

Electronic model for self-assembled hybrid organic/perovskite semiconductors: Reverse band edge electronic states ordering and spin-orbit coupling

J. Even,^{1,*} L. Pedesseau,¹ M.-A. Dupertuis,² J.-M. Jancu,¹ and C. Katan^{1,3}

¹*Université Européenne de Bretagne, INSA, FOTON, UMR 6082, 35708 Rennes, France*

²*Ecole Polytechnique Fédérale de Lausanne (EPFL), Laboratory of Quantum Optoelectronics, CH-1015 Lausanne, Switzerland*

³*CNRS, Institut des Sciences Chimiques de Rennes, UMR 6226, 35042 Rennes, France*

(Received 10 July 2012; revised manuscript received 13 September 2012; published 5 November 2012)

Based on density functional theory, the electronic and optical properties of hybrid organic/perovskite crystals are thoroughly investigated. We consider the monocrystalline 4F-PEPI as material model and demonstrate that the optical process is governed by three active Bloch states at the Γ point of the reduced Brillouin zone with a reverse ordering compared to tetrahedrally bonded semiconductors. Giant spin-orbit coupling effects and optical activities are subsequently inferred from symmetry analysis.

DOI: [10.1103/PhysRevB.86.205301](https://doi.org/10.1103/PhysRevB.86.205301)

PACS number(s): 71.20.-b

I. INTRODUCTION

Semiconductor optoelectronic devices are based on properties of direct band-gap crystals in the zinc-blende^{1,2} and wurtzite³ phases related to p -like valence-band states and s -like conduction-band states. Nowadays there is a growing interest in the development of hybrid inorganic-organic architectures that could enable superior optical functions and greatly enhanced device performances. Among them, self-assembled hybrid organic layered perovskites (SAHOP) structures are emerging as a powerful class of two-dimensional (2D) materials due to their broad technological potentialities for nanophotonics and nanoelectronics⁴⁻⁹ through perfectly controlled growth and organization. Both chemical insight and optical properties of various SAHOP are well documented. In particular, it has been shown that the optical spectra of lead halide organic semiconductors can be easily tailored as function of the organic group, thus improving luminescence efficiencies and/or tuning the emission wavelength.¹⁰ These systems exhibit extremely large exciton binding energies¹¹ as well as sharp resonances for the biexciton¹² and triexciton¹³ transitions. Excitonic switching and Peierls transitions have also been reported.¹⁴ Furthermore, SAHOP based on lead halides have recently demonstrated enhanced nonlinear optical properties in microcavities,^{7,8} ascribed to strong electro-optical couplings. However, manufacturing SAHOP microcavities is a challenging task because divergent technologies have to be accommodated.⁸ Besides, the underlying mechanism behind the optical process is poorly understood. Indeed, existing modeling of the optical properties and carrier injection is still scanty and does not capture the subtle interplay between the organic sheets and the semiconductor layer. Available theoretical studies either give a general description of the electronic band structure, limited to the inorganic 2D lattices, mostly using density functional theory (DFT)¹⁵ or focus on the excitonic coupling using effective parameters for the carrier dispersion and dielectric confinement.¹⁶ This work aims at bridging over this lack by means of a thorough description of the relevant electronic states and corresponding optical selection rules of a SAHOP material model based on 4F-PEPI^{8,17} ($[\text{pFC}_6\text{H}_5\text{C}_2\text{H}_4\text{NH}_3]_2\text{PbI}_4$).

II. MODEL

Our study is performed by using the DFT implementation available in the ABINIT package,¹⁸ with the PBE gradient correction for exchange-correlation¹⁹ and relativistic, norm-conserving, separable, dual-space Gaussian-type pseudopotentials of Goedecker, Teter, and Hutter for all atoms.²⁰ The electronic wave functions are expanded onto a plane-wave basis set with an energy cutoff of 950 eV and a $1 \times 4 \times 4$ Monkhorst-Pack grid is used for reciprocal space integration. The spin-orbit coupling (SOC) interaction is taken into account. Although numerous SAHOP systems with lead-halides have been studied, only a few related crystallographic structures are known precisely. In fact, growth of monocrystals for x-ray diffraction is difficult because of the lattice disorder and strain induced by the organic molecule that plays a fundamental role in the dielectric confinement. In a few cases, the cation packing is compatible with the inorganic framework, made of corner-shared PbX_6 octahedra ($X = \text{Cl}, \text{Br}, \text{I}$), leading to a perfectly ordered 2D system built on a single crystal hybrid organic perovskite (SCHOP). This is the case of 4F-PEPI with a monoclinic unit cell¹⁷ as shown in Fig. 1. Experimental lattice parameters (transformed to $P21/c$: $a = 16.7 \text{ \AA}$, $b = 8.6 \text{ \AA}$, $c = 8.8 \text{ \AA}$, $\beta = 110^\circ$) and atomic positions¹⁹ were used for the DFT calculations with C-H and N-H bond length fixed to 1.089 and 1.008 Å , respectively. As x-ray diffraction pattern of spin-coated films of 4F-PEPI lead to the same interlayer spacing (16.7 Å),¹⁷ the SCHOP 4F-PEPI is believed to offer a good reference framework to investigate the electronic and optical properties of its SAHOP counterpart.

III. RESULTS AND DISCUSSIONS

Figure 2 shows the band structure of monocrystalline 4F-PEPI with and without the spin-orbit interaction. No energy dispersion occurs along the Γ - X direction (characterizing the stacking axis in real space), which is an inherent consequence of the dielectric mismatch between PbI_4 and the organic sheet. As a result, the density of states close to the band gap exhibits a reduced 2D dimensionality in connection with the observed 2D character of excitons in the SAHOP counterpart.¹¹

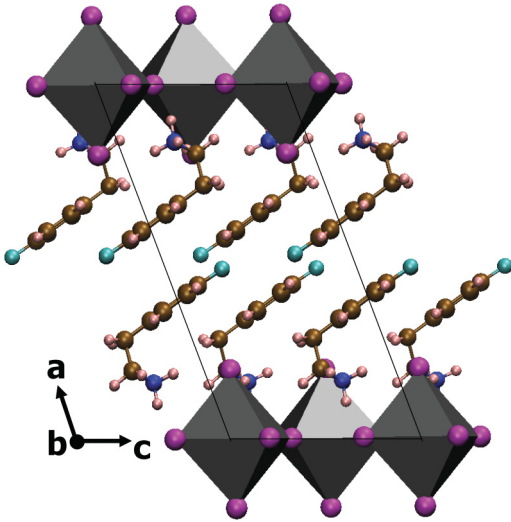


FIG. 1. (Color online) Overview of the crystal structure of 4F-PEPI ($[\text{pFC}_6\text{H}_5\text{C}_2\text{H}_4\text{NH}_3]_2\text{PbI}_4$).

The DFT electronic structure also reveals a direct band-gap character in agreement with the observed luminescence at room temperature.^{8,17} The fundamental transitions with and without SOC are 1.2 and 2.0 eV, respectively, to be compared to the measured value of 2.35 eV. The band gap is known to be underestimated in DFT ground state computation. This deficiency can be corrected by including many-body effects (GW self-energy correction for the band gap and Bethe Salpeter equation resolution for the exciton) but such calculations are beyond available computational resources for large systems. Despite this shortcoming, the overall conclusions related to the energy band dispersions and symmetries are reliable and can help to build accurately semiempirical Hamiltonians (e.g., in $k \cdot p$ theory and/or tight-binding approximation) where detailed information of Bloch states and selection rules are required. Similar conclusions can be drawn from the electronic band structure (Fig. 3) of the

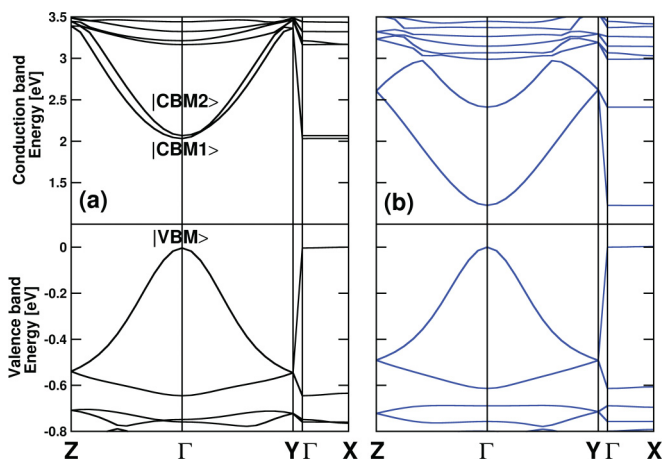


FIG. 2. (Color online) Electronic band structure of 4F-PEPI (a) without and (b) with the spin-orbit coupling interaction calculated by the density functional theory. The energy levels are referenced to the valence band maximum.

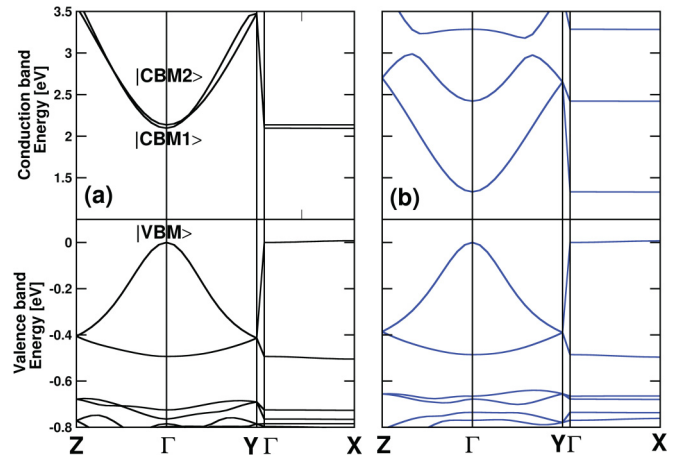


FIG. 3. (Color online) Electronic band structure of $[\text{C}_5\text{H}_{11}\text{NH}_3]_2\text{PbI}_4$ (a) without and (b) with the spin-orbit coupling interaction calculated by the density functional theory. The energy levels are referenced to the valence band maximum.

monoclinic crystal of $[\text{C}_5\text{H}_{11}\text{NH}_3]_2\text{PbI}_4$. It is a representative member of a large SCHOP and SAHOP family with alkane chains in the organic layer.^{14,16,21,22}

In the first approximation, the optical absorption near the band edge can be modeled without SOC [Fig. 2(a)] by three active Bloch states at the Γ point: A nondegenerate level for the valence-band maximum (VBM) and two nearly doubly degenerate levels for the conduction-band minimum (CBM). The associated wave functions are represented for 4F-PEPI in the bc^* plane in Fig. 4.

The VBM wave function is real and confined into the PbI_4 lattice and consists of antibonding hybridizations of Pb 6s and I 5p orbitals. It is associated with the nonpolar irreducible representation B_g of the point group C_{2h} . B_g is related to the twofold helical axis parallel to PbI_4 planes and transforms under $E_{1/2g}$ into the double group.²³ This twofold axis is a direct outcome of the particular stacking of the organic molecules and does not provide for the VBM states the expected A_g character. The in-plane energy dispersion of VBM is found as large and almost isotropic in the entire Brillouin zone [Figs. 2(a) and 3(a)], which further evidences the s character of the wave functions related to the inorganic semiconductor. The $|S\rangle$ symbol is proposed for SCHOP in this work (Fig. 4) to represent the Bloch state of the VBM, by analogy to CBM in conventional semiconductors.¹⁻³ A

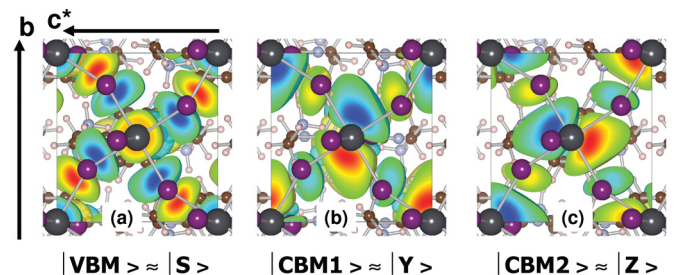


FIG. 4. (Color online) Electronic wave functions of the valence band maximum VBM and the first two excited states CBM1 and CBM2 as represented in the bc^* plane.

significant mixing with the molecular electronic states is observed only for the lower lying electronic states. In SAHOP structures, a crystal-field splitting Δ_{cr} should appear owing to the structural anisotropy between parallel to and normal to the stacking axis. It is associated with the dielectric confinement but also to the nonbonding of the iodine p orbitals along the a axis. Neglecting spin-orbit coupling, Δ_{cr} in 4F-PEPI will split the threefold-degenerate p -derived states into a nondegenerate level and a nearly doubly degenerate one. It is clearly evidenced in the conduction band structure [Figs. 2(a) and 3(a)] where the two first excited Bloch states, namely CBM1 and CBM2, are real and almost degenerated at the Γ point with an energy splitting of about 35 meV for 4F-PEPI. CBM1 and CBM2 correspond, respectively, to the irreducible polar representations B_u and A_u for 4F-PEPI of group C_{2h} resulting in almost in-plane perpendicular “ p ”-like states. As seen in Fig. 4, their wave functions are mainly distributed in the surrounding of the Pb shell. The $|Y\rangle$ and $|Z\rangle$ symbols are proposed for SCHOP in this work (Fig. 4), to represent the Bloch states of the CBM, by analogy to VBM in conventional semiconductors.¹⁻³ We calculate a crystal field of 1 eV that corresponds to the energy spacing between $(CBM1 + CBM2)/2$ and CBM3, the latter state displays a nonbonding character of iodine p orbitals. Contrarily to the valence band maximum, the effect of the spin-orbit interaction is huge at the conduction band minimum leading to a large SO splitting Δ_{SO} between the two first conduction states. This is a direct consequence of the s and p symmetries in the ground and excited wave functions. Moreover, the CBM1 and CBM2 wave functions are mixed by the SOC because B_u and A_u transform into the same irreducible representation $E_{1/2u}$ of the double group.²³ The DFT calculation gives $\Delta_{SO} = 1.2$ eV and this concurs with the experimental value of 0.966 eV of an equivalent SAHOP.²⁴

For optics, it is noteworthy that nonbonding electrons occur in our calculations at very high energies above the CBM and consequently are not involved in the excitation process. The DFT fundamental transition displays a nearly perfect transverse electric (TE) character in agreement with experimental results on SAHOP.¹⁶ It is similar to conventional zinc-blende quantum wells¹⁻³ with D_{2d} point symmetry or wurtzite bulk compounds with C_{6v} point symmetry. Symmetry and ordering of the Bloch states are however different for SCHOP. In 4F-PEPI, the organic layer stacking may yield small deviations from in-plane spectral activity. In order to get insight into the optical process, we have calculated without SOC the dipolar matrix elements between the first valence and conduction band states as defined by $M_{VBM,CBMj} = |\langle \psi_{VBM} | -i\hbar \frac{\partial}{\partial x_i} | \psi_{CBMj} \rangle|$, where x_i represents the crystal axis and j the two first excited levels. Figure 5(a) shows the polar plot of $M_{VBM,CB1}$ and $M_{VBM,CB2}$ in the bc plane. As expected from symmetry analysis, optical strengths of $M_{VBM,CB1}^2$ (taken as reference) and $M_{VBM,CB2}^2$ are maximum for light polarized parallel and perpendicular to the b^* axis, respectively. Figure 5(b) shows that $M_{VBM,CB2}$ is maximum along the c axis perpendicular to the perovskite layers (a^* direction). In analogy to tetrahedrally bonded semiconductors, one can define the Kane matrix element¹⁻³ $P_j = \frac{\hbar M_{VBM,CBMj}}{m_e}$ and corresponding energy $E_{pj} = \frac{2m_e p^2}{\hbar^2}$. For 4F-PEPI, the mean

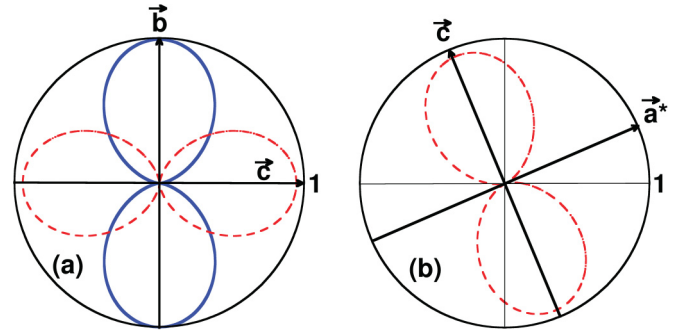


FIG. 5. (Color online) Dependence of the optical strengths $M_{VBM,CBj}^2$ of 4F-PEPI on the direction of the light polarization for the VBM-CBM1 (solid line) and VBM-CBM2 (dotted lines) transitions. The value of $M_{VBM,CB1}^2$ along the b axis is taken as reference both (a) in the bc plane and (b) in the plane perpendicular to the b axis.

value of E_{p1} is of about 5.5 eV and this explains the robustness of optoelectronic properties in SAHOP materials. Indeed, E_p amounts typically to 20 eV² for III-V semiconductors which are however characterized by extended Wannier-Mott excitons where binding energies are of few meV. Conversely, it has been demonstrated in SAHOP systems, excitons strongly localize in the inorganic layers constituted of PbX_6^{4-} octahedra due to the dielectric confinement,^{12,16} thus leading to very large binding energies of few hundreds of meV. Both the sizable E_p and exciton binding energy cooperatively contribute to generate appealing optical responses in SAHOP. Moreover, the optical anisotropy is small as shown by the ratio of Kane energies in 4F-PEPI: $E_{p2}/E_{p1} = 95\%$. As a consequence, the TE character of fundamental transition in a 4F-PEPI crystal is enforced. It has been clearly demonstrated¹⁶ in another

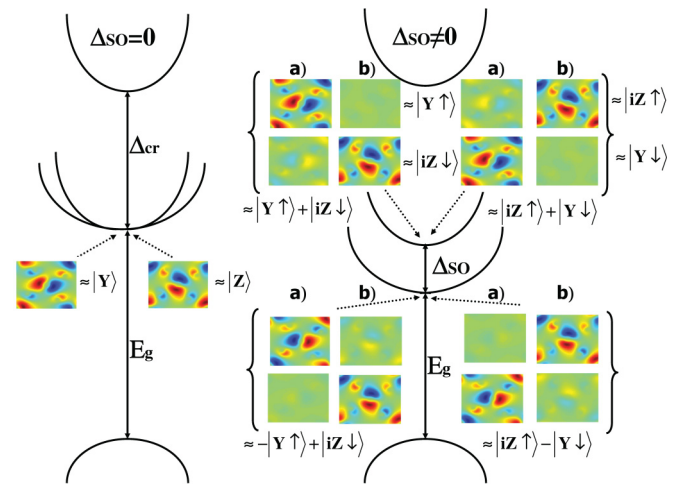


FIG. 6. (Color online) Schematic representation of SAHOP electronic band diagram without ($\Delta_{SO} = 0$, left) and with ($\Delta_{SO} \neq 0$, right) the spin-orbit coupling interaction Δ_{SO} . Δ_{cr} represents the anisotropy of the crystal field. The (a) real and (b) imaginary parts of the complex spinorial components of the CBM1 and CBM2 states are represented for 4F-PEPI (the spin up component is on top of the spin down component). The section plane and color code used for wave function representation are the same as the ones of Fig. 4. The conclusion concerning optical in-plane isotropy (Fig. 5) is not changed by the inclusion of the spin-orbit interaction.

SCHOP $[(C_{10}H_{21}NH_3)_2PbI_4]$ materials but it is expected to be a general property of the SCHOP family. A similar behavior is also anticipated for SAHOP counterparts and analogs, the TE character being further enhanced by the orientational disorder introduced by the organic layer, as observed in smectic liquid crystals.

Finally, a schematic representation of the SAHOP electronic band diagram without ($\Delta_{SO} = 0$, left) and with ($\Delta_{SO} \neq 0$, right) SOC is proposed in Fig. 6. This diagram is analogous to the one of III-V semiconductors in würtzite³ but with a reverse band edge electronic states ordering. The $|Y\rangle$ (CBM1) and $|Z\rangle$ (CBM2) real wave functions without SOC (left part of Fig. 5) are mixed by the SOC (right part of Fig. 6) into real and imaginary parts of the complex spinorial CBM components. The resulting complex spinorial components (for example: $|Y \uparrow\rangle + |iZ \downarrow\rangle$) in Fig. 6) can be predicted on the basis of a symmetry analysis of the Hamiltonian with and without the SOC effect, but this development analogous to the ones in conventional semiconductors is beyond the scope of the present work.

IV. CONCLUSION

In summary, based on DFT calculations and symmetry analysis of the Bloch states, the ordering of band edge states and the optical activity including Kane's energy of a prototype SCHOP crystal have been investigated. The significant value of the Kane's energy associated with the large excitonic binding energy reported for the corresponding SAHOP¹¹ account for the attractive optical responses evidenced in this class of hybrid materials. Additional insight can be gained from a $k \cdot p$ model starting from symmetry properties of the Bloch states which can efficiently model excitonic and spin-orbit couplings.

ACKNOWLEDGMENTS

This work was performed using HPC resources from GENCI-CINES/IDRIS Grant 2012-c2012096724. The work is supported by Agence Nationale pour la Recherche (PEROCAI project ANR-10-04). We gratefully acknowledge Professor M. Rikukawa and Dr. Y. Takeoka for providing unpublished atomic positions of 4F-PEPI.¹⁷

*jacky.even@insa-rennes.fr

¹E. O. Kane, *Semiconductors and Semimetals*, edited by R. K. Willardson and A. C. Beer (Academic, New York, 1966), Vol. 1, Chap. 3.

²S. Chuang, *Physics of Optoelectronic Devices*, edited by J. W. Goodman (Wiley, New York, 1995).

³S. L. Chuang and C. S. Chang, *Phys. Rev. B* **54**, 2491 (1996).

⁴D. B. Mitzi, S. Wang, C. A. Field, C. A. Chess, and A. M. Guloy, *Science* **267**, 1473 (1995).

⁵J. Ishi, H. Kunugita, K. Ema, T. Ban, and T. Kondo, *Appl. Phys. Lett.* **77**, 3487 (2000).

⁶A. Kojima, K. Teshima, Y. Shirai, and T. Miyasaka, *J. Am. Chem. Soc.* **131**, 6050 (2009).

⁷G. Lanty, A. Bréhier, R. Parashkov, J. S. Lauret, and E. Deleporte, *New J. Phys.* **10**, 065007 (2008).

⁸Y. Wei, J.-S. Lauret, L. Galmiche, P. Audebert, and E. Deleporte, *Opt. Express* **20**, 10399 (2012).

⁹I. Koutselas, P. Bampoulis, E. Maratou, T. Evagelinou, G. Pagona, and G. C. Papavassiliou, *J. Phys. Chem. C* **115**, 8475 (2011).

¹⁰S. Zhang, G. Lanty, J. S. Lauret, E. Deleporte, P. Audebert, and L. Galmiche, *Acta Mater.* **57**, 3301 (2009).

¹¹X. Hong, T. Ishihara, and A. V. Nurmikko, *Phys. Rev. B* **45**, 6961 (1992).

¹²Y. Kato, D. Ichii, K. Ohashi, H. Kunugita, K. Ema, K. Tanaka, T. Takahashi, and T. Kondo, *Solid State Commun.* **128**, 15 (2003).

¹³M. Shimizu, J. I. Fujisawa, and T. Ishihara, *Phys. Rev. B* **74**, 155206 (2006).

¹⁴K. Pradeesh, J. J. Baumberg, and G. V. Prakash, *Appl. Phys. Lett.* **95**, 173305 (2009).

¹⁵S. Sourisseau, N. Louvain, W. Bi, N. Mercier, D. Rondeau, F. Boucher, J.-Y. Buzaré, and C. Legein, *Chem. Mater.* **19**, 600 (2007).

¹⁶T. Ishihara, J. Takahashi, and T. Goto, *Phys. Rev. B* **42**, 11099 (1990).

¹⁷K. Kikuchi, Y. Takeoka, M. Rikukawa, and K. Sanui, *Current Appl. Phys.* **4**, 599 (2004).

¹⁸X. Gonze, B. Amadon, P. M. Anglade, J. M. Beuken, F. Bottin, P. Boulanger, F. Bruneval, D. Caliste, R. Caracas, M. Cote, T. Deutsch, L. Genovese, Ph. Ghosez, M. Giantomassi, S. Goedecker, D. R. Hamann, P. Hermet, F. Jollet, G. Jomard, S. Leroux, M. Mancini, S. Mazevet, M. J. T. Oliveira, G. Onida, Y. Pouillon, T. Rangel, G. M. Rignanese, D. Sangalli, R. Shaltaf, M. Torrent, M. J. Verstraete, G. Zerah, and J. W. Zwanziger, *Comput. Phys. Commun.* **180**, 2582 (2009).

¹⁹J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **77**, 3865 (1996).

²⁰C. Hartwigsen, S. Goedecker, and J. Hutter, *Phys. Rev. B* **58**, 3641 (1998).

²¹A. Lemmerer and D. G. Billing, *Dalton Trans.* **41**, 1146 (2012).

²²D. G. Billing and A. Lemmerer, *Acta Crystallogr. Sect. B* **63**, 735 (2007).

²³S. L. Altmann and P. Herzig, *Point-Group Theory Tables* (Clarendon, Oxford, 1994).

²⁴T. Kataoka, T. Kondo, R. Ito, S. Sasaki, K. Uchida, and N. Miura, *Phys. Rev. B* **47**, 2010 (1993).