



## Evidence for a $\nu = 5/2$ fractional quantum Hall nematic state in parallel magnetic fields

Yang Liu, S. Hasdemir, M. Shayegan, L. N. Pfeiffer, K. W. West, and K. W. Baldwin  
*Department of Electrical Engineering, Princeton University, Princeton, New Jersey 08544, USA*

(Received 25 February 2013; published 15 July 2013)

We report magnetotransport measurements for the fractional quantum Hall state at filling factor  $\nu = 5/2$  as a function of applied parallel magnetic field ( $B_{\parallel}$ ). As  $B_{\parallel}$  is increased, the  $5/2$  state becomes increasingly anisotropic, with the in-plane resistance along the direction of  $B_{\parallel}$  becoming more than 30 times larger than in the perpendicular direction. Despite the very large resistance anisotropy, the anisotropy ratio remains constant over a relatively large temperature range, yielding an energy gap which is the same for both directions. Our data are qualitatively consistent with a fractional quantum Hall *nematic* phase.

DOI: [10.1103/PhysRevB.88.035307](https://doi.org/10.1103/PhysRevB.88.035307)

PACS number(s): 73.43.Fj, 73.21.Fg, 73.43.Nq, 73.43.Qt

The origin and properties of the fractional quantum Hall state (FQHS) at the even-denominator Landau level (LL) filling factor  $\nu = 5/2$  (Ref. 1) have become of tremendous current interest. This is partly because the quasiparticle excitations of the  $5/2$  FQHS are expected to obey non-Abelian statistics<sup>2</sup> and be useful for topological quantum computing.<sup>3</sup> The stability and robustness of the  $5/2$  state, and its sensitivity to the parameters of the hosting two-dimensional electron system (2DES), are therefore of paramount importance. This stability has been studied as a function of 2DES density, quantum well width, disorder, and a parallel magnetic field ( $B_{\parallel}$ ) applied in the 2DES plane.<sup>4–18</sup> The role of  $B_{\parallel}$  is particularly important. It has been used to shed light on the spin polarization of the  $\nu = 5/2$  state, which in turn has implications for whether or not the state is non-Abelian.<sup>4,8,14</sup> But the application of  $B_{\parallel}$  in fact has more subtle consequences. It often induces anisotropy in the 2DES transport properties in the excited-state ( $N = 1$ ) LL and, at sufficiently large values of  $B_{\parallel}$ , leads to an eventual destruction of the  $\nu = 5/2$  FQHS,<sup>5,6,12</sup> replacing it by a *compressible*, anisotropic ground state. This anisotropic state is reminiscent of the nonuniform density, stripe phases seen at half-integer fillings in the higher ( $N > 1$ ) LLs.<sup>19,20</sup>

Here we study the  $\nu = 5/2$  FQHS as a function of  $B_{\parallel}$  in a very-high-quality 2DES. We find that the application of  $B_{\parallel}$  leads to a quick weakening of the  $5/2$  FQHS and a strong anisotropy in transport as the resistance along  $B_{\parallel}$  becomes much larger than in the perpendicular direction. Specifically, the resistance anisotropy ratio grows exponentially with  $B_{\parallel}$  up to  $B_{\parallel} \simeq 1.5$  T, where it reaches about 30. For  $B_{\parallel} > 1.5$  T, the anisotropy remains constant up to  $B_{\parallel} \simeq 3.6$  T, the  $B_{\parallel}$  above which the FQHS at  $\nu = 5/2$  disappears and the system turns into a compressible state. Remarkably, for  $B_{\parallel} \lesssim 3.6$  T and at low temperatures ( $T \lesssim 100$  mK), the resistances along the two in-plane directions monotonically decrease with decreasing temperature while the anisotropy ratio remains nearly constant. From the temperature dependence of the resistances, we are able to measure the energy gap ( $\Delta$ ) for the  $5/2$  FQHS along the two in-plane directions. Despite the enormous transport anisotropy,  $\Delta$  has the same magnitude along both directions. Our data therefore strongly suggest that the ground state of the system is an *anisotropic* FQHS. We discuss possible interpretation of such a ground state, including a FQH *nematic* phase.

In our sample, which was grown by molecular beam epitaxy, the 2DES is confined to a 30-nm-wide GaAs quantum well, flanked by undoped  $\text{Al}_{0.24}\text{Ga}_{0.76}\text{As}$  spacer layers and Si  $\delta$ -doped layers. The 2DES has a density of  $n = 3.0 \times 10^{15} \text{ m}^{-2}$  and a very high mobility,  $\mu \simeq 2500 \text{ m}^2/\text{Vs}$ . It has a very strong  $\nu = 5/2$  FQHS, with an energy gap of  $\Delta \simeq 0.4$  K, when  $B_{\parallel} = 0$ . The sample is 4 mm  $\times$  4 mm with alloyed InSn contacts at four corners. For the low-temperature measurements, we used a dilution refrigerator with a base temperature of  $T \simeq 20$  mK, and a sample platform which could be rotated *in situ* in the magnetic field to induce a parallel field component  $B_{\parallel}$  along the  $x$  direction (the  $[1\bar{1}0]$  crystal direction).<sup>21</sup> We use  $\theta$  to express the angle between the field and the normal to the sample plane, and denote the longitudinal resistances measured along and perpendicular to the direction of  $B_{\parallel}$  as  $R_{xx}$  and  $R_{yy}$ , respectively.

Figure 1 shows  $R_{xx}$  (red) and  $R_{yy}$  (black) measured as a function of the total magnetic field in the filling range  $2 < \nu < 3$ ; the Hall resistance  $R_{xy}$  is also shown (in blue) in Fig. 1(a). The traces in Fig. 1(a) were taken at  $\theta = 0$ , i.e., for  $B_{\parallel} = 0$ , and exhibit a very strong  $\nu = 5/2$  FQHS with an energy gap of  $\simeq 0.4$  K and an  $R_{xy}$  which is well quantized at  $0.4h/e^2$ . As seen in Figs. 1(b)–1(d), the application of  $B_{\parallel}$  causes a very pronounced anisotropy in the in-plane transport at and near  $\nu = 5/2$ , and  $R_{xx}$  becomes much larger than  $R_{yy}$ . At  $\theta = 26^\circ$ , e.g.,  $R_{xx}$  is about 30 times  $R_{yy}$ .<sup>23</sup> Note that in our experiments  $B_{\parallel}$  is applied along the  $x$  direction so that the “hard” axis we observe for in-plane transport is along the direction of  $B_{\parallel}$ . This is consistent with previous reports on  $B_{\parallel}$ -induced resistance anisotropy near  $5/2$ .<sup>5,6,12,21</sup>

In Fig. 2 we show the temperature dependence of  $R_{xx}$  and  $R_{yy}$  at  $\nu = 5/2$  for different values of  $\theta$ . In the temperature range  $50 < T < 100$  mK, both  $R_{xx}$  and  $R_{yy}$  are activated and follow the relation  $R \sim \exp(-\Delta/2k_B T)$ , where  $\Delta$  is FQH energy gap. At  $\theta = 0$   $R_{yy}$  is larger than  $R_{xx}$  by about a factor of 2. This anisotropy is caused by a mobility anisotropy, as the latter is often seen in very-high-mobility samples. With the application of a very small  $B_{\parallel}$  along the  $x$  direction ( $|\theta| \lesssim 5^\circ$ ), the anisotropy reverses so that  $R_{xx}$  exceeds  $R_{yy}$ . This trend continues with increasing  $\theta$  and, at  $\theta = 26^\circ$ ,  $R_{xx}$  becomes 30 times larger than  $R_{yy}$ . However, despite the very large anisotropy, both  $R_{xx}$  and  $R_{yy}$  remain activated and yield very similar values for  $\Delta$ .<sup>24</sup>

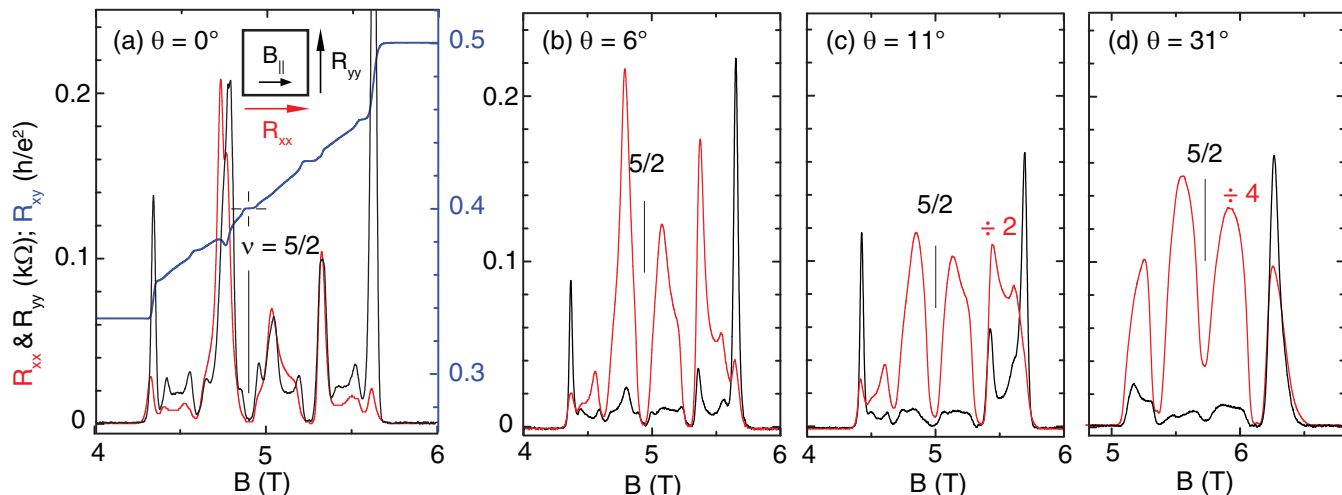


FIG. 1. (Color online) (a) Longitudinal resistances  $R_{xx}$  (red) and  $R_{yy}$  (black), and Hall resistance  $R_{xy}$  (blue) measured as a function of perpendicular magnetic field. The deep minima in  $R_{xx}$  and  $R_{yy}$ , as well as the well-quantized  $R_{xy}$  plateau, indicate a strong FQHS at  $\nu = 5/2$ . (b)–(d)  $R_{xx}$  and  $R_{yy}$  measured at finite tilting angles,  $\theta = 6^\circ$ ,  $11^\circ$ , and  $31^\circ$  are shown as a function of total magnetic field. The in-plane component of the magnetic field ( $B_{\parallel}$ ) is along the  $x$  direction. Note that the  $R_{xx}$  traces in (c) and (d) are divided by factors of 2 and 4. Strong transport anisotropy near  $\nu = 5/2$  grows as  $\theta$  increases. All traces were recorded at the base temperature of our measurements,  $T \simeq 20$  mK.

The transport energy gaps at  $\nu = 5/2$  measured as a function of  $B_{\parallel}$  up to  $\simeq 3.6$  T are summarized in Fig. 3. We denote the energy gaps deduced from the temperature dependence of  $R_{xx}$  and  $R_{yy}$  by  $\Delta_{xx}$  and  $\Delta_{yy}$ , respectively. It is clear in Fig. 3 that  $\Delta_{xx} \simeq \Delta_{yy}$ , despite the large anisotropy observed in  $R_{xx}$  and  $R_{yy}$ . In Fig. 3 we also plot the observed transport anisotropy as a function of  $B_{\parallel}$ . Here we used the values of  $R_{xx}$  and  $R_{yy}$  resistances at  $T = 60$  mK, converted them to *resistivities*  $\rho_{xx}$  and  $\rho_{yy}$  following the formalism presented in Ref. 25, and plot the ratio  $\alpha = \rho_{xx}/\rho_{yy}$ . As a function of  $B_{\parallel}$ , this ratio grows very quickly, approximately exponentially up to  $B_{\parallel} \simeq 1$  T, and then saturates at higher  $B_{\parallel}$ . The energy gaps  $\Delta_{xx}$  and  $\Delta_{yy}$ , however, exhibit a very steep drop at small  $B_{\parallel}$ , followed by a more gradual and monotonic decrease at higher  $B_{\parallel}$ . For  $\theta > 36^\circ$  ( $B_{\parallel} \gtrsim 3.6$  T) we cannot measure the gap for the  $5/2$  FQHS, as it becomes too weak.

The data presented above provide clear evidence for a strong  $\nu = 5/2$  FQHS whose in-plane transport is very anisotropic in the presence of applied  $B_{\parallel}$ . And yet its energy gap is the same for the two in-plane directions. These observations imply a  $\nu = 5/2$  FQHS whose transport is anisotropic at finite temperatures. A possible interpretation of our data is that we are observing a FQH *nematic* phase. It has been argued in numerous theoretical studies that such liquid-crystal-like FQH phases might exist in 2D systems where the rotational symmetry is broken.<sup>26–35</sup> Now in a 2DES with finite (non-zero) electron layer thickness, such as ours, it is known that  $B_{\parallel}$  breaks the rotational symmetry as it couples to the electrons' out-of-plane motion and causes an anisotropy of their real-space motion as well as their Fermi contours.<sup>36</sup> Recently it was demonstrated experimentally that such a  $B_{\parallel}$ -induced anisotropy is qualitatively transmitted to the quasiparticles at high magnetic fields, for example to the composite Fermions

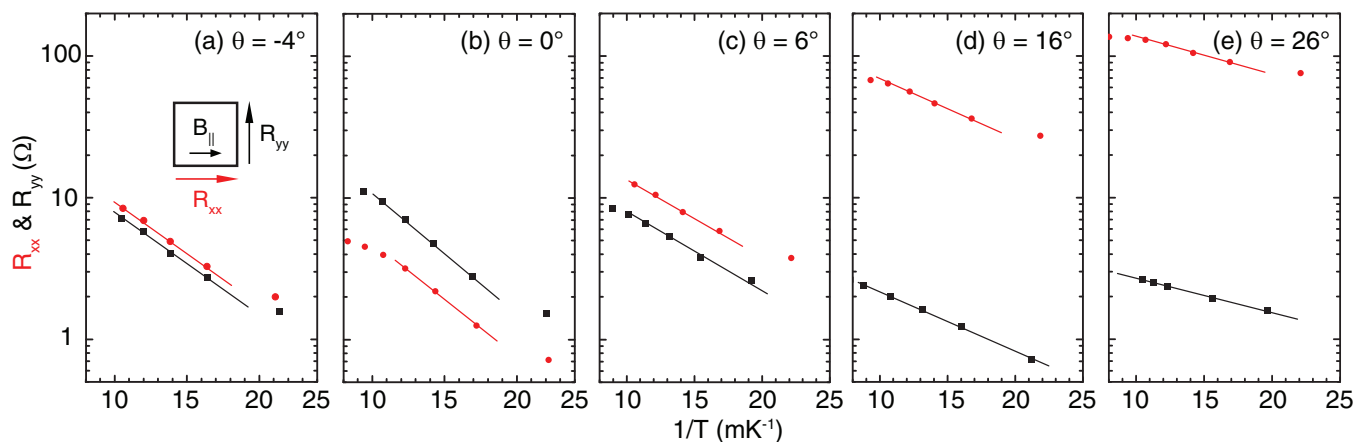


FIG. 2. (Color online) Temperature dependence of  $R_{xx}$  (red circles) and  $R_{yy}$  (black squares) at  $\nu = 5/2$ , measured at different tilting angles,  $\theta$ . The excitation gap deduced from the slopes of these plots decreases as  $\theta$  is increased, while the transport anisotropy increases.

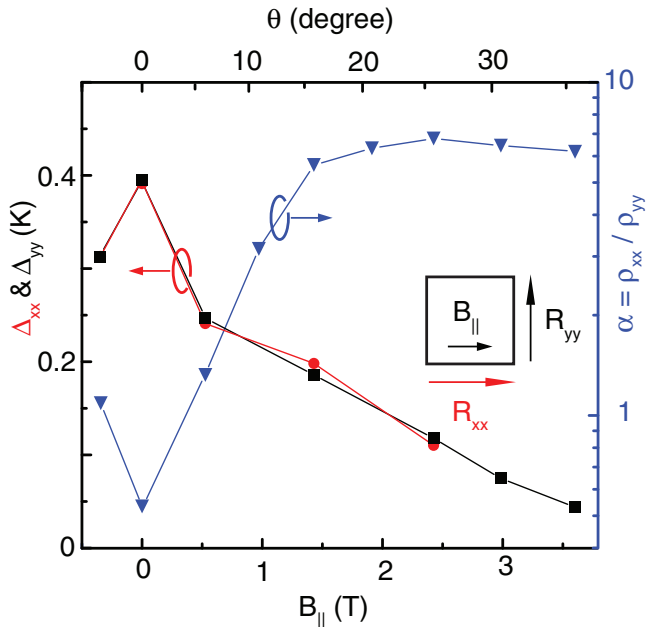


FIG. 3. (Color online) Measured excitation gaps,  $\Delta_{xx}$  (red circles) and  $\Delta_{yy}$  (black squares), are shown as a function of the in-plane magnetic field  $B_{||}$ .  $\Delta_{xx}$  and  $\Delta_{yy}$  nearly equal each other and decrease with increasing  $B_{||}$ . Also plotted (blue triangles) is the transport anisotropy factor  $\alpha$ , defined as the ratio between the resistivities  $\rho_{xx}$  and  $\rho_{yy}$ . Note the logarithmic scale on the right:  $\alpha$  grows exponentially with  $B_{||}$  at small  $B_{||}$ , and saturates at large  $B_{||} \gtrsim 1$  T.

near  $\nu = 1/2$  in the lowest LL.<sup>37</sup> It is therefore reasonable to expect that  $B_{||}$  also breaks the rotational symmetry in our 2DES in the  $N = 1$  LL and induces a FQH nematic phase at  $\nu = 5/2$ .

A FQH nematic phase was in fact recently proposed theoretically<sup>31</sup> to explain the experimental observations of Xia *et al.*<sup>38</sup> for another FQHS in the  $N = 1$  LL, namely, at  $\nu = 7/3$ . In the model of Ref. 31, the ground state is a FQHS but the dc longitudinal resistance at finite temperatures is anisotropic, as it reflects the anisotropic property of the thermally excited quasiparticles. The energy gap for the excitations, however, is predicted to be the same for  $R_{xx}$  and  $R_{yy}$ . These features are consistent with our experimental data. According to Mulligan *et al.*, the FQH nematic phase with anisotropic transport is stable only at very low temperatures.<sup>31</sup> As temperature is raised above a critical value that depends on the details of the sample's parameters and transport properties,  $R_{xx}$  should abruptly drop and  $R_{yy}$  suddenly rise so that they have the same value, signaling an isotropic FQH phase. Mulligan *et al.* also report that, thanks to the small symmetry-breaking  $B_{||}$  field, this finite-temperature transition might become rounded so that  $R_{xx}$  and  $R_{yy}$  approach each other more slowly at high temperatures (see Fig. 3 of Ref. 31). As mentioned above, our data at low temperatures are qualitatively consistent with the predictions of Ref. 31 for a FQH nematic state. At higher temperatures (Fig. 4), our data exhibit a downturn in  $R_{xx}$  as temperature is raised above  $\simeq 0.1$  K, signaling that transport is becoming less anisotropic, also generally consistent with Ref. 31 predictions. However, up to the highest temperatures achieved in our measurements ( $\simeq 0.2$  K, which is comparable to the  $\nu = 5/2$

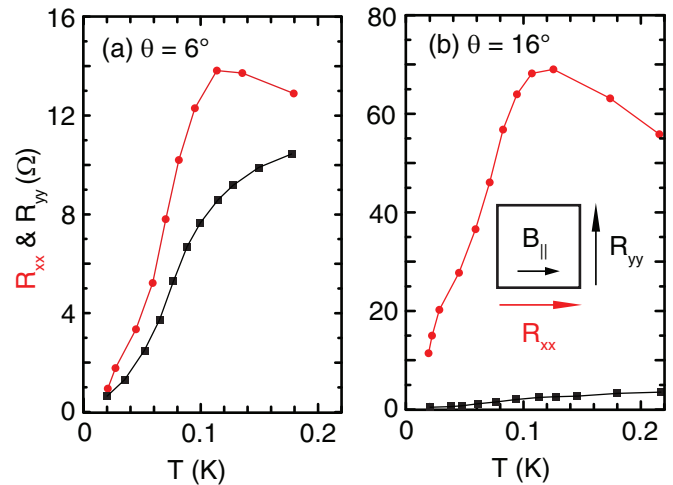


FIG. 4. (Color online)  $R_{xx}$  and  $R_{yy}$  are shown vs temperature for two values of tilt angle.  $R_{yy}$  monotonically increases with increasing temperature, while  $R_{xx}$  shows a downturn at high temperatures  $T \gtrsim 120$  mK, indicating a smaller anisotropy.

FQHS excitation gaps in our sample for  $\theta = 6^\circ$  and  $\theta = 16^\circ$ ), we do not see a transition to a truly isotropic state.<sup>39</sup>

While the above interpretation of our data based on a FQH nematic state is plausible, there might be alternative explanations. For example, it has been theoretically suggested that the low-energy charged excitations of the FQHSs in the  $N = 1$  LL have a very large size, as they are complex composite Fermions dressed by roton clouds.<sup>40</sup> Because of their large size, these excitations are prone to become anisotropic in the presence of  $B_{||}$ . Such anisotropy, even if small in magnitude, could lead to a much larger transport anisotropy of the quasiparticle excitations at finite temperatures, because this transport would involve hopping or tunneling of the quasiparticles between the localized regions.

To summarize, our magnetotransport measurements reveal that the application of a  $B_{||}$  leads to a  $\nu = 5/2$  FQHS, whose in-plane longitudinal resistance is highly anisotropic at low temperatures. The resistance anisotropy ratio remains constant over a relatively large temperature range, and the energy gap we extract from the temperature dependence of the resistances is the same for both directions. Our data are generally consistent with a FQH nematic phase, although other explanations might be possible. Regardless of the interpretations, our results attest to the very rich and yet not fully understood nature of the enigmatic  $\nu = 5/2$  FQHS.

We acknowledge support from the the National Science Foundation (DMR-1305691 and MRSEC DMR-0819860), and Moore and Keck Foundations. A portion of this work was performed at the National High Magnetic Field Laboratory, which is supported by National Science Foundation Cooperative Agreement No. DMR-1157490, the State of Florida, and the US Department of Energy. We thank R. Bhatt, J. K. Jain, D. Haldane, and Z. Papić for illuminating discussions, and E. Palm, S. Hannahs, J. H. Park, T. P. Murphy, and G. E. Jones for technical assistance.

- <sup>1</sup>R. L. Willett, J. P. Eisenstein, H. L. Stormer, D. C. Tsui, A. C. Gossard, and J. H. English, *Phys. Rev. Lett.* **59**, 1776 (1987).
- <sup>2</sup>G. Moore and N. Read, *Nucl. Phys. B* **360**, 362 (1991).
- <sup>3</sup>C. Nayak, S. H. Simon, A. Stern, M. Freedman, and S. Das Sarma, *Rev. Mod. Phys.* **80**, 1083 (2008).
- <sup>4</sup>J. P. Eisenstein, R. Willett, H. L. Stormer, D. C. Tsui, A. C. Gossard, and J. H. English, *Phys. Rev. Lett.* **61**, 997 (1988).
- <sup>5</sup>W. Pan, R. R. Du, H. L. Stormer, D. C. Tsui, L. N. Pfeiffer, K. W. Baldwin, and K. W. West, *Phys. Rev. Lett.* **83**, 820 (1999).
- <sup>6</sup>M. P. Lilly, K. B. Cooper, J. P. Eisenstein, L. N. Pfeiffer, and K. W. West, *Phys. Rev. Lett.* **83**, 824 (1999).
- <sup>7</sup>W. Pan, J. S. Xia, H. L. Stormer, D. C. Tsui, C. Vicente, E. D. Adams, N. S. Sullivan, L. N. Pfeiffer, K. W. Baldwin, and K. W. West, *Phys. Rev. B* **77**, 075307 (2008).
- <sup>8</sup>C. R. Dean, B. A. Piot, P. Hayden, S. Das Sarma, G. Gervais, L. N. Pfeiffer, and K. W. West, *Phys. Rev. Lett.* **100**, 146803 (2008); **101**, 186806 (2008).
- <sup>9</sup>H. C. Choi, W. Kang, S. Das Sarma, L. N. Pfeiffer, and K. W. West, *Phys. Rev. B* **77**, 081301 (2008).
- <sup>10</sup>J. Nuebler, V. Umansky, R. Morf, M. Heiblum, K. von Klitzing, and J. Smet, *Phys. Rev. B* **81**, 035316 (2010).
- <sup>11</sup>J. Shabani, Y. Liu, and M. Shayegan, *Phys. Rev. Lett.* **105**, 246805 (2010).
- <sup>12</sup>J. Xia, V. Cvicek, J. P. Eisenstein, L. N. Pfeiffer, and K. W. West, *Phys. Rev. Lett.* **105**, 176807 (2010).
- <sup>13</sup>A. Kumar, G. A. Csáthy, M. J. Manfra, L. N. Pfeiffer, and K. W. West, *Phys. Rev. Lett.* **105**, 246808 (2010).
- <sup>14</sup>C. Zhang, T. Knuuttila, Y. Dai, R. R. Du, L. N. Pfeiffer, and K. W. West, *Phys. Rev. Lett.* **104**, 166801 (2010).
- <sup>15</sup>W. Pan, N. Masuhara, N. S. Sullivan, K. W. Baldwin, K. W. West, L. N. Pfeiffer, and D. C. Tsui, *Phys. Rev. Lett.* **106**, 206806 (2011).
- <sup>16</sup>Y. Liu, D. Kamburov, M. Shayegan, L. N. Pfeiffer, K. W. West, and K. W. Baldwin, *Phys. Rev. Lett.* **107**, 176805 (2011).
- <sup>17</sup>G. Gamez and K. Muraki, [arXiv:1101.5856](https://arxiv.org/abs/1101.5856) [cond-mat].
- <sup>18</sup>N. Samkharadze, J. D. Watson, G. Gardner, M. J. Manfra, L. N. Pfeiffer, K. W. West, and G. A. Csáthy, *Phys. Rev. B* **84**, 121305 (2011).
- <sup>19</sup>M. P. Lilly, K. B. Cooper, J. P. Eisenstein, L. N. Pfeiffer, and K. W. West, *Phys. Rev. Lett.* **82**, 394 (1999).
- <sup>20</sup>R. R. Du, D. C. Tsui, H. L. Stormer, L. N. Pfeiffer, K. W. Baldwin, and K. W. West, *Solid State Commun.* **109**, 389 (1999).
- <sup>21</sup>We note that the  $B_{\parallel}$ -induced anisotropy at  $\nu = 5/2$  in 2DESs similar to ours, namely, those confined to GaAs quantum wells, is typically observed when  $B_{\parallel}$  is applied along the  $[1\bar{1}0]$  crystal orientation, but not when  $B_{\parallel}$  is along  $[110]$ ; see, e.g., Refs. 14 and 22. The origin of this anomalous behavior is not known.
- <sup>22</sup>C. Zhang, C. Huan, J. S. Xia, N. S. Sullivan, W. Pan, K. W. Baldwin, K. W. West, L. N. Pfeiffer, and D. C. Tsui, *Phys. Rev. B* **85**, 241302 (2012).
- <sup>23</sup>At large values of  $\theta$ , we could not reliably measure the Hall resistance in our sample, which has a van der Pauw geometry with a contact at each of the four corners. In such a geometry, it is not easy to measure the Hall resistance when the 2DES becomes very anisotropic. Similar problems have been discussed for measurements at  $\nu = 9/2$  and  $11/2$ , where stripe phases have been seen; see e.g., Ref. 5. The Hall resistance in principle can be measured more reliably in a patterned, Hall bar sample. But in our experience, when lithography is used to fabricate Hall bar geometry samples, the sample quality degrades; e.g., the FQHs exhibit smaller energy gaps compared to the unprocessed samples from the same wafer.
- <sup>24</sup>Some of the data points at the lowest temperatures in Fig. 2 are not included in the linear fits because the electron temperature starts to saturate.
- <sup>25</sup>S. H. Simon, *Phys. Rev. Lett.* **83**, 4223 (1999).
- <sup>26</sup>L. Balents, *Europhys. Lett.* **33**, 291 (1996).
- <sup>27</sup>K. Musaelian and R. Joynt, *J. Phys.: Condens. Matter* **8**, L105 (1996).
- <sup>28</sup>E. Fradkin and S. A. Kivelson, *Phys. Rev. B* **59**, 8065 (1999).
- <sup>29</sup>L. Radzihovsky and A. T. Dorsey, *Phys. Rev. Lett.* **88**, 216802 (2002).
- <sup>30</sup>M. M. Fogler, *Europhys. Lett.* **66**, 572 (2004).
- <sup>31</sup>M. Mulligan, C. Nayak, and S. Kachru, *Phys. Rev. B* **84**, 195124 (2011).
- <sup>32</sup>F. D. M. Haldane, *Phys. Rev. Lett.* **107**, 116801 (2011).
- <sup>33</sup>R.-Z. Qiu, F. D. M. Haldane, X. Wan, K. Yang, and S. Yi, *Phys. Rev. B* **85**, 115308 (2012).
- <sup>34</sup>B. Yang, Z. Papić, E. H. Rezayi, R. N. Bhatt, and F. D. M. Haldane, *Phys. Rev. B* **85**, 165318 (2012).
- <sup>35</sup>H. Wang, R. Narayanan, X. Wan, and F. Zhang, *Phys. Rev. B* **86**, 035122 (2012).
- <sup>36</sup>D. Kamburov, M. Shayegan, R. Winkler, L. N. Pfeiffer, K. W. West, and K. W. Baldwin, *Phys. Rev. B* **86**, 241302 (2012).
- <sup>37</sup>D. Kamburov, Y. Liu, M. Shayegan, L. N. Pfeiffer, K. W. West, and K. W. Baldwin, *Phys. Rev. Lett.* **110**, 206801 (2013).
- <sup>38</sup>J. Xia, J. P. Eisenstein, L. Pfeiffer, and K. West, *Nat. Phys.* **7**, 845 (2011).
- <sup>39</sup>It is worth contrasting our experimental data with those of Xia *et al.*,<sup>38</sup> which were taken at  $\nu = 7/3$ . Their data show an  $R_{xx}/R_{yy}$  anisotropy ratio which is typically small (less than about a factor of four) at high temperatures ( $T \gg 50$  mK). As the sample is cooled, near  $T \simeq 50$  mK,  $R_{xx}$  starts to increase while  $R_{yy}$  continues to decrease, and this trend continues down to the lowest achievable temperatures,  $T \simeq 15$  mK. Mulligan *et al.*<sup>31</sup> interpret  $T \simeq 50$  mK as the critical temperature below which the FQH nematic phase forms in the experiments of Ref. 38. Based on their theory, one would expect that both  $R_{xx}$  and  $R_{yy}$  should eventually decrease with decreasing  $T$  at the lowest temperatures and yield the same energy gap, but this is not seen in the temperature range of the experiments of Ref. 38.
- <sup>40</sup>A. C. Balram, Y.-H. Wu, G. J. Sreejith, A. Wójs, and J. K. Jain, *Phys. Rev. Lett.* **110**, 186801 (2013).