# NMR study for 4 f-localized ferromagnet CeRu<sub>2</sub>Ga<sub>2</sub>B

H. Sakai,\* Y. Tokunaga, and S. Kambe

Advanced Science Research Center, Japan Atomic Energy Agency, Tokai, Ibaraki 319-1195, Japan

R. E. Baumbach, F. Ronning, E. D. Bauer, and J. D. Thompson

MPA-CMMS, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

(Received 25 July 2012; published 4 September 2012)

Nuclear magnetic resonance (NMR) studies using <sup>11</sup>B and <sup>69,71</sup>Ga have been performed on the tetragonal Ce-based ferromagnet CeRu<sub>2</sub>Ga<sub>2</sub>B. The Knight shifts for the nuclei show an Ising-type anisotropy along the *c* axis, similar to results from the static susceptibility. From the Knight shift measurements, the hyperfine coupling constants have been determined. The anisotropy of the spin-lattice relaxation rates  $1/T_1$  indicates that the anisotropy of spin fluctuations are also Ising-like along the *c* axis. The localized character of the 4*f* electrons in this system is discussed.

DOI: 10.1103/PhysRevB.86.094402

PACS number(s): 75.20.Hr, 75.30.Gw, 75.40.Cx, 75.40.Gb

### I. INTRODUCTION

In heavy fermion systems the competition between the Ruderman-Kittel-Kasuya-Yosida (RKKY) exchange interaction and the Kondo effect leads to a rich variety of physical phenomena, such as non-Fermi-liquid behavior, peculiar magnetic ordering, and unconventional superconductivity. The strength of the hybridization between the f and conduction electrons is a key parameter to characterize heavy fermion systems. At the same time, it is very important to understand the anisotropy of the static and dynamic magnetic response, because the strong spin-orbit coupling makes the pseudospins anisotropic. Especially in the antiferromagnetic (AFM) case, systematic NMR studies have revealed that XY-type anisotropy of spin fluctuations correlates with d-wave superconductivity.<sup>1-3</sup> Such a hypothesis is important for developing basic principles to design new materials. It is similarly important to reveal the static/dynamic magnetic anisotropy for ferromagnetic cases. NMR is a powerful tool to microscopically determine the anisotropy of the static/dynamic magnetic response for 4felectrons since the nuclear spins are very low energy probes which allow for the investigation of the electronic responses without strongly perturbing the system. The 4f-electron ferromagnetic (FM) system CeRu<sub>2</sub>Ga<sub>2</sub>B is suitable for detailed studies of the anisotropy of FM spin fluctuations since there are several NMR-active nuclei (i.e., <sup>69,71</sup>Ga and <sup>11</sup>B).

CeRu<sub>2</sub>Ga<sub>2</sub>B is a metallic ferromagnet with a Curie temperature  $T_{\rm C} = 16.3 \text{ K}.^4$  Specific heat measurements suggest that the FM transition is weakly first order and, additionally, that the Ce 4 *f*-electron states do not hybridize strongly with the conduction electron states, that is, the 4f electrons are well localized. The isomorphic CeRu<sub>2</sub>Al<sub>2</sub>B is also a ferromagnet with  $T_{\rm C} = 12.8$  K, but it additionally exhibits antiferromagnetism just above  $T_{\rm C}$  ( $T_{\rm N} = 14.2$  K).<sup>5,6</sup> Such complex magnetic behavior indicates a competition between FM and AFM exchange interactions in CeRu<sub>2</sub>Al<sub>2</sub>B. Very recently, an NMR study of CeRu<sub>2</sub>Al<sub>2</sub>B revealed that the Ising-type magnetic anisotropy comes from the  $\Gamma_7^{(1)}$  doublet ground state, that is, a nearly pure  $|J_z\rangle = |\pm 5/2\rangle$  state arises due to crystal electric field (CEF) effects.<sup>7</sup> Each CEF level is well separated in energy, where the first excited CEF state  $\Gamma_6 = |\pm 1/2\rangle$  is proposed to lie at ~550 K above the ground state. In both compounds, T<sub>C</sub> increases under applied pressures up to about 2.6 GPa, while the  $T_{\rm N}$  decreases and finally disappears for CeRu<sub>2</sub>Al<sub>2</sub>B.<sup>8</sup> To reach the possible FM quantum critical region, further pressure or alternative chemical substitutions are required.

The crystal structure for CeRu<sub>2</sub>Ga<sub>2</sub>B is displayed in Fig. 1. It is expressed as a stuffed version of the tetragonal CeMg<sub>2</sub>Si<sub>2</sub> structure with the space group P4/mmm.<sup>9</sup> In this layered structure, the Ce atoms form a square lattice in the Ce layer and the Ru and B atoms form nesting square lattices. The Ga layers are sandwiched between the Ce and Ru-B layers, which are stacked alternately along the c direction. The lattice parameters for CeRu<sub>2</sub>Ga<sub>2</sub>B are a = 4.187 Å and c = 5.580 Å, respectively.<sup>4</sup> Such a layered tetragonal crystal structure often gives a versatile template, as is seen for the tetragonal ThCr<sub>2</sub>Si<sub>2</sub>- and HoCoGa<sub>5</sub>-type structures. Indeed, the isostructural compounds  $LnRu_2X_2X'$  (Ln = La, Ce, Pr, Nd, Sm; X = Al, Ga; X' = B, C) are already reported, <sup>5,6,8,9</sup> and show a variety of magnetic properties. Systematic investigations on those compounds may provide a route to explore new heavy fermion systems. It is noted that the ratio  $c/a \sim 1.3$  for CeRu<sub>2</sub>Ga<sub>2</sub>B is not large when compared with the typical values of  $\sim 2.4$  for the heavy fermion superconductors CeCu<sub>2</sub>Si<sub>2</sub>  $(ThCr_2Si_2 type)^{10}$  and ~1.6 for CeCoIn<sub>5</sub> (HoCoGa<sub>5</sub> type).<sup>11</sup>

In this paper, <sup>11</sup>B and <sup>69,71</sup>Ga-NMR measurements for CeRu<sub>2</sub>Ga<sub>2</sub>B are reported using both single crystal and polycrystalline specimens. First, the NMR spectra under applied fields are shown, then the hyperfine coupling constants for <sup>69,71</sup>Ga and <sup>11</sup>B are determined via Knight shifts in the paramagnetic state under applied fields. The nuclear quadrupolar parameters are also obtained, which reflect the electric field gradients (EFGs) on the subjective nuclear sites. Second, the NMR spectra under zero applied field are shown in order to determine the internal fields on the nuclear sites. Finally, we discuss the dynamic magnetic response of 4f electrons in this system via nuclear spin-lattice relaxation rates  $(1/T_1)$  measurements.

# **II. EXPERIMENT**

Polycrystalline specimens of CeRu<sub>2</sub>Ga<sub>2</sub>B were synthesized by arc melting stoichiometric quantities of Ce, Ru, Ga, and B under an Ar atmosphere. The resulting boules were flipped and remelted several times to encourage homogeneity and



FIG. 1. (Color online) Crystal structure of CeRu<sub>2</sub>Ga<sub>2</sub>B.

subsequently were annealed at 900 °C for two weeks in evacuated quartz tubes. These specimens were checked by x-ray diffraction (XRD) measurements to confirm the single phase without any secondary phases. The resulting XRD patterns indicated a phase-pure LaRu<sub>2</sub>Al<sub>2</sub>B structure, and the obtained lattice parameters were in good agreement with previously reported values. Single crystals for CeRu<sub>2</sub>Ga<sub>2</sub>B were grown by the Czochralski pulling method.<sup>4</sup>

Magnetization was measured using a SQUID magnetometer (Quantum Design Magnetic Property Measurement System) with applied fields of 1 kOe along the *a* and *c* axes of the single crystal. Magnetic susceptibility ( $\chi$ ) below  $T_C$  is defined as the magnetization (*M*) divided by the applied field ( $H_0$ ), that is,  $\chi \equiv M/H_0$ .

NMR measurements were carried out using a phasecoherent, pulsed spectrometer. Frequency-swept spectra were taken by tuning the rf network at each point. To form the nuclear spin echoes, 90°–180° conditions were used with a first pulse duration of 2–3  $\mu$ s. The separation  $\tau$  between first and second pulses was typically 10–20  $\mu$ s. External magnetic fields were applied using a homogeneous superconducting magnet specified for NMR. In the paramagnetic state, a single crystal with dimensions of 0.6 × 0.6 × 5 mm<sup>3</sup> was used for the NMR measurements. In the FM ordered state, the zero applied field NMR measurements were performed using the polycrystalline sample. Using the internal fields on the active nuclei, the NMR spectra were taken by sweeping the frequency.

Using conventional notation, the quadrupole frequency parameter is defined as  $v_Q \equiv \frac{3e^2qQ}{2I(2I-1)h}$ , where eQ is the nuclear quadrupolar moment, *I* is the nuclear spin quantum number, and  $eq \equiv V_{ZZ}$  is the principal component of the electric field gradient (EFG) tensor. Here  $V_{ii}$  denotes EFG tensor components in the principal coordinate system, such that  $|V_{XX}| \leq |V_{YY}| \leq |V_{ZZ}|$  for each ionic site. The EFG components satisfy LaPlace's equation, that is,  $V_{XX} + V_{YY} + V_{ZZ} = 0$ . The EFG asymmetry parameter is defined as  $\eta \equiv \frac{|V_{YY} - V_{XX}|}{|V_{ZZ}|}$ . At the tetragonal sites,  $\eta$  becomes 0. Nuclear quadrupolar moments are  ${}^{11}Q = 0.0355 \times 10^{-24} \text{ cm}^2$ ,  ${}^{69}Q = 0.178 \times 10^{-24} \text{ cm}^2$ , and  ${}^{71}Q = 0.112 \times 10^{-24} \text{ cm}^2$ , respectively. Nuclear gyromagnetic ratio values used here are  ${}^{11}\gamma_N/2\pi = 1.366 \text{ MHz/kOe}$ ,  ${}^{69}\gamma_N/2\pi = 1.022 \text{ MHz/kOe}$ , and  ${}^{71}\gamma_N/2\pi = 1.29855 \text{ MHz/kOe}$ .

The nuclear spin-lattice relaxation time  $T_1$  was measured using the inversion-recovery method with a  $\pi$  pulse. Values of  $T_1$  were obtained from fits to an appropriate relaxation function. The magnetization recovery  $[\{M(\infty) - M(t)\}/M(\infty)]$  for the center and satellite NMR lines of the <sup>11</sup>B and <sup>69,71</sup>Ga (I = 3/2) nuclei gave satisfactory fits to the single- $T_1$  functions  $0.1 \exp(-t/T_1) + 0.9 \exp(-6t/T_1)$  and  $0.1 \exp(-t/T_1) + 0.5 \exp(-3t/T_1) + 0.4 \exp(-6t/T_1)$ , respectively.

### **III. RESULTS AND DISCUSSIONS**

#### A. Static magnetic response

Figure 2(a) shows the frequency-swept NMR spectra taken at 80 K under a constant field of ~72 kOe along the *c* axis of a single crystal. In this case, the observed NMR lines are successfully assigned as shown in Fig. 2(a). On the other hand, the NMR for <sup>69,71</sup>Ga with  $H_0 \parallel a$  could not be observed, as



FIG. 2. (Color online) Frequency-swept NMR spectra taken at 80 K for the single crystal of CeRu<sub>2</sub>Ga<sub>2</sub>B (a) under an external field of  $H_0 \sim 72$  kOe along the *c* axis, and (b) under an external field of  $H_0 \sim 35$  kOe along the *a* axis.

shown in Fig. 2(b), even under the higher field of  $\sim$ 72 kOe (not shown). The reason why the <sup>69,71</sup>Ga NMR signals are not observed may be due to the fast nuclear spin-spin relaxation rates  $1/T_2$  and not due to  $1/T_1$ , as discussed later.

Each set of spectra for <sup>11</sup>B and <sup>69,71</sup>Ga should be composed of three equally separated lines, that is, one center  $(1/2 \Leftrightarrow -1/2)$  and two satellite  $(-1/2 \Leftrightarrow -3/2 \text{ and } 3/2 \Leftrightarrow 1/2)$ transitions since all the nuclear spins are I = 3/2 and all the nuclear sites have tetragonal symmetry  $(\eta = 0)$ . Within first order perturbation of the nuclear quadrupolar interaction, in the case of  $H_0 \parallel V_{ZZ}$ , the resonance frequency for the transition of  $m \Leftrightarrow m - 1$  is described as  $v_m = v_0(1 + K_c) + v_Q(m - 1/2)$ , while in the case of  $H_0 \perp V_{ZZ}$ ,  $v_m = v_0(1 + K_a) - (v_Q/2)(m - 1/2)$  with  $v_0 \equiv \gamma_N H_0$ . While the second order perturbation gives a frequency shift of  $\frac{3v_Q^2}{16w_0}$  for the central transition in the case of  $H_0 \perp V_{ZZ}$ , the separations between the satellite lines are independent of a second order perturbation effect, that is,  $2v_Q$  and  $v_Q$  in the case of  $H_0 \parallel$  and  $\perp V_{ZZ}$ , respectively. The center line for the case of  $H_0 \parallel N_{ZZ}$  is also free from any second order perturbation.

From the site symmetry and magnetic anisotropy along the *c* axis, the principal axes for  $V_{ZZ}$  are determined to be along the *c* axis for both <sup>11</sup>B and <sup>69,71</sup>Ga. Indeed, in the case of  $H_0 \parallel c$ , the separations between satellite lines for <sup>11</sup>B are doubled, as compared to  $H \parallel a$  as shown in Fig. 2(b). It is noted that the direction of  $V_{ZZ}$  for <sup>69,71</sup>Ga is additionally confirmed by the NMR measurement under zero applied field, as described later. Since the  $v_Q$  are much less than the experimental  $v_0$  in the case of  $H_0 \sim 72$  kOe, as mentioned above, the second order perturbation is enough to be taken into account. The obtained ratio of  ${}^{69,71}v_Q$  accurately corresponds to the ratio of the nuclear quadrupolar moment  ${}^{69,71}\gamma_N$ .

The nuclear quadrupolar frequencies  $v_Q$  for each nucleus are estimated from the separation between satellite lines. The  $v_Q$  for <sup>11</sup>B and <sup>69</sup>Ga are plotted against temperature in Fig. 3, in which the results obtained in the FM ordered state under zero applied field are also plotted together as described below. The error bars in Fig. 3 are roughly estimated as a maximum error assuming  $\pm 10^{\circ}$  misalignment of the crystal relative to the external field. Although a small variation just below  $T_{\rm C}$  is seen for <sup>69</sup>Ga,  $\nu_{\rm Q}$  is estimated to be ~0.7 MHz for <sup>11</sup>B and ~2.4 MHz for <sup>69</sup>Ga in the paramagnetic state. The  $\nu_{\rm Q}$  for <sup>11</sup>B was not estimated in the ordered state since the NMR frequencies were lower than the experimental frequency range under zero applied field.

Here  $v_Q$  for <sup>11</sup>B in CeRu<sub>2</sub>Ga<sub>2</sub>B is similar to the experimental value of 0.75 MHz in isostructural CeRu<sub>2</sub>Al<sub>2</sub>B. The calculation of  $v_Q$  based on a full potential linear augmented plane wave (FLAPW) method within the local density approximation (LDA) assuming itinerant 4*f* electrons<sup>7</sup> has found similar values for <sup>11</sup>B in CeRu<sub>2</sub>Al<sub>2</sub>B (0.78 MHz) and LaRu<sub>2</sub>Al<sub>2</sub>B (0.73 MHz). These nearly independent values for <sup>11</sup>B from CeRu<sub>2</sub>Ga<sub>2</sub>B and LaRu<sub>2</sub>Al<sub>2</sub>B suggest that the Ce 4*f* electrons hardly contribute to the EFG on the B sites with very low hybridization with B 2*p* electrons, even if 4*f* itinerancy is assumed. The EFG  $V_{ZZ}$  on the B sites is ~1.4 × 10<sup>17</sup> V/cm<sup>2</sup>. In the case of the Ga sites, the <sup>69</sup> $v_Q$  yields  $V_{ZZ} \approx 1.0 \times 10^{17}$  V/cm<sup>2</sup>. The EFGs on the B and Ga sites are very similar.

Next, the static magnetic response to an applied field  $H_0(q = 0, \omega = 0)$  for CeRu<sub>2</sub>Ga<sub>2</sub>B is shown. The bulk magnetic susceptibility  $\chi(q = 0, \omega = 0) \equiv \chi(0, 0)$  along the a and c axes shows Curie-Weiss behavior in the paramagnetic state, as shown in Fig. 4. The Curie temperature  $T_{\rm C}$  in zero external field is estimated to be 16.3 K from specific heat measurements,<sup>4</sup> which corresponds to a sudden increase of M below  $\sim 20$  K in Fig. 4. T<sub>C</sub> rapidly broadens and slightly increases under an applied magnetic field, as expected for a ferromagnet. In this temperature region,  $\chi$  is strongly suppressed by applied field. The magnetic susceptibility along the c axis is much larger than that along the a axis below  $\sim$ 200 K. In the ordered state below T<sub>C</sub>, the magnetic anisotropy is uniaxial along the c axis. Curie-Weiss fits for the a and c axes data above 300 K lead to effective moments  $\mu_{\rm eff}$  of  $\sim 1.0 \ \mu_{\rm B}/{\rm Ce}$  and  $\sim 1.8 \ \mu_{\rm B}/{\rm Ce}$  and the Weiss temperatures  $\Theta$  of positive ~45 K and negative ~34 K, respectively. The temperature-independent term is fitted to be  $\chi_0 \sim 0.001$ emu/mol for both axes. The reduced effective moment from the free-ion Ce<sup>3+</sup> value of 2.54  $\mu_{\rm B}$  is suggested to originate



FIG. 3. (Color online) Temperature dependence of the nuclear quadrupolar frequency  $v_0$  for <sup>11</sup>B and <sup>69</sup>Ga.



FIG. 4. (Color online) Temperature dependence of magnetic susceptibility  $\chi \equiv M/H_0$  for a single crystal of CeRu<sub>2</sub>Ga<sub>2</sub>B measured at  $H_0 = 1$  kOe. The *T* axis is logarithmic.



FIG. 5. (Color online) Temperature dependence of Knight shifts for (a)  $^{11}$ B and (b)  $^{69}$ Ga in CeRu<sub>2</sub>Ga<sub>2</sub>B.

from the CEF effect, not due to hybridization.<sup>7</sup> The sign change of  $\Theta$  may suggest a competition between FM and AFM interactions. From the magnetization curve at 2 K up to 50 kOe using the polycrystalline sample, the saturated moment is roughly 1.25  $\mu_{\rm B}$ /Ce and the coercive magnetic force is very small, less than 0.2 kOe.<sup>4</sup> Probably the upturn in the static  $\chi_a$  below ~30 K may come from a small misalignment of the crystal relative to the external field since the Knight shift for <sup>11</sup>B-NMR corresponding to the  $\chi_a$  is nearly temperature independent, as shown below.

In Fig. 5 the temperature dependence of the Knight shift for <sup>11</sup>B and <sup>69</sup>Ga is shown, which are determined from the center NMR lines. In general, the Knight shift *K* reflects the local magnetic susceptibility on the nucleus due to the static field  $H_0$ , that is,  $K = A_{hf}\chi(0,0) \propto H_{local}$ , where  $A_{hf}$  is the hyperfine coupling constant. As seen in *K* for <sup>69</sup>Ga along the *c* direction, *K* is field dependent below ~30 K, similar to  $\chi(0,0)$ , that is, <sup>69</sup> $K_c$  in this temperature range is strongly suppressed by an applied field. Although <sup>69</sup> $K_a$  could not be determined, *K* for <sup>11</sup>B shows an Ising-type anisotropy along the *c* axis, which is similar to the static  $\chi(0,0)$ . <sup>11</sup> $K_a$  is nearly zero and almost temperature independent, as noted already.

The Knight shifts for <sup>11</sup>B and <sup>69</sup>Ga are plotted against the static susceptibility  $\chi$ , with temperature as an implicit parameter, to derive the hyperfine coupling constants, that is, the so-called K- $\chi$  plot as shown in Fig. 6. Since K and  $\chi$ 



FIG. 6. (Color online)  $K \cdot \chi$  plots for (a) <sup>11</sup>B and (b) <sup>69</sup>Ga in CeRu<sub>2</sub>Ga<sub>2</sub>B. The symbols are the same as in Fig. 5.

are field dependent below  $\sim 30$  K, a bending of  $K \cdot \chi$  is seen near  $\sim 30$  K. Here the data above 30 K are plotted. Above  $\sim 30$  K, the  $K \cdot \chi$  plots show a linear relationship which gives the hyperfine coupling constants  ${}^{11}A_{a,c} = 19$  kOe/ $\mu_{\rm B}$  and  ${}^{69}A_c = 30$  kOe/ $\mu_{\rm B}$ . The classical dipolar hyperfine coupling constants can be estimated to be at most  $\sim 0.3$  kOe/ $\mu_{\rm B}$  for the Ga sites and  $\sim 2$  kOe/ $\mu_{\rm B}$  for the B sites. Since these values are much smaller than the experimental values, the transferred hyperfine fields are mainly caused by RKKY-type oscillations through conduction electrons from Ce 4 f moments. As for  ${}^{11}A$ , since the  $K_a$  and  $\chi_a$  are located on an extension of the  $K_c$  vs  $\chi_c$  line as shown in Fig. 6(a), it is reasonable to assume that the coupling constant is isotropic. Therefore, anisotropy in the spin-lattice relaxation rates  $1/T_1$ , as shown later, cannot be explained by an anisotropy in hyperfine coupling constants.

## **B.** Zero-field NMR measurement

In ferromagnets, using the internal fields transferred on the nuclei, zero-field NMR measurement are possible at temperatures well below  $T_{\rm C}$ . As shown in Fig. 7, the frequencyswept NMR spectra at 3.3 K under zero applied field are successfully obtained for CeRu<sub>2</sub>Ga<sub>2</sub>B. Each line is quite narrow, with a width about 100 kHz, which reflects the good sample quality. It is noted that no NMR lines were observed in the frequency range 16 to ~35 MHz. The NMR signal under



FIG. 7. (Color online) Zero applied field NMR spectra taken at 3.3 K. The site assignments for the observed lines are indicated. The solid curves and hatched Lorentzians are drawn based on a simulation with the natural width of 100 kHz.

zero field is observable up to  $\sim$ 13.5 K. The signal above 14 K cannot be detected because the relaxation rates become shorter.

In this frequency range, six NMR lines are observed, which are successfully assigned to <sup>69,71</sup>Ga as indicated in Fig. 7. The spectra can be explained by the internal field  $H_{int}$  on the Ga sites parallel to the *c* axis. The  $v_Q$  and  $H_{int}$  are estimated by numerical diagonalization of the Hamiltonian matrix, including Zeeman ( $\gamma_N H_{int}$ ) and quadrupolar terms. The assignment is fully validated by the ratio of central frequencies for <sup>69,71</sup>Ga corresponding to the ratio of gyromagnetic ratios  $\gamma_N$  and the ratio of the width between satellite frequencies corresponding to the ratios of quadrupolar moment Q.

In ferromagnets, rf fields  $(H_1)$  for the nuclear spin excitation are effectively enhanced due to the electronic spin oscillations which give an enhancement factor of  $\sim 10-100$  and/or due to FM domain wall motion which gives a factor of  $10^3-10^4$  to the "bare"  $H_1$ . This is the so-called  $H_1$  enhancement. In the ligand NMR, the former enhancement by on-site electronic oscillations would be small. Indeed, in the present case, the  $H_1$  enhancement is not so large (it is less than a factor of 10, at most) as compared with the pulse conditions in paramagnetic materials. The FM softness with low coercive magnetic force and the good purity without domain wall pinning by impurities are also known to reduce the enhancement factor by domain wall motions.

The obtained  $v_Q$  values of ~2.8 MHz in the ordered state are plotted in Fig. 3 and are a bit larger than the estimate of ~2.4 MHz in the paramagnetic state, even if errors due to misalignment are considered in the case of NMR under applied fields. A small change of EFG may result from a lattice expansion below  $T_C$ , which could occur if the FM phase transition is first order, although the local site symmetry on Ga sites remains tetragonal through  $T_C$  according to the NMR spectra. It may be interesting to determine the volume change by thermal expansion measurements.

The estimated internal field  $H_{int}$  from  $v_{res}/\gamma_N$  is plotted against temperature in Fig. 8. Below ~8 K,  $H_{int}$  is almost saturated to 9.6 kOe. Again, it cannot be explained by the classical dipolar fields from Ce ions with about 1  $\mu_B$ . The hyperfine mechanism should be due to the RKKY interaction through the conduction electrons, meaning that it would be predominantly isotropic. If we adopt the hyperfine coupling



FIG. 8. (Color online) Temperature dependence of the transferred internal field on the Ga sites. The dotted curve is a guide to eyes.

constant obtained in the paramagnetic state, the ordered moment can be estimated to be 1.3  $\mu_{\rm B}/{\rm Ce}$  with the hyperfine coupling constant  ${}^{69}A'_c = {}^{69}A_c/4$  divided by the number of nearest-neighboring Ce ions from the Ga sites. This estimate of the ordered moment is in good agreement with the saturation moment in magnetization measurements.<sup>4</sup> Thus, in the ordered state, the NMR spectra can be well understood by localized moments on Ce ions.

In the ordered state below  $T_{\rm C}$ , there is no additional anomaly in the temperature dependence of  $H_{\rm int}$  and  $\nu_{\rm Q}$ , although a small anomaly around 6 K in specific heat and magnetization measurements<sup>4</sup> is reported. The origin of the 6 K anomaly is not clear.

### C. Dynamic magnetic response

To deduce the dynamic magnetism, the nuclear spin-lattice relaxation rates  $1/T_1$  are measured on the <sup>69</sup>Ga sites under applied fields of ~35 and ~72 kOe, and under zero applied field. Figure 9(a) shows the temperature dependence of  $1/T_1$  for <sup>69</sup>Ga. In the paramagnetic state,  $1/T_1$  for <sup>11</sup>B is also measured as shown in Fig. 9(b).

Above  $T_{\rm C}$ , as seen in  $1/^{69}T_1$ , an external field suppresses  $1/T_1$  significantly in the temperature region below ~40 K. This means that an applied field quickly quenches the lowenergy spin fluctuations in the FM enhanced susceptibility around q = 0. Such a suppression of  $1/T_1$  has been widely observed in FM materials. Thus, the dynamical susceptibility is ferromagnetically enhanced below ~40 K. Above ~40 K,  $1/T_1$  becomes rather field independent. Interestingly,  $1/^{11,69}T_1$ decreases above ~40 K as temperature increases. Typically in the localized case of 4f electrons, only fluctuations by the intersite exchange interaction  $J_{\rm ex}$  govern the  $T_1$  process, and  $1/T_1$  becomes temperature region should originate partly from the relaxation dominated by intrasite exchange  $J_{\rm cf}$  via conduction electrons.

In general, NMR  $1/T_1$  can be expressed<sup>12</sup> as

$$\frac{1}{T_1} = \frac{k_{\rm B}T}{(\gamma_{\rm e}\hbar)^2} 2(\gamma_{\rm N}A_{\perp})^2 \sum_{\boldsymbol{q}} f_{\perp}^2(\boldsymbol{q}) \frac{{\rm Im}\chi_{\perp}(\boldsymbol{q},\omega_0)}{\omega_0}, \qquad (1)$$



FIG. 9. (Color online) (a) Temperature dependence of the nuclear spin-lattice relaxation rates  $1/T_1$  for <sup>69</sup>Ga, and (b) for <sup>11</sup>B in CeRu<sub>2</sub>Ga<sub>2</sub>B. The dotted curve is a guide to eyes for extrapolation of  $1/T_1$  in zero field. The cross marks (×) indicate the estimates for <sup>69</sup>Ga in the case of  $H_0 \parallel a$  from the observed values for <sup>11</sup>B.

where  $\gamma_e$  is the electronic gyromagnetic ratio,  $f_{\alpha}(q)$  is the hyperfine form factor,  $\text{Im}\chi(q,\omega_0)$  is the imaginary part of dynamical susceptibility,  $\omega_0$  is the nuclear Larmor frequency, and the suffix  $\perp$  refers to the component perpendicular to the quantization axis. In this case, since the principal mode of spin fluctuations is FM (q = 0), f(q) can be set to unity for simplicity. The corresponding  $1/T_1$  for <sup>71</sup>Ga in the paramagnetic state (not shown) is larger by a factor of  $\gamma_N^2$ . Thus, the relaxation mechanism is confirmed to be magnetic and the uniform dynamical susceptibility of 4f electrons governs the  $T_1$  process.

To discuss the anisotropy of the dynamical susceptibility, a new rate  $R_i$  along the quantization *i* axis is defined as  $R_i \equiv k(\gamma_N A_i)^2 \sum_{\mathbf{q}} \text{Im}\chi_i(\mathbf{q},\omega_0)/\omega_0$  (i = a, c) with a numerical constant *k* of  $k_B/(\gamma_c \hbar)^2$ . Then, from Eq. (1),  $(1/T_1T)_{H_0||c} = 2R_a$ and  $(1/T_1T)_{H_0||a} = R_a + R_c$  are given. In this way, the  $R_i$ divided by  $(\gamma_N A_i)^2$  corresponding to the  $\sum_{\mathbf{q}} \text{Im}\chi_i(\mathbf{q},\omega)$  are decomposed from the anisotropy in  $1/T_1$ , as shown in Fig. 10. Here  $A_a$  for <sup>69</sup>Ga is assumed again to be  $A_a = A_c$ . Since  $R_a/(\gamma_N A_a)^2$  from <sup>69</sup>Ga NMR is in good agreement with that from <sup>11</sup>B NMR, this assumption is justified. As shown in Fig. 10,  $\sum_{\mathbf{q}} \text{Im}\chi_c(\mathbf{q},\omega)$  is much larger than  $\sum_{\mathbf{q}} \text{Im}\chi_a(\mathbf{q},\omega)$ , that is, the *c*-axis spin fluctuations are dominant in CeRu<sub>2</sub>Ga<sub>2</sub>B and the 4*f* electron pseudospin also fluctuates with an Isingtype magnetic anisotropy even in the paramagnetic state. A comparison of  $R_i$  with the Knight shifts for <sup>11</sup>B is shown



FIG. 10. (Color online) (a) The temperature dependence of deduced  $R_i/(\gamma_N A_i)^2$  (i = a, c) for <sup>11</sup>B and  $R_a/(\gamma_N A_a)^2$  for <sup>69</sup>Ga corresponding to the **q**-summed imaginary part of dynamical susceptibility for the quantization *i* axis. See text for the detailed definition of  $R_i$ . (b) A comparison of anisotropy for  $R_i$  with the Knight shifts for <sup>11</sup>B corresponding to the static susceptibility  $\chi$ .

in Fig. 10(b). In the case of an itinerant FM,  $\sum_{q} \text{Im}\chi(q,\omega)$  should be simply proportional to the static susceptibility  $\chi(0,0) \propto K$ .<sup>13</sup> For example, such a scaling between  $\chi$  and  $R_i$  is seen in itinerant FM systems (e.g., UCoGe).<sup>14</sup> As shown in Fig. 10(b), however, this is clearly not the case for CeRu<sub>2</sub>Ga<sub>2</sub>B since the  $R_i$  do not scale with  $K_i$ .

With the obtained  $R_a$  and  $R_c$  from <sup>11</sup>B NMR, the unobservable  $1/T_1$  along the *a* axis for <sup>69</sup>Ga can be estimated, as plotted in Fig. 9. These  $1/T_1$  values do not exceed the NMR observable limit, which is roughly  $10^4$  s<sup>-1</sup>. Therefore, the main reason why the signal of <sup>69</sup>Ga is missed in the case of  $H_0 \parallel a$  is that the spin-spin relaxation rate  $1/T_2$  is too fast, that is, a much shorter separation  $\tau$  may be required but is experimentally limited.

In the high temperature region above ~40 K (well above  $T_{\rm C}$ ), the nuclear-spin relaxation can be regarded as being driven by fluctuations of the Ce local moments. In the simplified model for localized 4f electrons, assuming the isotropic hyperfine coupling  $A_{\rm iso}$  and q-independent  $\chi(q,\omega)$ ,  $1/T_1$  is known to be expressed from Eq. (1) as<sup>15</sup>

$$\frac{1}{T_{\rm l}} = \frac{\sqrt{2\pi} (\gamma_{\rm N} A_{\rm iso}/z')^2 p_{\rm ord}^2}{3\omega_{\rm fl}},$$
(2)

where  $\omega_{\rm fl}$  is the local-moment fluctuation rate,  $p_{\rm ord}$  is the ordered moment, and z' is the number of Ce ions around the nuclear sites.  $\omega_{\rm fl}$  is given by two major processes, that is,  $\omega_{\rm fl} = \omega_{\rm ex} + \omega_{\rm cf}$ . The  $\omega_{\rm ex}$  represents a fluctuation process caused by the intersite RKKY exchange interaction  $J_{\rm ex}$ , which is denoted as  $(\hbar\omega_{\rm ex})^2 = (2z/3\hbar^2)(J_{\rm ex}p_{\rm ord})^2$ , with z being the number of nearest-neighboring Ce ions. On the other hand,  $\omega_{\rm cf}$  is due to the spin-exchange interaction with conduction electrons and is written as  $\hbar\omega_{\rm cf} \approx (\pi/\hbar)(J_{\rm cf}\rho)^2 k_{\rm B}T$ , where  $J_{\rm cf}$  is the intrasite spin-exchange coupling between the Ce



FIG. 11. (Color online) (a) Temperature dependence of powder averaged  $\omega_{\rm fl} \propto T_1$  by <sup>11</sup>B NMR in CeRu<sub>2</sub>Ga<sub>2</sub>B.

local moments and conduction electrons.  $\omega_{cf}$  thus provides a *T*-linear dependence for  $T_1$ . Assuming the ordered moment is  $1.3 \,\mu_B/\text{Ce}$ , the temperature dependence of  $\omega_{fl}$  derived from the powder averaged  $1/T_1$  for <sup>11</sup>B is plotted as shown in Fig. 11, which can be fitted by  $\alpha + \beta T$ . The obtained  $\alpha = 6 \times 10^{12}$  s<sup>-1</sup> yields  $|J_{ex}|/k_B \sim 20$  K, which is the same order as  $T_C$ . The  $\beta = 3 \times 10^{11} \text{ s}^{-1} \text{ K}^{-1}$  gives an apparent estimate of  $J_{cf}\rho \sim 0.85$ , which is larger than typical for heavy fermion systems. For example, in the heavy fermion systems such as CeCu<sub>2</sub>Si<sub>2</sub>, UBe<sub>13</sub>, and CeCoIn<sub>5</sub>,  $J_{cf}\rho$  ranges in value from 0.1 to 0.2.<sup>16</sup>

This apparent value of  $J_{cf}\rho$  may be useful for a systematic comparison in the  $LnRu_2X_2X'$  (Ln = La, Ce, Pr, ...; X =Al, Ga; X' = B, C) series. For example, systematic NMR investigations of  $LnRh_3B_2^{17}$  may suggest that the strong hybridization of f electrons with conduction electrons causes a small ordered moment of ~0.38  $\mu_{\rm B}/{\rm Ce}$  as  $J_{\rm cf}\rho$  increases. Indeed, such a Korringa behavior, that is, a T-independent  $(T_1T)^{-1}$  corresponding to strong hybridization in the high temperature region, is seen in the highest  $T_{\rm C}$  of Ce-based FM materials CeRh<sub>3</sub>B<sub>2</sub> with  $T_{\rm C} \sim 112$  K.<sup>17,18</sup> Moreover, in CeRh<sub>3</sub>B<sub>2</sub>, by applying pressure (P), a decrease of  $T_{\rm C}$  is observed around  $J_{\rm cf} \sim 1.1 J_0~(P \sim 3.5~{\rm GPa})$  and the disappearance of  $T_{\rm C}$  around  $J_{\rm cf} \sim 1.2 J_0$  ( $P \sim 7$  GPa), where  $J_0$  is the value of  $J_{cf}$  under ambient pressure.<sup>19</sup> Thus, the shift of the apparent  $J_{cf}\rho$  by pressures or substitutions may become an indicator of proximity to FM quantum criticality.

As a last remark, in the ordered state below  $T_{\rm C}$ ,  $1/^{69}T_1$  decreases steeply as temperature decreases, and follows the power law  $T^5$ , as shown in Fig. 9(a). In a FM ordered state of localized moments, a two-magnon Raman or three-magnon process usually governs the relaxation mechanism, which yields  $T^2$  or  $T^{7/2}$  behavior, respectively.<sup>20</sup> In this case,

the steeper exponent of 5 may suggest that the relaxation mechanism is not governed by such a simple magnon process. Perhaps the strong Ising-type anisotropy and the polarization of the conduction bands in the FM ordered state may have to be considered to explain the  $T^5$  behavior for this system.

# **IV. SUMMARY**

<sup>11</sup>B and <sup>69,71</sup>Ga NMR measurements have been performed on the Ce-based FM system CeRu<sub>2</sub>Ga<sub>2</sub>B with  $T_{\rm C}(H_0 = 0) =$ 16.3 K. The values of  $v_0$  for <sup>11</sup>B and <sup>69</sup>Ga are estimated from the NMR spectra under applied fields. Isotropic hyperfine coupling constants are determined for <sup>11</sup>B and <sup>69</sup>Ga in the paramagnetic state through Knight shift measurements. The zero applied field NMR spectra for <sup>69,71</sup>Ga are successfully obtained, which gives precise values of the internal field on the Ga sites. At the same time, somewhat larger values of  $v_{\rm O}$  for <sup>69</sup>Ga are obtained, which may suggest magnetovolume expansion without symmetry lowering. Nuclear spin-lattice relaxation  $1/T_1$  measurements reveal the Ising-type anisotropy for the FM spin fluctuations. The absolute values and temperature dependence of  $1/T_1$  suggest a well-localized 4f picture for this system: The local moments of Ce<sup>3+</sup> fluctuate as a result of FM intersite coupling ( $J_{\rm RKKY} \sim 20$  K) above  $T_{\rm C}$  and individually fluctuate due to intrasite coupling  $J_{cf}$  well above  $T_{\rm C}$ . Thus, this NMR study has microscopically characterized the static and dynamic magnetic responses in the new Ce-based ferromagnet CeRu2Ga2B and provides the basis to understand this new series of  $\text{CeRu}_2 X_2 X'$  compounds.

# ACKNOWLEDGMENTS

We would like to thank Y. Haga, H. Chudo, and H. Yasuoka for stimulating discussions and suggestions. A part of this work was supported by a Grant-in-Aid for Scientific Research on Innovative Areas Heavy Electrons (No. 20102006 and No. 20102007) by the MEXT of Japan. This research was also partially supported by the REIMEI Research Program of JAEA. Work at Los Alamos National Laboratory was performed under the auspices of the US Department of Energy, Office of Basic Energy Sciences, Division of Materials Sciences and Engineering, PECASE funding from the US DOE, OBES, Division of Material Science and Engineering, and funded in part by the Los Alamos Laboratory Directed Research and Development program.

\*sakai.hironori@jaea.go.jp

- <sup>1</sup>S. Kambe, H. Sakai, Y. Tokunaga, T. Fujimoto, R. E. Walstedt, S. Ikeda, D. Aoki, Y. Homma, Y. Haga, Y. Shiokawa *et al.*, Phys. Rev. B **75**, 140509(R) (2007).
- <sup>2</sup>S.-H. Baek, H. Sakai, E. D. Bauer, J. N. Mitchell, J. A. Kennison, F. Ronning, and J. D. Thompson, Phys. Rev. Lett. **105**, 217002 (2010).
- <sup>3</sup>H. Sakai, S. Kambe, Y. Tokunaga, Y. Haga, S.-H. Baek, F. Ronning, E. D. Bauer, and J. D. Thompson, Mater. Res. Soc. Symp. Proc. **1264**, 69 (2010).
- <sup>4</sup>R. E. Baumbach, T. Shang, M. Torrez, F. Ronning, J. D. Thompson, and E. D. Bauer, J. Phys.: Condens. Matter **24**, 285702 (2012).

- <sup>5</sup>R. E. Baumbach, H. Chudo, H. Yasuoka, F. Ronning, E. D. Bauer, and J. D. Thompson, Phys. Rev. B **85**, 094422 (2012).
- <sup>6</sup>E. Matsuoka, Y. Tomiyama, H. Sugawara, T. Sakurai, and H. Ohta, J. Phys. Soc. Jpn. **81**, 043704 (2012).
- <sup>7</sup>H. Matsuno, H. Nohara, H. Kotegawa, E. Matsuoka, Y. Tomiyama, H. Sugawara, H. Harima, and H. Tou, J. Phys. Soc. Jpn. 81, 073705
- (2012).
- <sup>8</sup>R. E. Baumbach, X. Lu, F. Ronning, J. D. Thompson, and E. D. Bauer, J. Phys.: Condens. Matter **24**, 325601 (2012).
- <sup>9</sup>J. V. Zaikina, Y.-J. Jo, and S. E. Latturner, Inorg. Chem **49**, 2773 (2010).

- <sup>10</sup>H. F. Braun and J. L. Jorda, Physica B+C **135**, 72 (1985).
- <sup>11</sup>C. Petrovic, P. G. Pagliuso, M. F. Hundley, R. Movshovich, J. L. Sarrao, J. D. Thompson, Z. Fisk, and P. Monthoux, J. Phys.: Condens. Matter **13**, L337 (2001).
- <sup>12</sup>T. Moriya, J. Phys. Soc. Jpn. 18, 516 (1963).
- <sup>13</sup>T. Moriya, J. Magn. Magn. Mater. **100**, 261 (1991).
- <sup>14</sup>Y. Ihara, T. Hattori, K. Ishida, Y. Nakai, E. Osaki, K. Deguchi, N. K. Sato, and I. Satoh, Phys. Rev. Lett. **105**, 206403 (2010).
- <sup>15</sup>T. Moriya, Prog. Theor. Phys. 16, 23,641 (1956).

- <sup>16</sup>Y. feng Yang, Z. Fisk, H.-O. Lee, J. D. Thompson, and D. Pines, Nature (London) **454**, 611 (2008).
- <sup>17</sup>Y. Kishimoto, Y. Kawasaki, and T. Ohno, J. Phys. Soc. Jpn. **73**, 1970 (2004).
- <sup>18</sup>Y. Kitaoka, Y. Kishimoto, K. Asayama, T. Kohara, K. Takeda, R. Vijayaraghavan, S. K. Malik, S. K. Dhar, and D. Rambabu, J. Magn. Magn. Mater. **52**, 449 (1985).
- <sup>19</sup>A. L. Cornelius and J. S. Schilling, Phys. Rev. B 49, 3955 (1994).
- <sup>20</sup>D. Beeman and P. Pincus, Phys. Rev. **166**, 359 (1968).