Defect engineering of BaSnO₃ for high-performance transparent conducting oxide applications

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The high cost and low abundance of indium has driven research to find In-free *n*-type transparent conducting oxides (TCOs). La-doped cubic perovskite BaSnO₃ has been reported to possess electron mobilities as high as $320 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for carrier concentrations of $8 \times 10^{19} \text{ cm}^{-3}$, comparable to the very best TCOs. To date, however, the origins of conductivity in this material have remained unclear. Here we study the defect chemistry of BaSnO₃ using a hybrid density functional theory approach, in order to understand how to control the *n*-type conductivity. We show that in undoped samples, native defects cannot cause high levels of *n*-type conductivity; however, adventitious H present in samples can act as shallow donors. By studying the effect of a range of donor dopants, we pinpoint ideal growth conditions and donor dopants for high-performance *n*-type BaSnO₃ samples.

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The combination of electrical conductivity and optical transparency in a single material gives transparent conducting oxides (TCOs) an important role in modern optoelectronic applications such as in solar cells, flat panel displays, and smart coatings.^{1–3} The current industry standard *n*-type TCO is In₂O₃:Sn (ITO) which demonstrates conductivities of $\sim 10^4$ S cm⁻¹, while retaining >90% transparency.³ Typically extrinsic donor doping is necessary for high-performance *n*-type TCO materials, and *p*-type behavior (hole stability) is thermodynamically unfavorable.^{4,5} The overwhelming demand for ITO, coupled with the low natural abundance of indium, has made indium an increasingly expensive commodity, which has led to a large research drive to replace ITO as the industry standard *n*-type TCO.^{6,7}

Perovskite structured oxides, with the formula *ABO*₃, are key materials in the field of "oxide electronics," possessing many diverse physical properties including high-transition-temperature superconductivity, optical transparency, ferro-electricity, piezoelectricity, and photocatalytic activity.⁸ The emergence of all-perovskite multilayer heterostructures has refocused interest on the development of perovskite materials with improved functionalities.^{9,10} Very recently, the transparent perovskite BaSnO₃ has been reported to possess electron mobilities comparable with the best TCOs when La doped.^{11–13}

Cheong and co-workers synthesized bulk single crystals of La-doped BaSnO₃ possessing a Hall mobility of 103 cm² V⁻¹ s⁻¹, with an *n*-type carrier concentration of ~8–10 × 10¹⁹ cm⁻³.¹¹ The lowest resistivity achieved by the authors was ~5.9 × 10⁻⁴ Ω cm (a conductivity of ~1690 S cm⁻¹) at room temperature, which is higher than the industry standard TCOs.¹ Previous attempts to donor-dope polycrystalline or epitaxially grown BaSnO₃ samples with La or Sb had only managed to produce carrier mobilities up to 0.69 cm² V⁻¹ s⁻¹,¹⁴ but these poor results were attributed to grain boundary contributions in the polycrystalline samples.¹¹

Kim *et al.* subsequently reported single-crystal La-doped BaSnO₃ with a mobility of $320 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for a carrier concentration of $8 \times 10^{19} \text{ cm}^{-3}$, the highest reported for *any* TCO.¹² The authors also reported a mobility of 70 cm² V⁻¹ s⁻¹ for epitaxial thin films at a doping level of $4.4 \times 10^{20} \text{ cm}^{-3}$. The resistance did not change significantly even after thermal

cycles up to 803 K in air, indicating extremely good oxygen stability. 12,13

In this Rapid Communication, we utilize hybrid density functional theory (DFT) to present the first analysis of the effect of intrinsic and extrinsic defects in BaSnO₃. We demonstrate that (i) native defects in the bulk cannot act as a source of shallow donor in this system meaning that undoped samples will be predominately insulating, and (ii) hydrogen impurities and extrinsic donor dopants such as La, Sb, or F will donate electrons to the conduction band, and are the source of the high conductivities reported experimentally. We discuss the doping behavior of BaSnO₃ for a range of growth environments, and provide a blueprint for optimum growth conditions for heavily doped samples.

Computational method. All DFT calculations were performed using the VASP code.¹⁵ Interactions between the core and valence electrons were described within the PAW method.¹⁶ The calculations were performed using the PBE¹⁷ exchange-correlation functional augmented with 25% Hartree-Fock exchange, producing the PBE0 functional.¹⁸ PBE0 has been successful in reproducing the structural and band gap data for Sn(IV) containing metal oxide systems.^{5,19} A plane wave cutoff of 400 eV and a k-point sampling of $6 \times 6 \times 6$ for the 5 atom unit cell of BaSnO₃ were used, with the ionic forces converged to less than 0.01 eVÅ⁻¹. The optical transition matrix elements, calculated following Fermi's golden rule, were used to construct the imaginary dielectric function and the corresponding optical absorption spectrum.²⁰ Defects were calculated in a $3 \times 3 \times 3$ (135) atom supercell with a $2 \times 2 \times 2$ Monkhorst-Pack special k-point grid, and all calculations were spin polarized.

The formation energy of a defect with charge state q is given by

$$\Delta H_{\rm f}({\rm D},q) = (E^{{\rm D},q} - E^{\rm H}) + \sum_{i} n_i (E_i + \mu_i) + q \left(E_{\rm Fermi} + \epsilon_{\rm VBM}^{\rm H} \right) + E_{\rm align} [q], \quad (1)$$

where $E^{\rm H}$ is the total energy of the host supercell and $E^{{\rm D},q}$ is the total energy of the defect-containing cell. Elemental reference energies E_i were obtained from calculations on the constituent elements in their standard states, e.g., $O_2(g)$, $F_2(g)$,

TABLE I. Table showing geometrical and electronic structure data for BaSnO₃ calculated using HSE06 and PBE0, and compared to known experiments. *a*, $d_{\text{Sn-O}}$, and $d_{\text{Ba-O}}$ are the lattice parameter and cation-anion interatomic distances, measured in Å, E_g^{ind} is the indirect band gap in eV, and E_g^{dir} is the direct band gap in eV.

| | HSE06 | PBE0 | Expt. |
|----------------------|-------|------|----------------------------|
| a | 4.13 | 4.13 | 4.12 ³⁰ |
| d _{Sn-O} | 2.07 | 2.07 | 2.06^{30} |
| d _{Ba-O} | 2.92 | 2.92 | 2.92 ³⁰ |
| E_g^{ind} | 2.49 | 3.22 | $\sim 3.12 - 3.26^{25,31}$ |
| E_g^{dir} | 2.96 | 3.68 | $\sim 3.40 - 3.50^{25,31}$ |

H₂(g), Ba(s), Sn(s), La(s), and Sb(s). E_{Fermi} represents the electron chemical potential, which ranges from the valence to conduction band edges. $\epsilon_{\text{VBM}}^{\text{H}}$ is the eigenvalue of the valence band maximum (VBM) of the bulk material. $E_{\text{align}}[q]$ is a correction that (i) accounts for the proper alignment of the electrostatic potential between the bulk and the defective supercells and (ii) accounts for the finite-size effects in the calculation of charged impurities, as outlined by Freysoldt *et al.*²¹ All charged defects were calculated by adding (subtracting) the correct amount of electrons to (from) the system, with compensation by the jellium background. The dielectric constant used for BaSnO₃ was 20.²² A correction for band filling by defect levels resonant in the conduction band was also included.²³

Geometry and electronic structure. BaSnO3 crystallizes in the cubic perovskite structure (space group Pm3m), in which the Sn sits on the corner of the cube, coordinated to six oxygen in a perfect octahedron, and each oxygen sits in the middle of a cube edge, coordinated to two Sn. Ba occupies the center of the cubic cell. The calculated structural and band gap data for BaSnO₃ are shown in Table I. For comparison we compare the PBE0 functional results to the screened exchange functional (HSE06²⁴) and to experiment. Both PBE0 and HSE06 reproduce the experimental lattice constants to within $\sim 0.25\%$. HSE06 underestimates the experimentally measured *indirect allowed*²⁵ band gap of $\sim 3.2 \text{ eV}$ by about 0.7 eV, whereas PBE0 yields band gap data in much closer agreement with experiment. The conduction band minimum (CBM) is situated at the Γ point, with the VBM situated at the *R* point. The CBM is dominated by Sn 5s character, and the VBM is composed of O 2p states. The conduction band of BaSnO₃ is found to be dispersive around the zone center, with an electron effective mass of $0.22m_e$. This value is consistent with the electron effective masses of other high-mobility oxides.^{26–29}

To understand the difference between the *fundamental* indirect allowed band gap and the direct allowed *optical* band gap, we have computed the optical absorption spectra for BaSnO₃, with the results presented in Fig. 1(b). The onset of optical absorption occurs at 3.68 eV, corresponding to the VB-CB separation at the Γ point, in good agreement with experimental values.^{25,31} Analysis of the symmetry-allowed direct VB-CB transitions confirms that the band gap at the Γ point corresponds to the optical band gap.

Thermodynamic limits. By varying the chemical potentials μ_i , we can simulate the effect of varying the partial pressures

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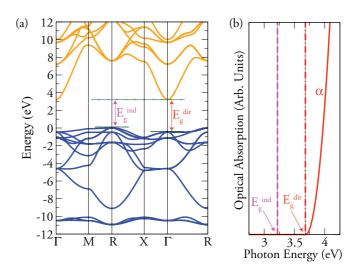


FIG. 1. (Color online) The PBE0 calculated (a) band structure for BaSnO₃, and (b) theoretical optical absorption onset of BaSnO₃.

experimentally, setting the conditions under which BaSnO₃ forms. In this way, we can determine the optimum conditions for *n*-type defect formation, within the constraint of the calculated enthalpy of the host: $\mu_{Ba} + \mu_{Sn} + 3\mu_O = \Delta H_f^{BaSnO_3}$. To avoid precipitation into solid elemental Ba, Sn, and gaseous O₂ we also require $\mu_{Ba} \leq 0, \mu_{Sn} \leq 0, \mu_O \leq 0$. The chemical potentials are further constrained by the decomposition of BaSnO₃ into binary compounds: $\mu_{Sn} + \mu_O \leq \Delta H_f^{SnO_2}, \text{ and } \mu_{Ba} + \mu_O \leq \Delta H_f^{BaO}$.

The PBE0 calculated accessible range of chemical potentials for BaSnO₃ is illustrated in Fig. 2, in a two-dimensional (μ_{Ba}, μ_{Sn}) plane, following the standard approach.^{32,33} The vertices of the stability triangle are formed from the host condition $(\mu_{Ba} + \mu_{Sn} + 3\mu_0 \le \Delta H_f^{BaSnO_3})$, giving the limits of Ba/Sn rich, Ba-poor, and Sn-poor environments. Taking into account the constraints imposed by the competing binary

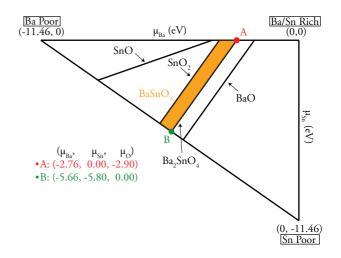


FIG. 2. (Color online) Illustration of the accessible (μ_{Ba} , μ_{Sn}) chemical potential range. The triangle vertices are determined by the formation enthalpy of BaSnO₃. Limits imposed by the formation of competing binary and ternary oxides result in the stable region shaded yellow. Environments A, B, C, D are indicated by the red, pink, green, and blue spheres, respectively.

oxides and the ternary Ba_2SnO_4 phase, the stable range of (μ_{Ba}, μ_{Sn}) for $BaSnO_3$ is shaded orange in Fig. 2. Within these boundaries, we explicitly considered two environments (A and B) as indicated in Fig. 2. A corresponds to Sn-rich, Ba-rich, and O-poor conditions, and is expected to be optimum for *n*-type defect formation, whereas B represents the Sn-poor/O-rich limit with Ba also poor, and is expected to favor the formation of *p*-type defects.

Under the different sets of conditions, the solubilities of extrinsic defect-related species are limited by the formation of secondary phases; i.e., $x\mu_{\rm M} + y\mu_{\rm O} \leq \Delta H_f^{\rm M_xO_y}$. We have therefore calculated the formation energy of La₂O₃, Sb₂O₅, and H₂O using the same calculation parameters as for bulk BaSnO₃. In the case of F, which substitutes on the O site, the solubility was determined by the formation of $\Delta H_f^{\rm SnF_4}$.

Defects considered. The native n-type defects considered in this study include the oxygen vacancy $(V_{\rm O})$, Sn on Ba antisite (Sn_{Ba}) , tin interstitial (Sn_i) , and barium interstitial (Ba_i) , while the *p*-type defects considered were the barium vacancy (V_{Ba}) , tin vacancy (V_{Sn}) , Ba on Sn antisite (Ba_{Sn}) , and oxygen interstitial (O_i) . In addition, H was incorporated in a number of lattice positions, namely hydrogen in an oxygen lattice site (H₀) and four different interstitial positions. The interstitial positions tested were the perfect interstitial site, two anion antibonding sites 1 Å from a lattice oxygen (one pointing towards a neighboring O atom, H_i^{AB1} , and one pointing towards a neighboring Ba, H_i^{AB2}), and one bond centered hydrogen, in the direction of the O-Sn bond (H_i^{BC}) , as illustrated in Fig. 3. As plausible *n*-type dopants, we have selected La and Sb as these have been routinely utilized as dopants in BaSnO₃, as well as previously untested F doping. Fluorine has long been known to be an excellent *n*-type dopant in SnO_2 .³⁴ La and Sb dopants have been considered on the Sn site (X_{Sn}) and the Ba site (X_{Ba}) , while F doping has been considered on the oxygen site (F_0) and as an interstitial (F_i) .

Intrinsic defects. Figures 4(a) and 4(b) show a plot of formation energy as a function of Fermi level for all intrinsic defects under our two chosen chemical potential environments. Under condition A, V_0 is the lowest energy intrinsic donor,

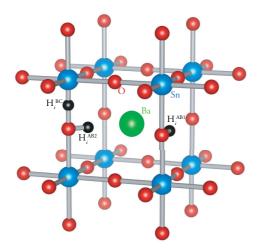


FIG. 3. (Color online) The geometry of H impurities in BaSnO₃. The Ba, Sn, O, and H atoms are represented by green, blue, red, and black spheres, respectively.

but is a negative-U defect, with the 2+/O transition level 0.37 eV below the CBM. It should be noted that this behavior is consistent with that of $V_{\rm O}$ in other wide band gap *n*-type TCOs, i.e., ZnO,^{23,35–37} SnO₂,³⁸ Ga₂O₃,³⁹ and In₂O₃.^{40,41} In all these cases, however, the 2+/0 transition level for the $V_{\rm O}$ is farther from the CBM than in the case of BaSnO₂; however, at 0.37 eV below the CBM V_O in BaSnO₃ is unlikely to provide high levels of conductivity in this system. Sn_{Ba} is the next most stable defect, and acts as an ultradeep donor with +1/0 and +2/+1 transitions levels 0.73 eV and 0.41 eV above the VBM, respectively. It should be noted that although "self-doping" by cation-on-cation antisites can dominate conductivity in other ternary TCOs,^{42,43} this is not the case for $BaSnO_3$. The Ba site is $BaSnO_3$ is so large that it can stabilize Sn in the 2+ charge state, and this is the origin of its deep donor nature. Sn_i and Ba_i both act as shallow donors, but are considerably higher in energy and are unlikely to play a large role in conductivity in BaSnO₃. The lowest energy native acceptor defect is the V_{Ba} , but it is too high in energy to compensate the $V_{\rm O}$ and the Sn_{Ba}.

Under oxygen-rich conditions (condition B), the native acceptor defects are much lower in energy and can compensate the native donors. The lowest energy acceptor defect is the oxygen interstitial; however, it relaxes from the ideal interstitial site towards a lattice oxygen, displacing it to form a peroxide (O-O dumbell-like) species, which we will now denote as O_{per} . An O_i on the perfect interstitial site is seen to be quite metastable relative to the Oper. This type of behavior has also been noted previously for other wide band gap oxides.^{26,29,44,45} Although the formation energy of O_i^{per} at \sim 2.40 eV under typical *p*-type conditions is much lower than that of the neutral formation energies of V_{Ba} , V_{Sn} , and Ba_{Sn} , its ionization levels are deep in the conduction band, indicating that it will not act as an effective charge compensating defect in BaSnO₃. V_{Ba} , V_{Sn} , and Ba_{Sn} are all deep acceptors, with V_{Ba} clearly the dominant acceptor defect for all growth conditions. Under metal-poor/O-rich conditions, the Fermi level will be trapped in the band gap, at the intersection of the V_0^{+2} and the V_{Ba}^{-2} . Therefore, under typical *p*-type conditions, BaSnO₃ will be an insulator, with *n*-type conductivity completely compensated. It also indicates that $BaSnO_3$ cannot be made p type by intrinsic defects under any conditions.

Extrinsic impurities. In Figs. 4(c) and 4(d) we present a plot of formation energy as a function of Fermi level for our chosen extrinsic defects in BaSnO₃ under our two chosen chemical potential environments. Under metal-poor/oxygen-rich conditions [Figs. 4(c)] we can see that the formation energies of H_0 , H_i^{AB1} , and H_i^{AB2} are very low, with all three acting as shallow donors in BaSnO₃. This is consistent with the reported shallow donor behavior of H in many wide band gap oxides.^{26,46–48} As BaSnO₃ has been used as a proton conductor,⁴⁹ H is very mobile in BaSnO₃, with experimentally measured activation energies of proton conduction of 0.35–0.40 eV.⁵⁰ La_{Ba}, Sb_{Sn}, and F_O are all shallow donors in this system, with F_O the most soluble defect, followed by La_{Ba} and then Sb_{Sn} . The 0/+1ionization level for Sb_{Sn} is just below the CBM, whereas the 0/+1 ionization levels for La_{Ba} and F_O are inside the CBM, which explains why La doping has been more successful at creating high-performance BaSnO₃ samples.¹¹⁻¹³ Sb_{Ba} is much higher in energy and will not play a role in determining

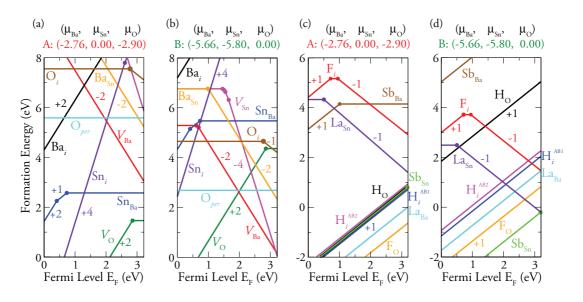


FIG. 4. (Color online) Formation energies for intrinsic defects [(a) and (b)] and extrinsic defects [(c) and (d)] in BaSnO₃ under the conditions chosen in Fig. 2. The slope of the lines denotes the charge state; the larger the slope, the bigger the charge state. The solid dots represent the transition levels $\epsilon(q/q')$.

conductivity in BaSnO₃ under O-poor conditions. It is a deep *single electron* donor, as once again the large Ba site stabilizes Sb in the +3 oxidation state. La_{Sn} has a formation energy of 4.32 eV and is a deep acceptor, but will not compensate La_{Ba} under these growth conditions. F_i is an amphoteric defect but is too high in energy to compensate the low-energy F_O , which indicates that F doping is a very viable alternative dopant to La for producing a high-performance *n*-type TCO. Hydrogen doping could also be used as a means to adjust the carrier density as it is in other TCOs.⁵¹

Under O-rich/metal-poor growth conditions [Fig. 4(d)], the formation energy of the H_O, F_O, H_i, and La_{Ba} are increased, as they are all strongly dependent on μ_O . The only shallow donor that becomes more stable under O-rich conditions is Sb_{Sn}, a trend that has also been reported for Sb-doped SnO₂.⁵² Under metal-poor conditions, however, it must be noted that the native acceptor defects will be dominant at the CBM, and so at the O-rich/metal-poor limit *n*-type conductivity could be compensated. Indeed we can clearly see that La_{Sn} will compensate La_{Ba} under these conditions. Thus to counteract the effect of compensation by native acceptors and La_{Sn}, care should be taken to produce La-doped samples grown at conditions that are not very metal-poor or very O-rich. F doping is not self-compensated by F_i formation under O-rich conditions, but will be compensated by native defect formation under metal-poor conditions.

Summary. We have demonstrated that none of the native impurities in BaSnO₃ can act as shallow defects, and that under O-rich conditions native *n*-type defects will be completely compensated by acceptor defects. Only the introduction of an extrinsic donor impurity can transform BaSnO₃ into a degenerate TCO, consistent with experimental reports.^{11,12} Adventitious hydrogen is shown to be a shallow donor when incorporated as interstitials and on the O site. We identify F doping as an excellent alternative donor dopant for high-performance TCO applications, and suggest that growth conditions which are not fully O-rich are necessary to limit-self compensation in this system. It is expected that these results will serve as a guide to experimentalists attempting to optimize BaSnO₃ and related perovskites for high-performance TCO applications.

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