



## Nonstoichiometric doping and Bi antisite defect in single crystal $\text{Bi}_2\text{Se}_3$

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We studied the defects of  $\text{Bi}_2\text{Se}_3$  generated from Bridgman growth of stoichiometric and nonstoichiometric self-fluxes. Growth habit, lattice size, and transport properties are strongly affected by the types of defects generated. Major defect types of the  $\text{Bi}_{\text{Se}}$  antisite and partial  $\text{Bi}_2$ -layer intercalation are identified through combined studies of direct atomic-scale imaging with scanning transmission electron microscopy in conjunction with energy-dispersive x-ray spectroscopy, x-ray diffraction, and Hall effect measurements. We propose a consistent explanation to the origin of defect type, growth morphology, and transport property.

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$\text{Bi}_2\text{Se}_3$  is a second-generation topological insulator with a nearly idealized single Dirac cone.<sup>1</sup>  $\text{Bi}_2\text{Se}_3$  is also the sister compound of  $\text{Bi}_2\text{Te}_3$ , which has been demonstrated to show a high thermoelectric figure of merit ( $ZT$ ) for commercial applications.<sup>2</sup> Both  $\text{Bi}_2\text{Se}_3$  and  $\text{Bi}_2\text{Te}_3$  samples show a nearly identical crystal structure composed of Bi-(Se,Te) quintuple layers with a van der Waals gap between Se(Te)1, as shown in Fig. 1(a). While  $\text{Bi}_2\text{Te}_3$  has been shown with  $n$ - or  $p$ -type conduction through fine tuning of the nonstoichiometry of the Bi/Te ratio, i.e., to dope the system by generating antisite defects of  $\text{Bi}_{\text{Te}}$  ( $p$  type) or  $\text{Te}_{\text{Bi}}$  ( $n$  type),<sup>3</sup> all  $\text{Bi}_2\text{Se}_3$  samples reported since 1960 have shown  $n$ -type semiconducting behavior without exception, and the lowest  $n$ -type carrier concentration reported is at the order of  $10^{16}$ – $10^{17}$   $\text{cm}^{-3}$ .<sup>4</sup>

A topological insulator is expected to be a band insulator with surface conduction and a spin-polarized surface state.<sup>1</sup> When the Fermi level is higher in the conduction band as a result of intrinsic  $n$ -type doping, it becomes difficult to interpret data for results containing contributions from both the bulk and the surface. Angle resolved photoemission spectroscopy (ARPES) studies require  $n$ -type doping to map out the shape of the Dirac cone for  $\text{Bi}_2\text{Se}_3$ , but transport property measurement faces more challenges on distinguishing conductivities from the bulk and the surface. Additional hole doping methods through Ca substitution and  $\text{NO}_2$  oxidation have been applied to provide the necessary fine tuning of the Fermi level near the Dirac cone.<sup>5,6</sup> It is desirable to have complete carrier type and level control for the topological insulator  $\text{Bi}_2\text{Se}_3$  at the stage of crystal growth.

In an effort to grow  $\text{Bi}_2\text{Se}_3$  single crystals of controlled carrier type and level for surface-sensitive studies, and to clarify the nature of defects responsible for the persistent  $n$ -type character, we have studied single crystals grown using the Bridgman technique with intentionally generated defects through nonstoichiometric self-fluxes. With the integrated studies of direct defect observation through scanning transmission electron microscopy in conjunction with energy-dispersive x-ray spectroscopy (STEM-EDX) imaging, x-ray diffraction lattice size analysis, and transport property investigation, we were able to find reasonable correlations

between the observed physical properties and the distribution of defects in the form of either a  $\text{Bi}_{\text{Se}}$  antisite or partially intercalated  $\text{Bi}_2$ -layer patches.

Single crystals studied in this Rapid Communication were grown using the vertical Bridgman method. The initial compounds were high purity bismuth (99.999%) and selenium (99.999%) powder mixed thoroughly in an argon-filled glove box. Three groups of sample were prepared in different Bi:Se molar ratios, including Bi:Se molar ratios of  $\text{Bi} : \text{Se} = 2 : 3$ ,  $(2 + x) : 3$ , and  $2 : (3 + x)$  with  $x = 0.05$ – $0.2$ . The mixed powder was sealed in quartz tubes under a vacuum of about  $3 \times 10^{-2}$  Torr after multiple argon gas purging cycles, preacted at  $650^\circ\text{C}$  for 18 h in a box furnace, and furnace cooled to room temperature. Single crystals were grown with a vertical Bridgman furnace starting from the preacted powder and vacuum sealed in quartz tubes 10 cm long and of 1.6 cm inner diameter. The temperature profile of the Bridgman furnace used for the whole series was maintained at  $850$ – $650^\circ\text{C}$  within 25 cm. Initial complete melting was achieved at  $850^\circ\text{C}$  for 24 h to ensure complete reaction and mixing. The temperature gradient of  $1^\circ\text{C}/\text{cm}$  was programmed around the solidification point near  $705^\circ\text{C}$ , and the quartz tube was then slowly lowered into the cooling zone at a rate of  $\sim 0.5$  mm/h. The crystal structure was examined by x-ray diffraction with an in-house powder x-ray diffractometer (Bruker D8). Transport properties were examined using a standard four-probe lock-in technique with a magnetic field up to 2 T and temperature down to 2 K. High-angle annular dark-field (HAADF) imaging and chemical mapping at atomic-column resolution were performed with a JEOL-2100F microscope equipped with a probe Cs corrector in conjunction with EDX, as detailed previously.<sup>7</sup> A chemical analysis was performed using electron probe microanalysis (EPMA) on pieces separated from the as-grown cone-shaped solidified boule. It is interesting to note that the Se-rich flux growth shows mostly growth morphology, but not always, with the (001) plane index perpendicular to the growth direction, as shown in Fig. 1(b). On the other hand, the growth from the Bi-rich flux has a (001) plane index always parallel to the growth direction and can be cleaved easily into parallel disks, as shown in Fig. 1(c).

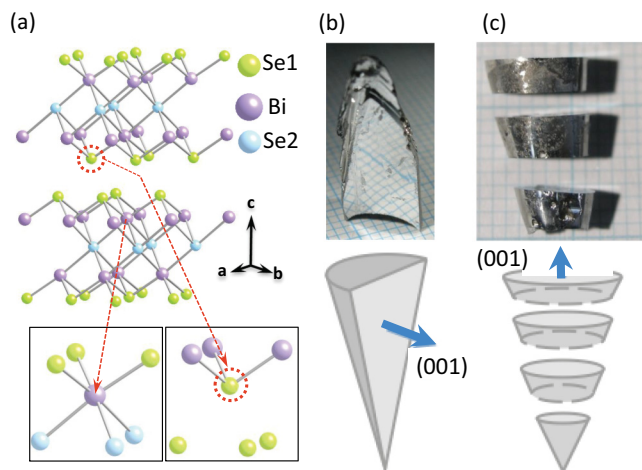


FIG. 1. (Color online) (a) The crystal structure of  $\text{Bi}_2\text{Se}_3$  can be described with space group  $R\bar{3}m$ , where the quintuple layer is the building block with Se2 (blue) in the middle and Se1 (green) near the van der Waals gap. The inset shows the  $\text{BiSe}_6$  octahedron and the Se1 (or  $\text{BiSe}_1$  antisite in dashed circle) environment. (b) Crystals grown using  $\text{Bi} : \text{Se} = 2 : 3$  and  $2 : (3 + x)$  of stoichiometric and Se-rich fluxes, with a (001) plane index mostly perpendicular to the growth direction. (c) Crystals grown using  $\text{Bi} : \text{Se} = (2 + x) : 3$  of Bi-rich flux show a (001) plane index along the growth direction.

STEM-HAADF images for samples selected from different initial growth flux ratios and positions are summarized in Fig. 2. Figure 2(a) can be viewed as the [100] projection sequenced as quintuple Se1-Bi-Se2-Bi-Se1, which shows two bright spots corresponding to the heavier Bi atoms and the three weaker ones corresponding to the Se atoms as expected, as well as the van der Waals gaps in between the quintuple layers. For crystals grown from Bi-rich flux at lower magnification, as shown in Fig. 2(b), bright domain boundaries can be found and verified to be Bi by using STEM-EDX characterizations. As expected for the Bi-rich flux growth, the excess Bi may aggregate into grain boundaries during cooling, most probably due to the low melting point of Bi (271 °C), while crystal solidification occurs near 705 °C. Moreover, a low density of  $\text{Bi}_2$ -layer patches was found sporadically in the van der Waals gap, for both the Bi- and Se-rich flux grown crystals, as shown in Fig. 2(c). To accommodate the intercalated  $\text{Bi}_2$ -layer patches, the quintuple units near the enlarged van der Waals gap are locally distorted. Interestingly, large areas of structures free from imperfections could only be found after 300 °C annealing for both the Se- and Bi-rich grown crystals, as shown in Fig. 2(d), which indicates that both Bi excess in the grain boundaries and the intercalated  $\text{Bi}_2$ -layer patches had been removed accordingly.

The lattice parameters of the  $c$  axis have been examined using x-ray diffraction for pieces selected from different sections of the grown boule. An additional annealing process has been applied at 300–600 °C in an evacuated sealed tube for part of the as-grown crystals. The lattice parameters are summarized in Fig. 3 and plotted in the  $a$  and  $c$  axes against lattice volume. Interestingly, all studied samples are clustered in groups of Bi-rich flux growth before annealing (Bi-rich), Se-rich flux growth before annealing (Se-rich), and Se-rich

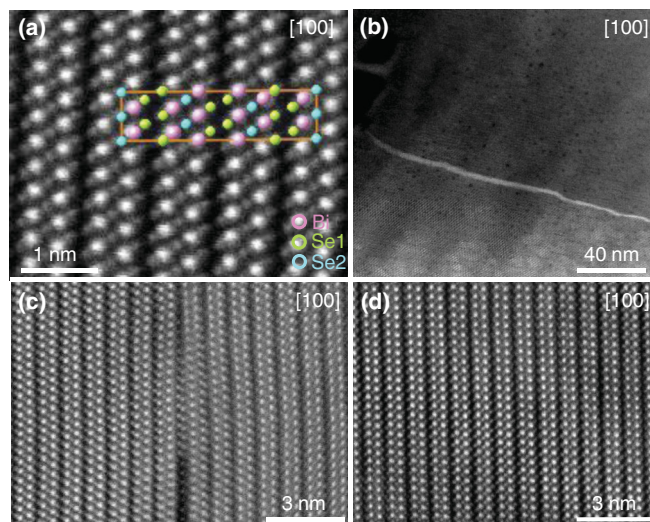


FIG. 2. (Color online) STEM-HAADF images of  $\text{Bi}_2\text{Se}_3$ . (a) A high resolution image shows that the quintuple of  $\text{Bi}_2\text{Se}_3$  consists of two bright spots (Bi) and three fainter spots (Se). (b) For the Bi-rich flux growth, a high density of Bi can be found in the grain boundary, as shown by the thick and bright lines at low magnification. (c) A low density of  $\text{Bi}_2$ -layer intercalated patches can always be found in the van der Waals gap for the as-grown crystals, whether using Bi- or Se-rich flux. The intercalated  $\text{Bi}_2$ -layer patches would deform the quintuple layer locally by opening up the van der Waals gap. (d) A large area of perfectly ordered quintuple layers without intercalated  $\text{Bi}_2$ -layer patch induced deformation can be found in samples after 300 °C annealing.

plus 300–600 °C postannealing (Se-rich + 300–600 °C), in a trend of increasing volume and  $c$  axis. In addition, a collection of lattice parameters of  $\text{Bi}_2\text{Se}_3$  published since 1960 are displayed together and are found to fall nicely along the same increasing trend.<sup>8</sup> It is clear that many of the inconsistent results published previously could be due to the subtle differences in the nonstoichiometry of Bi and Se.

We may postulate that the reason why crystals from Bi-rich flux growth have longer  $c$  axes is due to the larger amount of Bi intercalated into the van der Waals gaps, mostly in the form of randomly distributed patches of the neutral metal  $\text{Bi}_2$  layer as revealed in the STEM picture of Fig. 2(c), but not enough to form the metastable phases of staged  $(\text{Bi}_2)_m(\text{Bi}_2\text{Se}_3)_n$  at the high solidification point near 705 °C.<sup>9</sup> It should be noted that the staged phases beyond  $\text{Bi}_2\text{Se}_3$  can only be prepared at a much lower temperature range of ~400–560 °C as intercalated metastable compounds.<sup>10</sup> In particular, the average lattice volume increase should be viewed as randomly distributed intercalated  $\text{Bi}_2$ -layer patches without changing the original  $R\bar{3}m$  symmetry, especially when the local dilation of the van der Waals gap occurs only near regions with intercalated  $\text{Bi}_2$ -layer patches. In addition, 300 °C annealing reduces the lattice size significantly, which indicates that a small amount of intercalated Bi can be removed effectively with a temperature above the melting point of Bi, as supported also by the creation of a large area of the defect-free structure after 300 °C annealing, as shown in Fig. 2(d). On the other hand, a high annealing temperature up to 600 °C starts to partially decompose the sample, presumably as a result of too many

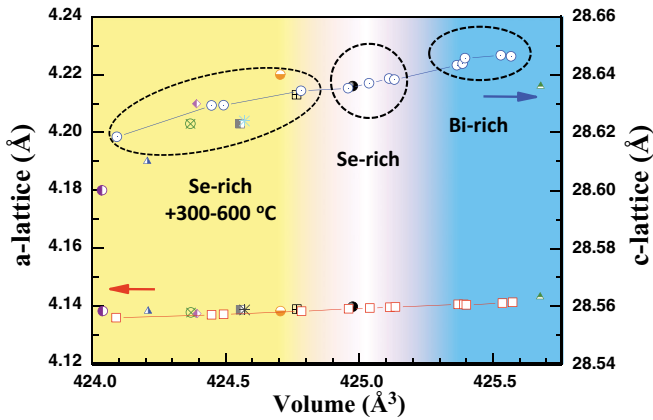


FIG. 3. (Color online) Lattice parameters vs lattice volume of all crystals studied, where  $c$  axes are shown as empty circles and  $a$  axes are shown as empty squares. All studied samples are clustered in groups of Bi-rich flux growth before annealing (Bi-rich), Se-rich flux growth before annealing (Se-rich), and Se-rich plus post annealing at 300–600 °C (Se-rich + 300–600 °C), in an increasing trend, as indicated by the connected experimental data points. A list of  $\text{Bi}_2\text{Se}_3$  lattice parameters reported in the literature since 1960 are shown as various solid symbols (Ref. 8).

Se vacancies created in an evacuated environment, which has also been verified by thermogravimetric analysis under argon flow with the following x-ray structure analysis.

All single crystal samples show metallic behavior down to about 20 K (not shown—similar to those published earlier),<sup>11</sup> below which the resistivity  $\rho$  becomes nearly temperature independent, as expected in the impurity scattering regime. Figure 4 summarizes the relationship between carrier concentration  $n$  and mobility  $\mu$  for all samples studied. The carrier concentration  $n$  was determined from a Hall effect measurement at 2 K, and the corresponding Drude mobility  $\mu$  was estimated using the Drude formula  $1/\rho = ne\mu$ . For the stoichiometric and Se-rich flux growth, samples are clustered at a low carrier concentration of  $\sim 5 \times 10^{18}/\text{cm}^3$  and a high mobility regime. On the other hand, crystals grown from Bi-rich flux have the highest carrier concentrations and the lowest mobility. In addition, 300 °C annealing has no significant impact on the already low carrier concentration from Se-rich flux growth, while the carrier concentrations for Bi-rich flux grown crystals are reduced to a common lower level near  $\sim 15 \times 10^{18}/\text{cm}^3$ .

Based on evidences from partial decomposition after 600 °C annealing in an evacuated tube, thermogravimetric analysis, and lattice size analysis, Se vacancy must be limited to a low threshold before the occurrence of decomposition. This is because Se has a vapor point of 685 °C, below the solidification point of  $\text{Bi}_2\text{Se}_3$  near 705 °C, which leads to the occurrence of solidification at the liquid-gas phase boundary in the Bridgman growth. It is nearly impossible to maintain a perfect Bi-Se stoichiometry upon Bridgman solidification near 705 °C, especially for the relatively weakly bonded Se1 at the van der Waals gap. We conclude that the Se vacancy is impossible to avoid under the current Bridgman growth condition of limited Se vapor pressure. The Se vacancy level must be determined mainly by the Se partial pressure during Bridgman growth,

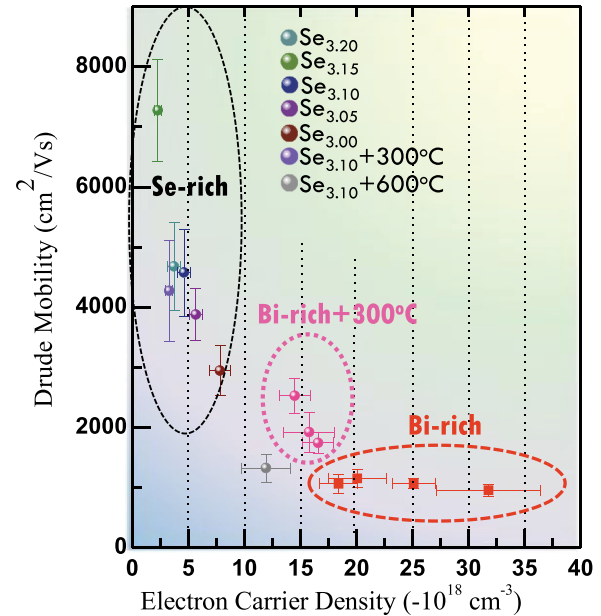


FIG. 4. (Color online) Drude mobility ( $\mu$ ) vs carrier concentration ( $n$ ) for all samples studied are shown; all are  $n$  type. Crystals grown from Bi-rich flux (Bi-rich) have the highest carrier concentration but the lowest mobility, and 300 °C postannealing (Bi-rich + 300 °C) reduces the carrier concentrations to the same level of  $\sim 15 \times 10^{18}$ . Crystals from stoichiometric and Se-rich flux growth (Se-rich) have the lowest carrier concentration and highest mobility, and the 300 °C postannealing ( $\text{Se}_{3.10} + 300$  °C) shows no significant impact on modifying the carrier concentration and mobility.

instead of the initial Bi to Se ratio, not to mention the fact that the liquid Bi in the flux prefers to intercalate into the van der Waals gap after the  $\text{Bi}_2\text{Se}_3$  solidification, instead of forming a Bi-Se quintuple layer of a high Se vacancy level. Although lacking rigorous quantitative evidence, current results seem to agree with the commonly accepted assumption that  $n$ -type carriers are generated from Se-vacancy formation, i.e., each Se vacancy donates at most two itinerant electrons as  $\text{Se}_{\text{Se}} \rightleftharpoons V_{\text{Se}}^{\cdot\cdot} + \text{Se}_{(\text{g})} + 2e^-$  in the Kroger-Vink notation of various doping efficiencies.<sup>12</sup>

In addition to the finding of intercalated  $\text{Bi}_2$ -layer patches, as revealed in Fig. 2(c), we also observed  $\text{Bi}_{\text{Se}}$  antisite defects in the bulk of  $\sim 25$  nm thickness along the incident beam direction, as shown in Fig. 5, using atomically resolved STEM-EDX mapping. We notice that some columns of the supposed Se1 arrays near the van der Waals gap show an unexpected enhanced contrast, as shown in Fig. 5(a). The atomically resolved chemical mapping by STEM-EDX shown in the right panels of Fig. 5(a) reveals that the enhanced contrast at the Se1 site actually corresponds to a Bi dominant character, which provides a direct proof of the partial substitution of Bi to the Se1 site, i.e., the  $\text{Bi}_{\text{Se}}$  antisite defect formation. The observed Se1 columns with an enhanced contrast towards the sample edge [Fig. 5(b)] signify the existence of more antisite defects near the surface layers. The antisite defects both in the bulk and near the surface region have been a general phenomenon throughout our STEM-EDX characterization of various batches of samples.



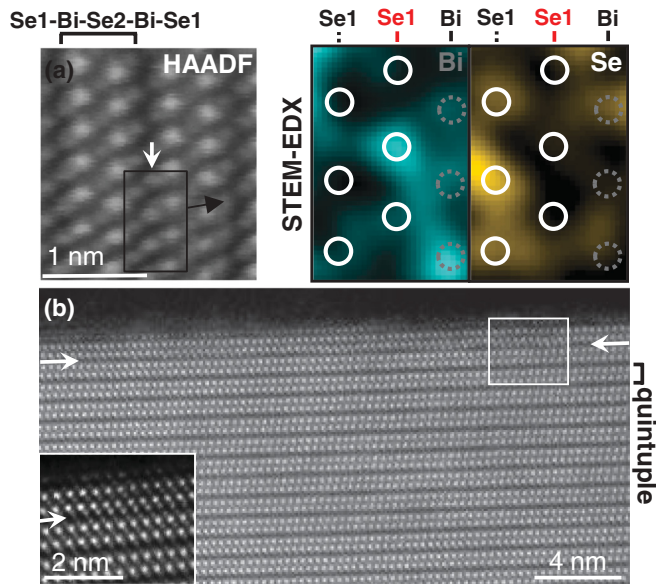


FIG. 5. (Color online) (a) STEM-HAADF image of a bulk region with thickness  $\sim 25$  nm along the incident beam direction. The Se1 column pointed out by the white arrow shows an anomalously enhanced imaging contrast. Further STEM-EDX chemical mappings of the corresponding boxed region are enlarged in the right panels (cyan, Bi map; yellow, Se map). The gray (white) circles in the mapping represent the Bi (Se) columns. The enhanced contrasts of the Se1 columns (signified by the red Se1 text) are shown to be correlated with the presence of Bi on the sites, i.e., the formation of  $\text{Bi}_{\text{Se}}$  antisite defects. (b) The enhanced Se1 contrasts are more regularly observed at the edge of the same specimen, as indicated by the white arrows, with a corresponding enhanced blowup of the white boxed region in the inset in the lower left corner.

The importance of the antisite defect in the tetradymite-type compounds has been discussed previously in the scope of a narrow band gap semiconductor,<sup>12</sup> yet quantitative evidence is difficult to obtain at the point defect level. Considering the number of outer shell electrons for  $\text{Bi}(6s^26p^3)$  and  $\text{Se}(4s^24p^4)$ , a simple argument borrowed from extrinsic semiconductors suggests that the  $\text{Bi}_{\text{Se}}$  antisite can be an acceptor. However, it would be a picture that is too simplified when the  $\text{Bi}_{\text{Se}}$  antisite defect is actually formed by the Bi substitution only to the Se1 vacancy site near the van der Waals gap, i.e.,  $\text{Bi}_{\text{Se1}}$  antisite, and chemically, the electronegativity difference between  $\text{Se}(2.55)$  and  $\text{Bi}(2.02)$  is too large for Bi to accept electrons further from the neighboring Bi/Se atoms. Originally, Se1 uses its four outer shell electrons in  $4p^4$  to bond with the neighboring Bi's and

the two  $4s^2$  electrons form lone pairs exposed to the van der Waals gap, as shown in the inset of Fig. 1(a).<sup>13</sup> The bonding nature of the substituted Bi in  $\text{Bi}_{\text{Se1}}$  antisite becomes unknown in view of a virtual octahedral environment of  $\text{Bi}(\text{Bi}_3\text{Se}_3)$  as depicted in the inset of Fig. 1(a). A current experimentally confirmed  $n$ -type donor and direct STEM observation of a  $\text{Bi}_{\text{Se1}}$  antisite defect supports a scenario that  $\text{Bi}_{\text{Se1}}$  might be viewed as a pair of  $V_{\text{Se1}}$  and Bi interstitials, i.e., the Se vacancy acts as electron donor and Bi remains neutral. This scenario is reasonable, considering that the van der Waals radius of Bi (2.07 Å) is very close to the ionic radius of  $\text{Se}^{2-}$  (1.98 Å for six-coordination).<sup>14</sup> Indeed, based on the formation energy calculated using first-principles calculations, the  $\text{Bi}_{\text{Se1}}$  antisite defect has been shown to be favorable, compared to the Se vacancy defect with a  $V_{\text{Se1}}$  character.<sup>15</sup>

The  $\text{Bi}_2$ -layer intercalation must introduce severe lattice distortion near regions where the van der Waals gap starts to dilate in order to accommodate the excess Bi, as shown in Fig. 2(c). The  $\text{Bi}_{\text{Se1}}$  antisite may introduce less strain to the system compared to the intercalated Bi in the van der Waals gap, but both can locally break the inversion symmetry, which might be associated with the observed symmetry-forbidden peaks found in the Raman spectrum of thin film studies.<sup>16–18</sup> There are relatively more  $\text{Bi}_{\text{Se1}}$  antisite defects found near the specimen edges than in the bulk from studies of multiple batches of either as-grown or 300 °C annealed samples, as demonstrated in Fig. 5(b). While surface defects could cause severe band bending away from the Dirac point at the surface, current findings based on STEM observation alone require other experimental techniques to verify.

In summary, we conclude that crystals grown using Se-rich flux for the Bridgman growth method can reduce significantly the Se vacancy level; however, it is not possible to prevent Se vacancy formation to achieve  $p$ -type doping using excess Se under the current Bridgman growth condition. Two major types of defects are observed in  $\text{Bi}_2\text{Se}_3$  crystals grown using Se- or Bi-rich flux: the randomly intercalated neutral  $\text{Bi}_2$ -layer patches in the van der Waals gaps, and the  $\text{Bi}_{\text{Se1}}$  antisite point defects that act presumably as the electron donor. Low temperature annealing of a Se-rich flux grown crystal at 300 °C helps to remove effectively the intercalated  $\text{Bi}_2$ -layer patches and can create a large area of an ordered near stoichiometric compound.

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