Physical properties of transparent perovskite oxides (Ba,La)SnO₃ with high electrical mobility at room temperature

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(Received 29 June 2012; published 19 October 2012)

Transparent electronic materials are increasingly in demand for a variety of optoelectronic applications, ranging from passive transparent conductive windows to active thin-film transistors. BaSnO₃ is a semiconducting oxide with a large band gap of more than 3.1 eV. Recently, we discovered that BaSnO3 doped with a few percent of La exhibits an unusually high electrical mobility of 320 cm² V⁻¹ s⁻¹ at room temperature and superior thermal stability at high temperatures [H. J. Kim et al., Appl. Phys. Express 5, 061102 (2012)]. Following that paper, here, we report various physical properties of (Ba,La)SnO₃ single crystals and epitaxial films including temperature-dependent transport and phonon properties, optical properties, and first-principles calculations. We find that almost doping-independent mobility of $200-300 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ is realized in the single crystals in a broad doping range from 1.0×10^{19} to 4.0×10^{20} cm⁻³. Moreover, the conductivity of $\sim 10^4$ Ω^{-1} cm⁻¹ reached at the latter carrier density is comparable to the highest value previously reported in the transparent conducting oxides. We attribute the high mobility to several physical properties of (Ba,La)SnO₃: a small effective mass coming from the ideal Sn-O-Sn bonding in a cubic perovskite network, small disorder effects due to the doping away from the SnO₆ octahedra, and reduced carrier scattering due to the high dielectric constant. The observation of the reduced mobility of ~70 cm² V⁻¹ s⁻¹ in the epitaxial films is mainly attributed to additional carrier scattering due to dislocations and grain boundaries, which are presumably created by the lattice mismatch between the substrate SrTiO₃ and (Ba,La)SnO₃. The main optical gap coming from the charge transfer from O 2p to Sn 5s bands in (Ba,La)SnO₃ single crystals remained at about 3.33 eV, and the in-gap states only slightly increased, thus, maintaining optical transparency in the visible spectral region. Based on all these results, we suggest that the doped BaSnO₃ system holds great potential for realizing all perovskite-based transparent high-temperature high-power functional devices as well as highly mobile two-dimensional electron gas via an interface control of heterostructured films.

DOI: 10.1103/PhysRevB.86.165205 PACS number(s): 81.05.Hd, 71.20.Nr, 72.10.Bg, 78.40.Fy

I. INTRODUCTION

Transparent oxide materials offer great potential for a wide range of device applications, e.g., transparent conductive windows for solar cells, flat-panel displays, light-emitting diodes, and transparent logic devices. Numerous oxide materials including ZnO, In₂O₃, and SnO₂ have been investigated for these purposes, successfully demonstrating passive transparent conductive windows to active semiconducting devices, such as pn junctions, field effect transistors, and UV lasers. 1-8 However, these well-known material systems still have limitations so that currently, there is active scientific research to find alternative transparent materials, which can potentially exhibit better physical properties. For example, high mobility is one essential ingredient for developing transparent logic devices with high density, and oxygen stability is crucial for overcoming interface degradation problems in the oxide pn junctions. Moreover, controlling and minimizing the density of defects or dislocations also becomes important for realizing useful devices based on transparent conducting oxides (TCOs) and transparent oxide semiconductors (TOSs).

Oxide materials with the perovskite structure have exhibited a plethora of interesting physical properties, such as superconductivity, colossal magnetoresistance, ferroelectricity, piezoelectricity, and multiferroicity. 9–12 Extensive research

effort has been performed to utilize such varied physical properties in the form of thin-film heterostructures. 13 The perovskite materials have also been investigated in the context of searching for new TCOs and TOSs as doped SrTiO₃ and doped CaTiO₃. 14-18 The alkaline-earth stannates with the chemical formula $ASnO_3$ (A = Ba, Sr, and Ca) are another perovskite system that has been used in industry for photoelectrochemical energy conversions, stable capacitors, and gas sensors. 19-21 In particular, BaSnO₃ (BSO) is known to form an ideal cubic perovskite structure [see Fig. 1(a)] in which the Sn-O-Sn bonding angle is close to 180° and corresponds to a transparent wide-band-gap semiconductor with an optical gap of $\sim 3.1 \text{ eV}$. In order to have electrical conduction in BaSnO₃, both Ba and Sn sites were doped to form compounds, such as (Ba,La)SnO₃ (BLSO) and Ba(Sn,Sb)O₃ in polycrystalline or thin-film forms. ^{23–27} However, the reported electrical mobility in the thin film was relatively low, less than $2 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, and the conductivity reached, at most, $500 \Omega^{-1} \text{ cm}^{-1}$. As those reported transport properties might not be intrinsic, possibly due to, e.g., grain boundary scattering or off stoichiometry, the growth of high-quality single crystals of doped BaSnO3 and the study of their intrinsic physical properties are of great interest.

Recently, we succeeded in growing single crystals^{28,29} of (Ba,La)SnO₃ and Ba(Sn,Sb)O₃ by the Cu₂O-flux method up

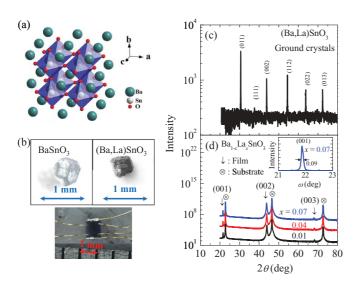


FIG. 1. (Color online) (a) The $2 \times 2 \times 2$ unit cells of cubicperovskite BaSnO₃. (b) Optical microscope images of the flux-grown BaSnO₃, (Ba,La)SnO₃, and a typical sample with electrical leads used in the transport measurements. (c) An x-ray θ - 2θ scan result of a (Ba,La)SnO₃ single crystal shows a single phase in the cubic perovskite structure. (d) An x-ray θ - 2θ scan results show the (00*l*) peaks in epitaxial thin films grown on the SrTiO₃ (001) substrate. The inset shows that the full width at half maximum (FWHM) of the ω -scan rocking curve is only 0.09° .

to a lateral size of ~ 2 mm. In particular, we discovered that a $(Ba,La)SnO_3$ single crystal showed an unprecedentedly high electrical mobility of $\sim\!320~\text{cm}^2~\text{V}^{-1}~\text{s}^{-1}$ with a carrier density of $1.0\times10^{20}~\text{cm}^{-3}$ at room temperature. In parallel with our discovery, there was a similar report on the growth of $(Ba,La)SnO_3$ single crystals by PbO and PbF $_2$ fluxes in which the highest electrical mobility was found to be $\sim\!103~\text{cm}^2~\text{V}^{-1}~\text{s}^{-1}$. We also found that the epitaxial thin films of $(Ba,La)SnO_3$ grown on the SrTiO $_3$ (001) substrate showed an electrical mobility as high as $70~\text{cm}^2~\text{V}^{-1}~\text{s}^{-1}$, which is much larger than the previously reported values 26,27 in thin films. Moreover, the resistivity of the $(Ba,La)SnO_3$ film has shown little change even at 500~°C in air, which suggests extremely good oxygen stability and related physical properties at high temperatures. 28

In order to further understand the origins of such high mobility in the (Ba,La)SnO₃ system, we systematically report various physical properties of the single crystals and epitaxial films in the following sections. In Sec. II, we describe the various experimental tools we have employed. In Sec. III, we present experimental and theoretical results in wide doping ranges in the crystals and films, including temperature-dependent transport properties, structural characteristics, band-structure calculations, and optical properties. From the Hall effect measurements in a broad doping range from 1.0×10^{19} to 4.0×10^{20} cm⁻³, we found that the mobility remained as high as $\sim 200-300 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ and did not show clear dependence on the carrier density. In Sec. IV, we mainly discuss the possible physical origins for obtaining the high electrical mobility. In Sec. V, we conclude that (Ba,La)SnO₃ has a great potential for being used as perovskite-based TOSs with high electrical mobility and superior thermal stability.

II. EXPERIMENTAL

For the single-crystal growth of $Ba_{1-x}La_xSnO_3$ (x = 0-0.04), the corresponding polycrystalline specimen was first synthesized as a seed material. High-purity $BaCO_3$, SnO_2 , and La_2O_3 powders were weighed in a stoichiometric ratio, were thoroughly mixed in an agate mortar, and were fired at $1250\,^{\circ}C$ for 6 h. After several intermediate grindings, the powders were pressed into a pellet and were sintered at $1400-1450\,^{\circ}C$ for 24-48 h. For the growth of $(Ba,La)SnO_3$ single crystals, the Cu_2O flux and the sintered powder were placed in a Pt crucible with a molar ratio of about 15:1, were fired in air above $1250\,^{\circ}C$, and then, were slowly cooled down to $1210\,^{\circ}C$, followed by a slow furnace cooling to room temperature. The crystals showed a cubelike shape as shown in Fig. 1(b).

We grew epitaxial films by the use of the pulsed laser deposition technique, using BaSnO₃, Ba_{0.96}La_{0.04}SnO₃, and Ba_{0.93}La_{0.07}SnO₃ targets. We used single-crystal SrTiO₃ (001) as a substrate and performed the deposition in an O₂ pressure of 100 mTorr at 750 $^{\circ}$ C. After the deposition, we cooled the samples in an O₂ pressure of about 600 mTorr.

We investigated the structural properties of the poly- and single-crystalline samples by the use of x-ray diffraction (XRD), for which we used a high-power x-ray diffractometer equipped with a single Cu $K\alpha_1$ source (EmpyreanTM, PANalytical). We performed temperature-dependent x-ray diffraction measurements for the polycrystalline powder of Ba_{0.999}La_{0.001}SnO₃ by the use of a closed-cycle cryostat (PheniXTM, Oxford Cryosystems), operating in the 20–300 K temperature range. We also characterized the structure of epitaxial films with a four-circle x-ray diffractometer.

The first-principles density functional theory (DFT) calculations were performed by using the Vienna *ab initio* simulation package code. ³¹ The projector-augmented-wave method ³² and the Ceperley-Alder parametrization were employed within the local-density approximation (LDA). ³³ To determine the electronic structure of La-doped BaSnO₃, we adopted a $3 \times 3 \times 3$ supercell containing 135 atoms and carried out the *k*-space integration by using a $2 \times 2 \times 2$ mesh within the Monkhorst-Pack *k*-point sampling. For the calculations, all atomic coordinates were relaxed, and the Hellmann-Feynman force reached less than 0.02 eV Å⁻¹. The cutoff energy used for the plane-wave basis set was 520 eV.

Temperature-dependent resistivity was measured by the conventional four-probe technique for the single crystals and films from 2 to 300 K either in a closed-cycle refrigerator or in a physical property measurement system (PPMSTM, Quantum Design). The five-wire configuration was employed to investigate the Hall effect in single crystals and some thin films as a function of temperatures in a magnetic field up to 9 T. To make electrical contacts, the single crystals were cut and were polished into a rectangular parallelepiped, of which lateral size and thickness were typically $\sim 1.5 \times 0.8 \text{ mm}^2$ and $\sim 50 \, \mu\text{m}$, respectively, as shown in Fig. 1(b). By use of a shadow mask, we subsequently deposited 100-nm-thick Au films as electrical pads on the top of the polished surface. Two electrical pads having a line shape were deposited at both ends

of the specimen as current pads. Similarly, four rectangular pads were deposited for the longitudinal (resistivity) and transverse (Hall effect) voltage measurements. In particular, to calculate the transport data accurately, we have tried to minimize the size of the rectangular pads to be less than $100 \times 100 \, \mu \text{m}^2$. Furthermore, we attached thin Au wires, of which the diameter is $50 \, \mu \text{m}$, inside the electrical pads with care by use of silver epoxy. The detailed shape for the electrical contacts can be found in the bottom of Fig. 1(b). A digital ruler was used to accurately obtain the geometry of the sample size and the distance of the electrical leads.

Optical transmission spectra were obtained in BaSnO₃ and (Ba,La)SnO₃ single crystals, which were optically polished to have thicknesses less than 100 μ m. The ultravioletvisible-near-infrared transmission spectra were measured by a fiber-optic spectrometer (StellaNet, EPP2000) equipped with a Xe-arc lamp as a light source. For the absorption coefficient (α), we repeated the transmission measurements of the same piece of sample in two different thicknesses and calculated α based on the formula = $-\ln(T_{\text{thick}}/T_{\text{thin}})/d$, where d is the thickness difference.

Heat-capacity data of BaSnO₃ single crystals were measured by using a commercial calorimeter provided by PPMSTM (Quantum Design). A custom-made program was developed to perform a least-squares fitting based on the relaxation method with the lumped- τ_2 model,³⁴ which is often called the curve-fitting method.³⁵ Based on the fitting, we first extracted the heat capacity of the sapphire platform and thermal grease (addenda) in a wide temperature range from 2 to 340 K. After obtaining the addenda heat capacity, we subsequently measured the total heat capacity including the BaSnO₃ single crystal (total mass = 20.33 mg) and the addenda to extract the heat capacity of the single crystal.

III. RESULTS

A. Chemical and structural properties

Figure 1(c) shows the XRD pattern (θ -2 θ scan) of a typical (Ba,La)SnO₃ single crystal after being ground into a fine powder form. The pattern reveals that the single crystal forms the cubic perovskite phase without any detectable impurity phase. We have, indeed, tried to grow high-quality single crystals by using various kinds of fluxes to investigate the intrinsic properties of La-doped BaSnO₃. Among those trials, we could also grow rather large size BaSnO₃ single crystals $(\sim 2 \times 2 \times 1 \text{ mm}^3)$ by using the mixed flux of PbO and PbF₂, which is similar to that in a recent paper.³⁰ However, the electron-probe-microanalyses (EPMA) result²⁸ showed that the grown single crystals using the Pb-containing flux unavoidably contained significant Pb impurities. On the other hand, the crystals grown by the Cu₂O flux did not contain any Cu-related impurities according to the EPMA paper. It is, thus, expected that our single crystals, without any Cu impurities from the Cu₂O flux, can offer a better chance to observe the intrinsic properties of (Ba,La)SnO₃.

In the case of $(Ba,La)SnO_3$ thin films, the XRD patterns in Fig. 1(d) show the (00l) peaks due to the epitaxial growth on $SrTiO_3$ (001) as demonstrated in the reciprocal mapping study in Ref. 28. The inset in Fig. 1(d) shows that the FWHM in

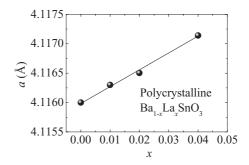


FIG. 2. (a) Cubic lattice parameter for polycrystalline $Ba_{1-x}La_xSnO_3$ ($x=0,\ 0.01,\ 0.02,\ and\ 0.04$) measured at room temperature. The line is drawn as a guide to the eye.

the rocking curve is only 0.09° , supporting a high degree of crystallinity in our epitaxial film. It is worth mentioning that the FWHM in a previous paper was about 0.57° , which is much larger than that of our films. This experimental result suggests that the quality of the thin films should be superior to those studied in previous papers. 26,27

Figure 2 shows the variation in the lattice parameters of polycrystalline $Ba_{1-x}La_xSnO_3$ ($x=0.00,\ 0.01,\ 0.02$, and 0.04) as obtained from the Rietveld refinement of the powder-diffraction data. It is noted that, as the La concentration (x) increases, the lattice parameter increases almost linearly. It is rather unusual to find such an increase in the lattice parameter while doping by the La^{3+} ion, which has a smaller ionic radius (0.103 nm) than that of Ba^{2+} (0.135 nm).³⁶ We will discuss the origin of this unusual lattice expansion in Sec. III B below.

B. First-principles calculations

Figure 3 presents the band structures of both BaSnO₃ and (Ba,La)SnO₃ as obtained by first-principles DFT calculations with LDA. To our knowledge, the band-structure calculation based on the LDA approximation was reported only for BaSnO₃²² not for (Ba,La)SnO₃. The band structures of BaSnO₃ and (Ba,La)SnO₃ were drawn for the $3 \times 3 \times 3$ supercell with 27 unit cells corresponding to the doping rate of x = 0.037 in Ba_{1-x}La_xSnO₃. According to the folded Brillouin zone of the $3 \times 3 \times 3$ supercell as shown in Fig. 3(a), BaSnO₃ seems to have an indirect band gap. Moreover, based on the

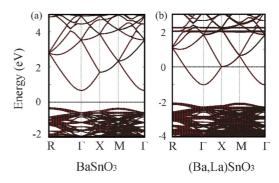


FIG. 3. (Color online) The band structure of (a) BaSnO₃ and (b) (Ba,La)SnO₃ obtained by first-principles calculations with 27 (3 × 3 × 3) unit cells. For (Ba,La)SnO₃, one of the Ba²⁺ ions is substituted by a La³⁺ ion corresponding to the doping rate of x = 0.037 in Ba_{1-x}La_xSnO₃.

band structure in Fig. 3(b), the La doping provides electron states directly well inside the conduction band of BaSnO₃, which is mainly characterized as the Sn 5s states with a Sn-O antibonding character. This means that a La ion acts as an electron donor and its ionic valence becomes La³⁺. The occupation in the antibonding state is likely to result in repulsive forces between Sn and O to lower the total energy of the crystal structure, thereby inducing expansion of the lattice. The theoretically calculated equilibrium lattice constants of BaSnO₃ and 3.7% La-doped BaSnO₃ are found to be 4.098 and 4.102 Å, respectively, clearly showing the increasing trend upon La doping, consistent with experimental results. This theoretical result supports that the experimentally found lattice expansion upon La doping comes from the antibonding nature of conduction bands.

It is further noted that the electronic structure of BaSnO₃ has a highly dispersive conduction band mainly composed of Sn 5s bands mainly due to the presence of an ideal Sn-O-Sn network with its bonding angle close to 180°. 22 The shape of the conduction band is, indeed, similar to the LDA result of the In₂O₃,³⁷ a mother compound of the well-known TCO material In₂O₃:Sn. This observation indicates that, similar to In₂O₃:Sn, there is a good possibility of obtaining highly mobile n-type carriers in BaSnO₃ upon doping. When the La doping is made to form (Ba,La)SnO₃, the Fermi level is formed well inside the Sn 5s band [the dotted line in Fig. 3(b)]. The change in the band structure by La doping is negligible near the Fermi level. The presence of La 4 f bands at 2 eV above the Fermi level did not affect the band dispersion of the original conduction band of BaSnO₃. The calculated effective masses of the conduction band turn out to be about $0.4m_0$ for both BaSnO₃ and (Ba,La)SnO₃, where m_0 is the free-electron mass. The Fermi level of (Ba,La)SnO₃ in Fig. 3(b) indicates that the 3.7% La-doped (Ba,La)SnO₃ is in a degenerately doped regime with n-type carriers, which is consistent with the temperature-dependent transport results explained below.

C. Transport properties

Figure 4 summarizes the resistivity and mobility variations as a function of carrier density at room temperature in both single crystals and thin films. The data from our earlier paper are also compared (closed squares and triangles). Previously, we found that the mobility of single crystals is roughly proportional to n^{-1} , whereas, the mobility of thin films is proportional to $n^{1/2}$ in a low-doping range smaller than $n=4\times10^{20}$ cm⁻³. The n^{-1} dependence of single crystals could be understood as an ionized-dopant scattering effect, which is known to be roughly proportional to the number of scattering centers, i.e., ionized-dopant density. In the case of films, the $n^{1/2}$ dependence could be mainly attributed to the dominant dislocation or grain boundary scattering effects, which are increasingly screened in roughly proportional to the square root of the mobile carrier density. The existence of the dislocations or grain boundaries in the films is expected due to the large lattice mismatch between (Ba,La)SnO₃ and SrTiO₃.

On the other hand, in the extended measurements for the single crystals in a broad doping range from 1.0×10^{19} to 4.0×10^{20} cm⁻³, we find that the measured electrical mobility values are, instead, scattered between 200 and

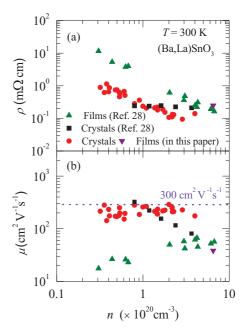


FIG. 4. (Color online) (a) Resistivity (ρ) and (b) mobility (μ) vs carrierdensity (n) plot. Closed (black) squares and (green) triangles are for the reported single crystals and films, ²⁸ respectively. Closed (red) circles are for the data of single crystals, and the inverse (purple) triangle represents a new point of the film measured in this paper.

300 cm² V⁻¹ s⁻¹ without showing clear dependence on the carrier density. It is noteworthy that the previous data for the single crystals (solid squares in Fig 4) show a rather large variation in mobility and reduced mobility at a high carrier density, although the crystals come from the same batch. Thus, we tentatively presume that the crystals studied in Ref. 28 might have a systematic increase in oxygen vacancy with the carrier density increase. We note that the present newly updated mobility values still mark the highest record among the wide-band-gap oxide semiconductors in a similar doping level; e.g., the highest mobility around the doping level of $n = \sim 1 \times 10^{20}$ cm⁻³ was ~ 160 cm² V⁻¹ s⁻¹ for indium oxide (In₂O₃), ³⁸ ~ 50 cm² V⁻¹ s⁻¹ for tin oxide (SnO₂), ³⁹ and $\sim 100 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for zinc oxide (ZnO).⁴⁰ We further note that, due to the high mobility of the (Ba,La)SnO₃ system, the conductivity value in the high doping regions above n = 2×10^{20} cm⁻³ is $\sim 10^4 \Omega^{-1}$ cm⁻¹ in the single crystal at room temperature [Fig. 4(a)], which is close to the highest value among the transparent conductors. The best conductivity of In_2O_3 : Sn is known to be $\sim 10^4 \Omega^{-1} \text{ cm}^{-1}$. Thus, (Ba,La)SnO₃ can also be used as a transparent conductor.

To further understand detailed electrical-transport properties, we performed the temperature-dependent resistivity measurements as summarized in Fig. 5. First, we note that the carrier densities are almost temperature independent in both single crystals and films [Figs. 5(a) and 5(b)]. The resistivities of both single crystals and films mostly increase as increasing temperature [Figs. 5(e) and 5(f)]. The positive temperature coefficient of the resistivity and temperature-independent carrier density clearly show the metallic behavior in both films and single crystals, indicating that all the materials are in a degenerately doped semiconducting regime. The resistivity

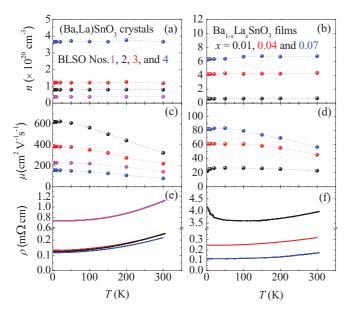


FIG. 5. (Color online) Temperature-dependent carrier density n, resistivity ρ , and mobility μ are plotted for selected (Ba,La)SnO₃ single crystals (BLSO Nos. 1, 2, 3, and 4) (a), (c), and (e) and thin films (b), (d), and (f). The nominal La composition (x) is presented for the thin films.

values of the single crystals decrease nearly by a factor of 2 upon being cooled from room temperature to 2 K [Fig. 5(e)], which then results in the increase in the corresponding mobility by the same factor [Fig. 5(c)]. The mobility increases at low temperatures seem to be a common property of both crystals and films. The factor of the resistivity, which decreases from room temperature to 2 K, as observed in the films with x = 0.04 and 0.07, is also reflected in the increase in the corresponding mobility [Fig. 5(d)]. On the other hand, it is found that the residual resistivity values of the films are generally larger than those of the crystals [Fig. 5(f)] upon being compared at a similar carrier concentration (e.g., 1 order higher near $n \approx 1 \times 10^{20}$ cm⁻³), implying that there exist extrascattering sources in the films, such as grain boundaries and dislocations.

D. Optical properties

Figure 6 compares the transmission and optical absorption spectra for the two single crystals, undoped BaSnO₃ and (Ba,La)SnO₃ with $n = 2.39 \times 10^{20}$ cm⁻³. Transmittance of the BaSnO₃ single crystal reaches as high as 0.71 in the visible spectral region (1.8-3.1 eV), although its thickness of 68.7 μ m is rather high. The significant suppression of the transmittance as well as a sharp increase in α near 3.1 eV reflects the development of an optical gap. Transmittance of the La-doped crystal is progressively suppressed at the low-frequency region, resulting in the Drude-type absorption tail, presumably due to the increase in free carriers. However, the transmittance level in the doped crystal remains finite around 0.2, albeit, it is rather thick ($\sim 53.7 \,\mu\text{m}$) and has a rather high doping level ($n = 2.39 \times 10^{20} \, \mathrm{cm}^{-3}$). The resultant α spectrum of the doped crystal is still less than 300 cm⁻¹ in the visible spectral region, predicting that the doped sample should have a transmittance of ~ 0.8 in, e.g., a thin film having

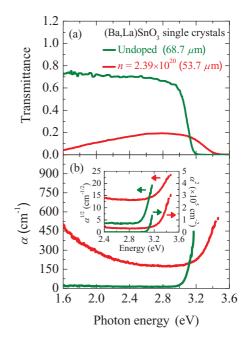


FIG. 6. (Color online) (a) Transmission spectra and (b) absorption coefficient (α) of BaSnO₃ and (Ba,La)SnO₃ single crystals are plotted as a function of photon energy. The absorption coefficient α for each undoped and doped sample ($n=2.39\times10^{20}\,\mathrm{cm^{-3}}$) was extracted by measurements of transmission spectra of the same specimen in two different thicknesses. The inset shows the curves of $\alpha^{0.5}$ and α^2 vs photon energy for both undoped BaSnO₃ and (Ba,La)SnO₃.

a thickness of about 100 nm. This high transparency has also been observed in previous optical studies on the thin films grown on SrTiO₃ substrates. ²⁶ It is also noted that the steeply increasing part in α has slightly shifted to a higher energy in the doped crystal, indicating the presence of the Burstein-Moss shift^{41,42} as often observed in degenerate semiconductors.

According to the band calculation in Fig. 3, BaSnO₃ is an indirect gap semiconductor in which the conduction-band minimum and the valence-band maximum have predominant Sn 5s and O 2p characters, respectively. To experimentally determine the gap nature of BaSnO₃, we plotted the curves of $\alpha^{0.5}$ and α^2 vs photon energy for both undoped BaSnO₃ and (Ba,La)SnO₃ in the inset of Fig. 6(b). For BaSnO₃, we could find a linearly increasing region in both curves. Upon applying a linear extrapolation, the indirect and direct band gaps are estimated as 2.95 and 3.10 eV, respectively. This observation suggests that the optical transition with the lowest energy reflects the indirect transition nature, whereas, the direct optical transition with a bit higher energy is quite strong in this material. This is somewhat expected because the direct optical transition between the Γ points of the valence and conduction bands satisfies an optical selection rule (from O 2p to Sn 5s), whereas, the indirect transition from the valence-band maximum (R point) to the conduction-band minimum (Γ point) is generally low. It is noteworthy that quite similar optical transition characters have also been observed in another cubic perovskite SrGeO₃, a new TCO candidate compound reported recently.⁴³

The experimentally estimated direct or indirect band gaps (2.95-3.10 eV) in BaSnO₃ are much larger than that $(\sim 1 \text{ eV})$

estimated from the band structure in Fig. 3. It is rather well known that the gap predicted by the band calculation based on the LDA approximation underestimates the actual gap in many transparent oxide materials because the LDA calculation does not take into account the electron-correlation effect properly. Even the well-known TCO In₂O₃:Sn exhibits a similar kind of discrepancy between the LDA calculation and the experimentally determined gap due to the correlation effect.³⁷ In addition, In₂O₃:Sn was found to show yet another discrepancy of 0.81 eV between the experimental optical gap and the gap measured by the photoemission and x-ray emission spectroscopy due to the presence of the optical selection rule.⁴⁴ Therefore, in the future, it will be interesting to study the origin of such an optical gap enhancement in BaSnO₃ as well. In reference to the case of In₂O₃:Sn, it will be worthwhile to check whether the electron-correlation effects alone can explain the discrepancy or an additional optical selection becomes necessary.

E. Debye temperatures

To extract the information on the Debye temperature, we used two methods, i.e., heat-capacity and thermal-expansion measurements. Figure 7(a) shows the specific heat of a BaSnO₃ single crystal at temperatures between 2 and 330 K. For the heat-capacity analysis, we found that the two Debye phonon modes become necessary because one phonon mode alone could not fully explain the experimental data. Based on the Debye theory, the temperature-dependent specific heat coming from the two phonon contributions can be described

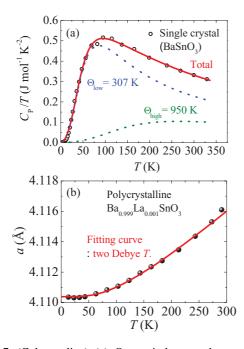


FIG. 7. (Color online) (a) Open circles are the temperature-dependent specific heat of the BaSnO₃ single crystal. The dotted lines are the two-phonon mode contributions (blue and green), and the solid line refers to their sum (red). (b) Thermally induced cubic lattice parameter expansion of polycrystalline Ba_{0.999}La_{0.001}SnO₃. The solid (red) line is the thermal-expansion fitting based on the Debye model with the two Debye temperatures.

as follows:45

$$C_v = 9qNk_B \left[x \left(\frac{T}{\Theta_{\text{low}}} \right)^3 \int_0^{\Theta_{\text{low}}/T} \frac{x^4 e^x}{(e^x - 1)^2} dx + y \left(\frac{T}{\Theta_{\text{high}}} \right)^3 \int_0^{\Theta_{\text{high}}/T} \frac{x^4 e^x}{(e^x - 1)^2} dx \right], \tag{1}$$

where Θ_{low} and Θ_{high} are the Debye temperatures of each phonon mode and x and y are the weights of the phonon modes. Open circles represent the temperature-dependent specific heat data of the BaSnO₃ single crystal, whereas, the lines refer to the two-phonon mode contributions (dotted lines) and their sum (solid line). The model fitting can successfully explain the experimental data at least above 20 K, and the resultant two Debye temperatures Θ_{low} and Θ_{high} are found to be 307 and 950 K, respectively. The resultant x/y ratio is around 1.5, implying that the heat capacity below 300 K is mainly governed by the low-energy Debye phonon.

Figure 7(b) displays the evolution of the temperature-dependent lattice constant of a $Ba_{0.999}La_{0.001}SnO_3$ polycrystalline specimen. Upon increasing the temperature, the lattice parameter increases, consistent with the lattice expansion due to anharmonic thermal vibration. To model the thermal-expansion data of $Ba_{0.999}La_{0.001}SnO_3$, we assumed that the two Debye temperatures as obtained from the heat-capacity data can explain the intrinsic energy of the lattice and, thus, its temperature-dependent expansion as well. Then, the temperature dependencies of the lattice parameter (a) can be described as⁴⁶

$$a = a_0 + bT \left(\frac{T}{\Theta_{\text{low}}}\right)^3 \int_0^{\Theta_{\text{low}}/T} \frac{x^3}{e^x - 1} dx + cT \left(\frac{T}{\Theta_{\text{high}}}\right)^3 \int_0^{\Theta_{\text{high}}/T} \frac{x^3}{e^x - 1} dx, \tag{2}$$

where a_0 and Θ_D (D = high or low) are the lattice constant at 0 K and the Debye temperatures, respectively, and b and c are the constant prefactors. Upon using the same Debye temperatures from the heat capacity, we could get a satisfactory fitting result, confirming that the two Debye temperatures of 307 and 950 K are quite effective in describing the lattice energy and related thermal properties. As the two Debye temperatures are quite different, one phonon mode around 300 K seems to be approximately effective in describing the phonon properties of BaSnO₃ at low temperatures. For example, upon fitting the thermal-expansion data with one Debye temperature of 365 K, we could obtain almost the same good fit results as the two-phonon approximation (not shown), supporting that the lower-energy phonon mode mostly contributes the thermal expansion as well.

IV. DISCUSSION

The electrical mobility (μ) in a simple one-band model is expressed by an electron effective mass (m^*) and a total electron scattering rate (τ^{-1}) ,

$$\mu = e\tau/m^*,\tag{3}$$

where e is an electron charge. Therefore, a high mobility can be realized with a small electron effective mass and a small total

electron scattering rate. In the following, we discuss the origins for achieving such a high mobility in (Ba,La)SnO₃ based on the peculiar characteristics reflected in the two key physical parameters, i.e., electron scattering rate and effective mass.

A. High mobility in the crystals and thin films

Controlling impurity scattering seems to be important for obtaining the highest mobility of $\sim\!320~\text{cm}^2~\text{V}^{-1}~\text{s}^{-1}$ in (Ba,La)SnO3 single crystals as observed in our previous paper²8 and 200–300 cm² V $^{-1}~\text{s}^{-1}$ as found in this paper. It was recently reported that single crystals grown by PbO + PbF2 flux produced a mobility³0 close to 103 cm² V $^{-1}~\text{s}^{-1}$ at a doping level of $\sim\!\!8$ –10 $\times\!10^{19}~\text{cm}^{-3}$. As the Pb impurity can enter both Ba and Sn sites in this flux, the observation of lower mobility implies that the presence of the additional impurity other than La might lead to the increased dopant scattering. As mentioned in Sec. III A, the absence of Cu impurity in our single crystals should then be helpful in reducing the additional impurity scattering and obtaining physical properties close to the intrinsic ones.

In the thin films, it is interesting to note that a previous paper found the mobility to be, at best, 0.69 cm² V $^{-1}$ s $^{-1}$, although the reported (Ba,La)SnO3 films were epitaxially grown on the same type of substrate, SrTiO3 (001), 26 as in the present paper. The FWHM in the rocking curve was 0.57° in the previous paper, 26 whereas, it is 0.09° in our paper [Fig. 1(d)], which represents a conspicuous improvement in the crystallinity. Therefore, the highest electrical mobility of $\sim\!70$ cm² V $^{-1}$ s $^{-1}$ realized in our thin films is most likely to be associated with the superior structural properties.

On the other hand, the highest mobility of \sim 70 cm² V⁻¹ s⁻¹ in our films is still much lower than the values in the single crystals. Even though our films were epitaxially grown, from the transmission electron microscopy study, we found that there exist significant grain boundaries and threading dislocations due to the large lattice mismatch (more than 4%) between the substrate and the (Ba,La)SnO₃. Those grain boundaries/dislocations are expected to act as double-Schottky barriers for the electron transport, ^{47,48} thereby giving rise to lower electrical mobility and higher residual resistivity than single crystals as demonstrated in Fig. 5. Therefore, it is expected that the mobility in thin films will be further improved when the dislocation density gets reduced by, e.g., using BaSnO₃ single-crystal substrates.

Related to the presence of such grain boundaries/dislocations, the room-temperature carrier densities in the films with nominal doping concentrations x = 0.01, 0.04, and 0.07 are 7.0×10^{19} , 4.0×10^{20} , and 6.8×10^{20} cm⁻³, respectively. The activation rates of dopants then become 45%, 69%, and 67%, respectively. The lower activation rate for the lowest doping indicates the existence of the enhanced charge-trapping mechanism. Moreover, as evident in Fig. 5(d), the mobility is reduced significantly when the carrier density is decreased. This observation implies that the higher carrier density effectively reduces the effect of dislocation/grain boundary scattering. Once the double-Schottky barrier is formed in the films, the higher carrier density is likely to induce thinner barrier width and smear out the barriers, resulting in the enhanced mobility as the carrier density increases up

to around $n \sim 4 \times 10^{20} \text{ cm}^{-3}$. However, as the doping rate becomes higher than $4 \times 10^{20} \text{ cm}^{-3}$, the scattering by ionized dopants seems to start dominating rather than dislocations or grain boundaries to induce a mobility decrease by the increased dopant level.

B. Effective mass

To understand the high mobility observed in the (Ba,La)SnO₃ single crystals within the band-structure framework, one should expect quite a small effective mass. As mentioned in the LDA calculation results (Sec. III B), the effective masses of BaSnO3 and (Ba,La)SnO3 are predicted to be $\sim 0.4m_0$. It turns out that the value of $\sim 0.4m_0$ is comparable to, but not particularly smaller than, the theoretically predicted effective masses of other wide-band-gap oxide semiconductors, e.g., In_2O_3 (0.30 m_0), ⁴⁹ SnO_2 (0.38 m_0), ⁵⁰ and ZnO $(0.24m_0)^{.51}$ The effective mass can also be estimated by the Burstein-Moss shift, 41,42 which predicts the energy difference in the optical band gap (ΔE) between undoped and doped semiconductors as $\Delta E = h^2 (3n/\pi)^{2/3} / (8m^*)$, where h is the Planck constant and m^* is the effective mass. As we estimate ΔE from the direct optical gaps of BaSnO₃ (3.10 eV) and (Ba,La)SnO₃ (~ 3.33 eV) in the inset of Fig. 6(b), $\Delta E = \sim 0.23$ eV so that the effective mass is estimated as $\sim 0.60m_0$. This value is slightly larger than the theoretical prediction but is small enough to guarantee a high mobility. On the other hand, there exists another recent prediction of $m^* = 0.06m_0$ (Ref. 52) or $0.2m_0$ (Ref. 53) based on the LDA calculations based on different approximations, such as the generalized gradient approximation or the use of a specific hybrid functional, respectively. The predictions of the effective mass at this stage are, thus, scattered, ranging from 0.06 to $0.4m_0$, indicating that it is rather sensitive to the approximation in the DFT calculation. Therefore, to pin down whether the effective mass is a dominant quantity for creating the high mobility or not, it would be necessary to determine an effective mass of (Ba,La)SnO₃ more accurately.

C. Effects of various scattering in the crystal

Another key physical quantity to determine the electrical mobility is the electron-scattering rate, which can be expressed by a sum of several scattering rates, according to Matthiessen's rule.

$$\tau^{-1} = \sum_{i} \tau_{i}^{-1},\tag{4}$$

where τ_i^{-1} are the electron-scattering rates from different scattering sources. In the single crystals of (Ba,La)SnO₃ with minimized extrinsic scattering sources, e.g., defects, the electron-phonon and ionized-dopant scatterings are likely to be the main sources of the electron scattering. It is generally known that the ionized-dopant scattering in the degenerately doped regime is almost temperature independent. Then, the majority of the temperature-dependent scattering can be attributed to the electron-phonon scattering in the (Ba,La)SnO₃ system in which the degenerately doped regime is clearly realized when the doping rate is higher than 1.0×10^{19} cm⁻³. Therefore, it is inferred that the temperature-dependence in

resistivity observed in Fig. 5(e) and 5(f) is mainly determined by the electron-phonon scattering, because the carrier density is mostly temperature independent.

The Debye temperature should be closely related to the electron-phonon scattering strength as the electron-phonon scattering will increase with the number of thermally activated phonons; e.g., a smaller Debye temperature will result in a higher amount of phonon population at a given temperature. The Debye temperatures of (Ba,La)SnO₃ are 307 and 950 K as determined by both heat-capacity and thermal-expansion measurements. The Debye temperature of 307 K is, indeed, a bit lower than the known Debye temperatures of In₂O₃ (420 K),⁵⁴ SnO₂ (500 K),⁵⁴ and ZnO (399.5 K).⁵⁵ Therefore, it is expected that the electron-phonon scattering in (Ba,La)SnO₃ should not be particularly smaller, to cause the higher mobility, than those of the other transparent electronic materials.

Another important contribution to the total scattering rate is the ionized-dopant scattering. In (Ba,La)SnO₃, the La³⁺ dopants are the main ionized impurities. In a degenerately doped semiconductor, the mobility due to the ionized impurity (μ_{ii}) can be expressed as^{56,57}

$$\mu_{ii} = \frac{3(\varepsilon_r \varepsilon_0)^2 h^3}{z^2 m^{*2} e^3} \frac{n}{N_i} \frac{1}{F_{ii}(\xi_d)} \quad \text{and} \quad \xi_d = (3\pi^2)^{1/3} \frac{\varepsilon_r \varepsilon_0 h^2 n^{1/3}}{m^* e^2},$$
(5)

where the screening function $F_{ii}(\xi_d)$ is given by

$$F_{ii}(\xi_d) = \left[1 + \frac{4\xi_{np}}{\xi_d} \left(1 - \frac{\xi_{np}}{8}\right)\right] \ln(1 + \xi_d) - \frac{\xi_d}{1 + \xi_d} - 2\xi_{np} \left(1 - \frac{5\xi_{np}}{16}\right) \quad \text{and} \quad \xi_{np} = 1 - \frac{m_0^*}{m^*}.$$
 (6)

Here, h is Planck's constant, N_i is a number of ionized dopants, and ε_r is a dielectric constant. m_0^* is the effective mass at the conduction-band edge and $m^* = m_0^*[1 + 2\alpha(E - E_C)]$, where α is the nonparabolicity parameter and $E - E_C$ is the electron energy relative to the conduction-band edge (E_C) . Equation (5) predicts that, in the ionized impurity scattering regime, μ_{ii} is generally proportional to the square of the dielectric constant. We should note that the dielectric constant of BaSnO₃ (about 20)⁵⁸ is almost two times larger than the well-known transparent electronic materials; In_2O_3 (about 9), SnO_2 (9.6–13.5), and ZnO (8.75–7.8).⁵⁶ Therefore, the high-mobility state in $(Ba,La)SnO_3$ may be due to greatly reduced ionized-dopant scattering, coming from the enhanced screening strength associated with the high dielectric constant.

Another important factor to reduce the ionized-dopant scattering could be the capability of doping the La dopant into the Ba site. It is expected that the ionized-dopant scattering should be greatly reduced if the dopant is located away from the SnO₆ octahedra, which are the main conduction paths. This would be favorable for realizing an almost defect-free Sn-O network. Empirical comparison of the residual resistivity supports this reasoning. The residual resistivity of the Ta-doped SnO₂ was $\sim 0.83~\text{m}\Omega$ cm at $n = \sim 1 \times 10^{20}~\text{cm}^{-3}$, ³⁹ which was seven times larger than that of the (Ba,La)SnO₃ single crystal, $\sim 0.12~\text{m}\Omega$ cm at $n = 1.18 \times 10^{20}~\text{cm}^{-3}$ (Fig. 5). Thus, it is postulated that the location of the La dopant, away from the Sn-O network, plays an important role in minimizing the ionized-dopant scattering as well.

One caveat in applying Eq. (5) to understand the ionizeddopant scattering in our single crystals lies in the screening function $F_{ii}(\xi_d)$. Once the ionized impurity level (N_i) and the actual carrier density (n) are proportional to each other, μ_{ii} is inversely proportional to $F_{ii}(\xi_d)$. In general, $F_{ii}(\xi_d)$ increases as the carrier density increases so that one should expect a reduced μ_{ii} with an increase in n in the ionized-dopant scattering regime. However, the new result in Fig. 4(b) is not yet decisive to draw the conclusion whether the mobility, indeed, shows any dependence on n. The mobility values near the same carrier density level exhibit large scatter. This indicates that the single crystals are not yet perfect so that they might have additional scattering sources, such as oxygen vacancies. If the oxygen vacancies are present inside the SnO₆ octahedral network, they are expected to act as stronger scattering centers than the La³⁺ ions. Moreover, the actual carrier density can also be fluctuating inside a single crystal or over different pieces, possibly resulting in the scattered mobility and carrier density as seen in Fig. 4(b). In light of the very small oxygen diffusion constant in the BaSnO₃ material system as we reported previously,²⁸ full and uniform oxygenation of millimeter-thick crystals may be difficult. Further studies are underway to reduce such additional scattering sources.

V. CONCLUSIONS

We found a high electrical mobility in the transparent perovskite material (Ba,La)SnO₃. The (Ba,La)SnO₃ single crystals grown by the Cu₂O-flux method showed an electrical mobility of $200-300~\text{cm}^2~\text{V}^{-1}~\text{s}^{-1}$ in a broad doping range from 1.0×10^{19} to $4.0\times10^{20}~\text{cm}^{-3}$, constituting the highest value among the known transparent electronic materials, such as doped In₂O₃, SnO₂, and ZnO. In the thin films grown epitaxially on SrTiO₃ (001), the maximum mobility reached only \sim 70 cm² V⁻¹ s⁻¹ due to the presence of dislocations/grain boundaries, which points out the possibility for enhancing the mobility in the thin-film form upon having a proper substrate material. We discussed that the high mobility can arise from several unique physical conditions of (Ba,La)SnO₃: a highly dispersive Sn 5s band coming from an ideal Sn-O-Sn bonding angle close to 180° and minimized ionized-dopant scattering from the high dielectric constant and the capability of setting the La³⁺ dopant away from the main conduction paths (SnO₆ octahedra network). Moreover, it is noteworthy that such a high mobility is linked to the high conductivity $\sim 10^4~\Omega^{-1}~{\rm cm}^{-1}$ at room temperature at a doping level of $n=2\times 10^{20}~{\rm cm}^{-3}$, which is comparable to the highest value among the transparent conducting oxides. Therefore, combined with the thermal stability of the oxygen diffusion, the (Ba,La)SnO₃ system offers an unprecedented opportunity for realizing all perovskite-based transparent high-temperature high-power functional devices.

ACKNOWLEDGMENTS

We thank T. W. Noh, Y. D. Park, and T. H. Lee for discussions. We acknowledge support from the NRF through the Accelerated Research Program (Grant No. R17-2008-33-01000-0), through the Creative Research Initiative (Grant No. 2010-0018300), and by MKE, through the Fundamental R&D program for Core Technology of Materials.

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