

Mott transition in multiorbital models for iron pnictides

Rong Yu and Qimiao Si

Department of Physics and Astronomy, Rice University, Houston, Texas 77005, USA

(Received 13 June 2010; revised manuscript received 13 November 2011; published 5 December 2011)

The bad-metal behavior of the iron pnictides has motivated a theoretical description in terms of a proximity to Mott localization. Since the parent compounds of the iron pnictides contain an even number of 3d electrons per Fe, it is important to determine whether a Mott transition robustly exists and clarify the nature of the possible Mott insulating phases. We address these issues in a minimal two-orbital model and a more realistic four-orbital model for the parent iron pnictides using a slave-spin approach. In the two-orbital model with two electrons per Fe, we identify a single transition from a metal to a Mott insulator, showing that this transition must exist as a result of orbital degeneracy. Depending on the ratio between the inter- and intraorbital Coulomb repulsions, the insulating state can be either a high-spin Mott insulator or a low-spin orbital-Mott insulator. In the four-orbital model with four electrons per Fe, we find a rich phase diagram for the metal-to-insulator transition. At strong Hund's couplings, a localization transition to a high-spin Mott insulator always occurs. At zero and weak Hund's couplings, on the other hand, we find a transition to an intermediate-spin insulating state. This transition can be viewed as an orbitally selective metal-to-insulator transition: the transition to a Mott insulator in the xz and yz orbitals takes place at the same critical coupling as the transition to either a band insulator at zero Hund's coupling or an orbitally polarized insulator at weak but finite Hund's coupling in the xy and $x^2 - y^2$ orbitals. The implications of our model studies for the physics of iron pnictides and iron chalcogenides are discussed.

DOI: [10.1103/PhysRevB.84.235115](https://doi.org/10.1103/PhysRevB.84.235115)

PACS number(s): 71.10.Hf, 71.27.+a, 71.55.-i, 75.20.Hr

I. INTRODUCTION

The microscopic physics of the iron pnictides and related high- T_c superconductors^{1,2} is a subject of extensive studies. The parent systems are antiferromagnetically ordered,³ implying that Coulomb interactions must play some role. The metallic nature of these systems gives rise to a tendency to treat the interactions perturbatively. However, various considerations have led to the notion that the parent iron pnictides and iron chalcogenides are on the verge of a Mott localization transition. These considerations have been based on the observed bad-metal properties,^{4,5} first-principles calculations,^{6,7} and related analyses.⁸⁻¹² The bad-metal properties are characteristic of metallic systems in proximity to a Mott localization. The electrical resistivity at room temperature corresponds to a short mean free path, on the order of the average interelectron spacing. The Drude weight seen in the room temperature optical conductivity is considerably suppressed compared to its noninteracting value.¹³⁻¹⁵ Finally, relatively small changes of temperature induce transfers of the optical spectral weight extending to the eV range.^{14,16,17} The lack of observation¹⁸ of any pronounced incoherent peaks in the high-energy electron spectrum has raised some questions about the incipient Mott picture, but recent microscopic calculations¹⁹ have suggested that this arises from a large damping whose effect is enhanced by the multiorbital nature of the system.

There is some evidence for the incipient Mott picture from the magnetic sector as well. High-energy spin-wave-like excitations have been seen at the zone boundaries.²⁰ In addition, the total spin spectral weight is sizable; for instance, it is more than $1\mu_B/\text{Fe}$ in CaFe_2As_2 .²⁰ These properties cannot be accounted for by the electrons close to the Fermi energy alone; in particular, since the Fermi surfaces comprise small electron and hole pockets, the spin spectral weight coming from the electronic states near the Fermi surfaces will be much smaller than that observed experimentally. Instead, the

observed spin excitation spectrum is more naturally associated with the electronic states far away from the Fermi energy, as would be the case in a metal close to a Mott localization.

The incipient Mott picture arises when U/t is not too far away from the critical value for a Mott transition. (Here t refers to the characteristic bandwidth of the Fe 3d electrons, and U refers to a combination of their Coulomb repulsions and Hund's couplings.) In order to further substantiate this picture, it is important to tune the system into a Mott insulating state. Recently, this has been demonstrated²¹ in the iron oxychalcogenides, which contain an Fe square lattice that is expanded compared to the iron pnictides and iron chalcogenides. The lattice expansion gives rise to a narrowing of the 3d bands and a concomitant enhancement of U/t , which pushes the system through the Mott transition and into the Mott-insulating regime.

Based on the above considerations, it is very important to show theoretically that a transition from a metal to a Mott insulator generally exists in multiorbital models appropriate for the parent compounds of the iron pnictides. This is especially so given that the number of 3d electrons per Fe is even in these systems. The Mott transition, which has long been a subject of fundamental interest,²² is studied in both the one-orbital Hubbard model with one electron per site^{23,24} and multiorbital systems at commensurate fillings.²² In the one-orbital model and paramagnetic phases, the Mott transition can be understood within the Brinkman-Rice picture,²⁵ with an interaction-induced suppression of the coherent one-electron spectral weight near the Fermi energy and the concomitant development of incoherent spectral weight away from the Fermi energy.²⁴ Focusing on the paramagnetic phases is advantageous for considering the Mott transition, since an odd number of electrons per unit cell means that any insulating state must be the result of interactions. The picture applies in the part of the phase diagram above the temperature of ordering

transitions (typically into antiferromagnetic phases); this part of the phase diagram widens with the increase of magnetic frustration.²⁶

In our case, since the parent iron pnictides contain an even number of (six) 3d electrons per Fe, an insulating state could in principle simply be a band insulator. The issue is particularly pertinent given that the Fermi surfaces of the iron pnictides and related systems are small pockets. Indeed, the noninteracting band structure consists of nondegenerate bands (two bands are called degenerate only when their energies are the same at every point in the momentum space) and is close to that of a semiconductor with a small overlap in energy between the bottom of the conduction bands and the top of the valence bands; each band is far away from half filling. It is *a priori* possible that, if an increasing U suppresses a metallic state, the system goes into a correlated band insulator first, thereby invalidating the picture of a bad metal on the verge of a Mott transition. In other words, it is a nontrivial question in the case of the iron pnictides as to whether the metallic state can be in proximity to a Mott transition and, if so, whether the Mott insulator resembles that for the canonical one-orbital Hubbard model with one electron per unit cell. Moreover, given that the bandwidths are very different from band to band, another nontrivial question is whether a Mott transition, when it exists, is a one-step transition or can be an orbital selective Mott transition (OSMT).²⁷

To address these issues, we study how a metal-insulator transition (MIT) in the paramagnetic phase may happen in multiorbital models of iron pnictides containing an even number of electrons filled. Our work builds on earlier studies of multiorbital models for transition metal oxides and related systems. Physics in these multiorbital models is very rich. For instance, many factors, such as inequivalent bandwidths, crystal-field splitting, and Hund's coupling, may affect the nature of the transition.^{28–33} We note that there is a tendency in the literature to work in the band representation and ignore the orbital characters.^{34,35} In our study, we show that the orbital characters serve as another important factor for the Mott transition.

We first study the MIT in a two-orbital Hubbard model with two electrons per site, with a kinetic-energy part given by the minimal band dispersion for the pnictides.³⁶ We analyze the model within a slave-spin (SS) formulation,^{37,38} which has the advantage of readily capturing both the coherent and incoherent part of the electronic spectrum and, in addition, the effect of Hund's coupling. We show that the orbital degeneracy guarantees the existence of a one-step metal-to-Mott-insulator transition in this model. Neither a band insulator nor an OSMT may take place. The critical coupling U_c , which is larger in multiorbital systems than in the single-orbital case,^{39,40} is greatly reduced by a nonzero Hund's coupling; this is consistent with earlier studies in other multiorbital contexts.⁴¹ We find that the nature of the Mott insulator depends on the ratio of the interorbital and intraorbital Coulomb repulsions. It can be either a high-spin Mott state which is driven by the intraorbital coupling or a low-spin orbital-Mott state driven by the interorbital coupling.

We then consider a more realistic four-orbital model including xz , yz , xy , and $x^2 - y^2$ orbitals. In this model, the nature of the MIT depends on the strength of the Hund's

coupling. A strong Hund's coupling stabilizes a high-spin Mott state on the insulator side. But when the Hund's coupling is either zero or weak compared to the crystal-field splitting, we find a novel orbital selective MIT. The xz and yz orbitals experience a transition to a Mott insulator; at the same, critical coupling, a transition to either a band insulator (at zero Hund's coupling) or an orbitally polarized insulator (at nonzero albeit weak Hund's coupling), takes place in the xy and $x^2 - y^2$ orbitals. In this case, the insulating state always has an intermediate-spin value, even at zero Hund's coupling. We establish this to be a direct consequence of the double degeneracy of the xz and yz orbitals.

The remainder of the paper is organized as follows. In Sec. II we summarize the slave-spin formulation and introduce the two-orbital model. Section III is devoted to the MIT in the two-orbital model at half filling. In particular, we propose the concept of low-spin orbital-Mott state. The investigation of MIT in the four-orbital model is presented in Sec. IV, where a rich phase diagram is given. Section V contains some concluding remarks.

II. MULTIORBITAL HUBBARD MODEL AND SLAVE-SPIN REPRESENTATION

The Hamiltonian for the multiorbital Hubbard model is $H = H_0 + H_{\text{int}}$. Here, H_0 is a noninteracting tight-binding Hamiltonian with the general form

$$H_0 = \sum_{\alpha\beta\nu} t_{\alpha\beta}^{\nu} \sum_{i,\sigma} d_{i\alpha\sigma}^{\dagger} d_{i+\nu\beta\sigma} + \sum_{i,\alpha\sigma} (\epsilon_{\alpha} - \mu) d_{i\alpha\sigma}^{\dagger} d_{i\alpha\sigma} \quad (1)$$

in real space, where $d_{i\alpha\sigma}^{\dagger}$ creates an electron on site \mathbf{i} , in orbital α , and with spin σ . ϵ_{α} is the onsite potential of orbital α that incorporates the crystal-field splitting. μ is the chemical potential determined by the electron filling. The interaction reads

$$H_{\text{int}} = U \sum_{i\alpha} n_{i\alpha\uparrow} n_{i\alpha\downarrow} + (U' - J/2) \sum_{i,\alpha<\beta} n_{i\alpha} n_{i\beta} - J \sum_{i,\alpha<\beta} [2\mathbf{S}_{i\alpha} \cdot \mathbf{S}_{i\beta} - (d_{i\alpha\uparrow}^{\dagger} d_{i\alpha\downarrow}^{\dagger} d_{i\beta\downarrow} d_{i\beta\uparrow} + \text{h.c.})], \quad (2)$$

in which U (U') denotes the intraorbital (interorbital) Coulomb repulsion and J the Hund's coupling. These three parameters satisfy $U' = U - 2J$ based on the consideration of rotational symmetry. It is strictly satisfied for an isolated atom in free space where all the d orbitals are degenerate and the Coulomb potential has the full rotational symmetry, and it is assumed to be also valid in solids.⁴² We will adopt this widely used relation unless otherwise specified (see discussion in Sec. III B). The spin operators are $\mathbf{S}_{i\alpha} = \frac{1}{2} \sum_{\sigma\sigma'} d_{i\alpha\sigma}^{\dagger} \vec{\tau}_{\sigma\sigma'} d_{i\alpha\sigma'}$, where $\vec{\tau} = (\tau^x, \tau^y, \tau^z)$ are the Pauli matrices.

It is now generally accepted that the degenerate d_{xz} and d_{yz} orbitals contribute most to the low-energy physics of the parent iron pnictides. Hence, in this paper, we will first consider a two-orbital model introduced in Ref. 36. The simplicity of the model makes it easier to bring out some essential insights, which will also be instructive for the understanding of more realistic models with a larger number of orbitals. Defining $\psi_{\mathbf{k}\sigma}^{\dagger} = (d_{\mathbf{k}x\sigma}^{\dagger}, d_{\mathbf{k}y\sigma}^{\dagger})$, we have

$H_0 = \sum_{\mathbf{k}\sigma} \psi_{\mathbf{k}\sigma}^\dagger [(\varepsilon_+ - \mu)\mathbf{1} + \varepsilon_- \tau^z + \varepsilon_{xy} \tau^x] \psi_{\mathbf{k}\sigma}$, where ε_+ , ε_- , and ε_{xy} are the intra- and interorbital hopping matrices in the momentum space. In the notation of Eq. (1), the orbital degeneracy requires an α -independent ε_α which can be set to zero. We also notice that the tight-binding Hamiltonian in this model is symmetric under the orbital interchange $xz \leftrightarrow yz$. The parent compound has a half filling, i.e., two electrons per site.

We study the MIT in this two-orbital model using the SS formulation.^{37,38} This formulation involves a much smaller number of slave fields, compared to the atomic-configuration-based slave-boson representation of Ref. 43, and more readily treats the full Hund's coupling compared to the slave-rotor representation of Refs. 35 and 44. Here, a slave quantum $S = 1/2$ spin is introduced on each site for each orbital and spin degree of freedom: $d_{i\alpha\sigma} \rightarrow 2S_{i\alpha\sigma}^x f_{i\alpha\sigma}$. The Hilbert space spanned by the SS and auxiliary fermions is limited to the physical part by imposing the constraint $S_{i\alpha\sigma}^z + 1/2 = n_{i\alpha\sigma}$ on each site. The SS formulation handles the electron interactions by rewriting H_{int} in terms of SS operators. The density-density interactions in Eq. (2) (including the Ising-type Hund's coupling) are easily handled by the z component of the SS operator. The spin-flip part of the Hund's coupling and the pair-hopping term are approximately treated by substituting the fermion operators by SS operators that have the same effect on the SS quantum numbers of the Hilbert space, $-J \sum_i [S_{i1\uparrow}^+ S_{i1\downarrow}^- S_{i2\downarrow}^+ S_{i2\uparrow}^- - S_{i1\uparrow}^+ S_{i1\downarrow}^- S_{i2\downarrow}^- S_{i2\uparrow}^+ + \text{H.c.}]$. This approximation should capture the qualitative physics because the SU(2) spin-rotational symmetry of the Hund's coupling is still preserved in the Hilbert space spanned by the slave spins.⁴⁵

The SS formulation is treated at the mean-field (MF) level by fully decoupling the SS and auxiliary fermion operators via a saddle-point approximation. This leads to two decoupled MF Hamiltonians for the SS and the auxiliary fermions:

$$H^S = 4 \sum_{\alpha\beta\sigma} \sum_{i\nu} S_{i,\alpha\sigma}^x S_{i+\nu,\beta\sigma}^x \langle t_{\alpha\beta}^\nu f_{i,\alpha\sigma}^\dagger f_{i+\nu,\beta\sigma} \rangle + \sum_{i,\alpha\sigma} h_{\alpha\sigma} (S_{i,\alpha\sigma}^z + 1/2) + H_{\text{int}}^S, \quad (3)$$

$$H^f = 4 \sum_{\alpha\beta\sigma} \sum_{i\nu} \langle S_{i,\alpha\sigma}^x S_{i+\nu,\beta\sigma}^x \rangle t_{\alpha\beta}^\nu f_{i,\alpha\sigma}^\dagger f_{i+\nu,\beta\sigma} + \sum_{i\alpha\sigma} (\varepsilon_\alpha - h_{\alpha\sigma} - \mu) f_{i,\alpha\sigma}^\dagger f_{i,\alpha\sigma}, \quad (4)$$

where

$$H_{\text{int}}^S = \sum_i \left\{ \frac{U'}{2} \left(\sum_{\alpha\sigma} S_{i\alpha\sigma}^z \right)^2 + \frac{U - U'}{2} \sum_\alpha \left(\sum_\sigma S_{i\alpha\sigma}^z \right)^2 - \frac{J}{2} \sum_\sigma \left(\sum_\alpha S_{i\alpha\sigma}^z \right)^2 - J [S_{i1\uparrow}^+ S_{i1\downarrow}^- S_{i2\downarrow}^+ S_{i2\uparrow}^- - S_{i1\uparrow}^+ S_{i1\downarrow}^- S_{i2\downarrow}^- S_{i2\uparrow}^+ + \text{H.c.}] \right\}, \quad (5)$$

and $h_{\alpha\sigma}$ is a Lagrangian multiplier taking account of the constraint. To solve these two Hamiltonians, we further apply the mean-field decomposition to the term $S_{i,\alpha\sigma}^x S_{i+\nu,\beta\sigma}^x$ in H^S , i.e., $S_{i,\alpha\sigma}^x S_{i+\nu,\beta\sigma}^x \approx \langle S_{i,\alpha\sigma}^x \rangle S_{i+\nu,\beta\sigma}^x + S_{i,\alpha\sigma}^x \langle S_{i+\nu,\beta\sigma}^x \rangle -$

$\langle S_{i,\alpha\sigma}^x S_{i+\nu,\beta\sigma}^x \rangle$, and assume $\langle S_{i,\alpha\sigma}^x \rangle$ to be site independent. The Hamiltonian for the SS operators is then reduced to (up to a constant)

$$H_{\text{MF}}^S = \sum_{i,\alpha\sigma} [K_{\alpha\sigma} S_{i,\alpha\sigma}^x + h_{\alpha\sigma} (S_{i,\alpha\sigma}^z + 1/2)] + H_{\text{int}}^S, \quad (6)$$

where $K_{\alpha\sigma} = 8 \sum_\beta \langle S_{\beta\sigma}^x \rangle \sum_{i\nu} \langle t_{\alpha\beta}^\nu f_{i,\alpha\sigma}^\dagger f_{i+\nu,\beta\sigma} \rangle$. The quasiparticles near the Fermi level are described by the auxiliary fermion Hamiltonian H^f . Introducing the quasiparticle spectral weight $Z_\alpha = 4 \langle S_{\alpha\sigma}^x \rangle^2$, H^f is written as

$$H_{\text{MF}}^f = \sum_{\alpha\beta\sigma} \sum_{i\nu} \sqrt{Z_\alpha Z_\beta} t_{\alpha\beta}^\nu f_{i,\alpha\sigma}^\dagger f_{i+\nu,\beta\sigma} + \sum_{i\alpha\sigma} (\varepsilon_\alpha - h_{\alpha\sigma} - \mu) f_{i,\alpha\sigma}^\dagger f_{i,\alpha\sigma}, \quad (7)$$

which has a similar form as H_0 , with the hopping $t_{\alpha\beta}^\nu$ renormalized to $\sqrt{Z_\alpha Z_\beta} t_{\alpha\beta}^\nu$. In practice, Eqs. (6) and (7) are self-consistently solved by iteratively determining the parameters $h_{\alpha\sigma}$ and $K_{\alpha\sigma}$ (hence Z_α). The metallic behavior corresponds to the Bose condensation of the slave spins, which is marked by a nonzero Z_α . The Mott insulating behavior of orbital α is then identified by $Z_\alpha = 0$.

III. RESULTS FOR THE TWO-ORBITAL MODEL

A. Mott transition in the two-orbital model

In the two-orbital model for iron pnictides, the noninteracting tight-binding Hamiltonian contains an interorbital hopping ε_{xy} and cannot be diagonalized by a uniform (\mathbf{k} -independent) orbital rotation. This leads to two nondegenerate bands which have asymmetric local density of states (LDOS) with respect to the chemical potential. The Fermi surface consists of small electron and hole pockets, indicating that both bands are far away from half filling. It is then important to ask whether, when the interactions are turned on, the system undergoes a transition to a Mott insulator, or the band degeneracy can be fully lifted so that a correlated band insulator may be stabilized. If a Mott transition does take place, it is also interesting to ask whether the transition to the Mott insulator is through a single MIT or via an OSMT.

Most of the previous studies on the MIT in multiorbital systems work in the band presentation, assuming a diagonalized band structure with zero interband hopping. This oversimplified treatment neglects the orbital character of the model. Within this representation, the only way to generate two bands with asymmetric LDOS is to introduce a finite crystal-field splitting which breaks the orbital degeneracy in the model. In this study we choose to work in the orbital representation, which takes into account the full orbital characters of the model. In this orbital representation, the symmetry of H_0 and H_{int} under interchanging of the xz and yz orbitals guarantees that both orbitals contribute equally to the band structure.

The above considerations lead to two important consequences. First, $n_{xz,\sigma} = n_{yz,\sigma} = 1/2$ for any value of U ; i.e., each orbital is exactly at half filling. So a Mott transition is possible at finite U . Second, $Z_{xz} = Z_{yz} = Z$, and an OSMT cannot take place even though the widths of the two bands are very different. At finite U , the hopping parameter t_{lm}^ν is uniformly renormalized to $\sqrt{Z_l Z_m} t_{lm}^\nu = Z t_{lm}^\nu$ since

the crystal-field splitting is zero in this model. Hence the dispersion $\epsilon_{\mathbf{k}}$ (the Fourier transformation of t_{lm}^v) is also normalized to $Z\epsilon_{\mathbf{k}}$. We thus see that the topology of the band structure is unchanged by the interactions. At $T = 0$, the chemical potential is determined by $\int \Theta(\mu - Z\epsilon_{\mathbf{k}}) = 2N_s$, where $\Theta(x)$ is the Heaviside step function and N_s is the number of sites. Taking $Z = 1$ and $\mu = \mu_0$ at $U = 0$, we see that $\int \Theta(\mu - Z\epsilon_{\mathbf{k}}) = \int \Theta[Z(\mu_0 - \epsilon_{\mathbf{k}})]$, implying that $\mu = Z\mu_0$. The Fermi surface is determined by $Z(\mu_0 - \epsilon_{\mathbf{k}}) = 0$. Therefore, the Fermi surface of the interacting system is *identical* to the one in the noninteracting system. Furthermore, the filling factor of each quasiparticle band does not depend on the interaction and must be identical to the value in the noninteracting case. Therefore, in the presence of nonzero interaction, the quasiparticle bands are still partially occupied, and a band insulator never emerges. The system stays in the metallic state until the quasiparticle spectral weight $Z = 0$, where both bands go through a transition to a Mott insulator. Our argument generally applies to any system with degenerate orbitals.

The above analysis is supported by the full solution to the slave-spin mean-field (SSMF) equations. Figure 1 shows the evolution of spectral weight Z with increasing U . For both $J = 0$ and nonzero J , Z drops to zero at finite U , indicating a Mott transition. At $J = 0$, this takes place at $U_c/D = 2.66$, where $D = 12$ is the full bandwidth of the two-orbital model (in the unit of t_1 , the nearest-neighbor intra- xz -orbital hopping along the x direction). The critical coupling is reduced to $U_c/D = 1.49$ at $J/U = 0.2$. As a complementary method, we have also applied the slave-rotor formulation³⁵ to the two-orbital model with $J = 0$ and the same values for the other model parameters. The results (not shown) are qualitatively the same as the SSMF results at $J = 0$: a Mott transition takes place at $U_c/D \approx 2.0$.

The Mott transition is best seen in the variation of the spectral function with increasing U . We calculate the spectral function by convoluting the SS and auxiliary fermion

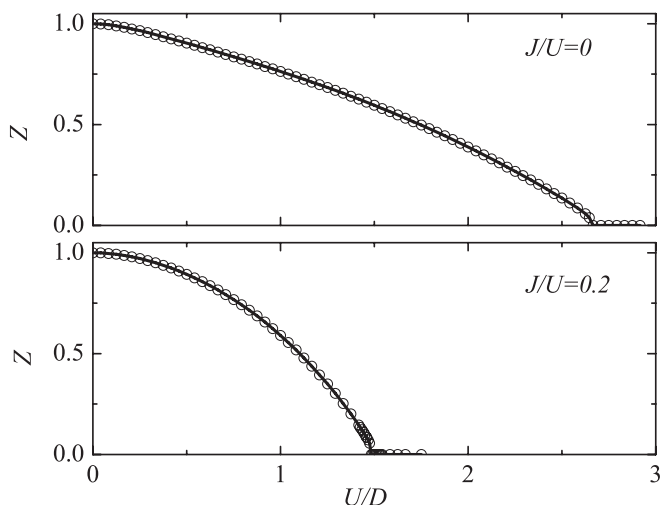


FIG. 1. Evolution of the spectral weight Z in the two-orbital model with (a) $J = 0$, $U' = U$ and (b) $J/U = 0.2$, $U'/U = 0.6$. $D = 12$ is the full bandwidth of the noninteracting band structure.

Green's functions: $G_{\alpha\beta}^{rd}(\mathbf{k}, \omega) = i \int d\omega' [G_{\alpha\beta}^{>S}(\omega') G_{\alpha\beta}^{rf}(\mathbf{k}, \omega - \omega') + G_{\alpha\beta}^{rS}(\omega') G_{\alpha\beta}^{<f}(\mathbf{k}, \omega - \omega')]$, where G^r is the retarded Green's function, $G_{\alpha\beta}^{>S}(t) \equiv -i \langle S_{\alpha}^x(t) S_{\beta}^x(0) \rangle$, and $G_{\alpha\beta}^{<f}(t) \equiv i \langle f_{\beta}^{\dagger}(0) f_{\alpha}(t) \rangle$ and α, β denote orbital indices. Note that in the above expression the SS Green's function is independent of \mathbf{k} . This is a consequence of the MF approximation. Expressing the SS Green's function using the Lehmann representation and taking into account that the Hamiltonian of f fermions describes free fermions, the spectral function is written as

$$A(\mathbf{k}, \omega) = \frac{2\pi}{Z} \sum_{\alpha\lambda\sigma} \sum_{n,m} |\langle n | S_{\alpha\sigma}^x | m \rangle|^2 |\Lambda_{\mathbf{k}}^{\alpha\lambda}|^2 \delta(\omega - E_{nm} - \epsilon_{\lambda\mathbf{k}}) \times [e^{-\beta E_m} (1 - n_{\lambda\mathbf{k}}^f) + e^{-\beta E_n} n_{\lambda\mathbf{k}}^f], \quad (8)$$

where E_n and $|n\rangle$ are eigenenergy and eigenvector of the SS Hamiltonian, $Z = \sum_n e^{-\beta E_n}$, $E_{nm} = E_n - E_m$, and $n_{\lambda}^f = 1/(e^{\beta\epsilon_{\lambda}} + 1)$. The matrix $\Lambda_{\mathbf{k}}$ diagonalizes the f -fermion Hamiltonian H_{MF}^f with eigenenergy $\epsilon_{\lambda\mathbf{k}}$.

Taking $m = n = 0$ ($|0\rangle$ denotes the ground state of H_{MF}^S) in Eq. (8), one sees that the coherent part of the spectral function is normalized by a factor of Z since $Z = |\langle 0 | S_{\alpha\sigma}^x | 0 \rangle|^2$. As mentioned above, an advantage of the SSMF is that the incoherent part is also accessible. At low temperatures this comes from terms with $n = 0, m \neq 0$. The LDOS is calculated from Eq. (8). As shown in Fig. 2, when U is increased from zero, one sees clearly that the coherent part is renormalized by Z . There is a significant spectral weight transfer to the incoherent part in the metallic phase. Our results provide a natural explanation of both the renormalization of the coherent bands and the appearance of the incoherent spectral weights^{13,46} within a unified framework. At $U > U_c$, the coherent peak vanishes, signaling the Mott insulator state; the incoherent parts, at the same time, develop into the lower and upper Hubbard bands.

As discussed in previous studies,⁴¹ a finite Hund's coupling may strongly affect the Mott transition. We show this effect in the two-orbital model by presenting the J - U phase diagram

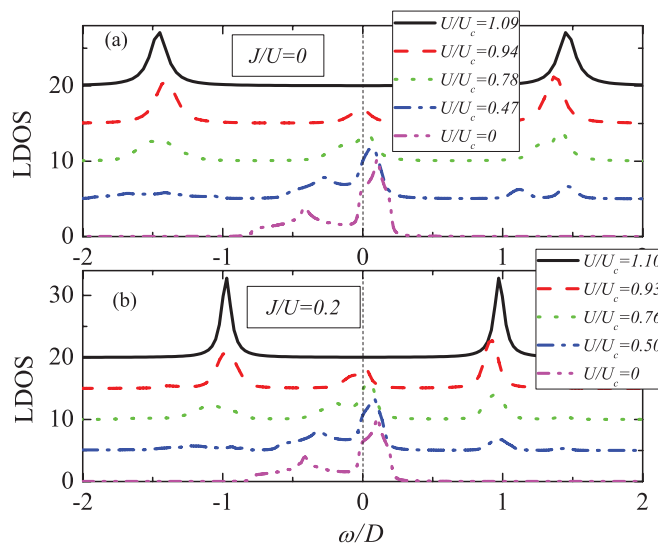


FIG. 2. (Color online) DOS in the two-orbital model at various U values with the same model parameters as in Fig. 1.

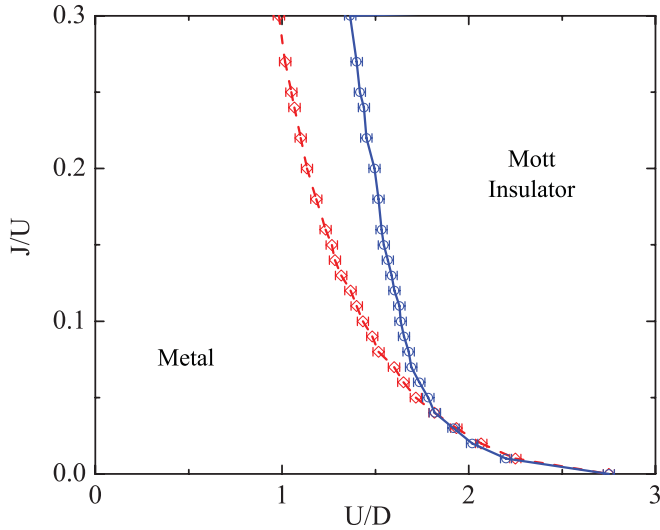
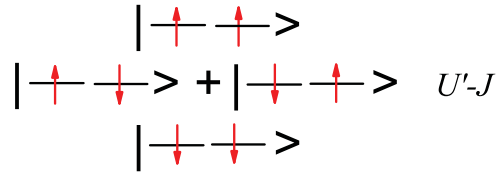


FIG. 3. (Color online) Phase diagram in the J - U plane of the two-orbital model at half filling. Here we have taken $U' = U - 2J$. The blue circles (red diamonds) give the phase boundary of the metal-to-Mott-insulator transition for the case of full (Ising-type) Hund's coupling.

in Fig. 3. It is seen in Fig. 3 that U_c is rapidly reduced with increasing J/U ; this is also illustrated in Fig. 1. The reduction of U_c can be understood by solving the mean-field Hamiltonian in Eq. (6) at an infinitesimal K ($K \equiv K_{\alpha\sigma}$). We first diagonalize H_{int} and the term including $S_{i,\alpha\sigma}^z$ in Eq. (6) and label the eigenstates as $|n\nu\rangle$, where n is the electron occupation number and ν denotes the degenerate multiplets. We then treat the term $KH' = K \sum_{\alpha\sigma} S_{\alpha\sigma}^x$ perturbatively. To the first order in K , U_c can be obtained by solving $1/\bar{\epsilon} = 2\mathcal{E}$. Here $\bar{\epsilon} = 1/N_{\text{site}} \sum_{\alpha\beta} \epsilon_{\mathbf{k}}^{\alpha\beta} \langle f_{\mathbf{k}\alpha\sigma}^\dagger f_{\mathbf{k}\alpha\sigma} \rangle$ is the average kinetic energy for the noninteracting system, and \mathcal{E} is the lowest eigenvalue diagonalizing the matrix \mathbf{M} , where $\mathbf{M}_{\mu\nu} = \sum_{n \neq 2, \lambda} \langle 2\mu | H' | n\lambda \rangle \langle n\lambda | H' | 2\nu \rangle / (E_2 - E_n)$ and E_n is the eigenenergy of state $|n\nu\rangle$. $M_{\mu\nu}$ is nonzero only when $n = 1$ or $n = 3$. For either n value, $E_2 - E_n = -\Delta_2/2$ where $\Delta_2 = U + J$ is the Mott gap of the two-orbital model at half filling. Hence U_c is determined by $\Delta_2 \propto |\bar{\epsilon}|$, i.e., $U_c \propto |\bar{\epsilon}|/(1 + J/U)$. This clearly indicates that U_c decreases with an increasing J/U ratio. Similar behavior has also been discussed in a three-orbital model.³²

Interestingly, we find that U_c is reduced more significantly for the Ising-type Hund's coupling [i.e., in the absence of the spin-flip and pair-hopping terms in Eq. (5)] at a large J/U ratio, as shown in Fig. 3. This is quite consistent with the results in previous studies,⁴¹ and can also be understood from the above perturbation theory. When J is small, for either Ising-type or full Hund's coupling, all six configurations associated with two electrons occupying the two orbitals, denoted by $|2\mu\rangle$ with μ ranging from 1 through 6, are nearly degenerate and are strongly mixed in the (perturbed) ground state. But when the full Hund's coupling J is large, only the triplet configurations in $|2\mu\rangle$, shown in Fig. 4, contribute most to the ground state. For the Ising-type Hund's coupling, the ground state only strongly mixes the doublet: $|\uparrow\rangle_{xz}|\uparrow\rangle_{yz}$ and $|\downarrow\rangle_{xz}|\downarrow\rangle_{yz}$. More configurations mixed in the ground state correspond to more scattering processes between the

High-Spin Mott:



Low-Spin Orbital-Mott:

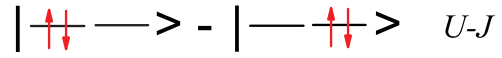


FIG. 4. (Color online) Illustration of the high-spin Mott and low-spin orbital-Mott states in the two-orbital model at the atomic limit. In this model, the high-spin Mott state has $S = 1$ and the ground-state energy has $U' - J$; the low-spin orbital-Mott state has $S = 0$ and the ground-state energy has $U - J$.

nearly degenerate $|2\mu\rangle$ and $|2\nu\rangle$ states, which promote a larger kinetic-energy gain in the metallic phase, thereby favoring the metal over the Mott insulator. Following the perturbation theory, $U_c = 12|\bar{\epsilon}|/(1 + J/U) \approx 2.7D/(1 + J/U)$ for infinitesimal J/U ; here, a nearly degenerate perturbation is used involving all six low-energy multiplets. At sufficiently large J , $U_c = 8|\bar{\epsilon}|/(1 + J/U)$ for full Hund's coupling and $U_c = 4|\bar{\epsilon}|/(1 + J/U)$ for Ising-type Hund's coupling; here, the degenerate perturbation respectively involves the three and two lowest multiplets for the two cases. These expressions are qualitatively⁴⁷ consistent with the numerical results in Fig. 3: At $J/U < 0.01$, $U_c \approx 2.66D/(1 + J/U)$ for both full and Ising-type Hund's couplings, while for $J/U \gtrsim 0.03$ the largest reduction of U_c is found in the Ising-type Hund's coupling. It is interesting to note that the effect of Hund's coupling on the value of U_c is quite similar to the effect of having more orbitals in degenerate multiorbital Hubbard models.⁴⁸ Indeed, the underlying physics is related: in both cases, U_c is higher when the ground state mixes more nearly degenerate configurations; as already mentioned, involving more configurations helps stabilize a metallic state by lowering the kinetic energy.

Another difference from the $J = 0$ case is that the MIT becomes discontinuous at nonzero J . It is especially significant for the Ising-type Hund's interaction. For the full Hund's coupling, the discontinuity of Z is only significant at small J values. For $J/U \gtrsim 0.2$, the discontinuity is rather small (see Fig. 1), and it is hard to distinguish the transition from a continuous one. These results from our SSMF calculation are consistent with the DMFT results on the effect of finite Hund's couplings in multiband Hubbard models with degenerate bands.⁴¹

B. High-spin Mott versus low-spin orbital-Mott state

As seen in Fig. 2, the Mott transition at half filling in the two-orbital model is quite similar to the Brinkman-Rice picture of the one-orbital case. It is then interesting to see whether the Mott insulating state is similar to that of the one-orbital case. For $J > 0$, the Mott insulator of the two-orbital model is an $S = 1$ interorbital triplet state. This state is characterized by a vanishing onsite double occupancy

$\langle n_{i\uparrow}n_{i\downarrow} \rangle$ in each orbital and is the two-orbital analog of the Mott insulator in the one-orbital model. We denote the triplet state as the high-spin Mott state in the two-orbital model.

The Mott insulating state at $J = 0$ in the two-orbital model is somewhat different. It mixes the high-spin (triplet) states with low-spin (singlet) configurations, which are degenerate when $J = 0$. Therefore, the insulating state has a finite double occupancy (see Fig. 4). This implies that a spin-singlet state might be stabilized in some parameter regime. Note that the relation $U' = U - 2J$ puts a strong constraint on the parameters, which may limit the ground-state configurations to a relatively smaller subset. To fully study all the possible ground-state configurations, in this section, we relax the above constraint so that U' becomes a free parameter independent of U and J .^{49,50} Indeed, by studying the Hamiltonian in the atomic limit, one sees that for any $J > 0$ the interorbital triplet state is only stabilized at $U' < U$. When $U' > U$, the ground state is an orbital antisymmetric spin-singlet state $1/\sqrt{2}(|\uparrow\downarrow; 0\rangle - |0; \uparrow\downarrow\rangle)$, as shown in Fig. 4.⁵¹ Though this state shares some characters as a band insulator, such as finite double occupancy and spin singlet, it is still a Mott insulator because the orbital degeneracy is preserved by the Hamiltonian. This can be immediately seen by noticing that each orbital is at half filling and the spectral weight is zero in this state. Note that $U' > U$ is not enough to drive the system to a band insulator because the existence of the Mott insulator is guaranteed by the orbital degeneracy. To distinguish this Mott state at $U' > U$ from the high-spin (triplet) Mott state, we will denote it as a low-spin orbital-Mott state.

To see the difference between the high-spin Mott and low-spin orbital-Mott insulators, we study the MIT in the two-orbital model at several different U'/U ratios and show the results in Fig. 5. We find the MIT is discontinuous for general U , U' , and J values except for $J = 0$ and $U = U'$, where a continuous transition is observed. Moreover, the behaviors in the metallic state at different U'/U ratios are quite similar. This is not surprising since the electron hopping mixes all configurations. Besides the double occupancy, the difference between the high-spin Mott and low-spin orbital-Mott states can also be seen by both the average value of the total spin operator $\mathbf{S}^2 = (\sum_{\alpha} \mathbf{S}_{\alpha})^2$ and the orbital correlation function $C_o^{1,2} = \langle (n_1 - 1)(n_2 - 1) \rangle$. (We have defined the orbital indices $1 = xz$, $2 = yz$.) In the high-spin Mott state, $\langle \mathbf{S}^2 \rangle = 2$ and $C_o^{1,2} = 0$. By contrast, in the low-spin orbital-Mott state, $\langle \mathbf{S}^2 \rangle = 0$ and $C_o^{1,2} = -1$. All these are consistent with the numerical results shown in Fig. 5. At $U' = U$, the ground state is a mixture of the two Mott states, hence both $C_o^{1,2}$ and $\langle \mathbf{S}^2 \rangle$ take intermediate values.

For a fixed J/U ratio, we find the critical coupling U_c for the MIT is the largest for $U = U'$. It is slightly reduced for $U' < U$ but greatly decreased when $U' > U$. We show that this nonmonotonic behavior of U_c is related to the different nature of the Mott states. Note that the two Mott states at $U' < U$ and $U' > U$ have different Mott gaps. In the high-spin Mott state, $\Delta_2 = U + J$, is independent of U' . On the other hand, the Mott gap in the low-spin orbital-Mott state is $\Delta_2 = 2U' - U + J$, which increases with U' . Therefore, U_c decreases drastically when U'/U increases from 1 but is almost insensitive to U'/U for $U' < U$. These considerations allow us to understand the numerical results given in Fig. 5.⁵² The fact that U_c at $U' < U$

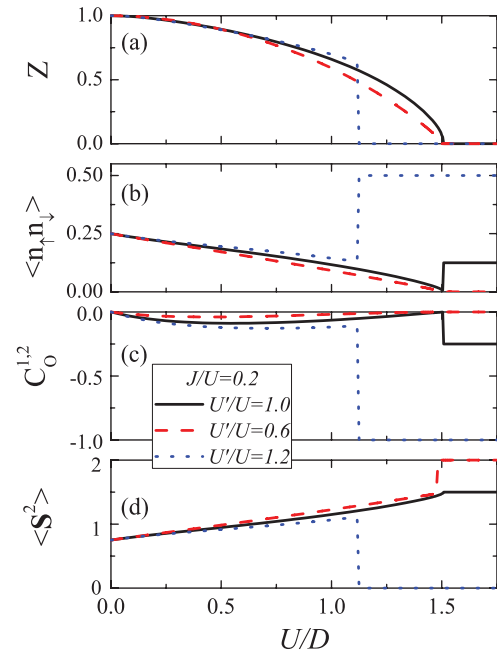


FIG. 5. (Color online) (a) The evolution of Z at half filling with $J/U = 0.2$ and different U'/U ratios showing the transition to different Mott states. (b)–(d): The evolution of $\langle n_{\uparrow}n_{\downarrow} \rangle$, $C_o^{1,2}$, and \mathbf{S}^2 (see text for the definitions of these quantities) for the same set of parameters.

is smaller than U_c at $U' = U$ can be further understood by the different ground-state degeneracy in the two states. From Sec. III A we know that a higher ground-state degeneracy increases the effective kinetic-energy gain, thereby enhancing the stability of the metallic state. The ground state is threefold degenerate when $U' < U$ but is fourfold degenerate when $U' = U$ (it is sixfold if further $J = 0$). Thus, U_c is the largest for $U = U'$ and is slightly reduced when $U' < U$.

The orbital-Mott state exists only in systems with degenerate orbitals and $U' > U$. When the orbital degeneracy is broken by a crystal-field splitting, it is unstable toward either a band insulator or more generally, as will be discussed in the next section, an orbitally polarized insulator.

IV. RESULTS FOR THE FOUR-ORBITAL MODEL

We have so far shown how the Mott transition takes place in the minimal two-orbital model for parent iron pnictides. It has been recognized that, to more realistically reproduce the electron structure of the iron pnictides, all five Fe orbitals need to be included in the tight-binding dispersion.^{53,54} This raises the question as to whether our main results for the two-orbital model are applicable to the more realistic models with a larger number of orbitals. In the five-orbital model of Ref. 53, the electron filling is about 0.8 per site per spin in the $3z^2 - r^2$ orbital but very close to 0.5 per site per spin in all other four orbitals. The $3z^2 - r^2$ orbital hardly contributes to the band structure near the Fermi level. These suggest that one may study a model including only xz , yz , xy , and $x^2 - y^2$ orbitals by assuming that the $3z^2 - r^2$ orbital lies far below the Fermi level and is fully occupied. Taking model parameters of Ref. 53 but keeping only those four orbitals gives rise to Fermi surfaces

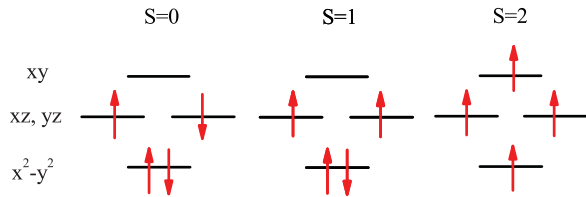


FIG. 6. (Color online) Three candidate ground states in the atomic limit in the four-orbital model. The $S = 2$ state is an analog of the high-spin Mott state in the two-orbital model.

that are almost identical to the ones for the five-orbital cases. Hence the four-orbital model represents a good approximation to the five-orbital one. For simplicity, here we study the MIT in this four-orbital model.

We argue that the main results for the two-orbital model still hold in the four-orbital model. Though the orbital degeneracy of other orbitals are lifted, the xz and yz orbitals are still degenerate. In the atomic limit, with four electrons occupied, the ground state may be either a high-spin $S = 2$ state, an intermediate-spin $S = 1$ state, or a low-spin $S = 0$ state, as shown in Fig. 6. In either case the xz and yz orbitals are half filled just as in the two-orbital model. Therefore, a Mott transition similar to the two-orbital case is expected.

In Figs. 7–11 we show the results from SSMF calculation, in which the full Hund's coupling and the constraint $U' = U - 2J$ are taken into account. For both $J = 0$ and $J > 0$, an MIT is observed. For $J = 0$, $U_c = 12.5$ eV. A nonzero J may significantly reduce U_c . At $J/U = 1/4$, U_c is reduced to 3.82 eV. Interestingly, we find that the nature of the insulating state, and hence the MIT, is significantly affected by the competition between the Hund's coupling J and the crystal-field splitting Δ between the xy and $x^2 - y^2$ orbitals. For $J/U \gtrsim 0.009$ the insulating state is a high-spin state with $S = 2$, as illustrated in Fig. 6. This state is analogous to the high-spin Mott state discussed in the two-orbital model. One may directly check from Figs. 9(d) and 10(c) that the interorbital correlations are very small in the metallic state

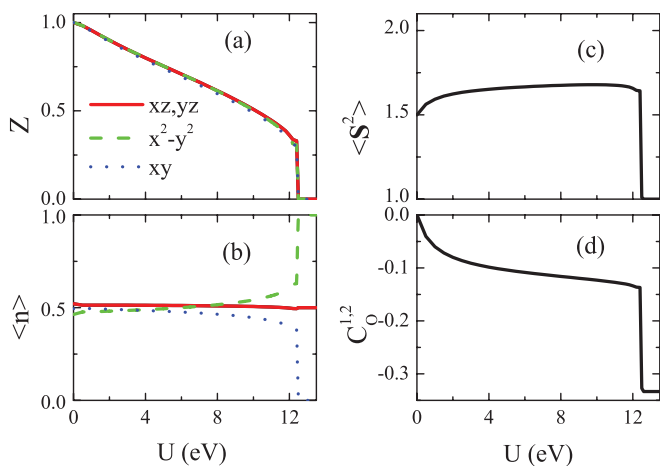


FIG. 7. (Color online) SSMF results for the four-orbital model at $J = 0$, showing evolution of (a) Z , (b) average electron filling per site per spin, (c) average of total spin, and (d) interorbital correlation between xz and yz orbitals.

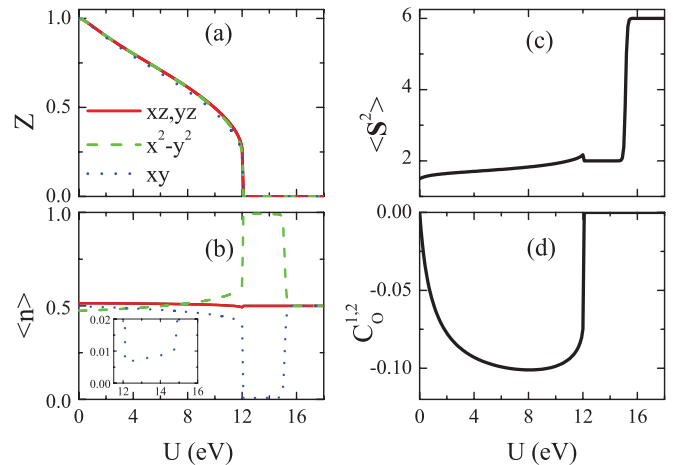


FIG. 8. (Color online) SSMF results for the four-orbital model at $J/U = 0.007$.

and vanish in the insulating state, with a behavior similar to the two-orbital case at finite J .

The transitions at small and zero J/U ratios are of special interest. As shown in Fig. 7(c), the insulating state at $J = 0$ has an intermediate spin between $S = 0$ and $S = 1$. We call this an IS1 state, which is shown in the phase diagram, Fig. 11. This transition to the IS1 state can be understood as follows: at $J = 0$, the xy orbital is empty and the $x^2 - y^2$ orbital is fully occupied in the insulating state due to the crystal-field splitting. Hence at $U = U_c$ these two orbitals undergo a transition to a band insulator. On the other hand, the degenerate xz and yz orbitals are at half filling, and a Mott transition takes place at the same U_c value. Since at $J = 0$ all the six $n = 2$ configurations in xz and yz orbitals are degenerate, the Mott insulator is a mixture of $S = 0$ and 1 states. This gives the IS1 state an intermediate spin value. The transitions to the band insulator and Mott insulator are reflected in the behavior of the interorbital correlation functions $C_O^{1,2}$ and $C_O^{3,4}$, where $C_O^{\alpha,\beta} = \langle (n_\alpha - 1)(n_\beta - 1) \rangle$ for $\alpha, \beta = 1, 2, 3, 4$. Here 1, 2, 3, 4 denote $xz, yz, x^2 - y^2$, and xy , respectively. At $J = 0$, $C_O^{3,4}$ jumps to -1 at U_c , indicating a transition to a

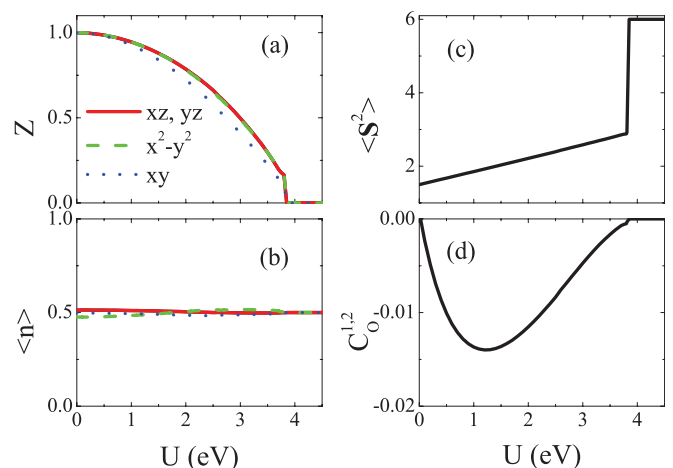


FIG. 9. (Color online) SSMF results for the four-orbital model at $J/U = 1/4$.

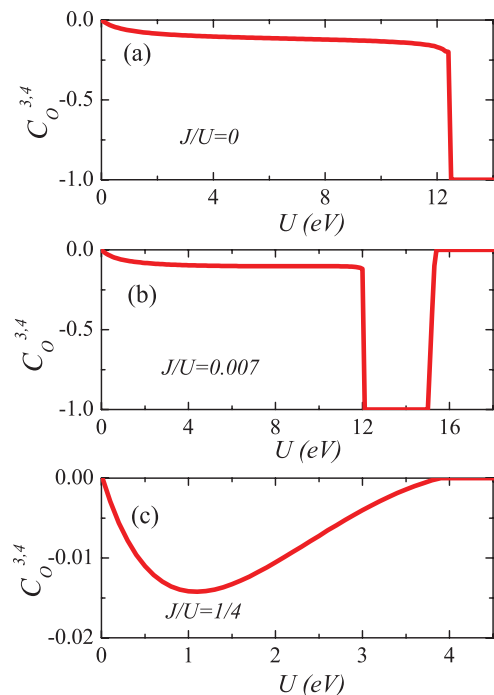


FIG. 10. (Color online) The evolution of interorbital correlation between the xy and $x^2 - y^2$ orbitals, $C_0^{3,4}$, in the four-orbital model at $J = 0$, $J/U = 0.007$, and $J/U = 1/4$, respectively.

band insulator. But $C_0^{1,2} > -1$ even in the insulating phase, signaling that the insulating state is a mixture of $S = 1$ and 0 Mott states, just as in the two-orbital model at $U = U'$. In

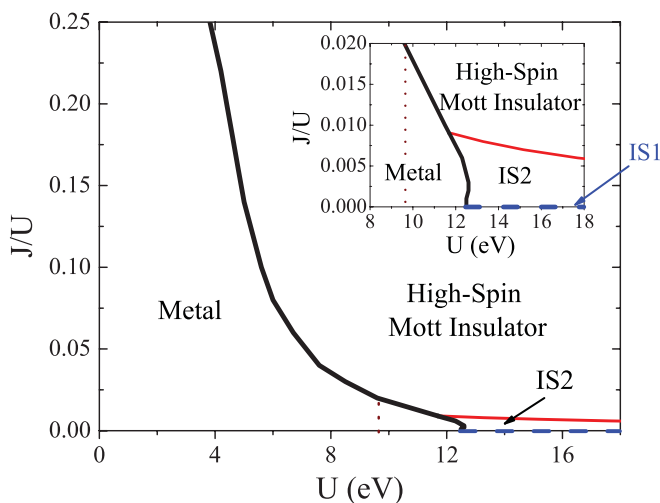


FIG. 11. (Color online) Phase diagram in the $J-U$ plane of the four-orbital model. The thick solid (black) line shows the phase boundary between the metallic and insulating states. The blue dashed line at $J = 0$ refers to the intermediate-spin insulating state IS1, and the thin solid (red) line refers to the low-spin to high-spin transition between the IS2 state and the high-spin Mott state. The dotted line at $U \approx 10$ eV separates the metallic phase into two regimes. To the left of this line, the Fermi surface topology is identical to the noninteracting case, while, in the regime between this dotted line and the thick solid line, the topology of the Fermi surface changes (see text). The inset shows a closer view of the lower-right corner of the phase diagram.

general, the Mott transition in the xz and yz orbitals may take place at a U value different than U_c . But in this four-orbital model, U_c for the transition to the band insulator in the xy and $x^2 - y^2$ orbitals is larger than the critical value for the Mott transition in two degenerate orbitals. Hence when the other two orbitals become band insulators at U_c and thus are decoupled from the xz and yz orbitals, the xz and yz orbitals enter the Mott insulating state immediately via a first-order transition. We call this special transition at U_c an orbitally selective MIT. This transition is different from the OSMT in that it takes place at a single U_c , with different orbitals entering different insulating states.

We find that the orbitally selective MIT extends to nonzero J values up to $J/U \approx 0.009$. For nonzero J in this range, the state on the insulator side has an intermediate-spin value $S = 1$. We denote this state as the IS2 state. Shown in Fig. 8 is the transition to the IS2 state in the case of $J/U = 0.007$, for which the IS2 state is found to be stabilized for $12 \lesssim U \lesssim 15.2$ eV. Similar to the IS1 state at $J = 0$, the IS2 state is stabilized because different orbitals undergo transitions to different insulating states: an $S = 1$ Mott insulator for the xz and yz orbitals and an $S = 0$ orbitally polarized insulator for the xy and $x^2 - y^2$ orbitals. The orbitally polarized insulator can be understood by studying the atomic limit of an effective two-orbital model including xy and $x^2 - y^2$ orbitals.⁵⁵ In this effective model, the pair-hopping term couples the two states $|\uparrow\downarrow\rangle_{xy}|0\rangle_{x^2-y^2}$ and $|0\rangle_{xy}|\uparrow\downarrow\rangle_{x^2-y^2}$. When $\Delta > 2\sqrt{2}J$, the ground state is a spin singlet $\cos\theta|0\rangle_{xy}|\uparrow\downarrow\rangle_{x^2-y^2} - \sin\theta|\uparrow\downarrow\rangle_{xy}|0\rangle_{x^2-y^2}$, where $\tan\theta = \sqrt{(\Delta/J)^2 + 1} - \Delta/J$. One may check that $n_{xy} = \sin^2\theta$, and $n_{x^2-y^2} = \cos^2\theta$. In general, each orbital is only partially occupied, and $n_{xy} \neq n_{x^2-y^2}$, which is clearly shown in Fig. 8(b) within $12 < U < 15.2$ eV. Hence this state is different from either a band insulator or a Mott insulator and is denoted as an orbitally polarized insulating state. From Fig. 10, we see that the interorbital correlation in the orbitally polarized state behaves the same as in the band insulator. To understand this, note that there are two special limits in the orbitally polarized insulator. First, when $J = 0$ and $\Delta > 0$, $\sin\theta = 0$ and this state describes the band insulator with the fully occupied $x^2 - y^2$ orbital and empty xy orbital. The other limit appears when $\Delta = 0$ but $J > 0$. This leads to $\sin\theta = \cos\theta = 1/\sqrt{2}$, and the state is identical to the low-spin orbital-Mott state discussed in Sec. III B. Thus the band insulator and the low-spin orbital-Mott insulator are adiabatically connected by the orbitally polarized insulating state.

Further increasing J in the effective two-orbital model for xy and $x^2 - y^2$ orbitals eventually leads to a low-spin-to-high-spin transition.⁵⁵ The ground-state manifold changes from the $S = 0$ orbitally polarized state to the $S = 1$ Mott state. In the four-orbital model, this corresponds to a first-order transition in the insulating states from the IS2 state to the high-spin Mott insulator, which takes place at $\Delta = 2\sqrt{6}J$. Since in this study we assume J is proportional to U , the low-spin-to-high-spin transition is accessible by increasing U . In Fig. 8 we identify that it takes place at $U \approx 15.2$ eV for $J/U = 0.007$: the total spin jumps from $S = 1$ to 2, and the filling factors of xy and $x^2 - y^2$ orbitals rapidly converge to half filling.

In Fig. 11 we show the $J-U$ phase diagram for the four-orbital model. For $J/U \gtrsim 0.009$ the MIT takes place between a paramagnetic metal and $S = 2$ high-spin Mott

insulator. In this regime, the phase diagram is similar to the one in the two-orbital model shown in Fig. 3. The main difference from the phase diagram in Fig. 3 lies at $U \gg \Delta$ and $J \ll \Delta$. In this regime we find two intermediate-spin states: the IS1 state at $J = 0$ and the IS2 state at finite J . The boundary between the IS2 and the $S = 2$ Mott insulator, $J/U = \Delta/2\sqrt{6}U$, is determined by solving the Hamiltonian of the four-orbital model in the atomic limit. Given that $\Delta = 0.52$ eV in this model, and assuming that U_c for the MIT at $J/U \ll 1$ stays the same value as $J = 0$, we may estimate the tricritical point where the transition between the IS2 and the high-spin Mott state and the MIT meet. It is located at $J/U \approx 0.0085$, which is consistent with the numerical result $J/U \approx 0.009$.

It is very important to check how the Fermi surface in the metallic state evolves in the presence of interactions. In the noninteracting case, the Fermi surface of the four-orbital model consists of two hole pockets centered at the $(0,0)$ point in the one-iron Brillouin zone and two electron pockets centered at the $(\pi,0)$ and $(0,\pi)$ points, respectively. We have checked that, for a large portion of the metallic regime in the phase diagram, i.e., to the left of the dotted line at $U \approx 10$ eV in Fig. 11, the Fermi surface of the interacting system has the same topology as that for the noninteracting system. In this regime, even near the high-spin Mott insulator, there are only very tiny changes in the size and shape of the hole and electron pockets. This is similar to the result of the two-orbital model, in which the Fermi surface is always identical to the one in the noninteracting system. But in the four-orbital model, we find that the topology of the Fermi surface may change when the system is close enough to the intermediate-spin states (in the regime between the dotted line and the thicker solid line in Fig. 11). In this regime, as U is increased, two additional small electron pockets centered at the $(\pi,0)$ and $(0,\pi)$ points and one additional hole pocket centered at the (π,π) point may appear. Such a change in the Fermi surface topology primarily reflects the difference in the electron occupancies of the different orbitals compared to the noninteracting case [cf. Figs. 7(b), 8(b), and 9(b)], which is a precursor to the orbitally selective MIT occurring in the small J/U regime.

MIT has also been discussed in spin-density wave (SDW) calculations in a number of multiorbital models for iron pnictides.^{56–58} An intermediate-spin insulating state was recently found in a five-orbital model within the SDW MF theory.⁵⁸ Though a full study of the MIT in the magnetically ordered state using SSMF theory is beyond the scope of this paper, we find it quite interesting to compare the intermediate-spin states found in our study with those in Ref. 58 in the atomic limit. In both works, the intermediate-spins states are found when U/t is large but J/U is small, indicating that these states all originate from the interplay of the crystal-field splitting and Hund's coupling. But there are some differences. First, in Ref. 58, a $S = 0$ state violating the Hund's rule is stabilized at $J = 0$. This state originates from the lifting of orbital degeneracy between the xz and yz orbitals by magnetic ordering. But in our case, the orbital degeneracy between the xz and yz orbitals stabilizes the IS1 state with a nonzero spin value at $J = 0$. A second difference lies in the method of treating the electron-electron interaction term H_{int} : we consider the full interaction in our SSMF calculation, while in Ref. 58 the spin-flip and the pair-hopping terms are neglected from the

MF approximation. This results in different insulating states: the IS2 state in our paper consists of an orbitally polarized insulator in the xy and $x^2 - y^2$ orbitals, but the bands with xy and $x^2 - y^2$ orbital characters in the $S^z = 1$ state in Ref. 58 are simple band insulators.

An interesting question is whether an OSMT may take place when more than two orbitals are included. Recently, a mechanism of the OSMT based on the lifting of orbital degeneracy is proposed.⁵⁹ According to this mechanism, in a system with more than two orbitals, if the orbital degeneracy is partially lifted by a crystal-field splitting, an OSMT may take place even when the bandwidths are equal. It is suggested that an OSMT triggered by this mechanism may exist in iron pnictides.⁶⁰ From Fig. 9 we find that, for $J > 0$, the bandwidth of the xy orbital gets stronger renormalization than the others. This effect becomes more pronounced for larger J . However, no OSMT is observed up to $J/U = 1/2$. This is not too surprising. On the one hand, the above mechanism is proposed by assuming zero interorbital hopping. The four-orbital model discussed in this section contains nonzero interorbital hoppings, which enhance the orbital correlations and favor a one-stage Mott transition. On the other hand, according to the mechanism, an OSMT is easier to be realized if the orbital whose degeneracy is lifted is at half filling but the degenerate orbitals are away from half filling, so that the lifted orbital is localized while the degenerate ones are still metallic. In the four-orbital model we consider, the degenerate xz and yz orbitals are exactly at half filling, making the Mott insulator more stable.

V. CONCLUSION

In conclusion, we have studied the metal-insulator transitions in several multiorbital Hubbard models for the parent iron pnictides using a slave-spin formulation.

In the two-orbital model, a transition to a Mott insulator generally exists at half filling. The Hund's coupling reduces the critical coupling significantly. We find that the nature of the Mott insulator depends on the ratio U'/U . For $U' < U$, the insulator is a high-spin Mott state with zero double occupancy but a spin triplet. For $U' > U$, by contrast, the insulator is an orbital-Mott state with spin singlet and finite double occupancy. The low-spin orbital-Mott state is unstable to a band insulator if the orbital degeneracy is lifted, and can be viewed as a special case of an orbitally polarized insulator.

The phase diagram for the metal-to-insulator transition in the more realistic four-orbital model contains additional features. We find a transition to a high-spin $S = 2$ Mott insulator when the Hund's coupling is strong enough ($J/U \gtrsim 0.009$). This high-spin Mott insulator is an analogy to the $S = 1$ Mott insulator in the two-orbital model. At weak including zero Hund's couplings ($J/U \lesssim 0.009$) we find a transition to intermediate-spin insulating states. Such a transition is an orbitally selective metal-insulator transition; namely, different orbitals undergo transitions to different insulating states at a single critical value U_c . At $J = 0$ the transition leads to a band insulator for two (xy and $x^2 - y^2$) orbitals and a Mott insulator for the other two (xz and yz) orbitals. For nonzero J in this regime, the transition in the xz and yz orbitals is to the Mott insulator, but an orbitally polarized

insulator is stabilized in the xy and $x^2 - y^2$ orbitals on the insulating side due to the pair-hopping term. As J is increased further, the intermediate-spin orbitally polarized insulator undergoes a low-spin-to-high-spin transition to a high-spin Mott insulator.

The existence of a Mott transition in the multiorbital models with an even number of electrons per Fe provides the theoretical basis for the recent finding of a Mott insulator in the iron oxychalcogenides with an expanded Fe lattice.²¹ In addition, it strengthens the notion that the iron pnictides are located in proximity to a Mott localization transition.

Finally, we note that, after this paper was first submitted for publication and posted on the arXiv preprint listing, several

studies also discussed the relation between the band and orbital pictures in related contexts,^{61,62} and a number of works used the slave-spin or a related slave-rotor method to investigate the metal-insulator transitions in related multiorbital models and systems.^{63–65}

ACKNOWLEDGMENTS

We would like to thank L. Baksmaty and P. Goswami for useful discussions. This work was supported by the National Science Foundation Grant No. DMR-1006985, the Robert A. Welch Foundation Grant No. C-1411, and the W. M. Keck Foundation.

-
- ¹Y. Kamihara, T. Watanabe, H. Hirano, and H. Hosono, *J. Am. Chem. Soc.* **130**, 3296 (2008).
- ²Z. A. Ren *et al.*, *Chin. Phys. Lett.* **25**, 2215 (2008).
- ³C. de la Cruz *et al.*, *Nature (London)* **453**, 899 (2008).
- ⁴Q. Si and E. Abrahams, *Phys. Rev. Lett.* **101**, 076401 (2008).
- ⁵Q. Si, E. Abrahams, J. Dai, and J.-X. Zhu, *New J. Phys.* **11**, 045001 (2009).
- ⁶K. Haule, J. H. Shim, and G. Kotliar, *Phys. Rev. Lett.* **100**, 226402 (2008).
- ⁷M. S. Laad, L. Craco, S. Leoni, and H. Rosner, *Phys. Rev. B* **79**, 024515 (2009).
- ⁸M. Daghofer, A. Moreo, J. A. Riera, E. Arrigoni, D. J. Scalapino, and E. Dagotto, *Phys. Rev. Lett.* **101**, 237004 (2008).
- ⁹C. Fang, H. Yao, W.-F. Tsai, J.-P. Hu, and S. A. Kivelson, *Phys. Rev. B* **77**, 224509 (2008).
- ¹⁰C. Xu, M. Muller, and S. Sachdev, *Phys. Rev. B* **78**, 020501(R) (2008).
- ¹¹H. Ishida and A. Liebsch, *Phys. Rev. B* **81**, 054513 (2010).
- ¹²H. Lee, Y.-Z. Zhang, H. O. Jeschke, and R. Valentí, *Phys. Rev. B* **81**, 220506(R) (2010).
- ¹³M. M. Qazilbash, J. J. Hamlin, R. E. Baumbach, L. Zhang, D. J. Singh, M. B. Maple, and D. N. Basov, *Nat. Phys.* **5**, 647 (2009).
- ¹⁴W. Z. Hu, J. Dong, G. Li, Z. Li, P. Zheng, G. F. Chen, J. L. Luo, and N. L. Wang, *Phys. Rev. Lett.* **101**, 257005 (2008).
- ¹⁵Q. Si, *Nat. Phys.* **5**, 629 (2009).
- ¹⁶J. Yang, D. Hüvonen, U. Nagel, T. Rööm, N. Ni, P. C. Canfield, S. L. Bud'ko, J. P. Carbotte, and T. Timusk, *Phys. Rev. Lett.* **102**, 187003 (2009).
- ¹⁷A. V. Boris, N. N. Kovaleva, S. S. A. Seo, J. S. Kim, P. Popovich, Y. Matiks, R. K. Kremer, and B. Keimer, *Phys. Rev. Lett.* **102**, 027001 (2009).
- ¹⁸W. L. Yang *et al.*, *Phys. Rev. B* **80**, 014508 (2009).
- ¹⁹A. Kutepov, K. Haule, S. Y. Savrasov, and G. Kotliar, *Phys. Rev. B* **82**, 045105 (2010).
- ²⁰J. Zhao, D. T. Adroja, D.-X. Yao, R. Bewley, S. Li, X. F. Wang, G. Wu, X. H. Chen, J. Hu, and P. Dai, *Nat. Phys.* **5**, 555 (2009).
- ²¹J.-X. Zhu, R. Yu, H. Wang, L. L. Zhao, M. D. Jones, J. Dai, E. Abrahams, E. Morosan, M. Fang, and Q. Si, *Phys. Rev. Lett.* **104**, 216405 (2010).
- ²²M. Imada, A. Fujimori, and Y. Tokura, *Rev. Mod. Phys.* **70**, 1039 (1998).
- ²³E. Dagotto, *Rev. Mod. Phys.* **66**, 763 (1994).
- ²⁴A. Georges, G. Kotliar, W. Krauth, and M. Rozenberg, *Rev. Mod. Phys.* **68**, 13 (1996).
- ²⁵W. F. Brinkman and T. M. Rice, *Phys. Rev. B* **2**, 4302 (1970).
- ²⁶T. Ohashi, T. Momoi, H. Tsunetsugu, and N. Kawakami, *Phys. Rev. Lett.* **100**, 076402 (2008).
- ²⁷V. I. Anisimov, I. A. Nekrasov, D. E. Kondakov, T. M. Rice, and M. Sigrist, *Eur. Phys. J. B* **25**, 191 (2002).
- ²⁸A. Liebsch, *Phys. Rev. Lett.* **91**, 226401 (2003).
- ²⁹A. Koga, N. Kawakami, T. M. Rice, and M. Sigrist, *Phys. Rev. Lett.* **92**, 216402 (2004).
- ³⁰C. Knecht, N. Blümer, and P. G. J. van Dongen, *Phys. Rev. B* **72**, 081103(R) (2005).
- ³¹R. Arita and K. Held, *Phys. Rev. B* **72**, 201102(R) (2005).
- ³²P. Werner, E. Gull, and A. J. Millis, *Phys. Rev. B* **79**, 115119 (2009).
- ³³H. Lee, Y.-Z. Zhang, H. O. Jeschke, R. Valentí, and H. Monien, *Phys. Rev. Lett.* **104**, 026402 (2010).
- ³⁴Y. Ono, M. Potthoff, and R. Bulla, *Phys. Rev. B* **67**, 035119 (2003).
- ³⁵S. Florens and A. Georges, *Phys. Rev. B* **70**, 035114 (2004).
- ³⁶S. Raghu, X.-L. Qi, C.-X. Liu, D. J. Scalapino, and S.-C. Zhang, *Phys. Rev. B* **77**, 220503(R) (2008).
- ³⁷L. de'Medici, A. Georges, and S. Biermann, *Phys. Rev. B* **72**, 205124 (2005).
- ³⁸S. R. Hassan and L. de'Medici, *Phys. Rev. B* **81**, 035106 (2010).
- ³⁹J. P. Lu, *Phys. Rev. B* **49**, 5687 (1994).
- ⁴⁰M. J. Rozenberg, *Phys. Rev. B* **55**, R4855 (1997).
- ⁴¹J. Bünenmann, W. Weber, and F. Gebhard, *Phys. Rev. B* **57**, 6896 (1998); K. Inaba, A. Koga, S.-I. Suga, and N. Kawakami, *ibid.* **72**, 085112 (2005); K. Inaba and A. Koga, *ibid.* **73**, 155106 (2006).
- ⁴²C. Castellani, C. R. Natoli, and J. Ranninger, *Phys. Rev. B* **18**, 4945 (1978); E. Dagotto, T. Hotta, and A. Moreo, *Phys. Rep.* **344**, 1 (2001).
- ⁴³G. Kotliar and A. E. Ruckenstein, *Phys. Rev. Lett.* **57**, 1362 (1986).
- ⁴⁴S. Florens and A. Georges, *Phys. Rev. B* **66**, 165111 (2002).
- ⁴⁵The preservation of the SU(2) symmetry can be seen by checking that the pseudospin operators, defined in terms of slave-spin operators as $\tau^+ = S_\uparrow^+ S_\downarrow^-$, $\tau^- = S_\downarrow^+ S_\uparrow^-$, and $\tau^z = (S_\uparrow^z - S_\downarrow^z)/2$ for each orbital, satisfy the SU(2) spin commutation relation.
- ⁴⁶H. Ding *et al.*, *J. Phys.: Condens. Matter* **23**, 135701 (2011).
- ⁴⁷Quantitatively, the perturbation theory works well only at $J \approx 0$ since only here is the MIT continuous. At finite J/U , we find the MIT is discontinuous, similar to the result in a recent

slave-boson study [F. Lechermann, A. Georges, G. Kotliar, and O. Parcollet, *Phys. Rev. B* **76**, 155102 (2007)]. The discontinuous nature of MIT may invalidate the perturbative expressions.

⁴⁸O. Gunnarsson, E. Koch, and R. M. Martin, *Phys. Rev. B* **54**, R11026 (1996); J. E. Han, M. Jarrell, and D. L. Cox, *ibid.* **58**, R4199 (1998).

⁴⁹Note that $U' = U - 2J$ is strictly satisfied for an isolated atom in free space, where the Coulomb interaction has the full rotational symmetry. In solids, the rotational symmetry is reduced. Taking into account the many-body effects between the electrons and ligand ions, this constraint may not be strictly satisfied. Specific to the two-orbital model with xz and yz orbitals, this constraint implies that the interaction is invariant under a continuous rotation in the xy plane [an $O(2)$ symmetry]. However, this $O(2)$ symmetry is not necessarily satisfied in a solid, where only the discrete point group symmetry is respected. So the $U' = U - 2J$ may not be always valid in a solid. For instance, as discussed in Ref. 50, it is broken due to the electron-phonon interaction in pnictides. Although Ref. 50 discussed a generalized 16-band model including both Fe $3d$ and As $4p$ orbitals, the electron-phonon interaction does not lift the orbital degeneracy. Hence, by breaking the constraint $U' = U - 2J$, our two-orbital model may just serve as a minimal model with effective U , U' , and J taking account of the electron-phonon interaction.

⁵⁰Y. Yanagi, Y. Yamakawa, and Y. Ōno, *Phys. Rev. B* **81**, 054518 (2010).

⁵¹Relaxing the constraint $U' = U - 2J$ corresponds to picking up a specified set of orbital bases and making the couplings basis dependent since the continuous rotational symmetry in the orbital space is broken. This leads to the two spin-singlet states $1/\sqrt{2}(|\uparrow\downarrow; 0\rangle - |0; \uparrow\downarrow\rangle)$ and $1/\sqrt{2}(|\uparrow; \downarrow\rangle - |\downarrow; \uparrow\rangle)$, with energies $U - J$ and $U' + J$, respectively, which are no longer degenerate. But

relaxing the constraint will not lift the orbital degeneracy of the xz and yz orbitals. Therefore our discussion on the Mott transition in Sec. III A is still valid.

⁵²Performing the perturbative treatment as in Sec. III A, we find, for $U' > U$, $U_c = 4|\tilde{\epsilon}|/(2U'/U - 1 - J/U)$. U_c decreases monotonically when increasing U'/U from 1.

⁵³S. Graser, T. A. Maier, P. J. Hirschfeld, and D. J. Scalapino, *New J. Phys.* **11**, 025016 (2009).

⁵⁴K. Kuroki, S. Onari, R. Arita, H. Usui, Y. Tanaka, H. Kontani, and H. Aoki, *Phys. Rev. Lett.* **101**, 087004 (2008).

⁵⁵P. Werner and A. J. Millis, *Phys. Rev. Lett.* **99**, 126405 (2007).

⁵⁶R. Yu, K. T. Trinh, A. Moreo, M. Daghofer, J. A. Riera, S. Haas, and E. Dagotto, *Phys. Rev. B* **79**, 104510 (2009).

⁵⁷A. Moreo, M. Daghofer, A. Nicholson, and E. Dagotto, *Phys. Rev. B* **80**, 104507 (2009).

⁵⁸E. Bascones, M. J. Calderon, and B. Valenzuela, *Phys. Rev. Lett.* **104**, 227201 (2010).

⁵⁹L. de'Medici, S. R. Hassan, M. Capone, and X. Dai, *Phys. Rev. Lett.* **102**, 126401 (2009).

⁶⁰L. de'Medici, S. R. Hassan, and M. Capone, *J. Supercond. Nov. Mat.* **22**, 535 (2009).

⁶¹J. Knolle, I. Eremin, and R. Moessner, *Phys. Rev. B* **83**, 224503 (2011).

⁶²A. Nicholson, Q. Luo, W. Ge, J. Riera, M. Daghofer, G. B. Martins, A. Moreo, and E. Dagotto, *Phys. Rev. B* **84**, 094519 (2011).

⁶³R. Yu, J.-X. Zhu, and Q. Si, *Phys. Rev. Lett.* **106**, 186401 (2011).

⁶⁴Y. Zhou, D.-H. Xu, F.-C. Zhang, and W.-Q. Chen, *Europhys. Lett.* **95**, 17003 (2011).

⁶⁵W.-H. Ko and P. A. Lee, *Phys. Rev. B* **83**, 134515 (2011).