# **Polarization-controlled Ohmic to Schottky transition at a metal/ferroelectric interface**

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Ferroelectric polar displacements have recently been observed in conducting electron-doped BaTiO<sub>3</sub> ( $n$ -BTO). The coexistence of a ferroelectric phase and conductivity opens the door to new functionalities that may provide a unique route for novel device applications. Using first-principles methods and electrostatic modeling, we explore the effect that the switchable polarization of  $n$ -BTO has on the electronic properties of the SrRuO<sub>3</sub>/ $n$ -BTO (001) interface. Ferroelectric polarization controls the accumulation or depletion of electron charge at the interface, and the associated bending of the *n*-BTO conduction band determines the transport regime across the interface. The interface exhibits a Schottky tunnel barrier for one polarization orientation, whereas an Ohmic contact is present for the opposite polarization orientation, leading to a large change in interface resistance associated with polarization reversal. Our calculations reveal a five orders of magnitude change in the interface resistance because of polarization switching.

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## **I. INTRODUCTION**

Complex oxide heterostructures exhibit an abundance of physical phenomena that involve the interplay among magnetism, electricity, and conductivity.<sup>1</sup> This is largely due to the presence of interfaces that have unique properties, often not existing in the bulk counterparts. $2-4$  Especially interesting are interfaces that contain a ferroelectric material as one of the constituents. Due to their electrically switchable spontaneous polarization, ferroelectric materials are attractive for technological applications.<sup>[5–8](#page-5-0)</sup> Interface effects induced by ferroelectric polarization involve a number of interesting phenomena,<sup>[9](#page-5-0)</sup> such as electrically controlled interface magnetization,  $10-13$  magnetic order,  $14,15$  magnetic anisotropy, <sup>[16–18](#page-5-0)</sup> in-plane<sup>[19](#page-5-0)</sup> and perpendicular-to-the-plane transport,<sup>20,21</sup> transport spin polarization,<sup>[22,23](#page-5-0)</sup> interface carrier density, $^{24}$  and superconductivity. $^{25}$  $^{25}$  $^{25}$  Polarization-controlled interface effects are promising for potential application in novel electronic devices.

While ferroelectric materials are normally considered as insulators, semiconducting ferroelectrics have been known for a long time. $26$  The coexistence of the ferroelectric phase and conductivity is interesting because such a conducting bistable material introduces new functionalities. For example, experiments have found that the ferroelectric phase persists deeply into the metallic phase of oxygen reduced BaTiO<sub>3− $\delta$ </sub> .<sup>[27,28](#page-5-0)</sup> Theoretical studies have demonstrated that ferroelectric displacements persist up to the doping level of about 0.1 *e* per unit cell (u.c.) in BaTiO<sub>3</sub> (BTO; ~10<sup>21</sup>/cm<sup>3</sup>) consistent with the experimental findings[.29,30](#page-5-0) Although in such a material an external electric field induces a flow of electric current that makes switching of the ferroelectric polarization difficult, sufficiently resistive materials may sustain the coercive voltage. For example, ferroelectric tunnel junctions are switchable despite the current flowing across them.[8](#page-5-0) Furthermore, ferroelectric switching can be realized by an applied voltage that rises sufficiently fast in time. A recent prominent example is the resistive switching behavior of semiconducting ferroelectric  $BiFeO<sub>3</sub>.<sup>31</sup>$  $BiFeO<sub>3</sub>.<sup>31</sup>$  $BiFeO<sub>3</sub>.<sup>31</sup>$  The semiconducting

behavior of  $BiFeO<sub>3</sub>$  has recently been exploited in the demonstration of polarization-controlled charge transport $32,33$  and switchable photovoltaic effects. $34,35$  The latter behavior was qualitatively explained by a ferroelectrically driven transition from a Schottky to Ohmic contact at the interface. $36$  It has also been demonstrated that a Schottky contact consisting of semiconducting  $PbTiO<sub>3</sub>$  and a high work function metal, Au, exhibits bistable conduction characteristics.<sup>37</sup> An on-off ratio of two orders in magnitude was observed and explained by a model in which the depletion width of the ferroelectric Schottky barrier is determined by the polarization dependence of the internal electric field at the metal/ferroelectric interface.

Driven by these developments, we explore the effect of polarization on the transport regime across the interface formed between an oxide metal and a doped ferroelectric, using density-functional methods and electrostatic modeling. We predict, from first principles, a switchable potential barrier driven by the accumulation or depletion of screening charge at the interface in response to ferroelectric polarization reversal. We demonstrate a ferroelectrically induced change from the Ohmic transport regime, where interface conductance is metallic, to the Schottky regime, where a tunneling barrier is formed at the interface, as depicted in Fig. [1.](#page-1-0) This switching leads to a five orders of magnitude change in the interface resistance and therefore demonstrates interesting potential for device applications.

## **II. STRUCTURE AND METHODS**

We explore the polarization-controlled contact by considering an epitaxial interface between a metallic oxide,  $SrRuO<sub>3</sub>$ , and electron doped BTO (*n*-BTO). First-principles calculations are performed using the plane-wave pseudopotential code QUANTUM ESPRESSO,<sup>[38](#page-5-0)</sup> where the exchange and correlation effects are treated within the local-density approximation (LDA). We assume that the doping of *n*-BTO is 0.06 *e* per formula unit (f.u.), which is realized by the virtual crystal approximation<sup>39</sup> applied to the oxygen potentials in BTO. For this doping ( $n \approx 1.9 \times 10^{21}$  cm<sup>-3</sup>), the ferroelectric

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FIG. 1. (Color online) Polarization-controlled band alignment at in the interface between a metal (M) and electron-doped ferroelectric (*n*-FE). Arrows indicate the polarization direction. (a) Polarization pointing away from the interface leads to electron depletion, pulling the *n*-FE conduction band upward. (b) Polarization pointing into the interface leads to electron accumulation, pushing the *n*-FE conduction band down. In the case shown here, polarization reversal leads to a transition from a Schottky tunnel barrier (a) to an Ohmic contact (b) between M and *n*-FE.

displacements remain sizable, being about 70% of those in the undoped BTO. $29$  The calculations are performed using periodic boundary conditions on a supercell constructed of 15.5 u.c. of BTO and 10.5 u.c.  $SrRuO<sub>3</sub>$ , as shown in Fig 2. We consider a SrO/TiO<sub>2</sub> interface termination at the SrRuO<sub>3</sub>/n-BTO (001) interface, which is experimentally found to be more stable, as compared to the  $RuO<sub>2</sub>/BaO$  interface.<sup>[40](#page-5-0)</sup> We assume the same  $SrO/TiO<sub>2</sub>$  terminations at both interfaces in the supercell, which allows us to study the effect of polarization reversal at a given interface by comparing the properties of the two interfaces in the supercell for a single polarization orientation. To simulate coherent epitaxial growth on a  $(001)$ -oriented SrTiO<sub>3</sub> substrate, we constrain the in-plane lattice constant of the supercell to be the calculated LDA lattice constant of cubic SrTiO<sub>3</sub>,  $a = 3.871$  Å. Using the same approach as in the previous work, $^{41}$  $^{41}$  $^{41}$  we perform full



FIG. 2. (Color online) Relative *z*-displacement between cation (M) and anion (O) on each atomic layer of the  $SrRuO<sub>3</sub>/n-BTO$ supercell. Light squares are for  $BO_2$  layers ( $B = Ti$  or Ru) and dark squares are for  $AO$  layers  $(A = Ba \text{ or } Sr)$ . A positive displacement indicates that polarization is pointing to left, as shown by the arrow. The left half of the supercell corresponds to the contact with polarization pointing into the metal, while the right half of the supercell corresponds to the contact with polarization pointing out of the metal, as in Fig. 1. The solid curve shows the polarization profile obtained from the electrostatic model.

relaxation of the internal *z*-coordinates and overall *c/a* ratio of the supercell.

## **III. RESULTS**

#### **A. Atomic and electronic structure**

Figure 2 shows the layer-resolved metal-oxygen (M-O) relative *z* displacements across the supercell, where positive displacements indicate polarization pointing to the left. Thus, the left interface corresponds to the contact with *n*-BTO polarization, pointing into the  $SrRuO<sub>3</sub>$  metal, while the right interface corresponds to *n*-BTO polarization, pointing away from the  $SrRuO<sub>3</sub>$ . In the middle of the supercell, *n*-BTO exhibits bulklike polar displacements. At the right interface, however, the M-O displacements drop sharply, while at the left interface they remain nearly constant (even slightly enhanced). This behavior is consistent with the electric field profile resulting from the competition between screening, polarization charges and the built-in dipole layer at the two interfaces, as described in the electrostatic modeling discussed later.

Figure 3 shows the calculated layer-resolved density of states (DOS) on the 3*d* Ti orbital across the *n*-BTO. It is seen that at the left interface the conduction-band minimum  $(CBM)^{42}$  $(CBM)^{42}$  $(CBM)^{42}$  lies below the Fermi energy, implying that for polarization pointing toward the  $SrRuO<sub>3</sub>$  metal the contact is metallic (Ohmic). On the other hand, for three  $TiO<sub>2</sub>$ monolayers at the right interface the CBM lies above the Fermi energy. This implies that for polarization pointing away from the  $SrRuO<sub>3</sub>$  metal the contact exhibits a Schottky barrier. The height of this barrier is about 0.4 eV, and the width is about 1 nm.

The major features of the CBM (Fig. 3) and polarization (Fig. 2) profiles of *n*-BTO can be captured by a continuum electrostatic model, as described in the appendix. The effects of the  $SrRuO<sub>3</sub>$  electrodes are incorporated by interfacial boundary conditions on the *n*-BTO layer assuming (i) a linearized Thomas-Fermi screening length *λ* and relative dielectric constant  $\varepsilon$  for SrRuO<sub>3</sub> and (ii) an electrostatic



FIG. 3. (Color online) Layer-resolved DOS on the 3*d* Ti orbital across *n*-BTO (filled curves). Open circles show the CBM obtained as described in the text. The solid curve shows the calculated CBM from the electrostatic model.

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FIG. 4. (Color online)  $\mathbf{k}_{\parallel}$ -resolved local DOS in the SrRuO<sub>3</sub>/*n*-BTO heterostructure, calculated at the Fermi energy for each atomic  $TiO<sub>2</sub>$  layer, numbered from the left to right interfaces corresponding to Fig. [2.](#page-1-0)

potential step going from  $n$ -BTO to SrRuO<sub>3</sub>,  $\Delta V$ , representing the built-in interface dipole, assumed to be the same at both interfaces. The polarization is modeled in the linear response regime,  $P(x) = \chi \varepsilon_0 E(x) + P_0$ , where  $P_0$  is the polarization of bulk *n*-BTO in the absence of applied fields and *χ* is the linear dielectric susceptibility of the ferroelectric in response to the local electric field  $E(x)$ . The local electron density in  $n-\text{BTO}, n(x)$ , is determined self-consistently with the potential by incorporating the local DOS of the conduction band, which is taken from calculations of bulk *n*-BTO, only shifted by the local potential  $-e\varphi(x)$ .

We solve the Poisson equation numerically and fit the results to the CBM profile in Fig. [3](#page-1-0) using  $\lambda$ ,  $\varepsilon$ ,  $\Delta V$ ,  $\chi$ , and  $P_0$  as adjustable parameters. The resulting profile for the polarization and CBM are plotted alongside the first-principles results in Figs. [2](#page-1-0) and [3,](#page-1-0) respectively, with  $\lambda/\varepsilon = 0.16$  Å,  $\Delta V = 0.8$  V,  $\chi = 55$ , and  $P_0 = 32 \mu C/cm^2$  providing the best fit.

Next, we explore the electronic structure of *n*-BTO in the supercell as a function of transverse wave vector  $\mathbf{k}_{\parallel}$ . In Fig. 4, we plot the  $k_{\parallel}$ -resolved DOS at the Fermi energy for each TiO<sub>2</sub> atomic layer in  $n$ -BTO. Here, we number the TiO<sub>2</sub> layers from 1 to 16 with layer 1 located at the left interface and layer 16 located at the right interface. The Fermi surface of bulk *n*-BTO is an open tube oriented along the *z* direction, with a *z*-dependent modulation of the radius (see Fig. [8](#page-4-0) in the appendix). The projection of the bulk Fermi surface on the *xy* plane is a slightly distorted ring, as shown in Fig.  $5(a)$ , whose inner and outer radii indicate the minimal and maximal radius of the tube. When  $n$ -BTO is placed between  $SFRuO<sub>3</sub>$ layers its Fermi surface changes. Comparing Fig. 4 to the **k**<sub> $\parallel$ </sub>-resolved DOS for bulk *n*-BTO [Fig. 5(a)], we see that in the middle of the supercell, e.g., for layer 7 in Fig. 4, the **k**-resolved DOS appears as a ring similar to that for bulk *n*-BTO. Closer to the left interface the ring is slightly distorted,



FIG. 5. (Color online) **k**<sub>1</sub>-resolved DOS at the Fermi energy in bulk  $n$ -BTO (a) and  $SFRuO<sub>3</sub>$  (b) and ballistic transmission across the  $SrRuO<sub>3</sub>/n-BTO$  junction with polarization pointing to the  $SrRuO<sub>3</sub>$ Ohmic contact (c), and polarization pointing away from the  $SrRuO<sub>3</sub>$ Schottky contact (d).

but qualitatively it remains similar to the bulk one. This is due to the layer-dependent CBM remaining nearly flat at the left interface, as is evident from Fig. [3.](#page-1-0) Only for interfacial layer 1 in Fig. 4, we see a significant change in the  $k_{\parallel}$ -resolved DOS, which appears a disk at the  $\bar{\Gamma}$  point. This feature is due to the up bending of the *n*-BTO band for this interface layer (see Fig. [3\)](#page-1-0) and electron density induced by the adjacent  $SrRuO<sub>3</sub>$ . Thus, for polarization pointing to the  $SFRuO<sub>3</sub>$  metal layer, the contact is nearly metallic (Ohmic), and we expect an efficient transmission across it. $43$ 

This behavior changes dramatically for the right interface. The upward bending of the conduction bands seen in Fig. [3](#page-1-0) corresponds to a shrinking Fermi surface, as reflected in the reduced radius of the ring in the  $k_{\parallel}$ -resolved DOS (layers 9–12 in Fig. 4) and the transformation of Fermi surface from an open tube to a closed ellipsoid (states appear at  $\Gamma$ ). The ring disappears at the third  $TiO<sub>2</sub>$  monolayer from the interface, and the  $k_{\parallel}$ -resolved DOS shows nil for layers 14–16. This is due to the CBM bending above the Fermi level. These three monolayers near the interface exhibit a gap for electron transport. Thus, for polarization pointing away from the  $SrRuO<sub>3</sub>$  metal layer, the contact is of Schottky type, and we expect a reduced transmission across it.

## **B. Electronic transport**

To confirm our expectations regarding the electronic transport we study the transmission across the  $S_{rRuO_3/n}$ -BTO (001) interface for two polarization orientations. The transmission is calculated using a general scattering formalism implemented in the QUANTUM ESPRESSO.<sup>[38](#page-5-0)</sup> In the calculation, we use the left interface and the right interface in the supercell (Fig. [2\)](#page-1-0) as separate scattering regions, each of which is ideally attached on one side to a semi-infinite  $S_rRuO_3$  electrode and on the other side to a semi-infinite *n*-BTO electrode. These geometries correspond to the same SrRuO3/*n*-BTO junction with polarizations pointing in the opposite directions. We assume perfect periodicity in the plane parallel to the interfaces so that the in-plane component of the Bloch wave vector,  $\mathbf{k}_{\parallel}$ , is preserved for all single-electron states.

Figures  $5(c)$  and  $5(d)$  show the calculated **k**<sub> $\parallel$ </sub>-resolved transmission for polarization pointing to the  $SrRuO<sub>3</sub>$  and away from the  $SFRuO<sub>3</sub>$ , respectively. The plots are limited to the region near the  $\Gamma$  point, where the transmission is nonzero. This region is sampled using a uniform  $51 \times 51$  **k**<sub>||</sub> mesh. The transmission distribution in the two-dimensional Brillouin zone has a similar shape for the two polarization orientations. It originates from the overlap of the Fermi surface projections of bulk *n*-BTO and SrRuO<sub>3</sub>, shown in Figs.  $5(a)$  and  $5(b)$ , respectively. The striking feature is a huge difference in the transmission magnitude for two polarization orientations. We find that polarization switching leads to a change of five orders in magnitude of transmission. The associated interface resistances<sup>[44](#page-5-0)</sup> are  $5.5 \times 10^2 \Omega \mu \text{m}^2$  for the Ohmic contact and  $3.78 \times 10^7 \Omega \mu \text{m}^2$  for the Schottky contact.

#### **IV. SUMMARY**

We have shown that the polarization driven accumulation or depletion of free carriers at the SrRuO<sub>3</sub>/n-BTO (001) interface alters the transport regime across the interface from metallic to tunneling. We find that polarization switching leads to a five orders of magnitude change in the interface resistance. We hope that the predicted polarization-controlled Ohmic to Schottky transition at the metallic oxide/doped ferroelectric interface will stimulate experimental investigations.

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#### **APPENDIX**

#### **1. Electrostatic model**

We consider a layer of *n*-BTO from  $x = 0$  to *L* bounded on the left and right by metallic  $SrRuO<sub>3</sub>$  electrodes held in short-circuit boundary conditions. The electrodes are modeled by Thomas-Fermi screening length *λ* and relative dielectric constant  $\varepsilon$ , and therefore the potential follows the typical form

$$
\varphi_l(x) = A_l e^{x/\lambda}, \quad \varphi_r(x) = A_r e^{-(x-L)/\lambda}.
$$
 (A1)

The potential inside the *n*-BTO,  $\varphi(x)$ , must satisfy the Poisson equation

$$
\frac{\partial^2 \varphi}{\partial x^2} = -\frac{e(n_0 - n(x))}{(\chi + 1)\varepsilon_0},\tag{A2}
$$

where the first term on the right-hand side corresponds to the uniform background density of *n*-type dopants  $n_0 = 0.06/ca^2$ ,

and the second term corresponds to the occupied states in the conduction band.

The local carrier density  $n(x)$  is assumed to depend on  $x$ only through the local potential  $\varphi(x)$  and the local DOS of the conduction band,  $N(E + e\varphi(x))$ , where

$$
N(E) = \begin{cases} 0 & E < E_c^0 \\ N_0 & E > E_c^0 \end{cases}
$$
 (A3)

 $N_0$  is a constant, which is determined by the nominal carrier concentration in the bulk  $n_0$ , and the position of the CBM with respect to the Fermi level  $E_F$ , calculated in bulk *n*-BTO from first principles:  $E_c^0 = -0.33$  eV. Therefore, the average DOS is  $N_0 = n_0 / |E_c^0|$  and the local carrier concentration is

$$
n(x) = (E_F - E_c^0 + e\varphi(x)) \begin{cases} 0 & E_c^0 - e\varphi(x) > E_F \\ N_0 & E_c^0 - e\varphi(x) < E_F \end{cases}.
$$
\n(A4)

Equation  $(A2)$  is subject to boundary conditions that connect  $\varphi(x)$  to (A1) at  $x = 0$  and *L*. *A<sub>l</sub>* and *A<sub>r</sub>* can be eliminated from these boundary conditions, and the following conditions on  $\varphi(x)$  emerge

$$
\varphi(0) + \Delta V + \frac{\lambda}{\varepsilon} \left( (\chi + 1)E(0) + \frac{P_0}{\varepsilon_0} \right) = 0
$$
  

$$
\varphi(L) + \Delta V - \frac{\lambda}{\varepsilon} \left( (\chi + 1)E(L) + \frac{P_0}{\varepsilon_0} \right) = 0,
$$
 (A5)

where  $E(x)$  is the electric field in the *n*-BTO. Note that the electrodes enter the boundary conditions only through the ratio  $\lambda/\varepsilon$ . Equation (A2) is solved numerically subject to the boundary conditions in (A5), and the CBM is related to the potential as  $CBM = E_c^0 - e\varphi(x)$ ).

#### 2. Dependence on  $\Delta V$

It is well known that the band gap calculated in density functional theory, especially in LDA, is underestimated (sometimes drastically) as compared to experiment. Therefore, attempts to determine band offsets from first-principles calculations must be approached with care. In LDA, we find a band gap of  $E_g^{\text{LDA}}$ <br>= 1.8 eV for BTO, whereas in experiment it is known that  $E_g^{\text{exp}}$  $= 3.2$  eV. While little can be done for the LDA calculations to account for this issue, in our model, we can make adjustments to correct for the band-gap problem.

The simplest correction we can make is to assume that, all else being equal, the CBM must lie higher in energy than what is predicted by LDA by a fixed difference  $\Delta E_g =$  $E_g^{\text{expt}} - E_g^{\text{LDA}} = 1.4 \text{ eV}$ . This correction enters our model in the interface dipole parameter  $\Delta V$ . In our best fit to the LDA results, we found  $\Delta V = 0.8$  V, and therefore corrections for the band gap will increase this value possibly up to  $0.8 V + 1.4 V =$ 2.2 V. In Fig. [6,](#page-4-0) we plot the CBM profile across the junction for several values of  $\Delta V$ , with all other parameters of the model held fixed at those of the best fit to the LDA data. Comparing the left and right interfaces, we see that for  $\Delta V > 1.2$  V that there is a crossover from Ohmic to Schottky transition with polarization reversal to the interface always being of Schottky type, but with a significant difference between Schottky barrier height (SBH) and width (*w*) depending on the polarization

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FIG. 6. (Color online) Profile of the CBM for various interface dipoles,  $\Delta V$  (in electron volts) but using the same best-fit values found for the other parameters of the model.

orientation. These differences are further clarified in Fig. 7, where we plot the dependence of the interface barrier on  $\Delta V$ for both polarization orientations. It is clear that the change in SBH with polarization reversal is roughly constant over a broad range of  $\Delta V$ , and even increases for larger  $\Delta V$ . Therefore, we expect that our prediction of a significant change in interface resistance with polarization reversal is quite robust and independent of the deficiencies of LDA to properly predict band alignments.

#### **3. Fermi surfaces of** *n***-BTO and SrRuO3**

One of most important considerations in the study of transport phenomena across epitaxial interfaces is the matching of Fermi surfaces. The ferroelectric displacements in *n*-BTO lead to an interesting Fermi surface due to the breaking of cubic symmetry. In cubic (i.e., nonpolar) BTO, the conduction band consists mainly of Ti *d* states, which are split by the octahedral crystal field of the oxygen cage into an upper



FIG. 7. (Color online) Dependence of the Schottky barrier width (*w*) and height (SBH) on the interface dipole  $\Delta V$  for the two polarization orientations. We use the same values found for the best fit to the LDA results for the other parameters. Negative values of SBH correspond to an Ohmic contact, where  $w = 0$ .



FIG. 8. (Color online) (a) The Fermi surface of bulk *n*-BTO with  $n = 0.06$  *e/f.u.* Polarization and transport is along *z*. (b) View of the Fermi surface along *z* showing the origin of the ringlike distribution seen in Figs. [4](#page-2-0) and [5.](#page-2-0)

doublet of  $e_g$  states and a lower triplet of  $t_{2g}$  states. The latter form the states around the CBM. The onset of polarization (i.e., off-centering of the Ti ions) leads to a splitting of the  $t_{2g}$ states into an upper doublet of  $d_{zx}$  and  $d_{zy}$  and a lower singlet of  $d_{xy}$ . Therefore, when electron-doped, the free carries fill states of primarily  $d_{xy}$  character. States with  $d_{xy}$  character are essentially two-dimensional, with stronger coupling in the *xy* plane than along the polarization axis *z*. This gives rise to large band-dispersion in the plane and weak dispersion out of the plane, leading to the tubelike Fermi surface, shown in Fig. 8, for  $n = 0.06$  *e/f.u* and the ringlike distributions shown in Figs. [4](#page-2-0) and [5.](#page-2-0)

The Fermi surface of bulk  $SrRuO<sub>3</sub>$ , plotted in Fig. 9, is significantly more complicated. Given the relatively limited span of the Fermi surface of *n*-BTO [Fig. 8(b)], however, the relevant features of the  $SrRuO<sub>3</sub>$  Fermi surface are limited to the crosslike region in the small range around the  $\bar{\Gamma}$  point [see Fig. 9(b)]. The projection of these states onto the *xy* plane give rise to the cross features shown in Fig.  $5(b)$ , and their overlap with the Fermi surface of *n*-BTO determine the shape of the transmission distributions in Figs.  $5(c)$  and  $5(d)$ . The tetragonal structure arising from the epitaxial strain gives rise to the opening of several Fermi sheets along the *z* direction.



FIG. 9. (Color online) (a) The Fermi surface of bulk SrRuO<sub>3</sub> strained in the *xy* plane with  $c/a = 1.03$ , corresponding to epitaxy with an SrTiO<sub>3</sub> substrate. (b) View of the Fermi surface along  $z$ showing the origin of the crosslike distribution seen in Fig. [5\(b\).](#page-2-0)

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- <sup>43</sup>We note a mismatch of the  $\mathbf{k}_{\parallel}$ -resolved DOS between this interfacial layer and bulk *n*-BTO, which creates a barrier for ballistically transmitted electrons. In practice, however, diffuse scattering will likely make this contact Ohmic.
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