

# Magnetic and transport properties of rare-earth-based half-Heusler phases $RPdBi$ : Prospective systems for topological quantum phenomena

K. Gofryk,<sup>1,2,\*</sup> D. Kaczorowski,<sup>2</sup> T. Plackowski,<sup>2</sup> A. Leithe-Jasper,<sup>3</sup> and Yu. Grin<sup>3</sup>

<sup>1</sup>Condensed Matter and Thermal Physics, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

<sup>2</sup>Institute of Low Temperature and Structure Research, Polish Academy of Sciences, P.O. Box 1410, 50-950 Wrocław, Poland

<sup>3</sup>Max-Planck-Institut für Chemische Physik fester Stoffe, Nöthnitzer Str. 40, 01187 Dresden, Germany

(Received 5 April 2011; published 29 July 2011)

$RPdBi$  ( $R = \text{Er, Ho, Gd, Dy, Y, Nd}$ ) compounds were studied by means of x-ray diffraction, magnetic susceptibility, electrical resistivity, magnetoresistivity, thermoelectric power, and Hall effect measurements, performed in the temperature range 1.5–300 K and in magnetic fields up to 12 T. These ternaries, except diamagnetic  $YPdBi$ , exhibit localized magnetism of  $R^{3+}$  ions, and order antiferromagnetically at low temperatures ( $T_N = 2\text{--}13$  K). The transport measurements revealed behavior characteristic of semimetals or narrow-band semiconductors. Both, electrons and holes contribute to the conductivity with dominant role of  $p$ -type carriers. The Hall effect of  $ErPdBi$  is strongly temperature and magnetic field dependent, reflecting complex character of the underlying electronic structures with multiple electron and hole bands.  $RPdBi$ , and especially  $DyPdBi$ , exhibit very good thermoelectric properties with a power factor coefficient  $PF$  ranging from 6 to 20  $\mu\text{W cm}^{-1} \text{K}^{-2}$ .

DOI: 10.1103/PhysRevB.84.035208

PACS number(s): 71.20.Eh, 71.55.Ak, 72.15.Eb, 72.15.Jf

## I. INTRODUCTION

The rare-earth ( $R$ )-based ternary compounds with the composition  $RTX$ , where  $T$  denotes a  $d$ -electron transition metal and  $X$  is a  $p$ -element, have been studied extensively during last years.<sup>1</sup> Specifically, phases crystalizing in a cubic  $MgAgAs$ -type of crystal structure which are also known under the very unlucky name “half-Heusler” phases, are well known because of many different intriguing and extraordinary physical properties observed in this family,<sup>2</sup> including half-metallic<sup>3</sup> and semiconducting-like behavior,<sup>4–6</sup> giant magnetoresistivity,<sup>7,8</sup> or heavy fermion state.<sup>9–11</sup> For this reason, these phases have been named “compounds with properties on request.”<sup>12</sup> Very recently, based on first-principle calculations, a topological insulating state has been predicted in heavy metal-element containing half-Heusler phases.<sup>13,14</sup> The topological insulator is a new state of quantum matter having a full insulating gap in the bulk, but with topologically protected gapless surface or edge states on the boundary. It has been demonstrated that some compounds from the series  $RAuPb$ ,  $RPtSb$ ,  $RPtBi$ , or  $RPdBi$  exhibit a band inversion similar to that discovered in  $HgTe$ .<sup>13,14</sup> Band structure calculations show that these phases should possess a semimetallic or narrow-band semiconducting state and the topological state may be created by applying strain (such as crystallographic distortion) or by designing an appropriate quantum-well structure, similar to the case of  $HgTe$ . Interestingly, since many of those  $MgAgAs$  compounds contain a rare-earth element, additional properties ranging from superconductivity to magnetism and heavy fermion behavior may be realized within a topological matrix. These properties can open new research directions in realizing the quantized anomalous Hall effect,<sup>15,16</sup> topological superconductors with Majorana fermion excitations,<sup>17</sup> and/or image magnetic monopole effect.<sup>18</sup> In this paper, we present the magnetic and electrical transport properties of a series of rare-earth-based  $RPdBi$  phases. The compounds are either paramagnetic or antiferromagnetic with Néel temperatures of several kelvin (except of  $YPdBi$  which shows diamagnetic behavior) due to well localized  $4f$  electrons. The transport

measurements revealed semimetallic behavior with likely dominance of  $p$ -type carriers. The electronic structure has complex character with the presence of multiple electron and hole bands. Moreover, this family of compounds seems to possess very good thermoelectrical parameters, prospective for practical applications.

## II. EXPERIMENTAL DETAILS

Polycrystalline samples of  $ErPdBi$ ,  $HoPdBi$ ,  $GdPdBi$ ,  $YPdBi$ ,  $DyPdBi$ , and  $NpPdBi$  were prepared by arc melting the constituents ( $RE$ : 99.9 wt%, Pd: 99.999 wt%, Sb: 99.999 wt%) under ultra pure argon atmosphere. Since additional heat treatment led to multiphase products, the as-cast samples were used for physical measurements. The quality of the obtained materials was checked at 300 K by powder x-ray diffraction (Huber Guinier G670 image plate camera with  $\text{CuK}\alpha_1$  radiation,  $\lambda = 1.5406 \text{ \AA}$ , and silicon as an internal standard,  $a = 5.43119 \text{ \AA}$ ), optical metallography (Zeiss Axioplan 2 optical microscope with a CCD camera), and EDX analysis [Philips XL30 scanning electron microscope with integrated EDXS system and S-UTW-Si-(Li) detector]. All these studies have shown that the samples studied were single phase with a cubic structure of the  $MgAgAs$  type (space group  $F\bar{4}3m$ ). This crystal structure is shown in Fig. 1, together with a unit cell adopted by so-called Heusler phases ( $\text{MnCu}_2\text{Al}$  type; space group  $Fm\bar{3}m$ ). The lattice parameters obtained from the x-ray diffraction data are:  $a = 6.5952, 6.6012, 6.6343, 6.6391, 6.6906, \text{ and } 6.7257 \text{ \AA}$  for  $ErPdBi, HoPdBi, DyPdBi, YPdBi, GdPdBi, \text{ and } NdPdBi$ , respectively. The derived values are in a good agreement with those given in the literature.<sup>19</sup>

Magnetization measurements were carried out in the temperature range 1.7–300 K and in magnetic fields up to 5 T using a Quantum Design MPMS-5 magnetometer. The electrical resistivity was measured from 4 to 300 K by a standard four-point dc technique. The Hall effect measurements were performed in the temperature range 1.5–300 K and in applied fields up to 12 T (Oxford Instruments TESLATRON). The

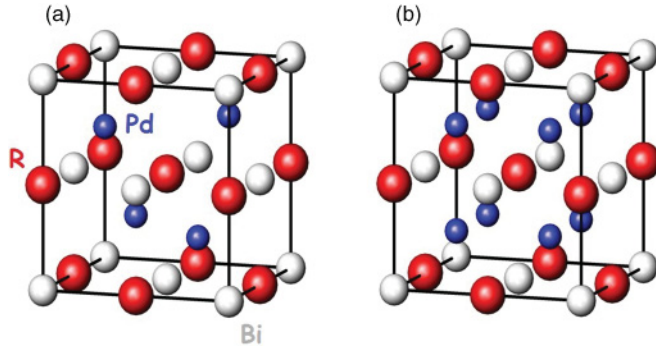


FIG. 1. (Color online) Crystal structure of (a) MgAgAs- and (b) MnCu<sub>2</sub>Al-type phases.

thermoelectric power was studied from 6 to 300 K, employing a home-built setup using pure copper as a reference material.

### III. RESULTS AND DISCUSSION

The magnetic measurements revealed that HoPdBi, DyPdBi, GdPdBi, and NdPdBi order antiferromagnetically at 2, 3.5, 13, and 4 K, respectively, while ErPdBi remains paramagnetic down to the lowest temperature studied [see Fig. 2(a)]. In wide temperature ranges, the  $\chi^{-1}(T)$  exhibit linear temperature dependence. They may be well described by the Curie-Weiss law and the effective magnetic moments  $\mu_B$  being close to those expected for free  $R^{3+}$  ions within Russell-Saunders coupling scenario,  $\mu_{\text{eff}}^{R^{3+}} = g[J(J+1)]^{1/2}$ . This indicates good localization of the magnetic moments on the rare-earth atoms. Moreover, the obtained values of the paramagnetic Curie temperature are small and negative, consistent with the type of magnetic ordering in these systems. As the only exception, YPdBi, which does not contain  $4f$  electrons, shows a diamagnetic behavior [see Fig. 2(b)] that may reflect the formation of a time-reversal-invariant spin-orbit ground state. It is worth to recall that it is one of the conditions for realizing a  $Z_2 = -1$  topological insulating state.<sup>14</sup>

The temperature dependencies of the electrical resistivity of the  $RPdBi$  phases are shown in Fig. 3. In general, the magnitude and the temperature variations of the resistivity are characteristic of semimetals or narrow-gap semiconductors.<sup>20</sup> In the case of ErPdBi, GdPdBi, NdPdBi, and DyPdBi, the  $\rho(T)$  exhibits two different regimes. At high temperatures, the electrical resistivity displays a semiconducting-like character ( $d\rho/dT < 0$ ), signaling carrier excitations over a small energy gap  $E_g$  near the Fermi level. This behavior is followed at lower temperatures by a metallic-like dependence of  $\rho(T)$  ( $d\rho/dT > 0$ ). In general, the observed behavior is reminiscent of those typical for doped semiconductors where, due to atomic disorder, defects and/or wrong stoichiometry some donor or acceptor levels are present, leading to metallic-like  $\rho(T)$ . In order to account for this rather complex temperature behavior a simple model of the electronic band structure in narrow-gap semiconductors may be used (see Refs. 6,21–23). Recently, this model has been successfully applied to describe the temperature dependence of the resistivity in some filled skutterudites<sup>22</sup> as well as in compounds ErPdSb,<sup>6</sup> HoPdSb,<sup>21</sup> and DyPdBi.<sup>21</sup> In this approach, one considers two rectangular

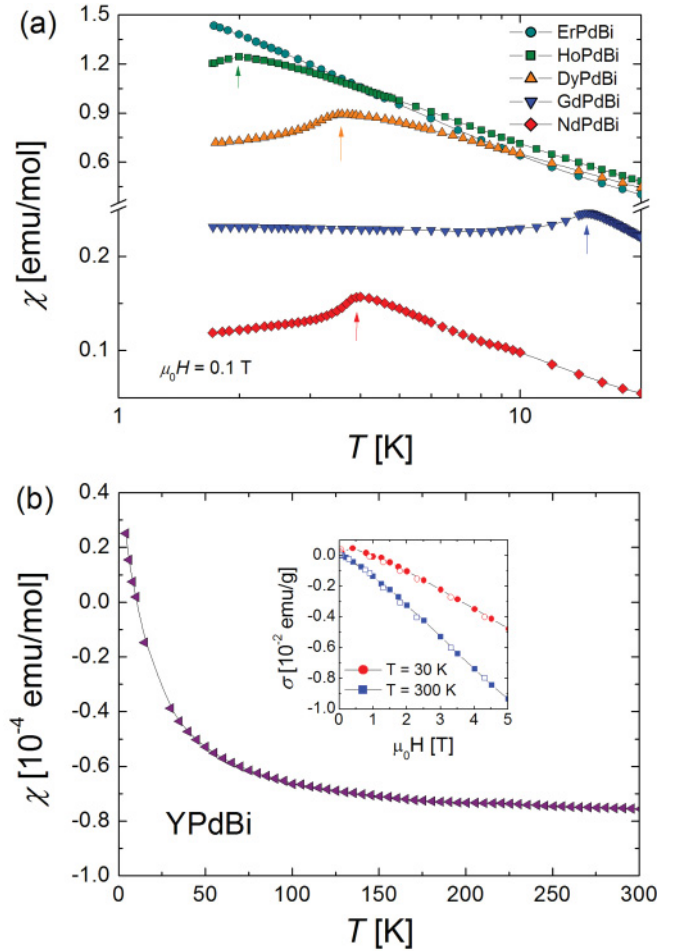


FIG. 2. (Color online) (a) Low temperature dependencies of the magnetic susceptibility of  $RPdBi$  compounds. Arrows mark the antiferromagnetic phase transition. (b) Temperature dependence of the magnetic susceptibility of YPdBi. (Inset) Magnetic field variation of the magnetization in YPdBi taken at 30 and 300 K with increasing (solid symbols) and decreasing (empty symbols) field.

bands of height  $N$ , separated by an energy gap  $E_g$ , and the Fermi level situated just below the gap. In order to describe the metallic conductivity at low temperatures, the presence of some temperature-independent amount of carriers  $n_0$  is assumed. Thus, the total number of carriers can be expressed as

$$n(T) = n_0 + \sqrt{n_e(T)n_h(T)}, \quad (1)$$

where the concentrations of electrons  $n_e(T)$  and holes  $n_h(T)$  are given by

$$n_e(T) = -NE_g + Nk_B T \ln 2 \left[ 1 + \left( \frac{E_g}{k_B T} \right) \right], \quad (2)$$

$$n_h(T) = -Nk_B T \ln 2. \quad (3)$$

Based on these assumptions and approximations,  $\rho(T)$  can be defined as

$$\rho(T) = \frac{n_0 \rho_0 + \rho_{\text{ph}}(T)}{n(T)}. \quad (4)$$

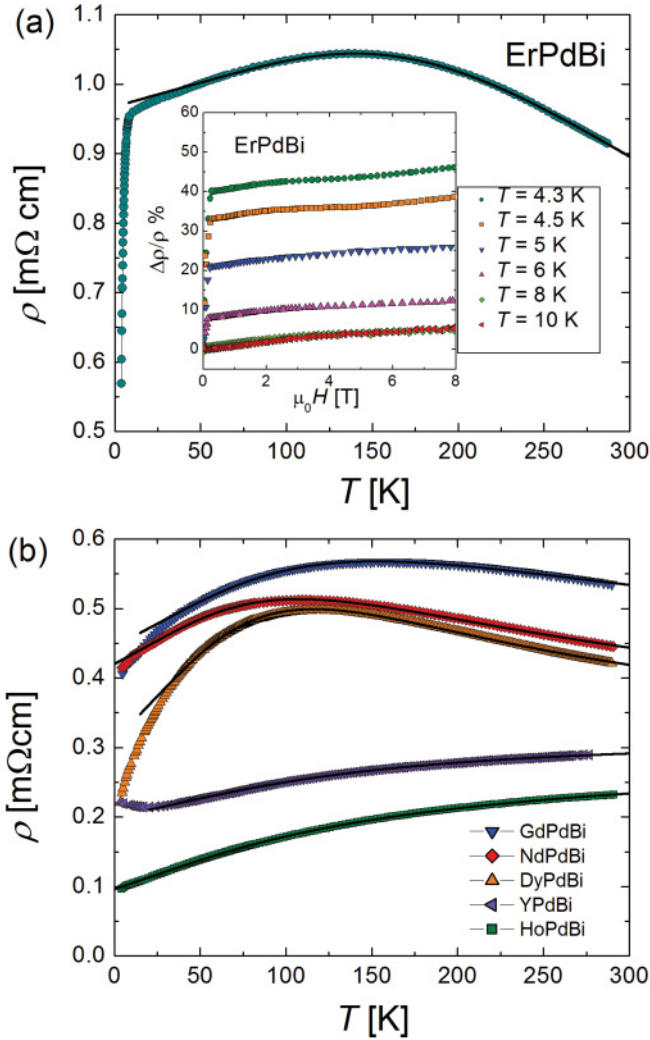


FIG. 3. (Color online) Temperature dependencies of the electrical resistivity of  $RPdBi$  compounds. The solid lines are the fits to Eq. (4) to the experimental data (see text). (Inset) Magnetoresistivity isotherms vs. field taken for  $ErPdBi$ .

In this formula,  $\rho_{ph}(T)$  represents the phonon contribution to the resistivity, which is further assumed to be  $\rho_{ph}(T) = AT$  for temperatures above  $\Theta_D/10$ , where  $\Theta_D$  is the Debye temperature (see also Ref. 21).

As is seen in Fig. 3, above  $\sim 25$  K, the above model provides a quite satisfactory description of the electrical resistivity of all of the compounds studied (see solid lines in Fig. 3). The obtained parameters are collected in Table I. As may be seen, the number of carriers  $n_0$  as well as the parameters characterizing the bands and the gap ( $N$  and  $E_g$ ) nicely reflect the differences between the compounds studied as regards the character and magnitude of their electrical conductivity.

For  $ErPdBi$ , a pronounced drop in  $\rho(T)$  at about 7 K is observed. This behavior is very similar to that previously observed in the  $RPdSb$  system, especially for  $ErPdSb$  (see Refs. 6,21,23). As can be inferred from the inset to Fig. 3(a), the anomaly in  $\rho(T)$  can be suppressed by magnetic field, in a manner typical for superconductivity. However, neither  $ErPdBi$  nor  $ErPdSb$  are bulk superconductors, as no corresponding features are observed in their magnetic and heat capacity data (see Ref. 23 for a more detailed discussion of this issue). Thus, the origin of the unusual low-temperature behavior of the resistivity of  $ErPdBi$  is unknown. Similarly, at the present stage, we cannot reliably interpret the anomalous feature seen in  $\rho(T)$  of  $YPdBi$ , i.e., an increase of the resistivity below 19 K.

As the thermopower is a sensitive probe of energy relative to the Fermi level, it can be used as a tool to characterize the electronic structure, especially in the vicinity of the narrow gap or pseudogap. Figure 4 shows the temperature dependencies of the Seebeck coefficient of the  $RPdBi$  series. The magnetic phase transitions in these compounds manifest themselves as tiny anomalies in  $S(T)$ , better seen on the temperature derivative  $dS/dT$  (as an example, see, the behavior of  $GdPdBi$  in the inset in Fig. 4). In general, the overall magnitude and the temperature variations of the thermopower of  $RPdBi$  are characteristic of low carrier density semimetals.<sup>24–26</sup> At 300 K, the thermoelectric power is as large as about 40–90  $\mu V/K$ , which corresponds within a single band model to the effective carrier concentration of the order of  $10^{20} \text{ cm}^{-3}$ . For all the compounds studied, the Seebeck coefficient is positive in the entire temperature range, thus suggesting that holes may dominate the electrical and heat transport. However, strongly curvilinear character of  $S(T)$  hints at the presence of complex electronic structure in the vicinity of the Fermi energy. Indeed, the most recent theoretical calculations have revealed a fairly complex electronic structure in  $YPdBi$  (Ref. 13) and in other  $RTX$  systems,<sup>14</sup> with electron and hole bands close to the Fermi energy.

To account for this complexity, the temperature dependencies of the thermoelectric power of the  $RPdBi$  compounds

TABLE I. Transport parameters for  $RPdBi$  ( $R = Er, Ho, Dy, Gd, Nd, \text{ and } Y$ ).  $n_0$ : number of carriers at  $T = 0$  K,  $\rho_0$ : residual resistivity,  $N$ : density of states,  $\rho_{300K}$ : resistivity measured at  $T = 300$  K,  $S_{300K}$ : thermopower measured at  $T = 300$  K,  $E_g$ : energy gap,  $\Delta_{N,W}$ , and  $\Gamma_{N,W}$ : position of the narrow and wide bands with relation to the Fermi energy and their width (see text).

Compound	$n_0$ (f.u. <sup>-1</sup> )	$N$ (eV <sup>-1</sup> )	$\rho_{300K}$ ( $\mu\Omega$ cm)	$E_g$ (meV)	$S_{300K}$ ( $\mu V/K$ )	$\Delta_N$ (meV)	$\Gamma_N$ (meV)	$\Delta_W$ (meV)	$\Gamma_W$ (meV)
$ErPdBi$	0.07	5.96	900	94	80	0.45	5.1	32	52
$HoPdBi$	0.17	8.01	234	32	50	0.12	5.5	110	130
$DyPdBi$	0.16	24.5	422	35	92	0.65	8.1	34	47
$YPdBi$	0.27	7.85	293	44.5	44	0.15	7.1	72	126
$GdPdBi$	0.13	8.1	533	43	79	0.65	5.8	44	65
$NdPdBi$	0.12	9.65	442	34.5	69	0.35	6.6	55	79



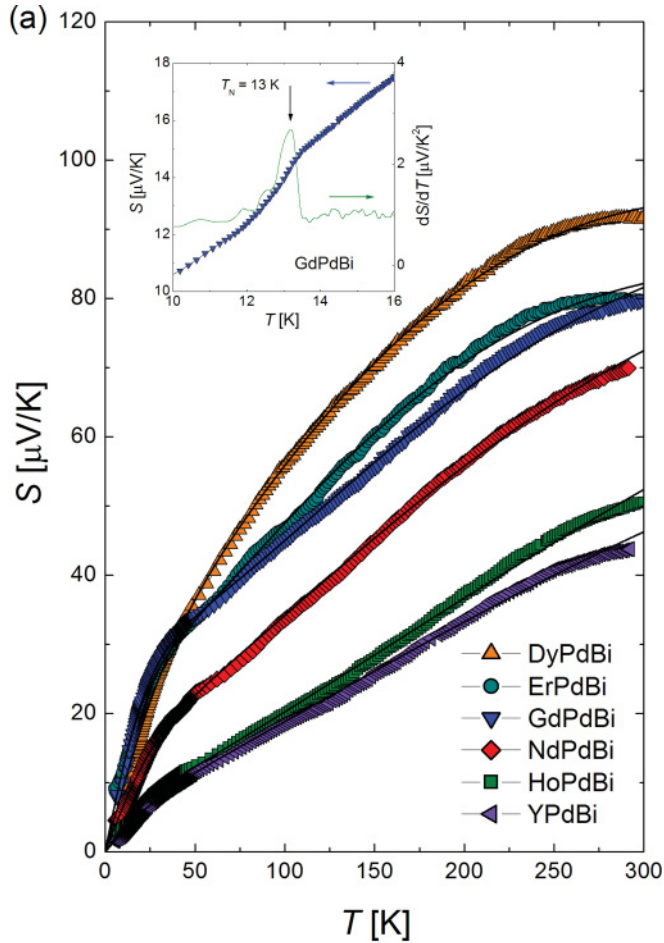


FIG. 4. (Color online) Temperature dependencies of the thermoelectric power of  $RPdBi$  compounds. The solid lines represent least-square fits of the two band model [Eq. (5)] to the experimental data (see text). Inset shows  $S(T)$  and  $dS/dT$  of  $GdPdBi$  in the vicinity of the magnetic phase transition.

were analyzed in terms of a phenomenological model, which describes scattering of carriers on two quasiparticle bands laying close to the Fermi level.<sup>27</sup> In this approach, it is assumed that the conduction electrons are scattered independently on a narrow  $N$  and a wide  $W$  bands approximated by Lorentzians. The thermoelectric power in such a system can be expressed by a modified Mott's formula<sup>27</sup>

$$S(T) = S_N(T) + S_W(T) = \frac{a_N T}{b_N^2 + T^2} + \frac{a_W T}{b_W^2 + T^2}, \quad (5)$$

where

$$a_{N,W} = \frac{2\Delta_{N,W}}{|e|}, \quad (6)$$

and

$$b_{N,W}^2 = \frac{3\Delta_{N,W}^2 + \Gamma_{N,W}^2}{\pi^2 k_B^2}. \quad (7)$$

In the above equations,  $\Delta_{N,W}$  represents the positions of the Lorentzians with relation to the Fermi energy, while  $\Gamma_{N,W}$  stands for their width. As shown by the solid lines in Fig. 4, the above model provides a good description of the

experimental data of  $RPdBi$ . The so-obtained parameters,  $\Delta_{N,W}$  and  $\Gamma_{N,W}$ , are listed in Table I.

The relatively large values of the Seebeck coefficient at room temperature together with rather small electrical resistivity found for the  $RPdBi$  materials yield quite enhanced magnitude of the thermoelectric power factor  $PF = S^2/\rho$ , ranging from  $6.3 \mu\text{W cm}^{-1} \text{K}^{-2}$  for  $YPdBi$  to  $20.3 \mu\text{W cm}^{-1} \text{K}^{-2}$  for  $DyPdBi$ . These values are much larger than the ones obtained for  $RPdSb$  compounds<sup>6</sup> and comparable with  $PF \sim 20\text{--}25 \mu\text{W cm}^{-1} \text{K}^{-2}$  derived for the  $(Zr,Hf)NiSn$  system doped by Ta or Nd.<sup>28</sup> It is worth emphasizing that a large value of the power factor is the main prerequisite for a good thermoelectrical efficiency, yet thermal conductivity studies are indispensable to fully characterize the thermoelectric potential of a given material. The performance of thermoelectric devices is quantified by a dimensionless figure of merit  $ZT = S^2/\rho\kappa$ , where  $S$  is the Seebeck coefficient,  $\rho$  is the electrical resistivity, and  $\kappa$  stands for the thermal conductivity. Such measurements would be needed especially for  $DyPdBi$  which seems to be the most promising in terms of thermoelectric performance usefulness for applications. It is worth noting that in the case of  $ErPdBi$ , the relatively low thermal conductivity results in figure of merit of approximately 0.08 at 500 K.<sup>29</sup> This value of  $ZT$  is similar to those found for doped  $3d$ -electron transition metal-based half-Heusler phases (see Refs. 28,30).

The temperature dependence of the Hall coefficient of  $ErPdBi$  is shown in Fig. 5(a). The positive sign of  $R_H$  throughout the entire temperature range indicates that holes dominate the electrical and heat transport. This is fully consistent with the positive sign of the Seebeck coefficient observed in this compound. As shown in Fig. 5(b) and in the inset to Fig. 5(a),  $R_H$  exhibits strong temperature and magnetic field dependencies. This finding further supports the conjecture on the complex electronic structure in  $ErPdBi$ , where the electron and hole bands have temperature and magnetic field dependent carrier concentrations and mobilities. At the lowest temperature, the Hall coefficient is about  $0.93 \times 10^{-7} \text{ m}^3/\text{C}$ . It is almost three times smaller than that found in the narrow-band semiconductor  $ErPdSb$  (Ref. 6) but still  $10^2\text{--}10^4$  times larger than  $R_H$  observed in simple metals. Within the single band model, one may estimate the carrier concentration  $n_H$  and the Hall mobility  $\mu_H$  to be of the order of  $10^{19} \text{ cm}^{-3}$  and  $100 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , respectively. These values were found to be strongly temperature dependent (not shown). The value of  $n_H$ , due to the crude approximation that neglects semimetallic character of the compound, can be considered as an upper limit of the real concentration in this material. It is about an order of magnitude smaller than the one derived from the thermoelectric data, yet close to  $n_H$  reported for semimetallic compounds  $MNiSn$  ( $M = \text{Hf}, \text{Zr}, \text{Ti}$ ).<sup>31,32</sup> In turn, the estimated mobility is much lower ( $\sim 8$  times) than the bulk mobility obtained for the topological insulator  $\text{Bi}_2\text{Te}_3$ .<sup>33</sup> It is also worth to mention that for the latter compound, the surface mobility reaches as large magnitude as  $10\,000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  (see Ref. 33).

#### IV. SUMMARY AND CONCLUSIONS

The bismuthides  $RPdBi$  ( $R = \text{Er}, \text{Ho}, \text{Gd}, \text{Y}, \text{Dy}, \text{Nd}$ ) crystallize in the cubic  $\text{MgAgAs}$ -type structure. These compounds, except diamagnetic  $YPdBi$ , exhibit localized magnetism due

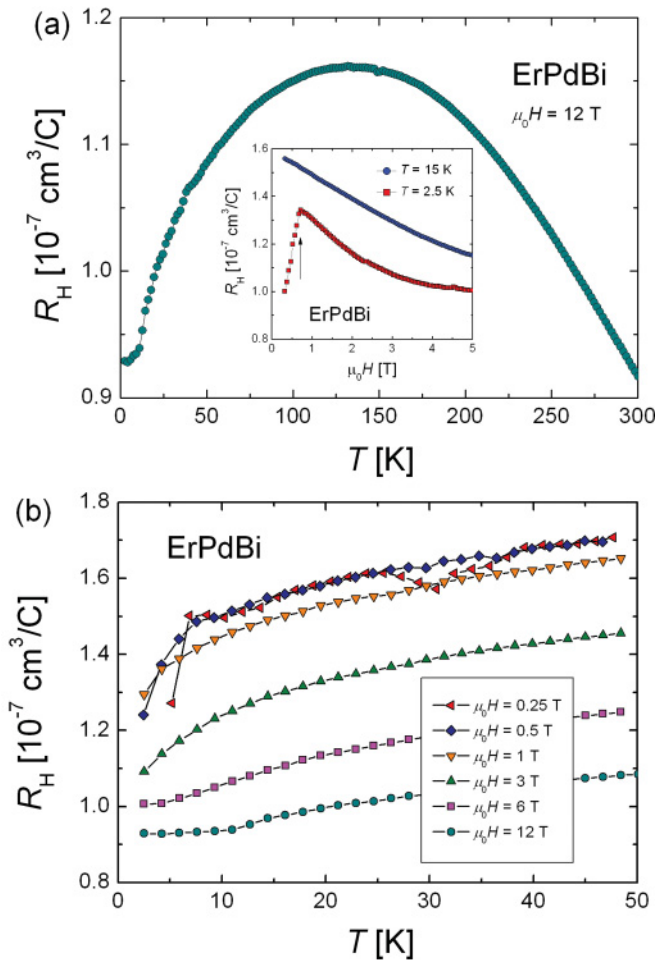


FIG. 5. (Color online) (a) Temperature dependence of the Hall coefficient of ErPdBi. (Inset)  $R_H(B)$  curves obtained at 2.5 and 15 K. (b) Low temperature dependence of  $R_H$  measured in several different magnetic fields.

to  $R^{3+}$  ions. Most of them order antiferromagnetically at low temperatures. All the samples studied showed the electrical conductivity reminiscent of semimetals or narrow-gap semiconductors. Their thermoelectric power behaves in a manner typical for semimetals with holes as majority carriers. Moreover, for ErPdBi, the Hall effect study revealed a complex

electronic structure with multiple electron and hole bands and different temperature and magnetic field variations of the carrier concentrations and their mobilities.

The results obtained for the RPdBi compounds seem to be fully compatible with the theoretical predictions for topological insulators.<sup>13,14</sup> In particular, a nontrivial zero-gap semiconducting state has been postulated for YPdBi, with relatively small topological band inversion strength, whereas a narrow-gap semiconducting state has been predicted for YPdSb (Ref. 14). These theoretical results agree well with the experimental data, presented in this work and in Ref. 6. It is worth noting that YPdBi (maybe also some other RPdBi compounds) is located very close to the inversion transition,<sup>14</sup> and hence it should be relatively easy to lift the degeneracy and open an inverted gap up at the Fermi level by small distortion of the cubic structure via alloying or external pressure. This intriguing hypothesis should motivate further studies in the field. In the latter context, one should stress that even though the RPdBi phases exhibit significant bulk carrier densities, the existence of topological state in these compounds cannot be ruled out. Hitherto studied materials such as  $\text{Bi}_2\text{Se}_3$  or  $\text{Bi}_{1-x}\text{Sb}_x$  have been predicted to be topological insulators only if they are perfectly crystalline. Real samples always have impurities and defects causing them not to be truly insulating, but to possess a finite bulk carrier density. Even materials which display a bulk insulating state, in surface sensitive experiments such as STM or ARPES, still show finite bulk carrier density in transport measurements.<sup>34,35</sup> Clearly, more investigations in this research field are required on well-defined samples with the highest quality, involving wide range of different experimental techniques.

Last but not the least, all the RPdBi compounds studied, and especially DyPdBi, exhibit the large power factor coefficients  $PF = 6\text{--}20 \mu\text{W cm}^{-1} \text{K}^{-2}$ . This result should motivate further work toward determining their figure of merit coefficient  $ZT$ , which measures the thermoelectric efficiency in real applications.

#### ACKNOWLEDGMENTS

We are indebted to U. Burkhardt and H. Borrmann for metallographic and x-ray powder analysis of the samples. We thank T. Durakiewicz and J. Lashley for valuable discussion.

\*gofryk@lanl.gov

<sup>1</sup>P. J. Webster and K. R. A. Ziebeck, *J. Phys. Chem. Solids* **34**, 1647 (1973).

<sup>2</sup>C. Felser, G. H. Fecher, and B. Balke, *Angew. Chem. Int. Ed.* **46**, 668 (2007).

<sup>3</sup>R. A. de Groot, F. M. Mueller, P. G. van Engen, and K. H. J. Buschow, *Phys. Rev. Lett.* **50**, 2024 (1983).

<sup>4</sup>C. Uher, J. Yang, S. Hu, D. T. Morelli, and G. P. Meisner, *Phys. Rev. B* **59**, 8615 (1999).

<sup>5</sup>H. C. Kandpal, C. Felser, and R. Seshadri, *J. Phys. D: Appl. Phys.* **39**, 776 (2006).

<sup>6</sup>K. Gofryk, D. Kaczorowski, T. Plackowski, J. Mucha, A. Leithe-Jasper, W. Schnelle, and Yu. Grin, *Phys. Rev. B* **75**, 224426 (2007).

<sup>7</sup>J. Pierre and I. Karla, *J. Magn. Magn. Mater.* **217**, 74 (2000).

<sup>8</sup>I. Karla, J. Pierre, and R. V. Skolozdra, *J. Alloys Compd.* **265**, 42 (1998).

<sup>9</sup>P. C. Canfield, J. D. Thompson, W. P. Beyermann, A. Lacerda, M. F. Hundley, E. Petersen, and Z. Fisk, *J. Appl. Phys.* **70**, 5800 (1991).

<sup>10</sup>M. F. Hundley, J. D. Thompson, P. C. Canfield, and Z. Fisk, *Phys. Rev. B* **56**, 8098 (1997).

<sup>11</sup>D. Kaczorowski, A. Leithe-Jasper, P. Rogl, H. Flandorfer, T. Cichorek, R. Pietri, and B. Andraka, *Phys. Rev. B* **60**, 422 (1999).

<sup>12</sup>J. Pierre, R. V. Skolozdra, J. Tobola, C. Hordequin, M. A. Kouacou, I. Karla, R. Currat, and E. Lelievre-Berna, *J. Alloys Compd.* **262-263**, 101 (1997).

- <sup>13</sup>S. Chadov, X. Qi, J. Kübler, G. G. Fecher, C. Felser, and S. C. Zhang, *Nat. Mater.* **9**, 541 (2010).
- <sup>14</sup>H. Lin, L. A. Wray, Y. Xia, S. Xu, S. Jia, R. J. Cava, A. Bansil, and M. Z. Hasan, *Nat. Mater.* **9**, 546 (2010).
- <sup>15</sup>L. Fu and C. L. Kane, *Phys. Rev. B* **76**, 045302 (2007).
- <sup>16</sup>X.-L. Qi, T. L. Hughes, and S.-C. Zhang, *Phys. Rev. B* **78**, 195424 (2008).
- <sup>17</sup>L. Fu and C. L. Kane, *Phys. Rev. Lett.* **100**, 096407 (2008).
- <sup>18</sup>X.-L. Qi, R. Zhang, and S.-C. Zhang, *Science* **323**, 1184 (2009).
- <sup>19</sup>M. G. Haase, T. Schmidt, C. G. Richter, H. Block, and W. Jeitschko, *J. Solid State Chem.* **168**, 18 (2002).
- <sup>20</sup>R. Dornhaus, G. Nimitz, and B. Schlicht, *Narrow-Gap Semiconductors* (Springer, Berlin, 1983).
- <sup>21</sup>K. Gofryk, D. Kaczorowski, T. Plackowski, A. Leithe-Jasper, and Yu. Grin, *Phys. Rev. B* **72**, 094409 (2005).
- <sup>22</sup>St. Berger, Ch. Paul, H. Michor, E. Bauer, G. Hilscher, A. Grytsiv, and P. Rogl, *Proc. 21st International Conference on Thermoelectrics* (IEEE, 2002), p. 48.
- <sup>23</sup>D. Kaczorowski, K. Gofryk, T. Plackowski, A. Leithe-Jasper, and Yu. Grin, *J. Magn. Magn. Mater.* **290-291**, 573 (2005).
- <sup>24</sup>K. Durczewski and M. Ausloos, *Z. Phys. B* **85**, 59 (1991).
- <sup>25</sup>F. G. Aliev, N. B. Brandt, V. V. Moshchalkov, V. V. Kozyrkov, R. V. Skolozdra, and A. I. Belogorokhov, *Z. Phys. B* **75**, 167 (1989).
- <sup>26</sup>F. G. Aliev, V. V. Kozyrkov, V. V. Moshchalkov, R. V. Skolozdra, and K. Durczewski, *Z. Phys. B* **80**, 353 (1990).
- <sup>27</sup>Y. Bando, T. Suemitsu, K. Takagi, H. Tokushima, Y. Echizen, K. Kato, K. Umeo, Y. Maeda, and T. Takabatake, *J. Alloys Compd.* **313**, 1 (2000).
- <sup>28</sup>H. Hohl, A. P. Ramirez, C. Goldmann, G. Ernst, B. Wölfing, and E. Bucher, *J. Phys. Condens. Matter* **11**, 1697 (1999).
- <sup>29</sup>T. Sekimoto, K. Kurosaki, H. Muta, and S. Yamanaka, *J. Appl. Phys.* **99**, 10370 (2006).
- <sup>30</sup>Q. Shen, L. Chen, T. Goto, T. Hirai, J. Yang, G. P. Meisner, and C. Uher, *Appl. Phys. Lett.* **79**, 4165 (2001).
- <sup>31</sup>F. G. Aliev, V. V. Moshchalkov, V. V. Kozyrkov, M. K. Zalyalyutdinov, V. V. Pryadun, and R. V. Skolozdra, *J. Magn. Magn. Mater.* **76**, 295 (1988).
- <sup>32</sup>F. G. Aliev, *Physica B* **171**, 199 (1991).
- <sup>33</sup>D.-X. Qu, Y. S. Hor, Jun Xiong, R. J. Cava, and N. P. Ong, *Science* **329**, 821 (2010).
- <sup>34</sup>J. G. Analytis, J. H. Chu, Y. Chen, F. Corredor, R. D. McDonald, Z. X. Shen, and I. R. Fisher, *Phys. Rev. B* **81**, 205407 (2010).
- <sup>35</sup>J. G. Analytis, R. D. McDonald, S. C. Riggs, J. H. Chu, G. S. Boebinger, and I. R. Fisher, *Nat. Phys.* **6**, 960 (2010).