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Identical effects of indirect and direct electron doping of superconducting BaFe₂As₂ thin films

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Electron doping of a 122-type iron pnictide $BaFe_2As_2$ by substituting the Ba site with an aliovalent ion (indirect doping), which had been unsuccessful by conventional solid-state synthesis methods, was achieved by a nonequilibrium film growth process. The substitution with La was substantiated by a systematic shrinkage of the *c*-axis lattice parameter due to the smaller ionic radius of La^{3+} than that of Ba^{2+} . A negative Hall coefficient indicated that the majority carriers were electrons, as is consistent with this aliovalent ion doping. The La substitution suppressed an antiferromagnetic transition and induced bulk superconductivity at a maximum onset critical temperature (T_c) of 22.4 K. The electronic phase diagram for $(Ba_{1-x}La_x)Fe_2As_2$ was built, which revealed that the indirect electron doping at the Ba site with La $[(Ba_{1-x}La_x)Fe_2As_2]$ exhibits almost the same T_c - doping level relation as that of the direct electron doping at the Fe site with Co $[Ba(Fe_{1-x}Co_x)_2As_2]$. This finding clarified that T_c in 122-type compounds is not affected by a crystallographic doping site, which is in sharp contrast to the 1111-type compounds, *RE*FeAsO (*RE* = rare earth). It is tentatively attributed to the differences in their dimensionality of electronic structures and electron pairing symmetries.

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Since the discovery of iron pnictide superconductors¹ with high critical temperatures (T_c) up to 55 K,² there has been intensive effort to elucidate superconductivity mechanisms. Among iron pnictide superconductors, 1111-type REFeAsO $(RE = \text{rare earth})^1$ and 122-type $AEFe_2As_2$ (AE = alkaline) earth)³ systems have been investigated extensively, and their electronic phase diagrams have been mapped out^{4-7} to discuss superconductivity mechanisms.^{8–10} Superconductivity in these compounds is induced by chemical substitution with aliovalent elements, which leads to the doping of electrons or holes into the parent materials, along with suppression of an antiferromagnetic (AFM) ordering and a tetragonal-to-orthorhombic structural phase transition.¹¹ The structures of these crystals are composed of alternating stacking of FeAs and REO/AE layers, where the former forms a Fermi surface and serves as a carrier conducting path (active pairing planes in a superconducting state), while the latter acts as a nonactive blocking layer, in particular, for 1111-type compounds with thicker three-atomic REoxide layers. Thus, carrier doping may be classified by crystallographic doping sites, i.e., aliovalent ion doping in the active FeAs layers ("direct doping") and in the nonactive REO/AE layers ("indirect doping") (see the inset to Fig. 4).

It is thought that direct doping causes a large deterioration on T_c , because impurity scattering and disorder in the active pairing layers provide a larger perturbation.¹² Indeed, it has been clarified that this is the case for the 1111-type *RE*FeAsO.⁵ On the other hand, recent theoretical studies have proposed that the sensitivity to impurity doping at Fe sites depends largely on the electron pairing symmetries.¹³ Due to unique multiorbital band structures at the Fermi levels of the iron pnictides, several pairing symmetries, such as a sign-reversal s_{+-} wave state^{8,9} and a non-sign-reversal s_{++} wave state,¹⁰ have been proposed theoretically. According to their first-principles calculation with Anderson's theorem by assuming the impurity potential for nonmagnetic dopants at Fe sites,¹³ although the sign-reversal s_{+-} wave state is sensitive to the impurity doping in the active pairing layers, the non-sign-reversal s_{++} wave state is robust, i.e., T_c remains almost unchanged with the doping level, opposite to the conspicuous T_c drop for the s_{+-} case. As noted above, it is reported that the 1111-type iron pnictides, REFeAsO, exhibit pronounced differences in the maximum $T_{\rm c}$ between direct electron doping [e.g., 17 K for $Sm(Fe_{1-x}Co_x)AsO(Ref. 5)$] and indirect electron doping [55 K for SmFeAs($O_{1-x}F_x$) (Ref. 2)]; therefore, the s_{+-} wave state mediated by an AFM spin fluctuation is now accepted for the electron-pairing symmetry for the 1111-type iron pnictides. This model is supported experimentally by observation of the half-flux-quantum effect in F-doped NdFeAsO polycrystals.¹⁴ However, for 122-type compounds, AEFe₂As₂, to the best of our knowledge, this hypothesis has not been examined experimentally, because indirect electron doping has not been achieved by conventional solid-state reactions^{15,16} (the only exceptions are Ref. 16 for AE = Sr achieved by a high-pressure synthesis and Refs. 17 and 18 for AE = Ca achieved by a melt-growth method) due to the electronic instability of the indirectly electron-doped $AEFe_2As_2$.¹⁹

In this Rapid Communication, we employ a nonequilibrium film-growth process to achieve metastable doping of La into the Ba sites of BaFe₂As₂. Although doping of a La ion has been unsuccessful for bulk polycrystalline samples, La dopants are successfully introduced into the BaFe₂As₂ epitaxial films grown by pulsed laser deposition (PLD). The electronic phase diagram obtained for indirect electron doping of Ba(Fe_{1-x}Co_x)₂As₂.⁷ The close similarity between the indirect and direct doping effects in BaFe₂As₂ differs from the trends in *RE*FeAsO materials.^{2,5}

Here 150–250 nm thick films of $(Ba_{1-x}La_x)Fe_2As_2$ were fabricated on MgO (001) single crystals at an optimized growth temperature of 850 °C by PLD using a neodymium-doped

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yttrium aluminum garnet laser as the excitation source and polycrystalline bulks of La-added BaFe₂As₂ as ablation targets synthesized by a solid-state reaction. The detailed fabrication process is reported in Ref. 20. The obtained phases and their lattice parameters were examined by powder x-ray diffraction (XRD; anode radiation: Cu $K\alpha$, D8 ADVANCE-TXS, Bruker AXS) for polycrystalline bulk samples, while high-resolution XRD (anode radiation: Cu $K\alpha_1$, Smart Lab, RIGAKU) was used for thin films. The chemical doping concentrations of the thin films (x_{film}) were estimated using a wavelengthdispersive x-ray electron-probe microanalyzer (EPMA), which also demonstrated the homogeneity of the La distribution in the $(Ba_{1-x}La_x)Fe_2As_2$ films (see Fig. S3 in the Supplemental Material for chemical composition mapping images²¹). Temperature dependences of electrical resistivity $(\rho - T)$ were measured by the four-probe method in a T range of 2-300 K with a physical property measurement system (PPMS, Quantum Design). The temperature dependences of magnetization were measured with a vibrating sample magnetometer (VSM) after zero-field cooling (ZFC) and during field cooling (FC). The Hall effect measurements were performed using a six-terminal Hall bar structure formed by photolithography and Ar ion milling. The external magnetic field was applied parallel to the c axis for both the magnetization and Hall effect measurements.

Figure 1 shows the evolution of the lattice parameters with doping concentration for bulk polycrystalline samples synthesized by a solid-state reaction and epitaxial films grown by PLD (see Figs. S1 and S2 in the Supplemental Material for XRD patterns²¹). Here, the doping concentrations are taken as the nominal values for the bulk polycrystalline samples (x_{bulk}) and as the chemical composition values measured by EPMA for the epitaxial films (x_{film}) . For the bulk polycrystals, neither the *c*- nor *a*-axis lengths were changed upon impurity doping, indicating that the La³⁺ ions were not incorporated into the BaFe₂As₂ phase by a solid-state reaction. In contrast, for the epitaxial films, the *c*-axis length systematically shrank



FIG. 1. (Color online) Variation in the unit cell dimension in La-doped BaFe₂As₂ thin films and bulk polycrystals with doping concentration. Data were taken at room temperature for bulk polycrystals (open symbols) and thin films (solid symbols). The doping concentrations are taken as the nominal values for bulk polycrystals (x_{bulk}) and those measured by EPMA for thin films (x_{film}).

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FIG. 2. (Color online) Variation of ρ -*T* curves with doping concentration in (Ba_{1-x}La_x)Fe₂As₂ epitaxial films ($x_{film} = 0-0.44$). Doping concentrations x_{film} are indicated in the figures. The right-hand panel shows an enlarged view around T_c ($T \le 35$ K). The arrows in the left- and right-hand panels indicate the positions of temperatures of resistivity anomaly (T_{anom}) and onset T_c (T_c^{conset}), respectively.

 $(\Delta c/c \sim -3.5\%$ for $x_{\rm film} = 0.44$), while the change in the *a* axis was much smaller ($\Delta a/a \sim -0.3\%$). These results substantiate that La³⁺ ion substitution for the Ba²⁺ sites is achieved in the epitaxial films.

Figure 2 summarizes the ρ -T curves for the $(Ba_{1-x}La_x)Fe_2As_2$ epitaxial films with $x_{film} = 0-0.44$. The ρ at room temperature gradually decreased with increasing x_{film} . The temperature of resistivity anomaly (T_{anom}) , which is associated with the structural and magnetic phase transitions,²² continuously shifted from 135 K to the lower T side as x_{film} increased. A superconducting transition with zero resistivity (an expanded view is shown in the right-hand panel of Fig. 2) was distinctly observed for $x_{\text{film}} = 0.08$, but the resistivity anomaly still remained as observed at $T_{anom} =$ 72 K, indicating that the superconductivity and the AFM ordering coexist. As x_{film} further increased, the resistivity anomaly was not detected in the ρ -T curves. Additionally, the onset T_c (T_c^{onset}) reached a maximum value 22.4 K at $x_{\text{film}} =$ 0.13, and then monotonically decreased to zero (normal metal state) as x_{film} further increased to $x_{\text{film}} = 0.44$. The maximum T_{c}^{onset} of $(Ba_{1-x}La_x)Fe_2As_2$ is comparable to T_{c}^{onset} of 22 K for $(Sr_{1-x}La_x)Fe_2As_2$ polycrystalline samples,¹⁶ but is much lower than T_c^{onset} of ~40 K for $(Ca_{1-x}RE_x)Fe_2As_2$ single crystals.^{17,18}

To confirm bulk superconductivity of the resulting epitaxial films, magnetization measurements were performed on the optimally doped $(Ba_{1-x}La_x)Fe_2As_2$ films with $x_{film} = 0.13$ [Fig. 3(a)]. The shielding signal for ZFC was detected from T = 18 K and corresponded to a 100% shielding volume fraction at T < 7 K, verifying bulk superconductivity. We also examined the effects of lattice strain because the $(Ba_{1-x}La_x)Fe_2As_2$ epitaxial films exhibited a shrinkage of lattice parameters by La doping and would be affected also by the tensile mismatch strain from the MgO substrate. However, no significant change in ρ -T curves was observed even after the films were subjected to postdeposition thermal annealing at 500 °C for 2 h in a high-vacuum condition. Therefore, we concluded that the observed electrical properties and superconductivity in the $(Ba_{1-x}La_x)Fe_2As_2$ epitaxial films are not due to a lattice-strain effect.

In addition, to investigate the polarity of the dominant carriers, Hall effect measurements were conducted for the



FIG. 3. (Color online) Electromagnetic properties of optimally doped $(Ba_{1-x}La_x)Fe_2As_2$ epitaxial films with $x_{film} = 0.13$. (a) Temperature dependence of the dc susceptibility under a magnetic field $\mu_0 H = 5$ G applied parallel to the *c* axis. (b) Transverse resistivity ρ_{xy} under magnetic fields up to 9 T at T = 300-25 K. The inset shows the *T* dependence of Hall coefficient $R_{\rm H}$ estimated from the high $\mu_0 H$ region (≥ 3 T).

optimally doped $(Ba_{1-x}La_x)Fe_2As_2$ epitaxial film. Figure 3(b) shows transverse resistivity ρ_{xy} in magnetic fields $\mu_0 H$ up to 9 T ($\mu_0 H \parallel c$) measured at T = 300-25 K. The slope $d\rho_{xy}/d(\mu_0 H)$ was negative in the high $\mu_0 H$ region, but a small increase in ρ_{xy} was observed in the low $\mu_0 H$ region. Similar to reports on Ba($Fe_{1-x}Co_x$)₂As₂ films,²³ the small increase might be due to anomalous Hall effects arising from a small magnetic impurity such as Fe and/or the $(Ba_{1-x}La_x)Fe_2As_2$ phase. The Hall coefficients (R_H) were estimated by excluding the anomalous ρ_{xy} region at low $\mu_0 H$ \leq 3 T and extracting the straight line region at the higher $\mu_0 H$. The inset in Fig. 3(b) shows the T dependence of $R_{\rm H}$. The negative $R_{\rm H}$ confirmed that electrons dominate the transport properties of $(Ba_{1-x}La_x)Fe_2As_2$ films, which is consistent with the supposition that the La^{3+} dopants occupy the Ba^{2+} sites. $|R_{\rm H}|$ gradually increased as T decreased without the sudden increase associated with an AFM transition,²⁴ and the $|R_{\rm H}|$ value at 25 K ($-2.5 \times 10^{-3} \text{ cm}^3/\text{C}$) is comparable to those of optimally doped $Ba(Fe_{1-x}Co_x)_2As_2$ single crystals $[(-2 \text{ to } -3) \times 10^{-3} \text{ cm}^3/\text{C}]^{23}$, which indicates that the carrier concentrations in the present $(Ba_{1-x}La_x)Fe_2As_2$ films are almost the same as the optimum concentration in the $Ba(Fe_{1-x}Co_x)_2As_2$ single crystals.

Figure 4 summarizes the electronic phase diagram of T_{anom} and T_c^{onset} for the $(Ba_{1-x}La_x)Fe_2As_2$ epitaxial films as a function of doping concentration. The previously reported phase diagram of directly electron-doped Ba(Fe_{1-x}Co_x)₂As₂ single crystals⁷ is superimposed in the figure. Here the doping concentrations are normalized as the doped carriers per Fe

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FIG. 4. (Color online) Electronic phase diagram of indirect electron-doped $(Ba_{1-x}La_x)Fe_2As_2$. Open and solid symbols indicate the T_{anom} and T_c^{onset} , respectively. Those reported for directly electron-doped Ba(Fe_{1-x}Co_x)_2As_2 single crystals (Ref. 7) are also shown for comparison. The inset figure illustrates the concept of indirect and direct dopings in the BaFe_2As_2 crystal.

(i.e., $x_{\rm film}/2$) to compare with the phase diagram of direct electron-doped Ba($Fe_{1-x}Co_x$)₂As₂. For the indirect electrondoped $(Ba_{1-x}La_x)Fe_2As_2$ films, T_{anom} rapidly decreased, and the plots of T_c^{onset} formed a bell-shaped dome. The superconductivity and the AFM state coexisted only in the low doping region ($x_{\text{film}}/2 \approx 0.04$). The maximum $T_{\text{c}}^{\text{onset}}$ position for the $(Ba_{1-x}La_x)Fe_2As_2$ films was $x_{film}/2 \cong 0.07$, which is very close to that reported for the direct-doped Ba($Fe_{1-x}Co_x$)₂As₂ single crystals (optimal doping concentration $x \cong 0.07$). It is noteworthy that the dome widths for the indirect-doped $(Ba_{1-r}La_r)Fe_2As_2$ and the direct-doped $Ba(Fe_{1-r}Co_r)_2As_2$ are almost the same. In addition, the suppression rate of T_{anom} (i.e., $|dT_{\text{anom}}/dx_{\text{Film}}|$) shows close agreement with that of $Ba(Fe_{1-x}Co_x)_2As_2$. It is noted that the variations of T_{anom} and $T_{\text{c}}^{\text{onset}}$ on the doping concentration closely overlap between the indirect-doped $(Ba_{1-x}La_x)Fe_2As_2$ and the direct-doped Ba($Fe_{1-x}Co_x$)₂As₂. These results show a sharp contrast with those of 1111-type iron pnictides, in which the T_c of indirect-doped SmFeAs($O_{1-x}F_x$) (55 K)² is far higher than that of direct-doped Sm(Fe_{1-x}Co_x)AsO (17 K),⁵ and the superconductivity dome width of T_c for direct doping is much narrower than that of indirect doping.^{4,5}

We consider that there are two plausible reasons for the observed prominent differences between the 1111-type compounds and the 122-type compounds. One is the different dimensionality of their electronic structures, i.e., the Fermi surfaces of the 1111-type compounds are highly two dimensional due to the thicker blocking layers formed by the three atomic REO layers, while those of the 122-type compounds are more three dimensional.^{25,26} Therefore, the wave functions are more extended to the AE layers and hence, upon substitution of the AE site, the superconducting properties are more affected in the 122-type compounds. Another possibility is the different pairing symmetries of the superconducting states, i.e., it is considered that the 1111-type compounds are attributed to the sign-reversal s_{+-} wave state that is sensitive to the doping sites, while the above observations in BaFe2As2 are more consistent with the non-sign-reversal s_{++} wave state.¹³ However, further effort is needed to clarify which idea is the controlling factor.

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It would also be important to compare the phase diagram of $(Ba_{1-x}La_x)Fe_2As_2$ with those of indirect electron-doped $(Ca_{1-x}RE_x)Fe_2As_2$ single crystals,¹⁷ because the latter's maximum T_c^{onset} (~47 K) is much higher than that of direct Co-doped [Ca(Fe_{1-x}Co_x)₂As₂] (~20 K),²⁷ which is totally different from the present BaFe₂As₂ case, in spite of similar material systems and electronic structures. However, we should notice that all of the RE-doped CaFe₂As₂ single crystals reported to date showed very small shielding volume fractions.^{17,18} In addition, $(Ca_{1-x}Pr_x)Fe_2As_2$ single crystals have two superconducting phases with T_c of 21 and 49 K, where the former would be the bulk T_c of $(Ca_{1-x}Pr_x)Fe_2As_2$ because of a large diamagnetism while the latter with a small shielding volume fraction may be attributed to a trace secondary phase or a strained surface phase.¹⁸ If one takes the bulk T_c of 21 K for $(Ca_{1-x}RE_x)Fe_2As_2$, it is consistent with the present results.

In conclusion, indirect electron doping into $BaFe_2As_2$ was attained by using epitaxial films of La-doped $BaFe_2As_2$

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on MgO (001) substrates. The nonequilibrium film-growth process is an effective way to stabilize the metastable doping of La at Ba sites. The La substitution rapidly suppressed the AFM transition and induced superconductivity at a maximum T_c^{onset} of 22.4 K for $(Ba_{1-x}La_x)Fe_2As_2$. We obtained clear superconducting domes closely overlapping with those of direct electron-doped Ba $(Fe_{1-x}Co_x)_2As_2$. The identical effect of the indirect and the direct electron doping clarified that T_c does not depend on whether or not impurity dopants exist in the active pairing layers, but depends solely on doped carrier concentrations. This result is consistent with the stronger three dimensionality of the Fermi-surface electron-doped BaFe_2As_2.

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