Experimental determination of conduction channels in atomic-scale conductors based on shot noise measurements

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We demonstrate a general procedure for determining the conduction channels of quantum conductors from shot noise measurements. This numerical approach allows multichannel analysis which was previously limited to superconductors. Channel analysis of Ag and Au atomic contacts reveals a remarkable behavior in which the channels fully open one by one with increasing conductance. These results allow us to unambiguously distinguish between free-electron and tight-binding descriptions for the conductance of monovalent contacts. Furthermore, the channel resolution uncovers the presence of tunneling channels in parallel to the conductance through the main contact and provides a means for distinguishing between the contacts reflecting their distinct valence orbital structures.

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The conductance of a coherent quantum conductor can be described as a sum of independent conduction channels, originating from the quantization of the electron wave modes when the transverse dimensions of the conductor are on the order of the electron Fermi wavelength.¹⁻³ The conductance associated with each channel is limited by the conductance quantum $G_0 = 2e^2/h$ while the total conductance is given by $G = G_0 \sum_{n=1}^{N} \tau_n$, where $0 \le \tau_n \le 1$ are the transmission coefficients of N conduction channels (i.e., transmission eigenvalues of the scattering matrix). This description is related to a wide variety of quantum systems such as mesoscopic scale quantum dots,⁴ nanowires and nanotubes,^{5,6} atomic contacts⁷ and molecular junctions.⁸ The set of coefficients $\{\tau_n\}_{n=1}^N$ can be viewed as a unique PIN code which describes the transport properties of the conductor.⁹ The possibility to measure the PIN code rather than merely the overall conductance would enable one to link between the observed conductance to the fundamental principles of electronic transport. For example, by analyzing the subgap structure of current-voltage curves in the superconducting state, Scheer and co-workers demonstrated that the number of channels in single-atom contacts is limited by the number of atomic valence orbitals.^{10,11} Experimental studies of conduction channels have shed light on the orbital structure,^{12,13} atomic configurations,¹⁴ and electron-vibration interactions¹⁵ in atomic-scale junctions. Still, up-to-date experimental data regarding the conduction channels is limited since obtaining the transmission coefficients has proven to be very challenging. While the transmission coefficients can be calculated from the subgap structure, these measurements are restricted to systems that can be driven to the superconducting state. For nonsuperconducting systems, several experiments on atomic-scale junctions showed that the transmission coefficients can be estimated from shot noise measurements at low temperatures¹⁵⁻¹⁷ and also at ambient conditions.¹⁸ Although shot noise can be measured in a wide variety of systems, analytical treatment of shot noise data allows calculating the transmission coefficients only when the conductance is known to be composed of at most two channels. Since in general this assumption cannot be made apriori, it is impractical to obtain the channels analytically.

In this Rapid Communication, we describe a straightforward approach to determine the conduction channels from shot noise measurements beyond the analytical limit of two channels. Our approach is based on enumerating the set of transmission coefficients and identifying the range of results which are consistent with the measured shot noise and conductance. Using a break junction setup to form Ag, Au, Al, and Pt atomic contacts we demonstrate how different aspects of electronic transport are revealed by numerically obtaining the channel resolution. A statistical analysis of transmission coefficients obtained for ensembles of Ag and Au contacts reveals a consistent tendency of the conduction channels to fully saturate one by one as the conductance of the contact is increased. In particular, in multiples of G_0 the conductance is composed of fully open channels. The presented channel analysis allows us to unambiguously distinguish between different theoretical models. In addition, it is found that partially open channels can originate from parallel tunneling contributions between atoms in the vicinity of the contact. The channel distribution obtained for Al contacts proves to be in excellent agreement with both sub-gap measurements and theoretical calculations. Finally, we show that the number of conduction channels through single-atom Pt contacts can vary significantly between two different contact configurations.

Combining shot noise and conductance data can provide information on the conduction channels. The conductance is driven from the average current, often referred to as the first moment of current. Distinctively, shot noise describes the second moment of current and therefore provides independent information.¹⁹ The suppression ratio of shot noise from Poissonian noise is expressed by the Fano factor $F = \sum_{n=1}^{N} \tau_n (1 - \tau_n) / \sum_{n=1}^{N} \tau_n$, which can be determined experimentally from the dependence of shot noise on applied bias voltage (see Supplemental Material²⁰). Therefore, the measured Fano factor (*F*) and conductance (*G*) provide two independent equations for the transmission coefficients. These expressions can be used to determine the coefficients $\{\tau_n\}_{n=1}^{N}$ when there are up to N = 2 conduction channels; however, for more than two channels, the exact set of transmissions cannot be uniquely determined. In general, a given combination of *F* and *G* can result from an infinite number of possible sets of transmission coefficients. However, certain values of *F* and *G* may limit the range of possible τ_n values. Without loss of generality, we assume the coefficients are ordered by decreasing transmission $\tau_1 \ge \tau_2 \ge$ $\dots \ge \tau_N$. Using a finite precision $\Delta \tau$ for the transmission coefficients limits the number of possible transmission sets to a finite number. Our procedure enumerates the $(1/\Delta \tau)^N$ possible sets. For each set, the Fano factor and conductance are computed and compared to the experimental values of *F* and *G*. A transmission set $\{\tau_n\}_{n=1}^N$ is considered to match the experimental values if it satisfies the following inequalities:

$$G - \Delta G \leqslant G_0 \sum_{n=1}^{N} \tau_n \leqslant G + \Delta G,$$
 (1)

$$F - \Delta F \leqslant \sum_{n=1}^{N} \tau_n (1 - \tau_n) \bigg/ \sum_{n=1}^{N} \tau_n \leqslant F + \Delta F, \quad (2)$$

where ΔF and ΔG are the experimental errors in F and G, respectively. We define $\{\tau_{i,n}\}_{n=1}^{N}$ as the *i*th set out of k transmission sets that match the experimental values. The transmission coefficient τ_n can now be determined to be in the range between $\tau_n^{\min} = \min\{\tau_{i,n}\}_{i=1}^k - \Delta \tau$ and $\tau_n^{\max} = \max\{\tau_{i,n}\}_{i=1}^k + \Delta \tau$. The additional margins $\Delta \tau$ are added to ensure all possible solutions for τ_n are included between τ_n^{\min} and τ_n^{\max} (more details can be found in the Supplemental Material²⁰). Note that spin degeneracy is assumed in this analysis; however, it is straightforward to extend the method to account for nondegenerate systems.

The extraction of the transmission coefficients is illustrated in Fig. 1 for a certain combination of $F = 0.20 \pm 0.01$ and $G = 2.00 \pm 0.01$. The panel for each coefficient τ_n (n = 1-4) displays the distribution $\{\tau_{i,n}\}_{i=1}^k$ of the computed values that match the given F and G. While in principle there are an infinite number of solutions, the histograms of the individual coefficients that match the given F and G imply that τ_n do not span the whole range between 0 and 1. Rather, they are limited to a much smaller range. As a consequence, each transmission coefficient can be determined up to a limited uncertainty, which is given by the edges of the corresponding distribution



FIG. 1. (Color online) Calculated transmission coefficients for four channels matching $F = 0.20 \pm 0.01$ and $G = 2.00 \pm 0.01$, using N = 4 and $\Delta \tau = 0.01$. The four left panels show the distribution of calculated values for $\tau_1 - \tau_4$. The rightmost panel shows the transmission range for each coefficient: $\tau_1 = 0.86-1.00$, $\tau_2 = 0.69-0.90$, $\tau_3 = 0.10-0.30$, and $\tau_4 = 0.00-013$.

(Fig. 1, rightmost panel). The resulting uncertainties in τ_n greatly depend on the measured *F* and *G* values. Detailed information on the sensitivity with respect to *F* and *G* can be found in the Supplemental Material.²⁰ As will be demonstrated below, in many cases the transmission coefficients of nanoscale conductors can be determined with sufficient accuracy to capture the important physical aspects of the conduction channels.

The presented analysis was used to examine the evolution of conduction channels in atomic contacts under variation of the contact geometry. Atomic contacts were formed at 4.2 K in cryogenic vacuum using a mechanical controllable break junction (MCBJ) technique.²¹ A microscopic wire (0.1 mm diameter) with a small notch at its center is pulled apart in a controlled fashion. During the elongation process the number of atoms in the cross section of the wire constriction is gradually reduced until reaching a single-atom contact. A three-point bending mechanism driven by a piezoelectric element was used to control the elongation of the contact with sub-angstrom resolution. The wires that were used are composed of pure (>99.99%) Ag, Au, Al, and Pt. The differential conductance (dI/dV) of the contacts was measured across the wire using a lock-in technique. In order to measure shot noise, two sets of voltage amplifiers were connected in parallel to the sample, and the cross spectrum of the two signals was calculated as function of applied bias current.²² Detailed information regarding shot noise measurements and the extraction of the Fano factor can be found in the Supplemental Material.²⁰ We then apply our numerical method to extract the conduction channels from the measured values $F \pm \Delta F$, $G \pm \Delta G$. The transmission coefficients are calculated using $\Delta \tau = 0.005$ and a maximum of N = 6 channels, which is a valid high limit since the number of channels for a single-atom contact is limited by the number of atomic valence orbitals.¹⁰ In general, the analysis can be repeated for N + 1 channels to verify the validity of the results for N channels.

We start by examining the monovalent metals Ag and Au. For these metals, the conductance of a single atom is expected to be carried by one conduction channel, explained by the dominant contribution of a single s valence orbital.¹⁰ For each metal, shot noise measurements were performed on more than 600 distinct atomic contacts. Before each measurement, the metal wire is reformed up to a conductance of $70G_0$ and pulled apart to reach a new atomic configuration. Figures 2(a) and 2(b) show the distribution of F and G values measured on Ag and Au contacts, respectively. The results show a clear tendency to follow the minimum Fano factor curve (represented in both figures as a black line). At integer conductance values, the majority of measurements show a strong suppression of the Fano factor. This suppression is a clear signature for quantized conductance through fully transmitting channels.^{11,22} For both metals a full suppression can be observed at $1G_0$ and $2G_0$. However, while at $3G_0$ the Fano factor is strongly suppressed in the case of Ag, a deviation to slightly higher values is observed for Au.

The numerical analysis of the sets of data that appear in Figs. 2(a) and 2(b) provides the range of values for the transmission coefficients. The coefficients are calculated to account for the statistical spread of the data in the following way. First, the Fano factor values are binned by conductance



FIG. 2. (Color online) (a), (b) *F* and *G* values measured on an ensemble of 633 Ag (a) and 702 Au (b) atomic contacts. The experimental errors do not exceed $\Delta G < 0.015G_0$ and $\Delta F < 0.02$. Black line reflects the theoretical minimum Fano factor. (c), (d) Computed transmission ranges for $\tau_1 - \tau_4$ extracted from the data in (a) and (b), respectively. Black, red, blue, and cyan areas represent the transmission ranges for τ_1 , τ_2 , τ_3 , and τ_4 , respectively.

intervals of 0.04 G_0 . Then, for each bin, the values of F and ΔF used in Eqs. (1) and (2) are set to $F = (F_{\min} + F_{\max})/2$ and $\Delta F = (F_{\max} - F_{\min})/2$, where F_{\min} and F_{\max} are the minimum and maximum Fano factor measured within the conductance bin. This ensures that the computed τ_n^{\min} and τ_n^{\max} capture all the possible transmission coefficients that correspond to the Fano factor values within the relevant conductance bin.

Figures 2(c) and 2(d) display the distribution of τ_n as a function of conductance for Ag and Au, respectively. The colored areas show the possible values for τ_n accounting for both the statistical spread in the Fano factor and the uncertainty in the numerical calculation. The transmission coefficients calculated for Ag [Fig. 2(c)] show that the conduction channels fully open, one by one, as the conductance of the contact increases. Around half-integer conductance values (i.e., $1.5G_0$, $2.5G_0$, and $3.5G_0$) the spread in the transmission range increases as a result of the limited accuracy of our analysis at these conductance values (see Supplemental Material²⁰). The spread is lower near integer conductance values, indicating that the conductance is composed of fully open channels. In the case of Au, a clear tendency for sequential channel saturation is also observed up to $2.5G_0$; however, at higher conductance values this behavior is less pronounced. Altogether, this analysis clearly demonstrates for both noble metals that the conductance is composed of saturated conduction channels and, in the case of noninteger conductance, an additional partly transmitting channel.

The possibility for sequential saturation of conduction channels was suggested before to explain the observed shot noise¹¹ and conductance fluctuations²³ in monovalent metals,

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although the transmission coefficients were not obtained directly. Conversely, subgap measurements on Au contacts showed that when $G > 1G_0$ the conductance can be composed of several partly opened channels.^{10,24} The latter experiments were carried out by inducing superconductivity on thin Au layers placed on Al contacts using the proximity effect. The discrepancy from subgap measurements could be explained by the difficulties in fitting the *I-V* characteristics in the nonideal case of superconductivity induced by the proximity effect.²⁵ Note that for bare Al contacts our results are in good agreement with subgap measurements, as will be shown.

A theoretical treatment of the transmission coefficients for Ag and Au was performed by a combination of molecular dynamics simulations and tight-binding calculations.^{24,26,27} For both metals, a single channel contributing up to $1G_0$ is found in agreement with our results; however, the sequential saturation behavior is not reproduced and several partially opened channels can be found above $1G_0$. Interestingly, our results are in very good agreement with a description of free electrons with disorder, in which the atomic neck is modeled by a smooth constriction.^{28,29} This is a surprising observation since one would expect that the transmission coefficients will depend on the details of the atomic configuration, rather than only on the diameter of the smallest cross section.

In order to study the effect of the atomic configuration, the transmission coefficients were obtained simultaneously during gradual narrowing of atomic contacts subject to mechanical stretching. Figure 3(a) presents an example trace for Ag, showing the evolution of the conductance (top panel) and transmission coefficients (lower panels) as a function of contact elongation. During elongation, the conductance exhibits a series of plateaus, which are related to stable atomic configurations, separated by sudden jumps due to plastic deformation.³⁰ The decomposition to transmission coefficients shows that the conductance of each plateau consists of saturated channels accompanying up to one partly open channel. The jumps do not necessarily result in a reduction of the number of channels, as can be seen in the first jump between $3G_0$ to $2.2G_0$, which results from a decrease in the transmission of τ_3 . In the presented Au trace [Fig. 3(b)], the last plateau begins with conductance slightly higher than $1G_0$ that gradually decreases to $1G_0$ at 1.8 Å. Resolving the conductance in terms of channels provides insight into this observation; throughout the elongation the main channel (τ_1) is fully open while a second channel (τ_2) shows a tunneling-like exponential dependence on electrode displacement. This indicates that tunneling between neighboring atoms can contribute to the overall conductance. Thus, the channel resolution provides a means to distinguish between parallel tunneling channels and direct electronic transport through the atomic contact.

We now turn to study the *sp* metal Al, where the conductance of a single-atom contact is composed by three main channels.^{12,13} An example for an Al trace showing the evolution of the conduction channels under elongation of a single-atom contact is presented in Fig. 3(c). At the beginning of the trace, the conductance is mainly composed of three approximately equally distributed channels. As the contact is stretched, one channel increases significantly while the other two decrease. This is a typical behavior observed in 15 Al traces examined in this communication. The number



FIG. 3. (Color online) Conductance traces (black circles) and transmission coefficients of the different channels measured on Ag (a), Au (b), Al (c), and Pt (d) point contacts. Black, red, blue, and cyan error bars represent the possible transmission ranges for τ_1 , τ_2 , τ_3 , and τ_4 , respectively. The dashed red line in the top panel of (b) marks the value of $1G_0$ to better visualize the contribution of the secondary channels to the conductance.

of observed channels and their dependence on elongation are in very good agreement with previous experimental results obtained using subgap measurements.¹² In contrast to previous subgap measurements on Au contacts, in which the superconducting state was induced by the proximity effect, for pure Al contacts the comparison between the two experimental methods is more straightforward.³¹

Finally, we examine the conduction channels in atomic Pt contacts. Figure 3(d) shows an example for a conductance trace measured during the elongation of a single-atom constriction. After an elongation of 1 Å, the conductance shows a sudden drop from $2.5G_0$ to a semiplateau ranging between $(1-1.5)G_0$. Similar conductance drops were associated with a geometric reordering of the contact from a single apex atom to a dimer configuration.^{26,32} After the transition, the number of observed channels drops from 3-4 channels down to 2 channels, with a possible small contribution from other channels. A similar behavior is observed in more than 30 measured traces. In all traces a highly transmitting channel $0.7 \leq \tau_1 \leq 1$ is observed during the whole elongation process. Interestingly, the main channel is less affected during the conductance drop while the other channels decrease significantly. These observations are in accordance with theoretical calculations,^{26,33} which predict a dominant conduction channel associated with a hybridization of s, p_z , and d_{z^2} orbitals, and two less transmitting channels, dominated by contributions from d_{zx} and d_{yz} orbitals. The significant spherical symmetry of the main channel could be the reason for its relative insensitivity to the structural changes occurring with elongation.

To conclude, we have presented a numerical method for directly obtaining the conduction channels of low-dimensional conductors from shot noise measurements. We stress that the presented procedure is universal and can, in principal, be applied to any low-dimensional conductor that can be described by Landauer formalism. The conduction channels obtained for a large ensemble of Ag and Au contacts show a remarkable tendency to fully saturate one by one with increasing conductance, uncovering the free-electron nature of these monovalent metals. Channel-resolved traces further reveal that partly open channels can originate from parallel tunneling between neighboring atoms. These results demonstrate the duality of the free-electron and atomistic descriptions for monovalent atomic contacts. For Pt contacts, the experimentally obtained channels are in excellent agreement with atomistic-based theoretical calculations, allowing us to probe the sensitivity of the orbital contributions to structural changes. Overall, these results demonstrate that experimental determination of conduction channels allows a direct comparison between experiment and theory and illuminates the underlying mechanisms for electronic transport beyond standard conductance measurements.

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