

Site preference and effect of alloying on elastic properties of ternary $B2$ NiAl-based alloys

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Using the exact muffin-tin orbitals method in conjunction with the coherent potential approximation, we study the site preference of transition metal impurities X ($X = \text{Sc, Ti, V, Cr, W, Re, Co}$) in $B2$ NiAl and their effect on its elastic properties. Analyzing interatomic bonding of NiAl- X alloys and elastic characteristics evaluated from the elastic constants C_{11} , C_{12} , and C_{44} , we predict that the addition of W, V, Ti, and Re atoms could yield improved ductility for $B2$ NiAl- X alloys without significant changes in the macroscopic elastic moduli.

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I. INTRODUCTION

The intermetallic compound $B2$ NiAl is widely used in aerospace applications due to its high melting temperature ($T = 1911$ K),¹ good oxidation resistance, and low density. The main problem for application of NiAl alloys is their low room-temperature ductility. The brittle behavior of these alloys can be managed by various techniques such as microstructural control through processing, fiber strengthening, and second-phase reinforcement, as well as microalloying and macroalloying.² For example, a substantial improvement in ductility has been achieved due to the modification of β -phase ($B2$ -type) grains by the γ phase (Al type) formed by the addition of Co, Fe, and Cr.³ Studies for fiber-reinforced NiAl- X eutectic alloys have shown that NiAl alloyed with the refractory bcc metals Cr, Mo, and W possesses promising strength at high temperatures and improved room-temperature ductility.⁴ Ductility enhancement was found in NiAl-Cr(Mo)-Hf-Ti alloys, where the disordered bcc (Ti, Hf) solid solution phase together with the Heusler phase Ni₂Al (Ti, Hf) precipitation presented at eutectic cell boundaries is responsible for the improved ductility due to the better deformation ability of the (Ti, Hf) solid solution phase.⁵ In the above-mentioned examples the ductility improvement was achieved mainly through the formation of a specific microstructure. Recently the structural, electronic, and elastic properties of NiAl with $4d$ alloying elements were studied using the first-principles pseudopotential method⁶ and it was found that Tc, Ru, Rh, and Pd are promising candidates to improve the mechanical properties of NiAl- X alloys.

In this work we study the effect of substitutional alloying on the elastic properties of $B2$ NiAl at the atomic level. We therefore concentrate on the effects characteristic of a solid solution and do not treat explicitly the effect of competing phases and microstructure evolution in alloys. In doing so, we rely on the phenomenological correlation between ductility and certain properties of the solution phases, discussed below. Also, we deal with site preference in NiAl- X alloys. It has been studied earlier by means of experimental⁷⁻¹⁴ and theoretical methods,¹⁵⁻¹⁹ and the results seem to be controversial. For example, the thermal conductivity measurement suggested that V, Nb, Ta, Mo, Fe, Ru, Co, and Pt atoms preferentially substitute for the Ni sublattice, but Cr and Cu atoms substitute for both Ni and Al sites.¹⁴ At the same time, using atom location by

channeling enhanced microanalysis (ALCHEMI), it was found that V^{10,11} and Cr¹² occupy the Al sublattice, although atom probe field ion microscopy (APFIM) experiments showed that about 70% of the detected atoms occupy Al sites.¹³ Results of theoretical studies are also inconsistent regarding some ternary additions. According to Refs. 15, 16, and 18, Cr, V, and Ti substitute for the Al sublattice. However, Hosoda *et al.*¹⁹ have shown the possibility for Cr, V, and Ti to occupy both the Al and the Ni sublattices. More detailed information on experimental and theoretical studies of site preference in NiAl- X alloys is given in Ref. 15.

In the present paper the site occupancy, electronic, and elastic properties of NiAl- X alloys ($X = \text{Sc, Ti, W, V, Cr, Co, Re}$) are studied using the first-principles density functional theory. We calculate the elastic constants C_{11} , C_{12} , and C_{44} , bulk modulus B , Young modulus E , and shear modulus G and use the phenomenological Pugh criteria (G/B ratio)²⁰ as well as the Cauchy pressure ($C_{12} - C_{44}$)²¹ to analyze the brittle vs ductile behavior of solid solutions. Analysis of the density of states (DOS) allows us to establish the direct connection between the changes in interatomic bonding and the elastic properties of alloys.

II. DETAILS OF THE CALCULATION

Calculations were performed using the exact muffin-tin orbital (EMTO) method within the coherent potential approximation (CPA).^{22,23} The accuracy of the method was shown to be close to that for full-potential methods. The full charge density (FCD)²⁴ was represented by a single-center expansion of the electron wavefunctions in terms of spherical harmonics with orbital moments $l_{\text{max}}^{\text{FCD}}$ up to 8. The EMTO-CPA method has been proven to be highly efficient and accurate enough for calculation of elastic properties of alloys.^{23,25-29} The CPA method was used to simulate substitutionally disordered alloys and the paramagnetic state for NiAl-Cr alloys in the disordered local moments (DLMs) approach, which assumes random collinear orientations of the local magnetic moments.³⁰ Self-consistent electron densities were obtained within the spherical cell approximation and the local density approximation (LDA), and then variational estimates of the total energies were calculated in the generalized gradient approximation (GGA) using the FCD formalism. Integration in the reciprocal space was performed over a grid of $29 \times 29 \times 29$ k points;

energy integration was carried out in the complex plane using a semielliptic contour comprising 24 energy points. Calculations were performed for a basis set including valence *spdf* orbitals and by means of the soft-core approximation; i.e., the core states were recalculated at each iteration. In our CPA calculations the screening contribution to the electrostatic potential and energy was taken into account in order to describe the charge transfer between the alloy components using screening constants³³ obtained by the locally self-consistent Greens function method.³⁴

Elastic properties of crystals with cubic symmetry are fully characterized by three elastic constants: C_{11} , C_{12} , and C_{44} .³⁵ The first two constants describe the crystal response to tension, while C_{44} describes the response to shear strain. In order to determine the elastic constants $C' = (C_{11} - C_{12})/2$ and C_{44} , we applied volume-conserving orthorhombic and monoclinic distortions, respectively, and calculated the internal energy response³⁶ to these small distortions. Elastic constants C_{11} and C_{12} can be obtained by the combination of C' and bulk modulus $B = (C_{11} + 2C_{12})/3$. The elastic constants derived from the total energy calculations correspond to single-crystal elastic properties. To estimate elastic moduli for polycrystalline materials we used the Voigt-Reuss-Hill approximation.³⁵

In order to analyze the brittle vs ductile behavior of solid solutions, we estimated the Pugh ratio (G/B) ²⁰ and the Cauchy pressure $P_C = (C_{12} - C_{44})$,²¹ then phenomenologically linked the plastic properties of materials with their elastic properties. According to the Pugh criterion,²⁰ a material behaves in a ductile manner if $G/B < 0.5$, because in this case the resistance to bond-length change exceeds that to bond-angle change; and vice versa, if $G/B > 0.5$, a material demonstrates brittleness. The higher the value of G/B , the more brittle the material should be.

Pettifor²¹ suggested that the angular character of atomic bonding in metals and compounds, which can be responsible for the brittle or ductile behavior of materials, might be described by the Cauchy pressure $P_C = (C_{12} - C_{44})$. The Cauchy relation $C_{12} = C_{44}$ (in the absence of external pressure) is the consequence of centrosymmetric forces, satisfied for inert gas crystals and approximately satisfied for ionic crystals and some metals. This means that interatomic interactions in these crystals could be reasonably described by pair potentials, like Lennard-Jones, the embedded atom potential, etc. Experimentally, in most cases for metals and compounds the Cauchy relation is not obeyed. To capture the correct response of these materials to shear and external pressure, one has to take into account the spatial orientation of bonds via many-body potentials as shown by Brovman and Kagan.³⁷ As a result, for covalent materials with a directional character of atomic bonds, the Cauchy pressure is negative ($C_{12} < C_{44}$), because in this case the material resistance to the shear strain (C_{44}) is much more than that for the volume change (C_{12}). On the other hand, for metallic-like bonding, where electrons are almost delocalized, the Cauchy pressure should be positive ($C_{12} > C_{44}$). Another important elastic property is the Zener anisotropy parameter, which is defined as $A_z = 2C_{44}/(C_{11} - C_{12})$,³⁸ showing the difference between the sound velocities for TA1 and TA2 modes traveling along the [110] and [001] directions in the [1 $\bar{1}$ 0] plane. For isotropic

crystals $A = 1$, while other values are a measure of elastic anisotropy.

III. RESULTS AND DISCUSSION

A. Site preference

First, we determine the site preference of the ternary additions in *B2* NiAl. Following the recipe given in Ref. 39, we calculate the so-called transfer energy E_X :

$$E_X = \frac{1}{c}(E((X_c\text{Ni}_{1-c})\text{Al}) - E((X_c\text{Al}_{1-c})\text{Ni}) + E(\text{Ni}_{\text{Al}})), \quad (1)$$

where c is the concentration of impurities in the corresponding sublattice. Equation (1) corresponds to the energy needed to move atom X from the Ni site to the Al site. In Eq. (1) $E((X_c\text{Ni}_{1-c})\text{Al})$ and $E((X_c\text{Al}_{1-c})\text{Ni})$ are energies of substitution alloys with ternary addition X on the Ni and Al sublattices, respectively, and $E(\text{Ni}_{\text{Al}}) = E((\text{Ni}_c\text{Al}_{1-c})\text{Ni}) - E(\text{NiAl})$ is the energy of the partial antisite defects on the Al sublattice.

If $E_X < 0$, then there is a strong Ni site preference, because atoms X prefer to go to the Ni sublattice despite the Ni antisite formation on the Al sublattice.⁴⁰ Besides, an atom X can occupy the Ni sublattice with the formation of two Al vacancies ($2V_{\text{Al}}$) to keep the Ni concentration constant. However, as shown in Ref. 40, this configuration is energetically unfavorable because $2E(V_{\text{Al}}) > E(\text{Ni}_{\text{Al}})$. In the case of $E_X > 0$ there are two possibilities. First, the X atom occupies the Al sublattice, with defect formation on the Ni sublattice. In Refs. 40 and 41 it was shown that the dominant thermal defect in stoichiometric NiAl is a triple Ni defect, which corresponds to two Ni vacancies and one antisite Ni atom on the Al sublattice ($2V_{\text{Ni}} + \text{Ni}_{\text{Al}}$). So, if $E_X > E(2V_{\text{Ni}} + \text{Ni}_{\text{Al}})$, then there is a strong Al preference, because atoms X always go to the Al sublattice, even at the cost of creating a triple defect. Second, if $0 < E_X < E(2V_{\text{Ni}} + \text{Ni}_{\text{Al}})$, then X atoms do not have any site preference and randomly occupy both Ni and Al sublattices. In our calculations we found that the triple defect formation energy $E(2V_{\text{Ni}} + \text{Ni}_{\text{Al}}) = 2.14$ eV. It is in good agreement with the theoretical result obtained in Ref. 40 (2.37 eV) and with experimental data (1.90 eV).⁴²

In Table I the calculated transfer energy and the site preferences of some ternary transition-metal additions to *B2* NiAl in the dilute limit ($c = 1$ at%) at $T = 0$ K are presented.

TABLE I. Transfer energy and site preference of some ternary additions in *B2* NiAl obtained in the dilute limit and at $T = 0$ K. The calculated formation energy of the triple defect is $E(2V_{\text{Ni}} + \text{Ni}_{\text{Al}}) = 2.14$ eV.

Element	Transfer energy (eV)	Site preference
Sc	3.00	Al
Ti	2.92	Al
V	1.95 d	Ni, Al
Cr (DLM)	1.41	Ni, Al
W	0.90	Ni, Al
Co	-0.28	Ni
Re	-0.39	Ni

TABLE II. Calculated lattice parameters (a), elastic constants (C_{11} , C_{12} , C_{44}), bulk moduli (B), Young moduli (E), and shear moduli (G) of $B2$ NiAl compared with previous calculations and available experimental measurements.

Ref. No.	Method(s)	a (Å)	C_{11} (GPa)	C_{12} (GPa)	C_{44} (GPa)	B (GPa)	E (GPa)	G (GPa)
Our results	EMTO	2.89	233	121	114	159	218	85
27	EMTO	2.89	232	121	111	158	214	84
46	LAPW, LDA, $a_{\text{equilibrium}}$	2.84	237	155	132		186	
46	LAPW, LDA, $a_{\text{experimental}}$	2.89	193	124	114	147	184	71
47	LAPW, LDA	2.84	262	146	138	185		
48	CASTEP GGA	2.90	161	150	117	153	180	70
49	FLAPW LDA	2.82	236	167	140	187		
49	FLAPW GGA	2.89	189	131	107	150		
50	VASP PAW GGA, $T = 0$ K		200	125	112			
51	VASP ultrasoft LDA	2.84	218	153	128			
52	VASP PAW GGA	2.89	203	140	113			
53	Elastic constants were determined by the slopes of measured acoustic phonon frequencies at 296 K		197	119	110	145		
54	Expt.	2.89	212	143	112	166	184	70
55	Expt., ultrasonic pulse-echo method at 298 K		199	137	116	158		
56	Expt., ultrasonic pulse-echo method at 295 K		205	135	117	159		

One can see that some substitutional metals X have a strong preference for either the Al or the Ni sublattice in $B2$ NiAl, but some of them do not have any particular site preference (i.e., atom X can substitute randomly the Al or the Ni sublattice). The early transition metals Sc and Ti are found to substitute preferentially Al, whereas Re and Co are found to have a strong preference for the Ni sublattice. Cr, W, and V are predicted to have no site preference. The results are in agreement with the site preference of $3d$, $4d$, and $5d$ transition metals in NiAl previously studied in Ref. 43 by the Vienna *Ab Initio* Simulation Package (VASP).^{44,45} The latter allows one to consider the effect of local atomic relaxations. Good agreement

between the two calculations demonstrates that their neglect in our calculations does not introduce significant inaccuracy for systems considered in this study.

The site preference behavior reported in Table I is valid in the dilute limit and at $T = 0$ K. As demonstrated in Ref. 39, it is possible for the site preference to be changed at a high temperature and concentration. Indeed, as shown in Ref. 43 using the Wagner-Schottky model, in stoichiometric NiAl, elements with no site preference randomly distributed between Al and Ni sites at low temperatures (V, W, Cr atoms) start to exhibit a preference for the Al sublattice at higher temperatures. The ground-state configuration at nonzero temperatures

TABLE III. Calculated lattice parameters (a), elastic constants (C_{11} , C_{12} , C_{44}), bulk moduli (B), Young moduli (E), shear moduli (G), and Zener anisotropy parameters (A_z) of NiAl-based alloys. For NiAl-Cr alloys we consider only the paramagnetic state in the disordered local moments approach.

	a (Å)	C_{11} (GPa)	C_{12} (GPa)	C_{44} (GPa)	B (GPa)	E (GPa)	G (GPa)	A_z
NiAl	2.89	233	121	114	159	218	85	2.1
(Re ₁₀ Ni ₉₀)Al	2.92	230	124	121	159	220	87	2.3
(Re ₅₀ Ni ₅₀)Al	3.00	232	154	138	180	216	83	3.5
(W ₀₅ Al ₉₅)(W ₀₅ Ni ₉₅)	2.92	234	132	117	166	215	84	2.3
(W ₂₅ Al ₇₅)(W ₂₅ Ni ₇₅)	3.00	241	154	128	183	217	83	3.0
(V ₀₅ Al ₉₅)(V ₀₅ Ni ₉₅)	2.91	223	125	113	158	207	81	2.3
(V ₁₀ Al ₉₀)(V ₁₀ Al ₉₀)	2.92	218	128	112	158	200	77	2.5
(Ti ₁₀ Al ₉₀)Ni	2.91	234	121	110	159	214	84	1.9
(Ti ₅₀ Al ₅₀)Ni	2.96	223	126	88	159	182	70	1.8
(Sc ₁₀ Al ₉₀)Ni	2.93	224	114	103	150	203	80	1.9
(Sc ₅₀ Al ₅₀)Ni	3.04	196	94	71	128	160	64	1.4
(Co ₁₀ Ni ₉₀)Al	2.89	235	123	117	161	221	87	2.1
(Co ₈₀ Ni ₂₀)Al	2.86	268	127	135	174	260	104	2.1
(Cr ₀₅ Al ₉₅)(Cr ₀₅ Ni ₉₅)	2.90	224	122	115	156	212	83	2.2
(Cr ₁₅ Al ₈₅)(Cr ₁₅ Ni ₈₅)	2.91	213	119	116	151	210	81	2.5
(Cr ₅₀ Ni ₅₀)Al	2.96	189	108	120	135	196	78	3.0
(Cr ₅₀ Al ₅₀)Ni	2.90	195	138	120	157	178	68	4.2

and nondilute concentrations can be obtained using more sophisticated computer simulation methods, for example, Monte Carlo simulations.

Our results are in good agreement with available experimental data. Using the extended x-ray absorption fine-structure spectroscopy (EXAFS) technique,⁷ it was found that Co predominantly occupies the Ni sites in *B2* NiAl, and by means of atom probe field ion microscopy (APFIM)⁸ it was found that Re has a strong preference for the Ni sublattice in NiAl. Using atom location by channeling enhanced microanalysis (ALCHEMI) for Ti⁹ and V,^{10,11} it was detected that these elements exhibit a strong preference for the Al sublattice. Although V in our calculation has no site preference, the experimental results can be explained by the fact that it can change site preference at high temperatures as shown in Ref. 43.

B. Elastic properties

In order to analyze the alloying effect of some *3d* and *5d* metals on the elastic properties of *B2* NiAl, the lattice parameters, elastic constants C_{11} , C_{12} , and C_{44} , Young modulus E , bulk modulus B , and shear modulus G of the studied materials were calculated. To verify the accuracy of our calculations, we first compare the calculated results of these properties for ordered NiAl with theoretical and experimental data from the literature^{27,46–56} (Table II). In

general, our results are in good agreement with experiments and previous theoretical calculations. Our results for C_{11} are closer to the upper bound of the available theoretical estimations, while for C_{12} and C_{44} we are closer to the lower bound. We note that there is a certain spread in the calculated elastic constants obtained by different groups, even when the same methodology is used.^{50,52} Thus, it is difficult to identify a particular reason for the deviations between different calculations. In comparison with experiment, an excellent correlation between our theoretical and the experimental lattice parameter, bulk modulus, and elastic constant C_{44} is found. The C_{11} obtained in our calculation is slightly higher than the experimental values and the C_{12} is slightly lower than most of the experimental results (Table II). Therefore, the Pugh ratio (G/B) is somewhat overestimated in comparison with the experimental data for *B2* NiAl, while the Cauchy pressure is underestimated. Thus in our calculations NiAl turns out to be “more brittle” than it actually is. Still, within the accuracy offered by the phenomenological criterion of brittle vs ductile behavior, we can analyze qualitatively trends upon alloying, which is the task of our study.

Selected results for studied alloys are summarized in Table III and the complete database is shown in the Appendix. We find that for NiAl-X alloys at a low X concentration the well-known criteria for mechanical stability of cubic crystals ($C_{11} - C_{12}$) > 0 and C_{44} > 0 are fulfilled if ternary additions

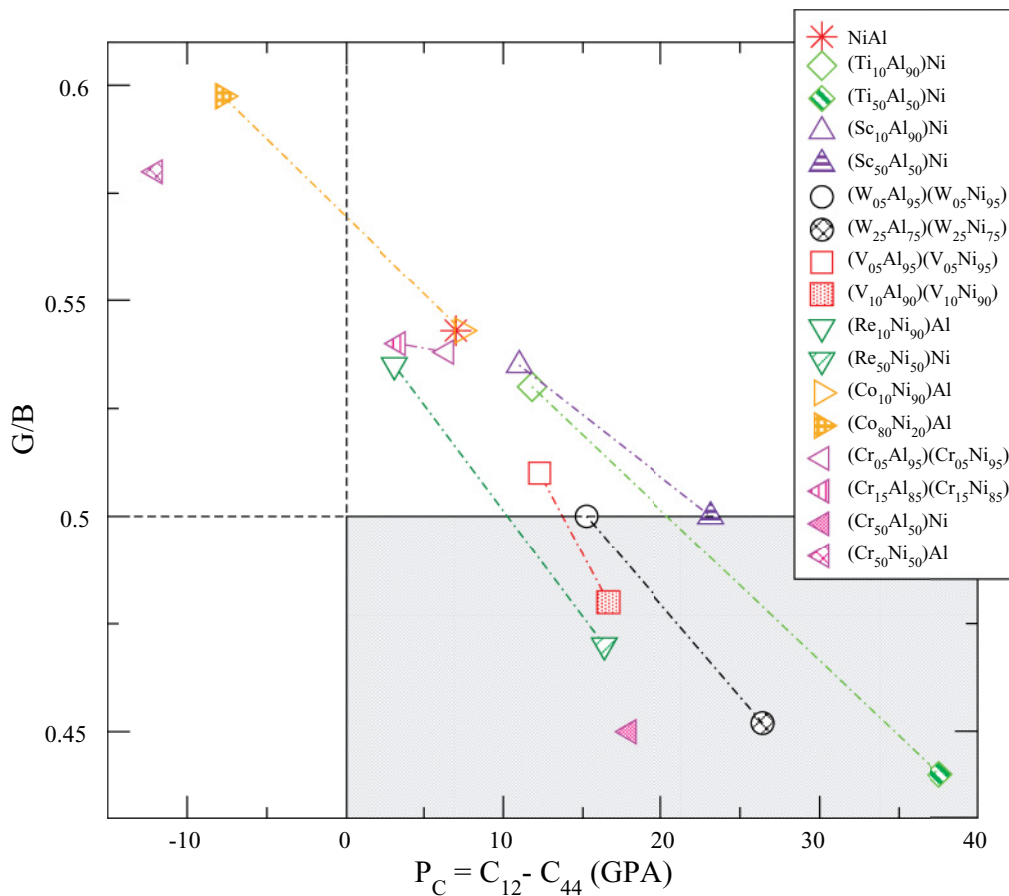


FIG. 1. (Color online) Calculated map of brittle/ductile transition for NiAl-X alloys. The shaded area indicates more ductile behavior according to both the Pugh ratio G/B and the Cauchy pressure $P_C = (C_{12} - C_{44})$ criteria.

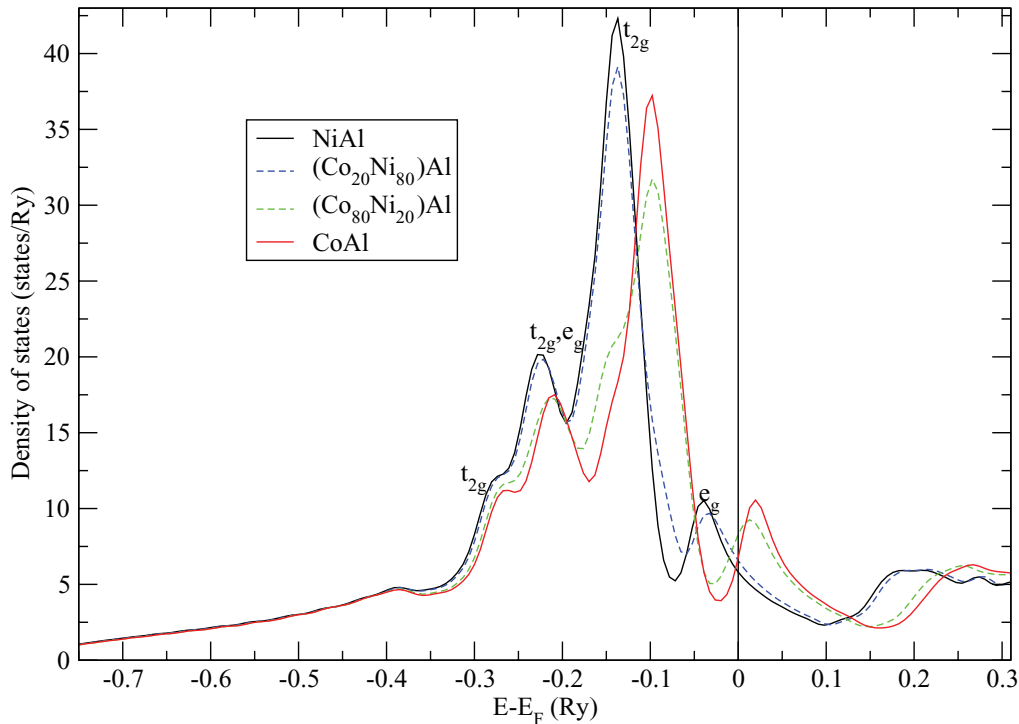


FIG. 2. (Color online) Total density of states for NiAl, CoAl, and $(\text{Co}_c\text{Ni}_{1-c})\text{Al}$ alloys calculated by means of the EMTO-CPA method. The Fermi level is set to 0.

are located in their preferred sites. Let us note that for the studied NiAl-X alloys, $B > G > C'$, indicating that the shear modulus C' is the limiting parameter for the mechanical stability of the alloys.

In Fig. 1 we present the phenomenological estimation of brittle vs ductile behavior of ternary NiAl-X alloys. Following Ref. 57, we plot the Pugh ratio G/B versus the Cauchy pressure. To understand the composition effect on the elastic properties and ductility, we show the results in the dilute limit (total concentration of ternary additions X is 5 at%) and at a few nondilute concentrations of alloys under the assumption that the ternary additions still occupy the positions following the site preference trend summarized in Table I. Note, however, that in principle, the site preference of particular ternary additions can be changed with increased concentration and temperature as mentioned above.³⁹

First, we consider alloying of $B2$ NiAl with Co. In this case we examined the elastic properties in the whole concentration range $c = 0-100$ at% because the type of interatomic interaction changes drastically with increasing Co concentration (see Fig. 4). The G/B ratio and Cauchy pressure P_C for NiAl-Co alloys change their values only slightly with Co concentration up to 50 at%, but in the concentration range 50–100 at% the ratio G/B increases sharply while P_C decreases and then becomes negative (Fig. 4). This indicates a change in the bonding character and an increase in the brittleness of the $(\text{Co}_c\text{Ni}_{1-c})\text{Al}$ alloys. Note that the negative Cauchy pressure for $B2$ CoAl was confirmed experimentally.⁵⁸ At a Co concentration of less than 50% C_{11} and C_{12} increase slightly; at a higher Co concentration C_{11} increases dramatically, while C_{12} is considerably reduced. C_{44} increases monotonically over

the whole concentration range. As a result, the shear modulus G and Young modulus E are enhanced. Note that B increases by only 12%, while E and G increase much more, by up to 30%.

In order to understand the reason for the changes of bonding character in the (Co-Ni)Al system, we analyzed the variation of the electronic DOS with increasing Co concentration in terms of the tight-binding model⁵⁹ (Fig. 2). For the $B2$ NiAl phase the main contribution to the DOS around E_f comes from narrow d bands of Ni. These bands form a pseudogap in the DOS between the so-called nonbonding,⁶⁰ predominantly t_{2g} states (from -0.25 to -0.1 Ry) with a small contribution from e_g states (from -0.25 to -0.2 Ry) and the antibonding e_g states right below the Fermi energy E_f . As a Co atom has one less valence electron than Ni, the Fermi level shifts toward a lower energy with increasing Co concentration, in agreement with what can be expected from the rigid bands model. Thus, as one can see from Fig. 2, in the case of pure $B2$ NiAl both t_{2g} and e_g states are filled, whereas in CoAl the antibonding e_g states remain almost empty. The t_{2g} (d_{xy} , d_{yz} , d_{zx}) electrons are directed toward the eight nearest-neighbor atoms in the bcc lattice, e.g., in our case, toward Al and Ni or Al and Co atoms, located on different sublattices of the $B2$ unit cell. The e_g ($d_{x^2-y^2}$ and d_{z^2}) electrons are directed toward the next-nearest-neighbor atoms located on the same sublattice. For NiAl, t_{2g} and e_g states are almost fully occupied, and therefore there should be no specific direction in the electron charge density distribution. On the other hand, in $B2$ CoAl the t_{2g} states are fully occupied while the e_g states are mostly located above the Fermi level. This promotes more directional electron charge density distribution toward the nearest neighbors. As a result,

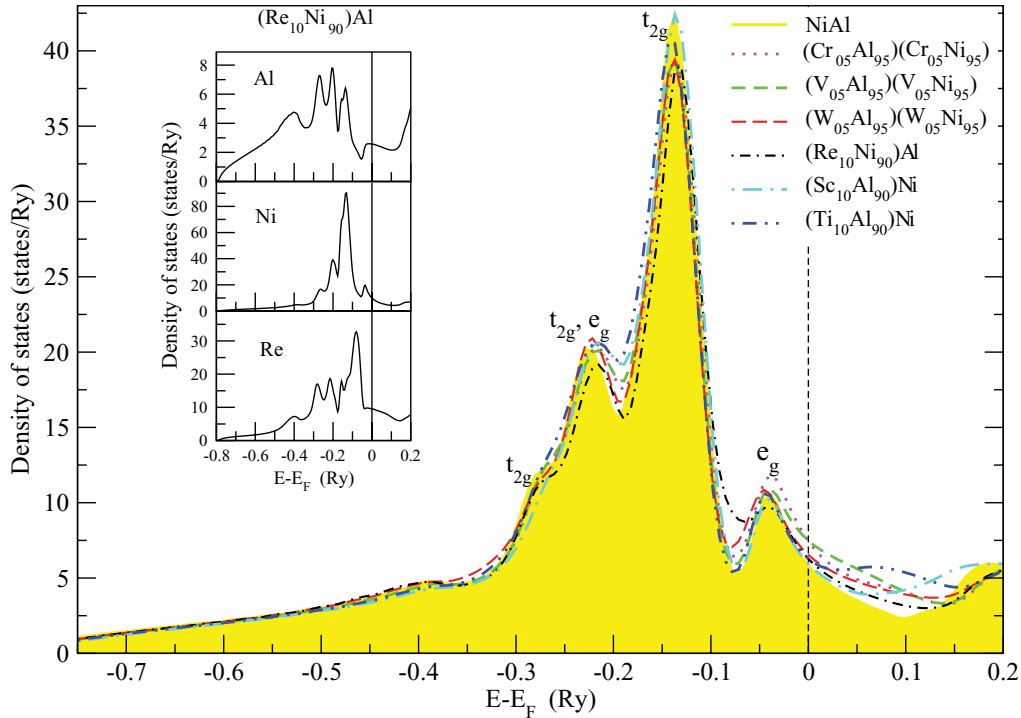


FIG. 3. (Color online) Calculated total density of states for NiAl containing Cr, V, W, Re, Sc, and Ti located on different sublattices of the $B2$ structure. Inset: Calculated atom-projected densities of electron states in $B2$ ($\text{Re}_{10}\text{Ni}_{90}$)Al alloy. The Fermi level is set to 0.

the character of bonding in these two intermetallics should be different: in NiAl metallic bonding is predominant (though covalent and ionic bonding are also present), while in CoAl the covalent type of bonding increases. The covalent component is responsible for more brittle behavior in Co-rich ($\text{Co}_c\text{Ni}_{1-c}$) Al alloys. A trend in the lattice constant dependence, i.e., its increase from CoAl to NiAl, is also consistent with the filling of the antibonding e_g states. The decrease in the lattice parameter in NiAl-Co alloys with increasing Co content also causes an enhancement of the elastic constant C_{11} , as a shorter distance provides a larger overlap between Co d states on next-nearest-neighbor Co atoms.

Let us return to the discussion of Fig. 1. For $(\text{W}_c\text{Ni}_{1-c})(\text{W}_c\text{Al}_{1-c})$ and $(\text{V}_c\text{Ni}_{1-c})(\text{V}_c\text{Al}_{1-c})$ alloys for the given concentration (Table III) and for $(\text{Re}_c\text{Ni}_{1-c})\text{Al}$ for $c > 10$ at%, both the Pugh ratio and the Cauchy pressure predict an improved ductility. For NiAl-Re and NiAl-W alloys the elastic modulus C_{11} is almost constant at low concentrations of Re and W, while C_{12} and C_{44} increase monotonically, despite the fact that C_{44} usually decreases with increasing ductility, as is the case in $(\text{V}_c\text{Ni}_{1-c})(\text{V}_c\text{Al}_{1-c})$ alloys (see the Appendix). This suggests that alloying of NiAl with Re or W enhances both metallic and covalent types of interactions: although bonds are mainly metallic ($C_{12} > C_{44}$), increased C_{44} indicates an enhanced partial covalent component of the bonding.

Figure 3 shows the calculated DOS for NiAl-X alloys with $X = \text{Cr}, \text{V}, \text{W}, \text{Re}, \text{Sc},$ and Ti . One can see that for NiAl-Re t_{2g} nonbonding and for NiAl-W alloys e_g antibonding peaks are smeared out and broadened. This delocalization of t_{2g} and e_g electrons provides an enhanced metallic component

to the bonding. The substitution of Ni with Re (W) increases the hybridization between Al p and Re (W) d states with t_{2g} symmetry due to the weaker spatial localization of $5d$ electrons of Re and W compared with $3d$ electrons of Ni [see the inset in Fig. 3, where the atom-projected DOS for the $B2$ ($\text{Re}_{10}\text{Ni}_{90}$)Al alloy is shown]. This increases the covalent component of bonding and enhances the shear resistance. For $(\text{V}_c\text{Ni}_{1-c})(\text{V}_c\text{Al}_{1-c})$ alloys the metallic bonding remains predominant, mainly owing to the contribution of e_g electrons of V to the antibonding peak (Fig. 3).

In the case of paramagnetic (DLM) $(\text{Cr}_c\text{Ni}_{1-c})(\text{Cr}_c\text{Al}_{1-c})$ alloys, changes in the parameter G/B and the Cauchy pressure are small, and the decrease in C_{11} is more pronounced compared to other moduli. Note that if Cr atoms are located only on the Ni sublattice, the Cauchy pressure becomes negative with increasing Cr concentration, as takes place for Co (Fig. 1). If Cr atoms are placed on the Al sublattice, as suggested in some experimental^{12,13} and theoretical studies,^{15,16,18} the Cauchy pressure is positive and increases (Fig. 1). The metallic component of the bonding formed in these alloys is due to Cr-Ni interactions, while the covalent component is formed by the interaction of Cr and Al atoms. But in $(\text{Cr}_c\text{Ni}_{1-c})(\text{Cr}_c\text{Al}_{1-c})$ alloys where Cr atoms occupy both Ni and Al sublattices with equal probability, interatomic interactions on different sublattices have the opposite effect on the elastic properties, and as a result, the brittle vs ductile behavior is affected only slightly (see Fig. 6).

In $(\text{Ti}_c\text{Al}_{1-c})\text{Ni}$ alloys elastic constants C_{11} and C_{44} decrease with increasing Ti concentration. At the same time, C_{12} increases slightly, and the decrease in C_{44} is more pronounced compared to C_{11} (see Fig. 5). This leads to a

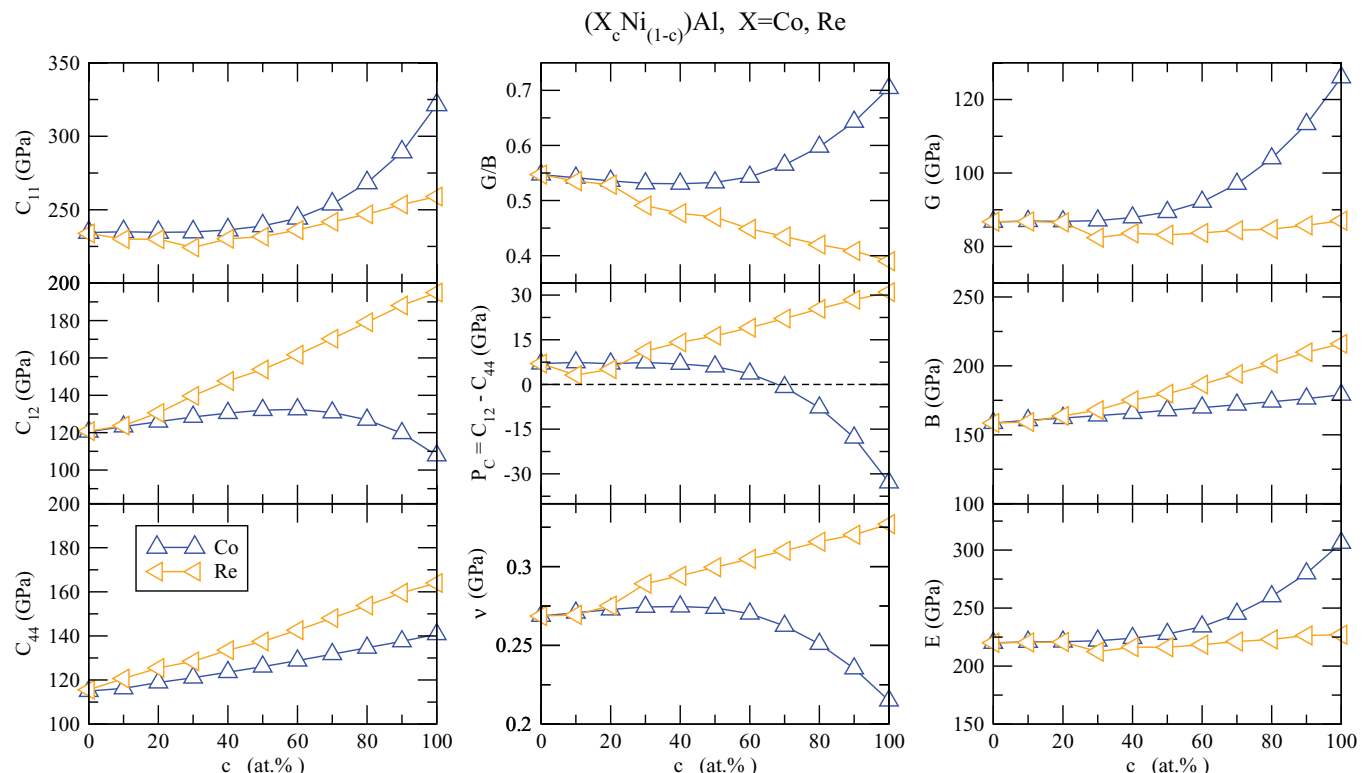


FIG. 4. (Color online) Calculated elastic constants C_{11} , C_{12} , and C_{44} , Pugh ratio G/B , Cauchy pressure $P_C = (C_{12} - C_{44})$, Poisson ratio ν , shear moduli G , bulk moduli B , and Young moduli E of NiAl-X alloys with $X = \text{Co}$ and Re located on the Ni sublattice.

decrease in the shear moduli C' , G , and the Young modulus E . The bulk modulus B is almost constant while the lattice parameter increases, meaning that the average valence electron density is not increased, despite the partial substitution of Al with Ti and the increased number of valence electrons. In comparison with NiAl the G/B ratio decreases; at the same time the Cauchy pressure becomes more positive with increasing Ti concentration. This indicates a reduction in the covalent contribution to the bonding.

Similar behavior of elastic constants is observed in the case of alloying of NiAl with Sc , where there is a strong decrease in C_{11} , C_{44} , G , and E (up to 60 at% Sc). In addition, the bulk modulus B and C_{12} are also reduced. In $(\text{Sc}_c\text{Al}_{1-c})\text{Ni}$ alloys we find a reduced covalent contribution to the interatomic bonds, as follows from the decreases in the G/B ratio and increases in the Cauchy pressure. Nevertheless, in this case changes in G/B and Cauchy pressure are not as significant as for $(\text{Ti}_c\text{Al}_{1-c})\text{Ni}$ alloys. This might be due to the fact that in $(\text{Sc}_c\text{Al}_{1-c})\text{Ni}$ alloys there is a stronger contribution of the ionic component to interatomic interaction, in addition to mainly metallic bonding. The charge transfer caused by the difference in electronegativities might lead to an ionic admixture to the bonding. For Sc , which has the largest difference in electronegativities from Ni of all studied ternary additions, we found the lowest Zener anisotropy parameter A_z (Table III), indicating more isotropic behavior of NiAl-Sc alloys.

Alloying of NiAl with Ti and Sc smears out the nonbonding peak of the DOS. The pseudogap located at -0.2 Ry is due to d electrons of Ti (Sc). There is significant charge transfer

from t_{2g} states of Ti (Sc) to e_g states of Ni . At the same time, antibonding states near the Fermi energy remain almost unchanged (Fig. 3).

IV. CONCLUSION

In this work we have carried out a systematic theoretical study of the influence of alloying on the elastic properties of $B2$ NiAl . First, we investigated the site preference of ternary additions at $T = 0$ K and observed that the early transition metals Sc and Ti preferentially substitute for Al , whereas Re and Co have a strong preference for the Ni sublattice. Cr , W , and V are predicted to have no site preference. Considering these impurities at their preferential sites, we created a database of *ab initio* elastic constants C_{11} , C_{12} , and C_{44} , shear moduli G , bulk moduli B , Young moduli E , Pugh ratio G/B , and Cauchy pressure P_C . The database was then used to analyze the mechanical behavior of the alloys using phenomenological correlations between ductility and elastic properties of solution phases. Our calculations have shown that the addition of W , V , Re , and Ti should improve the ductility of $B2$ NiAl without significant changes in the macroscopic elastic moduli (at a low concentration of W , V , and Ti). For these metals the main contribution to the bonding in the alloys has a metallic character. Changes in bonding of the $(\text{Ti}_c\text{Al}_{1-c})\text{Ni}$ and $(\text{V}_c\text{Ni}_{(1-c)})(\text{V}_c\text{Al}_{(1-c)})$ alloys, in comparison with NiAl , are mainly due to the delocalization of d electrons occupying antibonding states. The $(\text{Re}_c\text{Ni}_{(1-c)})\text{Al}$ and $(\text{W}_c\text{Ni}_{(1-c)})(\text{W}_c\text{Al}_{(1-c)})$ alloys also contain a directional covalent bonding contribution. Co , Sc , and Cr should not

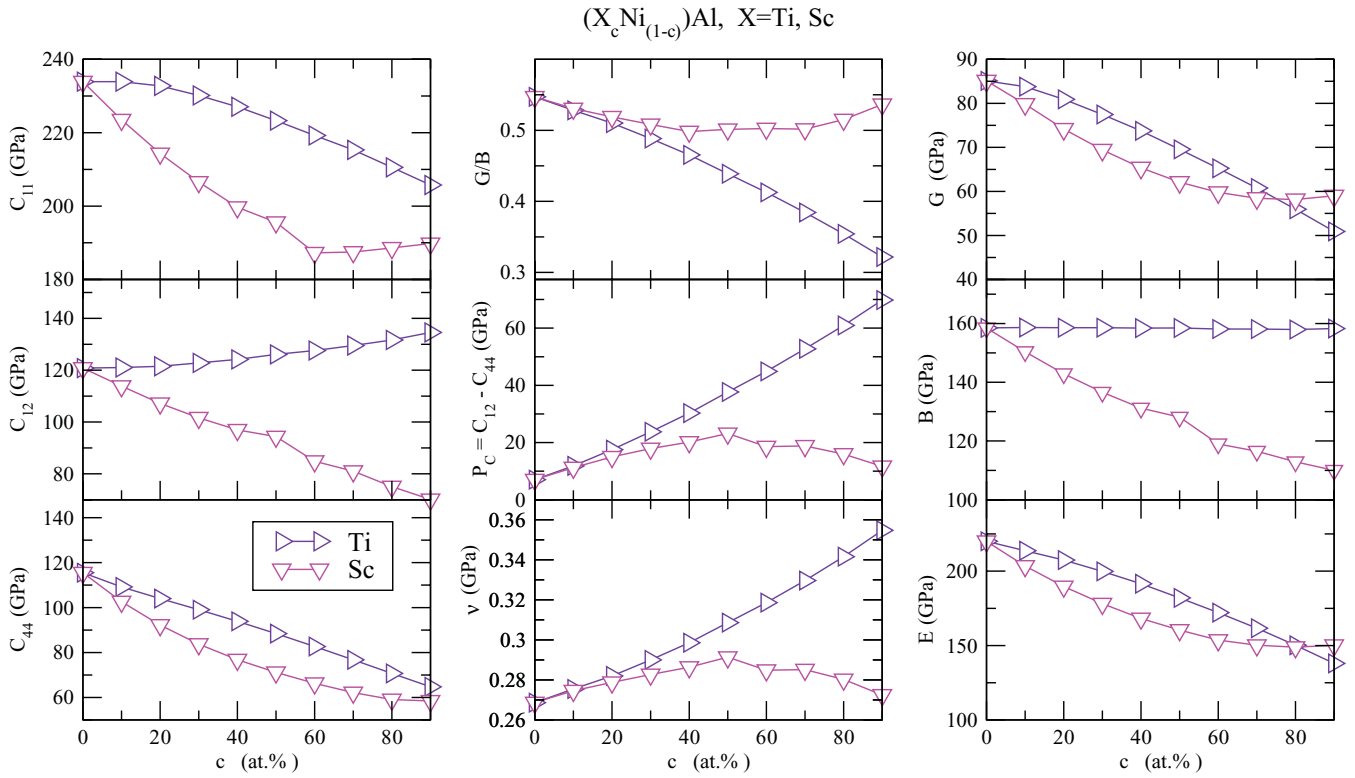


FIG. 5. (Color online) Calculated elastic constants C_{11} , C_{12} and C_{44} , Pugh ratio G/B , Cauchy pressure $P_C = (C_{12} - C_{44})$, Poisson ratio ν , shear moduli G , bulk moduli B , and Young moduli E of NiAl-X alloys with $X = \text{Sc}$ and Ti located on the Al sublattice.

lead to improvements in the ductility of B2 NiAl. In Co-NiAl alloys the type of interatomic interactions changes from predominantly metallic to covalent with increasing Co

concentration. The NiAl-Sc alloys are more isotropic than B2 NiAl due to the significant ionic component in addition to metallic bonding. Cr addition (located on both Ni and Al

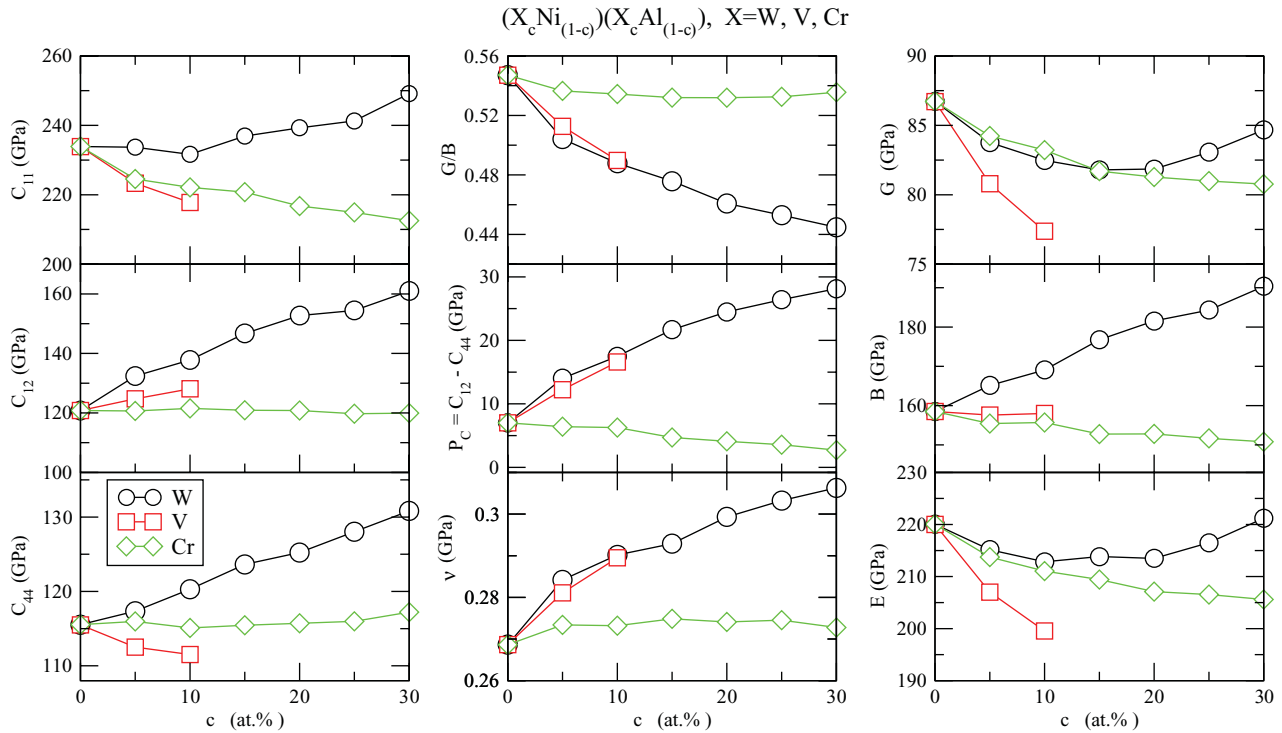


FIG. 6. (Color online) Calculated elastic constants C_{11} , C_{12} , and C_{44} , Pugh ratio G/B , Cauchy pressure $P_C = (C_{12} - C_{44})$, Poisson ratio ν , shear moduli G , bulk moduli B , and Young moduli E of NiAl-X alloys with $X = \text{W, V,}$ and Cr located on both the Ni and the Al sublattices.

sublattices) has a weak effect on the brittle vs ductile behavior in $B2$ NiAl alloys.

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at the Joint Supercomputer Center of the Russian Academy of Sciences (Moscow) and the Swedish National Infrastructure for Computing (SNIC) National Supercomputer Centre (NSC) in Linköping, Sweden.

APPENDIX

In the figures in this Appendix we plot the calculated elastic constants C_{11} , C_{12} , and C_{44} , Pugh ratio G/B , Cauchy pressure $P_C = (C_{12} - C_{44})$, Poisson ratio ν , shear moduli G , bulk moduli B , and Young moduli E of NiAl- X alloys with $X = \text{Co}$ and Re located on the Ni sublattice (Fig. 4), Sc and Ti located on the Al sublattice (Fig. 5), and W , V , and Cr located on both the Ni and the Al sublattices (Fig. 6).

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