0025237), the POSTECH BSRI grant, and the KISTI supercomputing center (Project No. KSC-2012-C2-094). S.K. acknowledges the support from the NRF project of Global Ph.D. Fellowship (Project No. 2011-0002351).

- M. Imada, A. Fujimori, and Y. Tokura, Rev. Mod. Phys. 70, 1039 (1998).
- [2] T. Toriyama, A. Nakao, Y. Yamaki, H. Nakao, Y. Murakami, K. Hasegawa, M. Isobe, Y. Ueda, A. V. Ushakov, D. I. Khomskii, S. V. Streltsov, T. Konishi, and Y. Ohta, Phys. Rev. Lett. 107, 266402 (2011).
- [3] M. Isobe, S. Koishi, N. Kouno, J.-I. Yamaura, T. Yamauchi, H. Ueda, H. Gotou, T. Yagi, and Y. Ueda, J. Phys. Soc. Jpn. 75, 073801 (2006).
- [4] T. Ozawa, I. Suzuki, and H. Sato, J. Phys. Soc. Jpn. 75, 014802 (2006).
- [5] K. Hasegawa, M. Isobe, T. Yamauchi, H. Ueda, J.-I. Yamaura, H. Gotou, T. Yagi, H. Sato, and Y. Ueda, Phys. Rev. Lett. 103, 146403 (2009).
- [6] K. Noami, Y. Muraoka, T. Wakita, M. Hirai, Y. Kato, T. Muro, Y. Tamenori, and T. Yokoya, J. Appl. Phys. 107, 073910 (2010).
- [7] M. Isobe, S. Koishi, S. Yamazaki, J. Yamaura, H. Gotou, T. Yagi, and Y. Ueda, J. Phys. Soc. Jpn. 78, 114713 (2009).
- [8] S. Horiuchi, T. Shirakawa, and Y. Ohta, Phys. Rev. B 77, 155120 (2008).
- [9] T. Toriyama, M. Watanabe, T. Konishi, and Y. Ohta, Phys. Rev. B 83, 195101 (2011).
- [10] O. Tamada, N. Yamamoto, T. Mori, and T. Endo, J. Solid State Chem. **126**, 1 (1996).
- [11] T. Endo, S. Kume, N. Kinomura, and M. Koizumi, Mater. Res. Bull. 11, 609 (1976).
- [12] M. Sakamaki, T. Konishi, and Y. Ohta, Phys. Rev. B 80, 024416 (2009); 82, 099903(E) (2010).
- [13] M. A. Korotin, V. I. Anisimov, D. I. Khomskii, and G. A. Sawatzky, Phys. Rev. Lett. 80, 4305 (1998).

- [14] S. Nishimoto and Y. Ohta, Phys. Rev. Lett. 109, 076401 (2012).
- [15] P. Mahadevan, A. Kumar, D. Choudhury, and D. D. Sarma, Phys. Rev. Lett. **104**, 256401 (2010).
- [16] G. Kresse and J. Furthmüller, Phys. Rev. B 54, 11169 (1996); Comput. Mater. Sci. 6, 15 (1996).
- [17] A. Togo, F. Oba, and I. Tanaka, Phys. Rev. B 78, 134106 (2008).
- [18] K. Parlinski, Z. Q. Li, and Y. Kawazoe, Phys. Rev. Lett. 78, 4063 (1997).
- [19] P. E. Blöchl, Phys. Rev. B 50, 17953 (1994).
- [20] G. Kresse and D. Joubert, Phys. Rev. B 59, 1758 (1999).
- [21] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996); 78, 1396(E) (1997).
- [22] A. Nakao, Y. Yamaki, H. Nakao, Y. Murakami, K. Hasegawa, M. Isobe, and Y. Ueda, J. Phys. Soc. Jpn. 81, 054710 (2012).
- [23] Local magnetic moments in the GGA are  $2.32\mu_B/\text{Cr}$ , -0.02 $\mu_B/\text{O}(1)$ , and -0.11 $\mu_B/\text{O}(2)$ , while those in the GGA + U are  $2.59\mu_B/\text{Cr}$ , -0.10 $\mu_B/\text{O}(1)$ , and -0.23 $\mu_B/\text{O}(2)$ .
- [24] T. Toriyama, M. Watanabe, T. Konishi, and Y. Ohta, Phys. Rev. B 88, 235116 (2013).
- [25] H. Takeda, Y. Shimizu, M. Itoh, M. Isobe, and Y. Ueda, Phys. Rev. B 88, 165107 (2013).
- [26] S. Biermann, A. Poteryaev, A. I. Lichtenstein, and A. Georges, Phys. Rev. Lett. 94, 026404 (2005).
- [27] M. W. Haverkort, Z. Hu, A. Tanaka, W. Reichelt, S. V. Streltsov, M. A. Korotin, V. I. Anisimov, H. H. Hsieh, H.-J. Lin, C. T. Chen, D. I. Khomskii, and L. H. Tjeng, Phys. Rev. Lett. 95, 196404 (2005).
- [28] S. Kim, K. Kim, C.-J. Kang, and B. I. Min, Phys. Rev. B 87, 195106 (2013).