

Transport scattering time probed through rf admittance of a graphene capacitor

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We have investigated electron dynamics in top gated graphene by measuring the gate admittance of a diffusive graphene capacitor in a broad frequency range as a function of carrier density. The density of states, conductivity, and diffusion constant are deduced from the low-frequency gate capacitance, its charging time, and their ratio. The admittance evolves from an rc-like to a skin-effect response at GHz frequency with a crossover given by the Thouless energy. The scattering time is found to be independent of energy in the 0- to 200-meV investigated range at room temperature. This is consistent with a random mass model for Dirac fermions.

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I. INTRODUCTION

Electron scattering in graphene is still a debated matter (see Refs. 1–3 and references therein). The situation is complicated in this two-dimensional crystal by the strong influences of the substrate, the surface contamination, the effects of static distortions, and phonons.^{4–10} By contrast, investigation technics are rather limited; the main diagnosis relies on the temperature and carrier density (n_c) dependencies of the conductivity. The former is weak for graphene on substrates and attributed to phonons.^{10–12} The latter comes from the dependence of the scattering time $\tau(k_F)$ on wave number which can be varied in a broad range due to efficient electrostatic gate doping. We have listed in Table I the most predicted behaviors for the $\tau(k_F)$ and the corresponding $\sigma(n_c)$ laws.^{13–19} They can be classified in two categories corresponding to a nearly linear density dependence of the conductivity (or $\tau \sim k_F$), or a constant conductivity ($\tau \sim k_F^{-1}$). The former is exemplified by the charge impurity mechanism and the latter by the local impurity model. Intermediate situations can be explained by an admixture of both mechanisms giving rise to a sublinear density dependence of conductivity. Alternatively, sublinearity could be accounted for by a single mechanism, like the Dirac-mass disorder associated with a random lifting of sublattice degeneracy.²³ Indeed, according to Ref. 15, a random Dirac-mass mechanism should give $\tau = \text{Const}$. It translates into a $\sigma \propto \sqrt{n_c}$ dependence of the bulk conductivity, which should not be confused with the $G \propto \sqrt{n_c}$ dependence of a two-terminal conductance in ballistic graphene.^{24,25}

Experimentally a linear dependence of conductivity is reported at low temperature with a tendency to sublinearity at high density. It is well explained by a Boltzmann conductivity $\sigma^{-1}(n_c) = (n_c e \mu + \sigma_0)^{-1} + \rho_s$,⁸ with a mobility $\mu = e v_F \tau / \hbar k_F$, a saturation at ρ_s^{-1} , and a conductivity minimum σ_0 . The weak effect of dielectric environment²⁰ and complementary measurements of the quantum scattering time²² suggest an interpretation in terms of resonant scattering.

In the present work we consider the case of top-gated graphene at room temperature. We investigate scattering using the rf gate admittance. From the in-phase and out-of-phase responses we obtain the thermal averages of the density of states $\rho(E_F)$ and the bulk conductivity $\sigma(E_F)$ as a function of energy $E_F = \hbar k_F v_F$ ($v_F \simeq 10^6$ m/s). We rely on the Einstein relation $\sigma = e^2 \rho D$ to deduce the diffusion constant $D(E_F)$

and the scattering time, $\tau = 2D/v_F^2$. We shall focus on the hole-doped regime, $E_F = -(0-200)$ meV, where we find that τ is energy independent. Finally, we discuss the possible origin of this observation.

II. EXPERIMENTAL PRINCIPLES

In an rf transport experiment, $\rho(E)$ can be obtained from the quantum capacitance $c_Q(E_F) = e^2 \int \rho(E) (-\partial f / \partial E) dE$, where E_F stands now (and below) for the chemical potential. c_Q is the thermal average of $\rho(E)$ and corresponds to the electronic compressibility, $\chi \equiv \partial n / \partial E_F = c_Q / e^2$ where $n = \int \rho(E) f(E) dE$. The finite compressibility is responsible for a chemical contribution ΔE_F in addition to the electrostatic one in the electronic charging energy. For a capacitor charge $q = -e \Delta n$ and bias U , $\Delta E_F = \Delta n / \chi = -eq / c_Q$ adds to the electrostatic term, $-eq / c_{\text{geo}}$, in the total energy $-eU = -eq / c_g$. Here c_{geo} and c_g are the geometrical and total gate capacitance (per unit area) so that one finally has $c_g(E_F)^{-1} = c_{\text{geo}}^{-1} + c_Q(E_F)^{-1}$. The quantum capacitance term is generally negligible in metals ($c_Q \rightarrow \infty$) or in back gated conductors ($c_{\text{geo}} \rightarrow 0$).

Using the previous definition, one can rewrite the Einstein relation as $\sigma = c_q \mathcal{D}$.² $c_Q(E_F)$ can be separated from the constant geometrical capacitance in graphene thanks to its energy dependence.^{26–31} At finite temperature the theoretical expression is²⁶

$$c_Q = \frac{2e^2 k_B T}{\pi (\hbar v_F)^2} \times \ln \left[2 + 2 \cosh \left(\frac{E_F}{k_B T} \right) \right]. \quad (1)$$

Using nanometers thick gate oxides, $c_{\text{geo}} \sim 10$ fF/ μm^2 becomes comparable to the quantum capacitance minimum, $c_Q(0) = 4e^2 k_B T \ln[2] / \pi (\hbar v_F)^2 \simeq 10$ fF/ μm^2 at neutrality and room temperature.

Top-gated graphene offers the possibility to manipulate ac gate currents for dynamical characterization³² which is also useful for technological applications.^{33,34} It has, however, the drawback of a nonlinear $n_c(V_g)$ relation between gate charge and voltage due to the quantum capacitance contribution that complicates the standard analysis. At $T = 0$ in pure graphene one has $n_c = n_{\text{gate}} - n_Q [(1 + 2n_{\text{gate}}/n_Q)^{0.5} - 1]$ where $n_{\text{gate}} = c_{\text{geo}} V_g / e$ (see, e.g., Ref. 2) and $n_Q = \frac{\pi}{2} (c_{\text{geo}} \hbar v_F)^2 / e^4 \simeq 2 \times 10^{11}$ cm⁻² ($c_{\text{geo}} \simeq 10$ fF/ μm^2) entails

TABLE I. Main scattering mechanisms proposed for graphene classified according to the carrier density dependence: Fermi vector dependence of the scattering time $\tau(k_F)$ and carrier density dependence of conductivity $\sigma(n_c)$. For the ripples model, $H \sim 1$ is the exponent of the correlation function for the lattice distortions. The expression for acoustic phonons scattering corresponds to a low temperature limit.

Mechanisms	Scattering time	Conductivity	Ref.
Local impurity	$\tau \sim 1/k_F$	$\sigma \sim \text{Const.}$	13
Local impurity	$\tau \sim \ln k_F/k_F$	$\sigma \sim \ln n_c$	14
Random Dirac-mass	$\tau \sim \text{Const.}$	$\sigma \sim \sqrt{n_c}$	15
Charged impurity	$\tau \sim k_F$	$\sigma \sim n_c$	16
Resonant scattering	$\tau \sim k_F \ln^2(k_F)$	$\sigma \sim n_c \ln^2 n_c$	17
Ripples	$\tau \sim k_F^{(2H-1)}$	$\sigma \sim n_c^H$	18
Acoustic phonons	$\tau \sim k_F^2$	$\sigma \sim n_c^{3/2}$	19

strong deviations from linear $\sigma(n_{\text{gate}})$ behavior. In experiment we shall express the measured quantities directly as a function of the chemical potential E_F using the relation,

$$E_F(V_g) = e(V_g - V_{np}) - \int_{V_{np}}^{V_g} c_Q/(c_{\text{geo}} + c_Q) e dV, \quad (2)$$

where V_{np} is the gate voltage at the neutrality point. Top gating gives in principle the possibility of characterizing charged impurity scattering by observing a cutoff in the Thomas-Fermi screening at wave vectors q_{TF} ($q_{\text{TF}} \gtrsim 1.5 k_F$ for graphene between SiO_2 and AlOx) smaller than a $q_{\text{gate}} = 1/2t_{\text{ox}}$.³⁵ However, with $t_{\text{ox}} \simeq 8$ nm, $q_{\text{gate}} \simeq 6 \times 10^5 \text{ cm}^{-1}$ still remains at the lower end of our investigated wave number range $k_F = 0\text{--}30 \times 10^5 \text{ cm}^{-1}$, where thermal and impurity effects are prominent.

The capacitor geometry of our experiment is described in Fig. 1. We have measured several graphene samples, both in the two-terminal capacitor and three-terminal transistor geometries, obtained by the exfoliation method on a thermally oxidized silicon substrate with a resistivity $\rho \geq 20 \text{ k}\Omega \text{ cm}$. AFM inspection, performed prior to gate deposition, shows a significant roughness of the silicon oxide, which contrasts with the relative smoothness of the area covered by graphene. Data presented here refer to two representative capacitor samples: Samples E9-Zc and C7-F are flakes of dimensions $L \times W \simeq 3 \times 1 \mu\text{m}^2$ (see Fig. 1) and $L \times W = 2 \times 0.6 \mu\text{m}^2$. The use of high resistivity silicon is important to minimize the spurious conductance through the substrate. This parasitic contribution can be very high at microwave frequencies, and effectively shunt the contribution of a small graphene sample. We use palladium for the drain electrode to minimize contact resistance and a gate oxide obtained by multistep oxidation of thin aluminum, for a nominal oxide thickness of about $t_{\text{ox}} \simeq 8$ nm, and finally gold-gate deposition. The distance L_a between the drain and the gate is reduced to $\simeq 200$ nm, i.e., $\sim 6\%$ of the gate length, to minimize the contribution of the access resistance R_a . With a permittivity $\kappa \simeq 7$ for AlOx we estimate $c_{\text{geo}} \simeq 8 \text{ fF}/\mu\text{m}^2$. The device is inserted in a coplanar wave guide used for rf characterization.³²

The samples are measured in an rf probe station at room temperature. Bias tees are used to control the DC gate-drain voltage V_g . The rf scattering parameters are measured

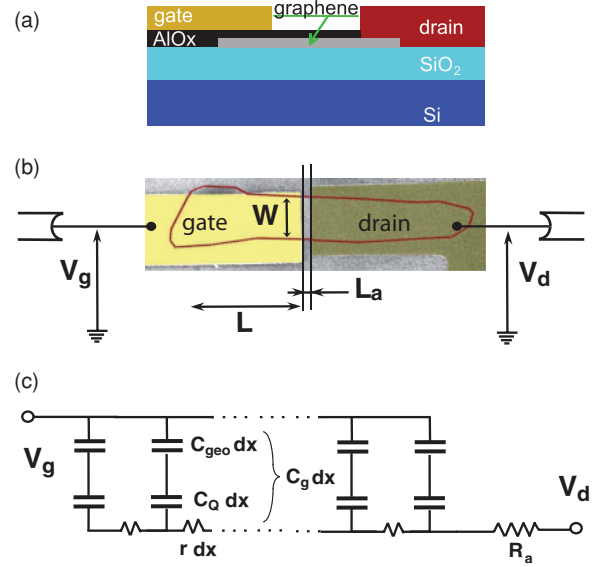


FIG. 1. (Color online) Graphene capacitor made of a monolayer graphene strip coupled to a metallic gate through a thin oxide (thickness $t_{\text{ox}} \simeq 8$ nm, permittivity $\kappa \sim 7$). (a) Sketch of the layout. (b) SEM picture of sample E9-Zc showing the palladium drain, the gold top gate, and the outline of the graphene flake. (c) One-dimensional lumped element description of the graphene capacitor, used for data analysis. It includes a distributed resistance $r = \sigma^{-1}/W$ and capacitance $c = c_g W$ where $c_g = c_{\text{geo}} c_q / (c_{\text{geo}} + c_q)$ is the gate capacitance and c_{geo} (respectively, c_q) its geometrical (respectively, quantum) contributions. R_a is a series access resistance.

with a network analyzer and used to calculate the gate-drain admittance $Y(\omega)$.³⁶ The background contribution, which corresponds to a parallel gate-drain capacitive coupling, $C_0 \simeq 1.8 \text{ fF}$, is measured in an identical but dummy structure and subtracted. Linear response conditions are secured by probing the device well below the thermal noise floor with an excitation voltage $V_{\text{rf}} \sim 1\text{--}10$ mV. We have measured admittance spectra $Y(\omega)$ up to 10 GHz in a gate voltage range $V_g = 0\text{--}1$ V corresponding to average electron and hole densities $n_c = 0\text{--}2 \times 10^{12} \text{ cm}^{-2}$. For a quantitative analysis, we shall concentrate in the following on the hole region where the contact resistance due to chemical hole doping of the palladium can be neglected.^{37,38}

III. EXPERIMENTAL RESULTS AND ANALYSIS

Figure 2 shows typical admittance spectra of sample E9-Zc for three representative gate voltages corresponding to charge neutrality (a), intermediate (b), and large (c) hole concentrations. The purely capacitive response [$\text{Re}(Y) \simeq 0$, $\text{Im}(Y) \simeq j\omega C_g$] is observed at low frequency. Strong deviations from this limit are seen above 1 GHz which are due to finite charge relaxation resistance. Solid lines are fits to the data using a one-dimensional distributed-rc model [Fig. 1(c)], with linear capacitance and resistance $c = c_g W$ and $r = (\sigma W)^{-1}$. The model gives

$$Y(\omega) = j\omega c L \times \left[\frac{\tanh(jqL)}{jqL} \right], \quad (3)$$

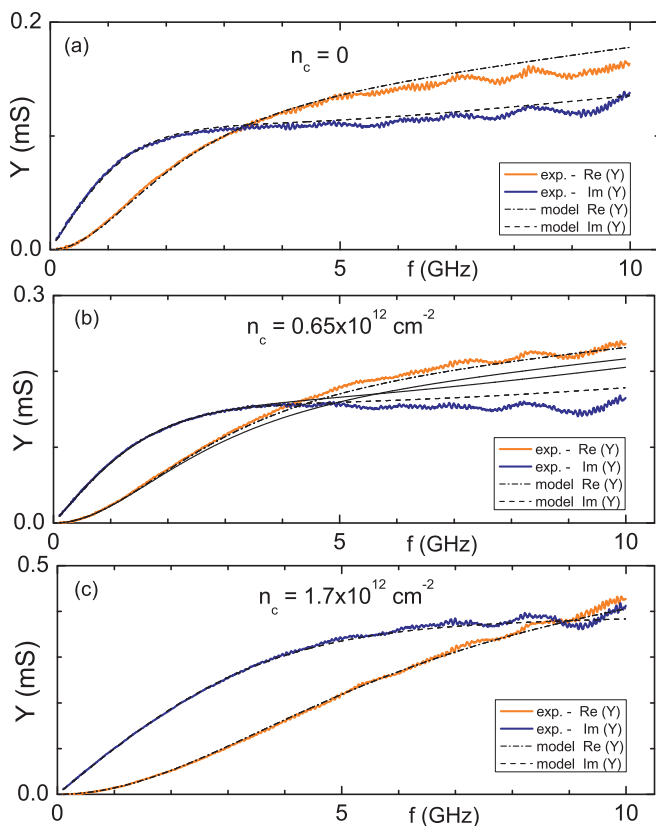


FIG. 2. (Color online) Admittance spectra of a diffusive graphene capacitor (sample E9-Zc) for three gate voltages $V_g = (0.68, 0.48, 0.18)$ V for the (a), (b), and (c) panels. The signature of skin effect [i.e., $\text{Re}(Y) \simeq \text{Im}(Y) \propto \sqrt{f}$] is seen at neutrality ($V_g = 0.68$ V) in panel (a) due to a larger resistivity. At all investigated densities, the admittance spectra are accurately fitted using the one-dimensional strip-line model and a small access resistance $R_a = 0.15R_g$. We find, respectively, $(C_g, R_g) = (12.5, 4.18), (14.0, 2.64), (16.0, 1.28)$ (fF, k Ω). For comparison we have added in panel (b) the fit obtained with $R_a = 0$ (dashed lines).

where $q = (-jrc\omega)^{0.5}$ ($rc = c_g/\sigma$) is the wave number of the probing rf field in the capacitor. We stress that the one-dimensional (1D) character of the rf probing field penetrating the capacitor should not be confused with the two-dimensional electronic diffusion probed by the rf field. This 1D field distribution is a powerful simplification in the analysis of the capacitor response as compared to the more complicated two-dimensional current distribution in a high-frequency drain-source conductivity measurement.

The low frequency development,

$$Y(\omega) \simeq j\omega C_g + R_g(\omega C_g)^2 + o(\omega^3), \quad (4)$$

gives the equivalent rc-circuit description which corresponds to an homogeneous charge distribution with a capacitance, $C_g = c_g LW$, and a resistance, $R_g = \sigma^{-1}L/3W$. Equation (4) will be used for the experimental determination of c_g and σ .

The high-frequency limit of Eq. (3) corresponds to an inhomogeneous charge distribution along the capacitor length cor-

responding to a penetration over a depth, $\delta = (2\sigma/c_g\omega)^{0.5} \ll L$, from the capacitor drain edge. The asymptotic admittance,

$$Y = \frac{(1+J)}{2} \sqrt{2W^2\sigma c_g\omega}, \quad (5)$$

has a constant phase $\arg(Y) = \pi/4$ and a $\sqrt{\omega}$ -dependent modulus. It is markedly different from that of an rc circuit with a frequency-independent charging resistance, such as a contact resistance R_c which gives $\text{Re}(Y) \rightarrow R_c^{-1}$ and $\text{Im}(Y) \rightarrow 0$. The observation of the asymptotic skin effect regime given by Eq. (5) will be taken as a proof that the measured conductivity is the bulk contribution equivalent to that measured in a four-terminal dc experiment.

The crossing of real and imaginary parts at $\omega_c \simeq \frac{\pi^2}{2}\sigma/c_g L^2$ defines the cutoff frequency of the capacitor. It can be expressed as the sum $\omega_c = \frac{\pi^2}{2}\sigma/c_{\text{geo}}L^2 + \frac{\pi^2}{2}D/L^2$. The first term is the cutoff of a classical capacitor; the second is a mesoscopic correction due to the finite density of state. The correction dominates at charge neutrality and low temperature in top gated devices ($\sigma/c_{\text{geo}}D = e^2\rho(E_F)/c_{\text{geo}} \rightarrow 0$). One can note that in these conditions, ω_c becomes a rather direct measurement of the diffusion constant, which is a further example of a mesoscopic effect where a microscopic property (the Thouless energy $\hbar D/L^2$) shows up in a macroscopic measurement (the cutoff frequency of a capacitor).

As shown in Fig. 2, both regimes are observed in experiment with a cutoff that increases with carrier density and levels off at 3 GHz at neutrality (see Fig. 3). In particular, the full spectrum of Eq. (3) can be verified at low hole doping demonstrating the prominent contribution of diffusion in charge relaxation. In the analysis we have also included the effect of the access region as a serial resistance R_a . We approximate $R_a \simeq \sigma^{-1}L_a/W \sim 0.15R_g$. The inclusion of R_a results in a small correction in the investigated frequency range, but becomes prominent at very high frequency with an asymptotic limit $Y \rightarrow R_a^{-1}$ and $\arg(Y) \rightarrow 0$ for $\delta \ll L_a$. In order to quantify the effect of R_a we have added in Fig. 2(b) (solid line) the spectrum

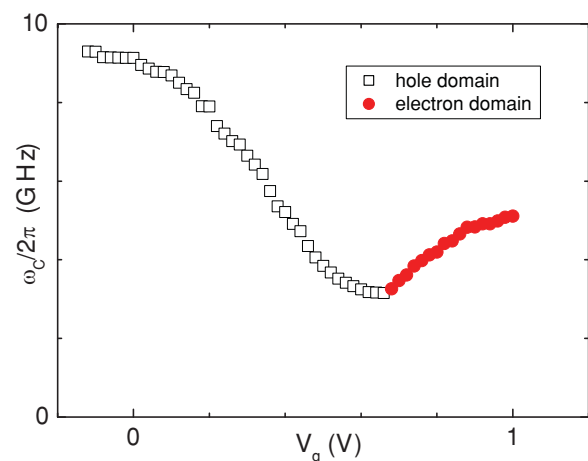


FIG. 3. (Color online) Gate voltage dependence of the cutoff frequency $\omega_c/2\pi$ of sample E9-Zc estimated by the crossing of the real and imaginary parts of the admittance spectrum $Y(\omega)$. The hole region shows a trend to saturation at neutrality ($V_{np} \simeq 0.67$ V) from which we deduce an (under-) estimate of the diffusion constant $D(V_{np}) \lesssim L^2\omega_c/5 \simeq 400$ cm²/s.

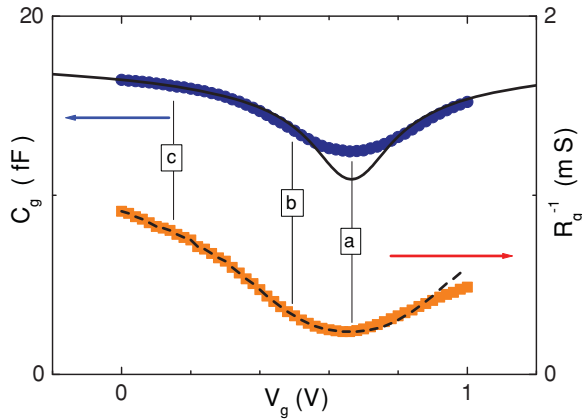


FIG. 4. (Color online) Gate capacitance C_g and charge relaxation conductance R_g^{-1} of sample E9-Zc deduced from fits of the admittance spectra with Eq. (3). Labels refer to the admittance spectra in Fig. 2 for hole densities $n_c = (0, 0.65, 1.7) \times 10^{12} \text{ cm}^{-2}$. The solid line is a theoretical fit to the data using Eq. (1) with $C_{\text{geo}} = 19.2 \text{ fF}$. The dashed line (lower curve) is a guide for the eye representing an electron-hole symmetric resistance fitted to the hole values.

obtained taking $R_a = 0$. Sample C7-F shows similar spectra with, however, a higher cutoff due to larger diffusion constant and smaller gate length.

From the fits of the full set of admittance spectra we obtain the gate capacitance C_g and the conductance R_g^{-1} as a function of gate voltage as displayed in Fig. 4. The capacitance and the conductance show a broad minimum at $V_g^{np} = 0.67 \text{ V}$ (sample E9-Zc) and $V_g^{np} = -0.07 \text{ V}$ (sample C7-F) which we have identified as the charge neutrality point, shifted from zero by chemical doping. The solid line is the theoretical expectation for $C_g^{-1}(V_g)$ with $C_{\text{geo}} = \text{Const.}$ and the finite temperature expression in Eq. (1). Deviation from theory at low carrier density in Fig. 4 is likely due to inhomogeneity in the chemical doping which is not taken into account in Eq. (1). Indeed, it is more pronounced in sample E9-Zc which has a larger doping. The fit at large density gives an accurate determination of the geometrical capacitance $c_{\text{geo}} = 6.4 \pm 0.5 \text{ fF } \mu\text{m}^{-2}$ (sample E9-Zc) and $c_{\text{geo}} = 5.9 \pm 0.5 \text{ fF } \mu\text{m}^{-2}$ (sample C7-F) in agreement with the rough estimates from geometry. In the following C_{geo}^{-1} is subtracted from C_g^{-1} to obtain C_Q . R_g shows an excess at large electron density ($V_g \sim 1 \text{ V}$) which can be estimated from the difference of the measured resistance to the electron-hole symmetric expectation (dotted guide line in Fig. 4). We assign this difference to the contact resistance due to the formation of a p - n junction in the access region with $R_c/W \lesssim 300 \text{ Ohms}/\mu\text{m}$. This value is consistent with theoretical expectation and experiment.³⁸ We also checked that the effect of R_c is also seen in the corresponding admittance spectra (not shown) with an increase in the series resistance at large V_g . For this reason the electron regime is thereafter disregarded. The gate conductance R_g^{-1} depicted in Fig. 4 is similar to the drain source conductance measured in graphene transistors of similar size. The order of magnitude of the mobility ($\mu \simeq 4500 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at $n_c \simeq 10^{12} \text{ cm}^{-2}$) is also typical of room temperature behavior.⁷

Relying on the overall good quantitative agreement of the admittance spectra with the 1D rf field model and that of the

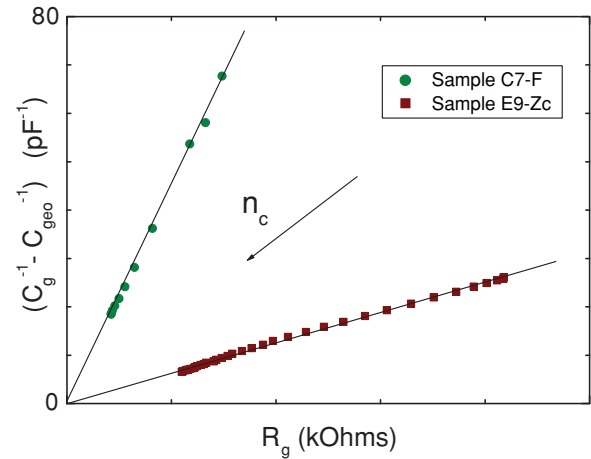


FIG. 5. (Color online) Inverse gate capacitance as function of gate resistance. The geometrical contribution $1/C_{\text{geo}}$ is subtracted to isolate the quantum capacitance term. Data correspond to the hole conduction regime where contribution from the contact resistance can be neglected. The observed linear dependencies indicate an energy-independent diffusion constant. The slopes ω^* give $D = L^2/3\omega^* \simeq 180 \text{ cm}^2 \text{ s}^{-1}$ (sample E9-Zc) and $D \simeq 540 \text{ cm}^2 \text{ s}^{-1}$ (sample C7-F).

gate voltage dependence of the capacitance, we proceed below to the quantitative analysis and deduce in Fig. 5 the diffusion constant D from the ratio $\omega^* = L^2/3D$ of the measured quantum capacitance C_Q to the charging resistance R_g . In both cases we observe a linear dependence $\sigma(c_Q)$ which corresponds to an energy-independent diffusion constant $D \simeq 180 \text{ cm}^2/\text{s}$ (sample E9-Zc) and $D \simeq 540 \text{ cm}^2/\text{s}$ (sample C7-F) and scattering times $\tau(k_F) = 2D/v_F^2$. This corresponds to scattering lengths $v_F \tau \simeq 40 \text{ nm}$ and $\simeq 100 \text{ nm}$ in agreement with standard estimates.²²

Using the experimental $c_Q(V_g)$ and Eq. (2), we can plot $c_Q(E_F)$ and $\sigma(E_F)$ in Fig. 6. Small deviations from the theoretical estimate for c_Q in Eq. (1) are observed in both samples which are due to experimental uncertainties and disorder contribution. Uncertainties are yet too large for a quantitative estimate of the disorder contribution. The precision of the high-frequency compressibility measurement can be increased by using larger flakes (more accurate de-embedding), thinner gate oxide (smaller electrostatic gate impedance), and working at low temperatures (larger contrast in c_Q). The conductivity data merely follow the density of states reflecting the fact that $D = \text{Const.}$

IV. DISCUSSION

We have observed a strong sublinear dependence of conductivity in a broad carrier density range at room temperature. Direct comparison between conductivity and compressibility in the capacitor geometry at room temperature shows that this sublinear behavior extends to the low density limit and is well described by an energy-independent scattering time or equivalently $\sigma \propto \sqrt{n_c}$. This result deviates from standard low temperature behavior ($\tau \sim k_F$) explained by charged impurity, resonant scattering models, or standard ripples. It could be accounted in a ripple scenario by taking a peculiar value for the correlation exponent, $2H = 3/2$,

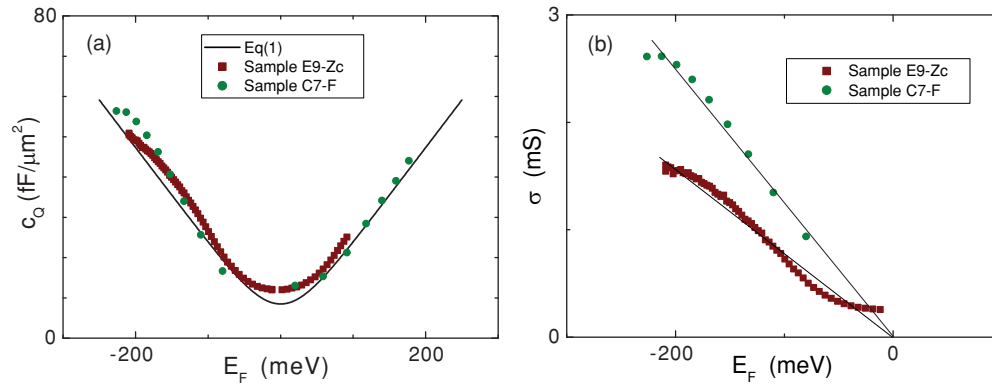


FIG. 6. (Color online) Chemical potential dependence of the quantum capacitance (a) and the conductivity (b) deduced from data in Fig. 4 using Eq. (2).

which deviates from standard expectation $H \simeq 1$.^{2,18} Another possible mechanism, less discussed in the literature, would be Dirac-mass disorder proposed in Ref. 15 and characterized, according to a numerical calculation, by $\sigma \propto E_F$ ($\tau = \text{Const.}$).

In conclusion, our rf admittance measurement of graphene capacitors provides new insight into the energy dependence of the transport scattering time. We report on a new behavior in top-gated graphene at room temperature characterized by a density-independent scattering time. Our experiment gives also access to the electronic compressibility via the quantum capacitance in fair agreement with theory. It can be implemented at low temperatures using a cryogenic probe station and used to characterize the different scattering mechanisms

in more detail. Our study may also prove useful for the design of high-frequency graphene transistors.

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