## Tuning the range, magnitude, and sign of the thermal expansion in intermetallic $Mn_3(Zn, M)_x N(M = Ag, Ge)$

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Neutron diffraction is used to reveal the origin and control of the thermal expansion properties of the cubic intermetallic compounds  $Mn_3Zn_xN$  and  $Mn_3[Zn-(Ag,Ge)]_xN$ . We show that the introduction of Zn vacancies induces and stabilizes an antiferromagnetic phase with huge spin-lattice coupling that can be tuned to achieve zero thermal expansion (ZTE) over a wide temperature range. We further show that the antiferromagnetic ordering temperature ( $T_N$ ) that controls this ZTE can be tuned by chemical substitution, again on the Zn site, to adjust the span of ZTE temperatures from well above room temperature to well below. This establishes a quantitative relationship and mechanism to precisely control the ZTE of a single material, enabling it to be tailored for specific device applications.

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Materials with negligible thermal expansion over large temperature ranges have been the subject of fundamental studies as well as being highly desirable for many modern technological applications, such as in spacecraft and for space telescopes,<sup>1,2</sup> thermomechanical actuators,<sup>3</sup> precision mechanics and positioning devices,<sup>4</sup> Bragg grating wavelength filters,<sup>5</sup> and microelectronic components. Presently the metallic materials of choice are Fe-Ni Invar-type alloys,<sup>6,7</sup> which generally have near-zero thermal expansion (NZTE) only near room temperature, but the temperature range for low thermal expansion recently has been extended to above 500 K by introducing stress, which produces microstrains around the Fe atoms.<sup>8</sup> ZTE materials avoid thermal strain in systems subject to large temperature variations, and thus have been a popular topic of longstanding focus.<sup>9–13</sup> It has been difficult to find new ZTE materials with metallic properties-most relatively new ZTE materials are ceramics<sup>14–19</sup>—but an exception has been found in manganese compounds  $Mn_3XB$  (X = Zn, Cu, Ni, Ge, ..., B = N and C),<sup>20–28</sup> because they may have isotropic ZTE, good electric and thermal conductivity, and other interesting physical properties. A clear guide on the origin of their thermal expansion behavior or how to control it is needed. In this Rapid Communication we use neutron powder diffraction (NPD) to uncover the origin of the isotropic zero thermal expansion of the cubic antiperovskite compounds  $Mn_3(Zn/Ag/Ge)_rN$ , focusing on the problem of how to control the temperature range of ZTE.

Polycrystalline samples of  $Mn_3Zn_xN(x = 0.99, 0.96, 0.93)$ ,  $Mn_3Zn_{0.41}Ag_{0.41}N$ , and  $Mn_3Zn_{0.5}Ge_{0.5}N$  were prepared by a solid-state reaction in vacuum (10<sup>-5</sup> Pa) using  $Mn_2N$ , Zn, Ag, and Ge as the starting materials. Stoichiometric amounts were mixed and pressed into pellets, wrapped in Ta foil, sealed in vacuum in a quartz tube, sintered at 800°C for several days, and then cooled to room temperature. NPD data were collected in the 10-300 K temperature range on the BT-1 high-resolution neutron powder diffractometer at the NIST Center for Neutron Research using a Cu (311) monochromator (neutron wavelength of 1.5403 Å). Collimators of 15', 20', and 7' were used before and after the monochromator and after the sample, respectively, and data were collected in steps of  $0.05^{\circ}$  in the  $2\theta$  range of  $3^{\circ}$ -168°. The temperature dependence of the nuclear and magnetic structures were determined by the Rietveld method with the General Structure Analysis System software, using scattering lengths of -0.375, 0.568, and  $0.936(\times 10^{-12} \text{ cm})$  for Mn, Zn, and N, respectively. Variable temperature x-ray diffraction data were also taken for the sample Mn<sub>3</sub>Zn<sub>0.5</sub>Ge<sub>0.5</sub>N from 110 to 580 K on a PANalytical X'Pert PRO powder diffractometer with a Cu target (wavelength 1.5406 Å). The sample was heated to the desired temperature at a rate of 10 K min<sup>-1</sup> and held for 10 min. The x-ray diffraction (XRD) patterns at different temperatures were used to determine the lattice parameters. The crystal and magnetic structures of Mn<sub>3</sub>ZnN, first reported by Fruchart et al.,<sup>29,30</sup> have Mn and N atoms forming Mn<sub>6</sub>N octahedra, and Zn [at 1a(000)] atoms on the corners of the cube, as shown in Fig. 1(c).

We first discuss the effect of Zn vacancies on the nature of the spin-lattice coupling by establishing the magnetic and structural properties for (refined) Zn site occupancies of x = 0.99, 0.96, and 0.93 (designated Zn99, Zn96, and Zn93; see Table I). All three compositions exhibit an identical antiferromagnetic ordering temperature of  $T_N = 185$  K, below which a strongly first-order magnetic phase transition occurs at the magnetic structure shown in Fig. 1(b). The cubic structure



FIG. 1. (Color online) (a)–(c) Observed crystal and magnetic phases for Mn<sub>3</sub>Zn<sub>x</sub>N. (d)–(f) Temperature dependence of the cubic lattice constant for three values of Zn vacancies. All three samples are paramagnetic (PM) above 185 K with a cubic crystal structure. The  $M_{\rm NTE}$  phase has the magnetic structure shown in (b), which for Zn99 is present between 185 and 135 K. (e)  $M_{\rm NTE}$  temperature range is enlarged (185–120 K) for the Zn96 sample, with a complete PM to  $M_{\rm NTE}$  transformation. The  $M_{\rm PTE}$  phase is stable below 120 K. (f) For the Zn93 sample the  $M_{\rm NTE}$  phase is stabilized in the entire temperature range below the PM- $M_{\rm NTE}$  transition at 185 K. In all three compounds the  $M_{\rm NTE}$  phase has very small thermal expansion with  $\alpha < 10^{-6}$  K<sup>-1</sup>. An external pressure of 0.55GPa ( $\Delta$ ) converts  $M_{\rm NTE}$  to  $M_{\rm PTE}$ , or  $M_{\rm PM}$  at higher T, where  $a_{\rm PM}$  and  $a_{\rm PTE}$  form the usual smooth curve observed in the Zn99 and Zn96 samples, without a detectable anomaly at the  $M_{\rm PTE}$ -PM transition.

is maintained, but there is an abrupt increase in the lattice parameter for this phase, as shown in Figs. 1(d)–1(f) for Zn99, Zn96, and Zn93, respectively. This signals a strong negative thermal expansion at  $T_N$ , so we label this phase  $M_{\rm NTE}$ . For the Zn99 composition only part of the sample transforms into the  $M_{\rm NTE}$  phase, as shown in Fig. 2, with

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FIG. 2. (Color online) Relationship between the lattice variation and phase fractions for sample Zn99. The  $M_{\rm NTE}$  phase is present between 185 and 135 K. The transition from PM to  $M_{\rm NTE}$  is incomplete; an 83%  $M_{\rm NTE}$  phase coexists with the PM phase between 185 and 160 K, and the  $M_{\rm NTE}$  phase fraction decreases gradually on further cooling and coexists with the  $M_{\rm PTE}$  phase between 160 and 135 K. Solid symbols represent phase fractions and open symbols depict lattice constants. Curves are guides to the eye.

the remainder of the sample initially remaining paramagnetic, and then transforming to the phase that exhibits a completely different magnetic structure shown in Fig. 1(a). The lattice parameter for this second magnetic structure follows the usual positive thermal expansion (PTE) and thus we designate this phase as  $M_{\rm PTE}$ . We find that there exist two completely different antiferromagnetic (AFM) phases, with  $M_{\rm NTE}$  having rhombohedral (R-3) magnetic symmetry while the  $M_{\rm PTE}$ AFM phase has tetragonal (P1) symmetry. Only the  $M_{\rm NTE}$ AFM displays intrinsic negative thermal expansion and ZTE. Figure 2 shows that we have phase coexistence of  $M_{\rm PM}$  and  $M_{\rm NTE}$  below  $T_N$ , then coexistence of  $M_{\rm NTE}$  and  $M_{\rm PTE}$ . Finally we have just the  $M_{\rm PTE}$  phase at low T when the  $M_{\rm NTE}$ phase abruptly collapses and transforms to the  $M_{\text{PTE}}$  phase, indicating that the transition is strongly first order. For Zn96 the sample fully transforms to the  $M_{\rm NTE}$  phase upon cooling below 185 K, which exists over a wider temperature range before the lattice collapses and fully converts to the  $M_{\rm PTE}$ phase. For Zn93 the sample fully transforms to the  $M_{\rm NTE}$  phase at 185 K, which is then stable over the full temperature range below  $T_N$ . Table I also gives the refinements for the AFM  $M_{\rm NTE}$  phase, emphasizing its extraordinary dependence on Zn vacancies. Additional crystallographic details are provided in the Supplemental Material.<sup>31</sup>

There are several important results revealed by the data of Fig. 1. First and most importantly,  $a_{\text{NTE}}$  is essentially independent of temperature. In particular, the coefficient of linear expansion  $\alpha_{\text{NTE}}$  ( $\Delta L/L\Delta T$ ) obtained directly from the diffraction data demonstrates that it is in the range of  $10^{-7}$  K<sup>-1</sup>, which is generally considered ZTE, over the full temperature range where the  $M_{\text{NTE}}$  exists. This value of  $\alpha$  is considerably smaller and can occur over a much wider temperature range than Invar itself.<sup>6–8</sup> More importantly, it is clear that the Zn vacancies control which magnetic structure is formed, and over what temperature range. Finally, we see that only the magnetic structure of Fig. 1(b) is strongly coupled to the lattice to produce the large NTE that compensates the ordinary thermal expansion behavior, to produce the ZTE phase. We

Sample No.	Zn99	Zn96	Zn93
Formula	$Mn_{3}Zn_{0.99}N$	Mn <sub>3</sub> Zn <sub>0.96</sub> N	Mn <sub>3</sub> Zn <sub>0.93</sub> N
A (Å)	3.90077(6)	3.90021(4)	3.89891 (1)
V (Å <sup>3</sup> )	59.342(1)	59.309 (1)	59.282(1)
Mn n	1.00	1.00	1.00
Zn n	0.99(1)	0.96(1)	0.93(1)
N n	0.98(2)	0.99(1)	0.99(1)
$R_{p}$ (%)	5.83	7.70	6.21
$R_{wp}$ (%)	7.54	11.24	8.59
$\chi^2$	1.565	1.090	1.307
Zn-Mn (Å)	2.75807(1)	2.75756(1)	2.75714(1)
Mn-N (Å)	1.95025(1)	1.94989(1)	1.94959(1)
Zn-N (Å)	3.37793 (1)	3.37731(1)	3.37679(1)
	For $M_{\rm N}$	TE phase	
Existing temperature range	135–185 K	125–185 K	4–185 K
Fraction	83%	100%	100%
Mean lattice constant (Å)	3.9106(2)	3.9089(2)	3.9114(2)
$\alpha_1 (10^{-7} \text{ K}^{-1})$ :	8.65	- 1.37	5.83

TABLE I. Crystal structure obtained from NPD Rietveld refinements for the  $Mn_3Zn_xN$  compounds at 295 K (space group: Pm-3m) and the data for the magnetic  $M_{NTE}$  phase. Uncertainties indicate one standard deviation.

note that Ref. 26 suggested that the large magnetovolume effect (MVE) had an intimate correlation with the cubic  $\Gamma^{5g}$ AF structure in  $Mn_3Cu_{1-x}Ge_xN$ , which can be explained in terms of geometrical frustration. This is in agreement with our experimental results in  $Mn_3Zn_xN$ , that only the magnetic phase  $M_{\rm NTE}$  exhibits the MVE effect. This behavior may originate from the additional Zn vacancies enhancing the magnetic frustration, thereby stabilizing the  $M_{\rm NTE}$  phase. On the other hand, Refs. 24 and 32 reported the competitive coexistence between the  $\Gamma^{5g}$  and  $\Gamma^{4g}$  antiferromagnetic components in Mn<sub>3</sub>Cu<sub>1-x</sub>Ge<sub>x</sub>N (x = 0.5) and suggested that the  $\Gamma^{5g}$ antiferromagnetic ordered moment induced by local lattice distortion is responsible for the negative thermal expansion, but guessed that the behavior was caused by slight differences in the nitrogen composition. Reference 33 observed a similar phenomenon as us in Mn<sub>3</sub>ZnN, but they hypothesized that it was due to the disorder on N site.

The juxtaposition of the NTE and PTE phases, along with the smooth variation of the lattice parameter of the PM and PTE phases, allows a quantitative evaluation of the magnetic coupling to the lattice for the  $M_{\rm NTE}$  phase. The behavior of this phase is a result of a competition between the expansion of the lattice upon cooling due to the magnetic ordering  $[a_M(T)]$ and the usual thermal contraction  $a_T(T)$ . For Zn99 and Zn96,  $a_T(T)$  can be readily extrapolated into the regions of existence of  $M_{\rm NTE}$  from the smooth variation of the lattice parameters  $a_{\rm PM}$  and  $a_{\rm PTE}$ . For Zn93 this is more difficult because of the large temperature range of  $M_{\rm NTE}$ . We could use the same extrapolation from the PM phase, but a better estimate can be obtained by noting that  $a_{\text{PTE}} < a_{\text{NTE}}$ , so that applying pressure should have a dramatic effect on the phases. NPD data were then collected for the Zn93 sample at a hydrostatic pressure of 0.55 GPa, which was sufficient to fully convert  $M_{\rm NTE}$ into  $M_{\rm PTE}$ , or PM at higher temperature. Then  $a_{\rm PM}$  and  $a_{\rm PTE}$ form the usual smooth curve, as shown by the open triangles in Fig. 1(f). These data were scaled and matched to the observed  $a_{\rm PM}$  at ambient pressure to estimate  $a_T(T)$  below  $T_N$  for Zn93.

Since there is no significant coupling of the magnetic moments and the lattice in the  $M_{\text{PTE}}$  phase, we can assume that  $a_{\text{PTE}}(T) = a_{\text{PM}}(T) = a_T(T)$  and take the difference  $\Delta a_m(T) =$  $a_{\text{NTE}}(T) - a_T(T)$  to isolate the effect of the NTE. The results are shown in Fig. 3. For all three compositions we see that  $\Delta a_m(T)$  increases modestly with decreasing temperature, but at approximately the same rate as the ordered moment increases. We find that the ratio  $r(T) = \Delta a_m(T)/m_{\text{NTE}}(T)$  is approximately independent of T, revealing that the size of the NTE effect is controlled by the size of the ordered moment. These data are shown by the solid purple squares, and fit to an offset plus a straight line are given in the figure. Note that for the Zn99 sample the  $M_{\rm NTE}$  phase exists only over a small temperature region, and then begins to convert to the  $M_{\rm PTE}$ phase. During this transformation the phase fraction decreases toward zero (also see Fig. 2) and it becomes difficult to extract the moment in the  $M_{\rm NTE}$  phase, but there appears to be some decrease in its value when the two phases coexist. For the Zn96 and Zn93 samples the transformations are abrupt and no coexistence or moment decrease is observed. It is clear that strong spin-lattice coupling is responsible for the abnormal thermal expansion behavior observed in the  $M_{\rm NTE}$  phase, with  $\Delta a_m(T)$  offsetting the usual contribution of the thermal vibrations almost exactly, yielding a system with extremely small thermal expansion.

Figure 3 also shows the ordered Mn moments for the  $M_{\text{PTE}}$  phase. This phase has two inequivalent magnetic atoms with different ordered magnetic moments  $m_{\text{PTE}}(T)$  and  $m'_{\text{PTE}}(T)$ , in agreement with Refs. 29 and 30. For the Zn99 sample both moments increase slowly with decreasing temperature [Fig. 3(a)], while they remain approximately constant for Zn96 [Fig. 3(b)]. Since there is no significant moment-lattice coupling in this  $M_{\text{PTE}}$  phase the moment values are unimportant as far as the thermal expansion is concerned.

A central result of the present study is that changes in the Zn content control the phases that occur and their temperature range of existence. This suggests that the properties can also



FIG. 3. (Color online) (a)–(c) Relationship between the lattice variation  $a_{\text{NTE}}$ - $a_T$ , ordered magnetic moments, and r(T) for three Zn occupancies. The data for (a) Zn99, (b) Zn96, and (c) Zn93 show that the temperature variation of the lattice parameter is proportional to the ordered magnetic moment in the  $M_{\text{NTE}}$  phase due to the presence of strong magnetoelastic coupling.

be controlled by appropriate chemical substitution on the Zn site, which changes both the ordered magnetic moment and lattice constant, and we now show this explicitly for the Mn<sub>3</sub>(Zn/Ag)<sub>0.82</sub>N and Mn<sub>3</sub>(Zn/Ge)N systems. We have prepared the compounds Mn<sub>3</sub>Zn<sub>0.41</sub>Ag<sub>0.41</sub>N and Mn<sub>3</sub>Zn<sub>0.5</sub>Ge<sub>0.5</sub>N and their thermal expansion properties are illustrated in Fig. 4 (also see Table S-II in the Supplemental Material<sup>31</sup>). For  $Mn_3(Zn/Ag)_{0.82}N$ ,  $T_N$  increases to 220 K by partially replacing Zn by Ag, which has a larger ionic size [Figs. 4(a) and 4(b)], and by inducing vacancies at the Zn site to stabilize the  $M_{\rm NTE}$  phase. A value of  $\alpha = 2.31 \times 10^{-6} {\rm K}^{-1}$  is obtained in the entire temperature range below  $T_N$ , measured by the variable temperature NPD technique. In the second case, with 50% of Zn replaced by Ge,  $T_N$  increases to 530 K and the  $M_{\rm NTE}$  phase with  $\alpha$  = 3.07  $\times$  10<sup>-6</sup> K<sup>-1</sup> occurs for an extended range [350-530 K, Fig. 4(c)] as determined by XRD. Reference 8 observed that stress could induce an expanded temperature region for low thermal expansion (LTE) in Invar and thought that microstrain around the Fe atoms introduced a slight increase in the Fe-Fe interatomic distances. This may be a common mechanism for the present system in correlating the micromagneto-structure and abnormal thermal expansion.

The results presented here elucidate how NTE for these cubic antiperovskite systems is intimately correlated with the magnetic structure and can be tuned by adjusting the chemical

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FIG. 4. (Color online) Temperature dependence of the cubic lattice parameter and ordered moment in  $Mn_3Zn_{0.41}Ag_{0.41}N$  and  $Mn_3Zn_{0.5}Ge_{0.5}N$ . (a) shows the lattice parameter and (b) the ordered magnetic moment for  $Mn_3Zn_{0.41}Ag_{0.41}N$ , demonstrating the ZTE behavior, with r(T) essentially constant. (c) Lattice parameter and phase fraction for  $Mn_3Zn_{0.5}Ge_{0.5}N$ , with an antiferromagnetic ordering temperature adjusted to 530 K.

and vacancy concentrations to work from well below to well above room temperature. We have shown how to stabilize the  $M_{\rm NTE}$  phase, adjust the magnetic ordering temperature and ordered magnetic moment to achieve ZTE, and have provided a quantitative relationship between the ordered magnetic moment and lattice variation that controls the ZTE mechanism. The tools developed here can be readily employed to tune the thermal expansion properties, including compensating for metallurgical defects such as grain boundaries or impurities if required, to the temperature range and breadth required for a wide variety of real world applications.

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- <sup>31</sup>See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.85.220103 for Crystallograhic refinement results are given in the Tables S-I through S-V, together with typical refinement data (Fig. S-I) and data demonstrating coexisting phase fractions (Fig. S-II).
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