Spectroscopic mapping of local structural distortions in ferroelectric PbTiO₃/SrTiO₃ superlattices at the unit-cell scale

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(Received 2 November 2011; published 7 December 2011)

The local structural distortions in polydomain ferroelectric PbTiO₃/SrTiO₃ superlattices are investigated by means of high spatial and energy resolution electron-energy-loss spectroscopy combined with high-angle annular dark field imaging. Local structural variations across the interfaces have been identified with unit-cell resolution through the analysis of the energy-loss near-edge structure of the Ti *L*2*,*³ and O *K* edges. *Ab initio* and multiplet calculations of the Ti *L*2*,*³ edges provide unambiguous evidence for an inhomogeneous polarization profile associated with the observed structural distortions across the superlattice.

DOI: [10.1103/PhysRevB.84.220102](http://dx.doi.org/10.1103/PhysRevB.84.220102) PACS number(s): 77*.*84*.*Cg, 79*.*20*.*Uv, 68*.*37*.*Ma

Complex oxide heterostructures offer a vast playground for exploring and combining the many functional properties of these interesting materials arising from the subtle interplay between their charge, spin, orbital, and lattice degrees of freedom. Bilayers, multilayers, and superlattices composed of ultrathin oxide layers not only shed light on our fundamental understanding of the constituent materials, but frequently reveal unexpected phases at their interfaces.¹ Superlattices composed of ferroelectric and paraelectric oxides have been the subject of numerous studies, motivated by fundamental questions about ferroelectric size effects, by the possibilities these artificially layered materials offer for tailoring their functional properties, and by the interesting interface physics they display. Ultrafine period superlattices, composed of ferroelectric PbTiO₃ (PTO) and paraelectric SrTiO₃ (STO), for example, have been shown to exhibit improper ferroelectricity driven by the coupling of the polar and nonpolar distor-tions at the interface.^{[2](#page-4-0)} More recently, regular ferroelectric nanodomains have been observed in PTO/STO superlattices with larger periodicities and were shown to be responsible for large enhancements in the effective dielectric constant. 3 Such domains are expected to give rise to complex inhomogeneous structural distortions and polarization profiles, 4.5 departing from uniform polarization models, frequently used to describe the properties of ferroelectric/paraelectric superlattices in the absence of domains.^{[6](#page-4-0)}

Thus a microscopic insight into the local structure is key to understanding the behavior of these artificially layered materials, and here transmission electron microscopy (TEM), with recent advances in spatial resolution, provides an invaluable tool. Individual ionic displacements within a single perovskite unit cell can now be identified from phase contrast images. The spatial resolution is high enough to determine the direction and even the magnitude of the local dipole moments in ferroelectric materials, $7-\overline{9}$ and has recently enabled the direct verification of the existence of polarization rotation at domain walls in $Pb(Zr,Ti)O_3$ ferroelectric thin films.^{[10](#page-4-0)}

In this Rapid Communication, we focus on an alternative spectroscopic technique to study local ferroelectric distortions at the single unit-cell scale. Atomically resolved electronenergy-loss spectra (EELS) and high-angle annular dark field (HAADF) images have been obtained to access the local structure $11-15$ of polydomain PTO/STO superlattices. We show that the energy-loss near-edge fine structure (ELNES) of the Ti $L_{2,3}$ edge is highly sensitive to very small atomic displacements $(0.1 Å). Changes in the tetragonal distortion$ of the perovskite unit cell as small as 1% have been detected, revealing a variation of tetragonality within individual PTO layers and thus providing direct evidence of local structural inhomogeneities in polydomain ferroelectric/paraelectric superlattices. *Ab initio* and charge transfer multiplet calculations show distinct differences between the spectra expected for polar and nonpolar structures, demonstrating that the EELS technique has sufficient energy and spatial resolution to probe ferroelectricity at the unit-cell scale.

We have studied a $(6|6)_{21}$ superlattice with 21 bilayers of six unit cells of PTO and six unit cells of STO on top of a single-crystalline STO substrate. Epitaxial top and bottom SrRuO3 electrodes were also deposited *in situ*. Details of sample growth and electrical characterization can be found in Ref. [3.](#page-4-0) Atomically resolved HAADF images and EELS spectra were acquired with an aberration-corrected scanning transmission electron microscope (STEM) Nion UltraSTEM 100.^{[16](#page-5-0)} Figure [1\(a\)](#page-1-0) displays a HAADF image of the superlattice projected onto the (010) plane. The variation in HAADF signal intensity for each atomic column reflects the difference in atomic numbers between Pb $(Z = 82)$ and Sr $(Z = 38)$ cations,^{[17](#page-5-0)} demonstrating the atomic sharpness of the interfaces. X-ray diffraction measurements reveal a periodic in-plane modulation attributed to 180◦ ferroelectric domains [Fig. $1(b)$]. The domain satellites are observed independent of the in-plane orientation of the sample, indicating an almost isotropic distribution of domain-wall alignments. The domain periodicity ranges from 55 Å (for domain walls along (100)) to 65 Å (along (110)). This means that, in general, the domain-wall orientation will be random with respect to the imaging plane and the HAADF and EELS images will average over the domains within the thickness of the TEM specimen.

As a reference for the characterization of the (6|6) superlattice, Ti *L*2*,*³ and O *K* EELS spectra were acquired from a 12-nm-thick PTO layer and from the STO substrate (7 nm away

FIG. 1. (Color online) (a) HAADF-STEM image of the [010] projection of a (6|6) PTO/STO superlattice. (b) X-ray reciprocal space scans around the (002) superlattice reflection show broad satellite peaks due to 180◦ ferroelectric domains.

from the interface). Figure $2(a)$ shows the Ti $L_{2,3}$ ELNES of the reference spectra for PTO and STO to be compared with those of the superlattice. The energy resolution (0.4 eV) achieved allows us to identify slight variations between the STO and PTO Ti *L*2*,*³ ELNES that can be correlated with structural differences between the two oxides. While the unit cell of the STO substrate has cubic symmetry $(a = b = c = 3.905 \text{ Å})$, the hybridization between the Pb 6*s* and the O 2*p* states induces a large tetragonal strain¹⁸ in the PTO unit cell $(c/a = 1.063)$ [Fig. $2(c)$]. Due to the reduction in symmetry from the cubic perovskite structure, the crystal-field splitting (CFS) of the Ti 3*d* e_g and t_{2g} orbitals is expected to decrease, leading to the observed reduction in the *L*³ edge energy splitting $(\Delta L_3)^{19,20}$ $(\Delta L_3)^{19,20}$ $(\Delta L_3)^{19,20}$ from 2.3 eV in the STO substrate to 1.65 eV for the PTO layer [Fig. $2(c)$]. The site symmetry of the Ti atom in the $TiO₆$ octahedra is also reduced in the PTO unit cell, the corresponding Ti L_3 - e_g peak showing an asymmetric broadening toward higher energies [see Fig. $2(a)$], that has been attributed to the noncentrosymmetric location of the Ti cation in the TiO₆ octahedra.^{[15](#page-4-0)[,21](#page-5-0)}

Comparing the O *K* ELNES of the STO substrate and the 12-nm-thick PTO layer in Fig. 2(b), clear differences between both spectra can be identified. The most pronounced one is the large shift observed in the position of the second peak (marked with an asterisk). This peak has been attributed to the hybridization of the O 2*p* with Sr 4*d* and with Pb 6*sp* states for STO and PTO, respectively,^{[22–24](#page-5-0)} making it possible to distinguish between Sr and Pb containing cells by identifying the position of this peak. The analysis of the Ti $L_{2,3}$ and O *K* edges therefore offers an excellent method for determining

FIG. 2. (Color online) (a) Ti *L*2*,*³ and (b) O *K* edges for the STO substrate (black upper curve) and the 12-nm-thick PTO layer (red/gray lower curve). (c) Schematic projection along the [010] zone axis of the STO and PTO unit cells. The displacement of the atomic position is displayed as *δ* (Ti), *δ* (O1), and *δ* (O2).

FIG. 3. (Color) (a) HAADF-STEM image and ELNES of Ti *L*2*,*³ and O *K* edges across the (6|6) superlattice. (b) Simultaneous dark field profile recorded along the line scan (black line) and concentration profiles of Sr (green line) and Pb (red line). Horizontal lines mark the interfaces. (c) Energy splitting values in PTO and STO layers across the superlattice. Dashed lines indicate the values for STO substrate and 12-nm-thick PTO. (d) High-resolution Ti *L*2*,*³ and (e) O *K* spectra across the PTO-STO interface after background substraction. (f) Ti *L*³ edges obtained after ten R-L iterations.

both structural and chemical variations within the PTO/STO superlattices.

Figure $3(a)$ shows a series of 512 individual EELS spectra acquired in spectrum-line mode with a dwell time equalling 125 ms, displaying the Ti *L*2*,*³ and the O *K* edges across four interfaces of the (6|6) superlattice. The high spatial resolution of STEM allows us to identify the core loss edges from individual atomic columns, while the dark field profile is simultaneously recorded along the scanning line [black line in Fig. 3(b)]. The Ti *L*2*,*³ and O *K* EELS spectra corresponding to seven consecutive unit cells across one of the PTO-STO interfaces (numbered from 6 to 12 in the image) are displayed in Figs. $3(d)$ and $3(e)$, respectively. Each spectrum is the sum of 22 individual spectra over one unit cell. In order to improve the energy resolution, the Ti $L_{2,3}$ spectra in Fig. $3(f)$ have been deconvoluted using the Richardson-Lucy (R-L) approach[.25](#page-5-0)

Consistent with their large tetragonality, the Ti *L*³ splittings in the PTO layers are smaller than those in STO layers. The value for each unit cell along the superlattice is displayed in Fig. 3(c). For better accuracy, the positions of the t_{2g} and e_g peak maxima were obtained from the first derivatives of the EELS spectra. The splitting value in the center of the PTO layers reaches 1.95 eV, significantly higher than the 1.65 eV obtained for the reference 12-nm PTO layer, and increasing further on approaching the interface. Interestingly, a gradual broadening of the L_3 - e_g band is also observed when moving from the interface (spectrum 9) to the center of the PTO layer (spectrum 12). The spectral splitting of the STO layers is closer to the value of the STO substrate (2.3 eV), but always \sim 50– 100 meV smaller. In order to rule out the interdiffusion of Sr and Pb as the cause of the gradual variation in PTO, chemical profiles across the interface were obtained by multiple leastsquares fitting of the O *K* edge signal from 536 to 540.8 eV

with the two reference components [red and green spectra in Fig. $3(e)$]. The resulting Sr and Pb distributions are plotted in Fig. [3\(b\)](#page-2-0) (green and red line, respectively). At interfaces, i.e., unit cells labeled 3, 9, 15, and 20, both signals clearly cross in between neighboring atomic columns, confining any possible Pb/Sr interdiffusion to ± 1 unit cell from the interface.

To relate the observed continuous evolution of the STO and PTO spectra across the superlattice to structural variations, density functional theory within the local density approximation $(LDA)^{26}$ $(LDA)^{26}$ $(LDA)^{26}$ and charge transfer multiplet calculations^{[27](#page-5-0)} were performed. Two sets of structural models, one for STO and one for PTO, were built by artificially varying the *c/a* ratio from 1 to 1.063, corresponding to the limits of bulk materials. To reproduce the experimental in-plane epitaxial constrain, we set $a = b = 3.905$ Å.

Figures $4(a)$ and $4(b)$ display the relaxed Ti and O atomic positions obtained for PTO and STO unit cells with different *c/a* ratios, respectively. For PTO, excellent agreement was found between the experimental and relaxed atomic positions of the room-temperature PTO unit cell (marked with a square).^{[28](#page-5-0)} Note that as the c/a ratio is reduced, the atomic position of Ti, O(1), and O(2) remain strongly displaced from the ideal centrosymmetric positions, except for the cubic unit cell $(c/a = 1)$. Our LDA calculations for STO confirm the paraelectric state $c/a = 1$ as the predicted ground state but, in this case, significant Ti off-centering is only observed once the tetragonality exceeds ∼1*.*02. From then on, the Ti, O(1), and O(2) atoms move further away from the centrosymmetric positions, but the resulting polar distortion is much smaller than that in PTO with the same *c/a*.

The electronic density of states was computed for the whole relaxed geometry.²⁹ The projected unoccupied density of states on Ti atoms was further projected onto the Ti *d* orbitals and decomposed according to the local symmetry C_{4v} , i.e., d_{z^2} , $d_{x^2-y^2}$, d_{xy} , and $d_{xz} + d_{yz}$.^{[30](#page-5-0)} This noncentrosymmetric point group is induced by the ferroelectric displacement of the Ti atom along the *c* axis. The resulting values obtained for the LDA CFS $[CFS = E(d_{z^2}, d_{x^2-y^2}) - E(d_{xy}, d_{xz} + d_{yz})]$ for STO and PTO unit cells with different *c/a* ratios are shown in Figs. 4(c) and 4(d), respectively.

These CFS, together with the tetragonal distortion energy differences $[\Delta_1 = E(d_{xy}) - E(d_{xz} + d_{yz})$ and $\Delta_2 = E(d_{z^2}) E(d_{x^2-y^2})$], displayed in Figs. 4(c) and 4(d), and the estimated bandwidths obtained by LDA for the STO and PTO were

FIG. 4. (Color) Relaxed atomic displacements as a function of the *c/a* ratio for (a) PTO and (b) STO structural models. CFS values for (c) PTO and (d) STO structural models as a function of the c/a ratio. (e) Simulated L_3 spectra for PTO (red) and STO (black). (f) Simulated L_3 spectra for a paraelectric (blue) and polar (red) tetragonally distorted PTO unit cell ($c/a = 1.063$).

used as input data for charge transfer multiplet calculations, yielding a qualitatively good match with the experimental measurements [Fig. $4(e)$]. In particular, the difference between the energy splittings of PTO and STO $[\Delta E(L_3)_{\text{STO}} - \Delta E(L_3)_{\text{PTO}}]$ is computed to be 0.60 eV, close to the measured value of 0.65 eV. Moreover, the asymmetric broadening in the L_3 - e_g band of the PTO simulated spectra with respect to STO spectra agrees with that experimentally observed in the PTO layers [spectra 9–12 in Fig. $3(f)$].

We have also performed similar calculations for PTO and STO structures with a tetragonal distortion but forcing a paraelectric state (atomic displacements $\delta = 0$), by using the Ti centrosymmetric local symmetry *D*4*^h*. The LDA calculations result in a smaller cubic crystal-field evolution but much larger tetragonal distortion energy that should induce some spectral difference in the EELS data. Although the charge transfer multiplet calculations of the Ti *L*2*,*³ edges using *ab initio* computed parameters are not reliable enough for a quantitative match with experiment, it can provide valuable information about the spectral differences expected between the ferroelectric (FE) and paraelectric (PE) state. Figure $4(f)$ shows the Ti $L_{2,3}$ spectra as obtained by the charge transfer multiplet calculations for the PE and FE tetragonally distorted PTO unit cell $(c/a = 1.063)$. The main splitting of the L_3 and of the *L*² line do not vary much, but features appear due to the strong *D*4*^h* distortion parameters. Such features are not observed either in our experimental EELS data or in previous reported x-ray absorption (XAS) data of tetragonally distorted STO or $\text{PTO.}^{30,31}$ $\text{PTO.}^{30,31}$ $\text{PTO.}^{30,31}$ These results thus exclude a possible centrosymmetric arrangement of the atoms in the PTO layers, confirming their ferroelectric nature, as already revealed by the presence of ferroelectric domains. The large cell-to-cell variation of the CFS in the PTO layers can thus be attributed to a variation in tetragonality and polarization, showing that the uniform polarization model, frequently used to describe monodomain superlattices, 6 does not apply to our polydomain samples.

Combining the results of the *ab initio* calculations and the measurements of the reference PTO and STO spectra allows us to estimate the local distortions within the superlattice layers.

The CFS of the central PTO layer in the superlattice is 0.3 eV larger than that of the reference PTO layer, corresponding to a significantly smaller *c/a* value of ∼1.025, which further decreases toward the interface. The STO layers show a weaker CFS variation, with the four central unit cells all showing splittings ∼0.1 eV below that of the cubic STO substrate. The small tetragonality is consistent with x-ray diffraction measurements on pure paraelectric STO films, which yield a *c*-axis lattice parameter of 3.92 Å, possibly signaling a slight off-stoichiometry[.32](#page-5-0) The very weak distortion in the STO makes it difficult to distinguish whether or not these layers are polar, but if any polarization is present, it is small and any electrostatic coupling between the PTO layers 33 is therefore likely to be weak. The structural distortions illustrated in Fig. $3(c)$ may arise from the inhomogeneous strains associated with the domain structure itself. However, we should note that a similar reduction of tetragonality at interfaces or surfaces of Pb-based ferroelectrics has also been observed in thin films without stripe domains,⁷ and hence the precise physical origin of these distortions requires further study.

In this Rapid Communication, we have illustrated that high-resolution EELS is a powerful alternative technique for studying local ferroelectric distortions at the perovskite unit-cell scale. The technique is sensitive enough to measure small variations in the $L_{2,3}$ edge down to 50 meV that can be semiquantitatively related to a *c/a* evolution as small as 1%, allowing us to map with ultrahigh sensitivity cell-to-cell variations in local structural distortions, and revealing an inhomogeneous polarization profile within the ferroelectric and paraelectric layers that previously only has been predicted theoretically or inferred by indirect means. Recent XAS measurements reveal that linear dichroism is sensitive to the polarization direction,^{[31](#page-5-0)} suggesting that this information could also be accessible through anisotropic EELS. However, achieving high spatial resolution in anisotropic EELS measurements is still a challenging task.

The authors acknowledge funding from the Swiss National Science Foundation through the NCCR MaNEP and division II, the EU OxIDes project and the ESTEEM program.

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