Ballistic transport at room temperature in micrometer-size graphite flakes

S. Dusari,¹ J. Barzola-Quiquia,¹ P. Esquinazi,^{1,*} and N. García²

¹Division of Superconductivity and Magnetism, Institut für Experimentelle Physik II, Universität Leipzig,

Linnéstraße 5, D-04103 Leipzig, Germany

²Laboratorio de Física de Sistemas Pequeños y Nanotecnología, Consejo Superior de Investigaciones Científicas, E-28006 Madrid, Spain (Received 28 September 2010; revised manuscript received 19 January 2011; published 9 March 2011)

The intrinsic values of the carriers mobility and density of the graphene layers inside graphite, the well-known structure built on these layers in the Bernal stacking configuration, are not well known mainly because most of the research was done in rather bulk samples where lattice defects hide their intrinsic values. By measuring the electrical resistance through microfabricated constrictions in micrometer small graphite flakes of a few tens of nanometers thickness we studied the ballistic behavior of the carriers. We found that the carriers' mean-free path is $\geq 1 \ \mu$ m large with a mobility $\mu \simeq 6 \times 10^6 \ \text{cm}^2/\text{Vs}$ and a carrier density $n \simeq 7 \times 10^8 \ \text{cm}^{-2}$ per graphene layer at room temperature. These distinctive transport and ballistic properties have important implications for understanding the values obtained in single graphene and in graphite as well as for implementing this last in nanoelectronic devices.

DOI: 10.1103/PhysRevB.83.125402

PACS number(s): 72.15.Lh, 72.80.Cw, 73.23.Ad

I. INTRODUCTION

The existence of massless-like quasiparticles (Dirac fermions) found in the quasi-two-dimensional graphite structure¹⁻³ and in single graphene layers^{4,5} enhanced enormously the interest in these materials, implying not only the start of a qualitative new physics⁶ but also the possibility of nanotechnological improvements.^{7,8} The search for highest-carrier mobility together with lowest-carrier density in graphene remains a main research issue of this twodimensional model system also because of their implications in future applications in nanoelectronics. It is nowadays known, however, that graphene properties can be sensitively affected by the environment, particularly by the substrate^{9,10} and by disorder.¹¹ This fact is supported by experiments done on suspended graphene layers where mobility approaching $\sim 5 \times 10^5$ cm²/Vs at carrier densities $n \sim 10^9$ cm⁻² at T < 30 K has been reached.^{12,13} Nevertheless, the expectations on the use of single graphene layer (SGL) on substrates are high⁷ and in spite of the detrimental substrate influence, SGL exhibits ballistic transport in the 100 nm range at room temperature¹⁴ and in the $\sim 1 \,\mu m$ range at very low temperatures.¹⁵

By measuring the resistance and its ballistic characteristics we studied the transport behavior of the carriers of the graphene layers inside the graphite structure. This study allows us to obtain the carriers' values for the mean-free path, carrier density, and mobility. Due to the natural packing of the graphene layers inside graphite we expect not only a natural shielding from the environmental influence but they should be actually more ideal than SGL standing alone or on a substrate. Although some experiments have been done in graphene bilayers, the actual intrinsic values of these transport parameters for the graphite structure remain still not well known simply because they are very sensitive to lattice defects,¹⁶ grain boundaries,^{17,18} and internal interfaces,¹⁹ which in general trigger high-carrier density with low mobility. Recent results obtained on bulk oriented pyrolytic graphite samples indicate ballistic transport in the micrometer range at T < 10 K with a very low-carrier density $n < 10^9$ cm⁻² and huge mobility $\mu > 10^6$ cm²/Vs.¹⁸

II. EXPERIMENTAL DETAILS AND USED METHOD TO OBTAIN THE MEAN-FREE PATH

The graphite flakes we report here were obtained by exfoliation of a highly oriented pyrolytic graphite sample of ZYA grade (rocking curve width 0.4°). Using an ultrasonic technique we obtained several flakes that were selected by measuring the resistance, its temperature dependence and micro-Raman signals and taking into account the overall shape and dimension of the sample, its surface and thickness. The Au contacts for longitudinal-resistance measurements were prepared using electron beam lithography, see Fig. 1.

The measurement of the carrier mean-free path ℓ is not straightforward and, in general, the value obtained depends on several other not well-known parameters within the selected transport model, usually based on a Drude-Boltzmann approach. However, in case of ballistic conduction, there is a transparent method to obtain ℓ without adjustable parameters, successfully used for macroscopic graphite samples as described in Ref. 18. The method is based on the measurement of the longitudinal resistance as a function of the geometry of a constriction located between the voltage electrodes (see Fig. 1). We prepared these constrictions with the focused-ion beam of a dual-beam microscope. We avoided the modification of the crystalline structure of the samples due to the ion beam spread by protecting them with a negative-electron beam resist (AR-N 7500) of \sim 300 nm thickness, a method successfully tested in graphite and described in Ref. 20.

As shown in Ref. 18 the resistance of a graphite sample of width Ω , thickness *t*, with a constriction of size *W* and length *L* connecting two half-parts of resistivity ρ is given by

$$R(T) = a \frac{\pi \rho(T)}{4Wt} \ell(T) + a \left. \frac{2\rho(T)\gamma(\kappa)\ln(\Omega/W)}{\pi t} \right|_{W < \Omega} + \frac{\rho(T)L}{Wt}.$$
(1)

At the right-hand side (rhs) of Eq. (1) the first term corresponds to the ballistic Knudsen-Sharvin resistance¹⁸; the second, logarithmic term to the ohmic, spreading resistance



FIG. 1. (Color online) Scanning electron microscope images of the two samples discussed here with the four electrodes and with one of the constrictions in between. The graphite flakes (white lines indicate their perimeter) cannot be seen directly because of the top 300 nm resin layer used to shield them from the Ga^+ focused ion beam. Two upper pictures correspond to sample A and bottom to sample B.

in two-dimensions with the smooth function $\gamma(\kappa = W/\ell) \simeq 1 - 0.33/\cosh(0.1\kappa) = 0.67, \ldots, 1$ for $\kappa = 0, \ldots, \infty$.²¹ The logarithmic dependence on the constriction width of this ohmic, diffusive contribution is due to the quasi-two-dimensionality of the transport in graphite¹⁸ and supports the assumption of weakly interacting graphene layers inside the sample.

The last term in Eq. (1) is due to the ohmic resistance of the constriction tube itself. The constant *a* takes care of the influence of the sample shape, the topology, and the location of the electrodes in the sample. It is equal to 1 for the geometry used in sample A where the voltage electrodes are deposited through the whole sample width and their distance is $\sim \Omega \gg$ *W*. This can be verified from the measurement of the resistance as a function of *W*, as it is shown below. To keep the third term, the ohmic contribution of the constriction, small enough we prepared constrictions with length $L < 0.4 \ \mu\text{m}$. The results presented here correspond to two samples, samples A and B with different geometry and resistivity. Sample A (B) had a size (distance between voltage electrodes × width × thickness) of $12.7 \times 16 \times 0.015 \ \mu\text{m}^3$ ($2.7 \times 9.2 \times 0.040 \ \mu\text{m}^3$) and a resistivity $\rho(300 \ \text{K}) = 89 \ \mu\Omega\text{cm}$ (18 $\mu\Omega\text{cm}$), see Fig. 1.

III. RESULTS AND DISCUSSION

The simplest and direct way to check the ballistic contribution and obtain the mean-free path (without further adjustable parameter) is just measuring the resistance *R* as a function of the constriction width in combination with Eq. (1). The results for sample A at two temperatures are shown in Fig. 2. In that figure one recognizes that for $W \leq 2 \mu m$ the ballistic contribution overwhelms the ohmic ones, see Eq. (1),



FIG. 2. (Color online) Measured resistance for sample A as a function of the constriction width W at (a) 60 K and (b) 250 K. The point with the largest W corresponds to the virgin sample without a constriction. The different lines correspond to the first ballistic term (dashed line) and the ohmic [second (dotted line) and third (dashed-dotted line) contributions in Eq. (1)] and the continuous line to the addition of the three. The only free parameter is the mean-free path ℓ , see Eq. (1). For (a) the continuous line is calculated with $\ell = 1.2 \,\mu\text{m}$ and for (b) $\ell = 0.8 \,\mu\text{m}$.

indicating that the mean-free path should be of this order. The theoretical lines in Fig. 2 were obtained using $\ell = 1.2 \,\mu m$ and 0.8 μm at 60 K and 250 K, respectively. We estimate an error of ~35% for these values determined by the errors in the measurement of the sample and constriction geometry. We can calculate now the Fermi wavelength per graphene layer using the relation

$$\lambda_F = 2\pi e^2 N_s \rho \ell / ht \tag{2}$$

with N_s the number of graphene layers in the sample. For sample A we obtain then $\lambda_F = 0.5(0.8) \pm 0.25 \,\mu\text{m}$ at 250 K (60 K).

In case λ_F is larger than the constriction size, the ballistic contribution to the resistance is better described by the inverse of a sum of an energy *E*-dependent and transverse wave vectors q_n -dependent transmission probabilities T_n , where $n = 0, \pm 1, \pm 2, \ldots^{22}$ The maximum possible *n* is determined by the constriction width *W*, decreasing the smaller *W*. In this case the increase in resistance is expected to show an oscillatory behavior as a function of *W* or $\lambda_F^{23,24}$ as observed experimentally in bismuth (Bi) nanowires²⁵ as well as in GaAs devices.^{26,27}

Note that the distance between voltage electrodes in sample A is larger than the obtained ℓ . The larger the sample the



FIG. 3. (Color online) Normalized resistance for sample B vs. constriction width W; note the semilogarithmic scale. (a) Data at 10 K. The line with steps is obtained dividing the ballistic term in Eq. (1) by $(\lambda_F/2W)$ trunc $(2W/\lambda_F)$ with parameters $\ell = 2.7 \,\mu\text{m}$ and $\lambda_F = 1.5 \,\mu\text{m}$. The continuous line is obtained multiplying the ballistic term in Eq. (1) by the exponential function $\exp(\lambda_F/2W)$. The dotted line follows Eq. (1) with $\ell = 2.7 \,\mu\text{m}$. (b) The same as in (a) but at 300 K. The used parameters are $\lambda_F = 1.0 \,\mu\text{m}$ and $\ell = 2.2 \,\mu\text{m}$. The dotted stepped function is obtained using the same λ_F but with a smaller $\ell = 1.3 \,\mu\text{m}$.

larger is the probability to have defective regions with larger carrier concentration and smaller mean-free path within the voltage electrodes.¹⁶ Therefore we repeated the experiment with sample B that shows lower resistivity and with a smaller voltage-electrode distance, see Fig. 1. Figure 3 shows the measured resistance normalized by its value at a constriction $W = 3 \mu m$; in this way we pay attention to the huge relative increase decreasing W and we need neither the absolute value of ρ nor of a to compare the data with theory.

In Fig. 3 one realizes that for sample B Eq. (1) does not describe the experimental data even assuming the largest possible mean-free path equal to the voltage-electrode distance of 2.7 μ m. The data can be reasonably well fitted dividing the ballistic term in Eq. (1) by the function trunc $(2W/\lambda_F)\lambda_F/2W$, which generates steps whenever the constriction width $W \simeq i\lambda/2$ with *i* an integer. From the fits we obtain the parameters $\lambda_F = 1.0(1.5) \mu m$ and $\ell = 2.2(2.7) \pm 0.3 \mu m$ at 300 (10) K, see Fig. 3. Using other values of ℓ , for example $\ell = 1.3 \mu m$, see Fig. 3, the function does not fit the data indicating indeed that the carriers behave ballistically between the voltage electrodes, leaving actually λ_F the only free parameter. The ballistic analytical function we use resembles the theoretical results with similar steps obtained in Ref. 24 where the conductance vs. *W* was calculated numerically for a SLG with an electrostatically potential landscape that resembles a constriction. An analytical average value or envelope of this stepped function is obtained replacing the truncation function by $\exp(-\lambda_F/2W)$, see Fig. 3. This exponential function represents the impossibility of an electron to propagate in the constriction when $W < \lambda_F/2$, as also occurs for the propagation of light in a tube.

The data appear to be better fitted by the stepped function than with the exponential one. The important result obtained for sample B is the huge increase of the resistance for $W < 2 \mu m$ indicating clearly a larger ℓ . The larger ℓ in sample B to the one obtained in sample A is compatible with the measured resistivity difference.

As a further proof that the huge increase of the resistance decreasing the constriction width in sample B is due to the ballistic contribution and not due to, e.g., a possible disorder produced by the ion beam on the graphite structure, we show in Fig. 4 the temperature dependence of the measured resistance without and with the different constriction widths. We observe that in spite of the huge resistance increase the temperature dependence remains similar. The small differences in the temperature dependence of the resistance, decreasing slightly more at T > 80 K at large values of W than at the smallest W, e.g., $R(2)/R(300) \simeq 1.6$ (sample without constrictions) to $\simeq 1.45$ for $W = 0.6 \,\mu \text{m}$ (see Fig. 4) can be explained taking into account that the ballistic contribution [first term in the rhs of Eq. (1)] is weakly T dependent. At low values of W the ohmic contributions start to be negligible compared with the ballistic one (see Fig. 2) and therefore the temperature dependence of R(T) slightly reduces decreasing W, see Fig. 4.



FIG. 4. (Color online) Resistance of sample B vs. temperature at different constriction widths and without constriction $[(+), \Omega]$ is the total sample width, i.e., data of the sample without constriction].



FIG. 5. Mobility vs. carrier density obtained for samples A and B. The points are obtained between 300 K and 10 K (60 K for sample A). The line corresponds to the data of a suspended SLG at 20 K from Ref. 12.

As shown in Ref. 18 the temperature dependence of R(T, W) can be used now to obtain $\lambda_F(T)$ and the mobility per graphene layer, this last given by $\mu(T) = (e/h)\lambda_F(T)\ell(T)$. Since the density of carriers per graphene layer can be calculated from $n = 2\pi/\lambda_F^2$ we show in Fig. 5 the mobility vs. carrier density for the two samples and compare them with data from literature for suspended SLG. From these results we clearly recognize the much larger mobility and smaller density of carrier for the thin graphite flakes, supporting the view that the graphene layers within graphite are of better quality than SLG and with a smaller carrier density. Obviously sample B is not free from defects and therefore we expect that the obtained values might still be improved in ideal, defect-free graphite structures.

The rather weak temperature dependence of n(T) (or λ_F) obtained for the here reported samples is a nontrivial result that deserves a comment. For the simple case of a linear dispersion relation we expect that the $\lambda_F(T) \propto 1/T$ and therefore $n(T) \propto T^2$ or $\propto T$ for a quadratic dispersion relation. The data obtained indicate that the carrier density increases at most a factor of ten between 10 K and 300 K. We may speculate the reason for this behavior, either by comparing our results with those found in Bi and a possible band splitting or the existence of an intrinsic energy gap in graphite.

Firstly, we note that both materials, graphite and Bi, have very small carrier densities with small anisotropic effective carrier mass. For a long time it was unclear why there was such a difference in the carriers' mean-free path between the two structures. While the carriers in Bi show $\ell(300 \text{ K}) > 2 \,\mu\text{m}$,^{28,29} the values reported for graphite in literature are more than one order of magnitude smaller at the same temperature. The results of this work finally put an end to this apparent difference showing that also in graphite the carriers' mean-free path can be micrometer large with a low carrier density.

The large λ_F of the order of the sample dimensions may affect the band structure. For $\lambda_F \sim 1 \,\mu$ m, and for the typical sample dimensions we report here only the first five quantized wave vectors in reciprocal space are occupied ($E_F \sim 4 \text{ meV}$) indicating that the usual continuous approximation of the band structure is inappropriate. As in Bi nanowires we expect that quantum confinement affects the electronic band structure and a split into sub-bands can occur.³⁰ It is interesting to note that the temperature dependence of the resistivity of our samples, see Fig. 4, is basically the same as for Bi nanowires of diameters $\phi < 70 \text{ nm.}^{30}$ Therefore, it may be possible that the carriers in the several micrometers-small graphite samples fill partially a narrow band with energy gap of the order of $\sim 10 \text{ meV}$, preventing a simple thermally activated excitation of the carriers to the conduction band.

Because macroscopic graphite samples have a much larger density of defects and therefore a larger carrier density $[n(T) \gg$ 1 K) $\gtrsim 10^{11} \text{ cm}^{-2}$ per graphene layer] than our samples,¹⁸ it appears plausible that the temperature behavior of the resistance observed here cannot be seen in bulk HOPG. Experimental evidence for the influence of interfaces to the transport properties of HOPG was reported recently¹⁹ supporting this statement. It remains unclear what we expect to happen in ideal graphene. The reported data in literature were taken mostly for samples with larger carrier density than in our samples. Therefore, we believe that one cannot clearly answer yet on the existence, or not, of an energy gap in ideal graphene (experiments at carrier concentration $<10^8$ cm⁻² were not yet reported). At such low-carrier densities, as it appears to manifest in graphite, electron correlations and possible localization effects should be considered. Electron interactions are large and for a small-enough carrier density, the expected screening will be very weak promoting therefore the existence of an energy gap. This is what it is observed in Monte Carlo simulations for the unscreened Coulomb interaction in graphene with Dirac flavor $N_s = 2$, see Ref. 31.

The obtained mobility in our thin several micrometers-small graphite samples is two orders of magnitude larger, with a carrier density three orders of magnitude smaller than those measured in bulk samples, see, e.g., Ref. 32, indicating that macroscopic samples do not provide necessarily the intrinsic properties of graphite due in part to the large density of lattice defects.¹⁶ The small carrier density obtained here, in agreement with the main conclusion from Ref. 16, provides us with a further important hint, namely that the coupling constants as well as the whole band structure obtained using the Slonczewski, Weiss, and McClure (SWM) model for graphite samples assuming *intrinsic* carrier densities at least 10² times larger (see, e.g., Ref. 32) than those obtained in this work, should be reconsidered.

The ballistic behavior obtained here with several micrometers-large mean-free path and low-carrier density was further verified by magnetoresistance and Hall effect measurements and by the observation of Aharonov-Bohm oscillations in the magnetoresistance. The magnetoresistance for fields normal to the graphene planes systematically decreases decreasing the constriction width, starting already with the largest *W* as shown in Fig. 6 for sample A (similar behavior is obtained for sample B), as observed in bulk HOPG



FIG. 6. (Color online) Magnetoresistance vs. magnetic field applied normally to the main surface of sample A for different constriction widths and at constant temperature of 250 K. The clear reduction of the magnetoresistance decreasing W supports the existence of a mean-free path of the order of several microns.

samples but at lower temperatures.¹⁷ This behavior indicates that $\ell \gtrsim 1 \,\mu\text{m}$ up to room temperature. From the data shown in Fig. 6 one realizes also that there is no Shubnikov–de Haas

*esquin@physik.uni-leipzig.de

- ¹I. A. Luk'yanchuk and Y. Kopelevich, Phys. Rev. Lett. **93**, 166402 (2004).
- ²G. Li and E. Y. Andrei, Nat. Phys. 3, 623 (2007).
- ³M. Orlita, C. Faugeras, P. Plochicka, P. Neugebauer, G. Martinez, D. K. Maude, A.-L. Barra, M. Sprinkle, C. Berger, W. A. de Herr, and M. Potemski, Phys. Rev. Lett. **101**, 267601 (2008).
- ⁴K. S. Novoselov, A. K. Geim, S. V. Morozov, S. V. Dubonos, Y. Zhang, and D. Jiang, Nature (London) **438**, 197 (2005).
- ⁵Y. Zhang, Y.-W. Tan, H. Störmer, and P. Kim, Nature (London) **438**, 201 (2005).
- ⁶A. H. C. Neto, F. Guinea, N. M. R. Peres, K. S. Novoselov, and A. K. Geim, Rev. Mod. Phys. **81**, 109 (2009).
- ⁷A. K. Geim, Science **324**, 1530 (2009).
- ⁸Y. Ouyang, H. Dai, and J. Guo, Nano Res. **3**, 8 (2010).
- ⁹J. Sabio, C. Seoánez, S. Fratini, F. Guinea, A. H. C. Neto, and F. Sols, Phys. Rev. B **77**, 195409 (2008).
- ¹⁰N. García, Z. Yan, A. Ballestar, J. Barzola Quiquia, F. Bern, and P. Esquinazi, J. Phys. Condens. Matter **22**, 045002 (2010).
- ¹¹S. V. Morozov, K. S. Novoselov, M. I. Katsnelson, F. Schedin, D. C. Elias, J. A. Jaszczak, and A. K. Geim1, Phys. Rev. Lett. 100, 016602 (2008).
- ¹²X. Du, I. Skachko, A. Barker, and E. Y. Andrei, Nature Nanotech. **3**, 491 (2008).

(SdH) oscillations in clear contrast to samples where the carrier density is $\gtrsim 10^{12}$ cm⁻². This absence of SdH oscillations, following the same reasoning as in Ref. 16, indicates that the main matrix of the sample has a Fermi wavelength $\lambda_F \sim 1 \,\mu$ m much larger than the cyclotron radius (at least for fields above 0.1 T), in agreement with the obtained results from the constriction width dependence.

IV. FINAL REMARKS

The field dependence of the Hall resistance, as well as its temperature dependence in similar graphite flakes as presented in this work, deviates clearly from measurements in bulk graphite samples, see, e.g., Ref. 33. Although the calculation of the carrier density through the Hall effect in semimetals due to the electron and hole contributions is nonsimple, the obtained results support not only the existence of the low-carrier density but also the weak temperature dependence of *n*. Finally, for fields parallel to the graphene planes and input current the magnetoresistance shows pronounced Aharonov-Bohm oscillations, similar to that found in Bi nanowires³⁴ and topological insulators,³⁵ demonstrating the coherent propagation of electrons around a length of several micrometers up to temperatures $T \sim 250$ K.³⁶

ACKNOWLEDGMENTS

We thank H. Peredo for technical support in the Hall effect measurements. This work is supported by the Deutsche Forschungsgemeinschaft under contract no. DFG ES 86/16-1; S.D. is supported by the Graduate School of Natural Sciences "BuildMoNa" of the University of Leipzig.

- ¹³K. I. Bolotin, K. J. Sikes, Z. Jiang, M. Klima, G. Fudenberg, J. Hone, P. Kim, and H. L. Stormer, Solid State Commun. **146**, 351 (2008).
- ¹⁴Y.-M. Lin, K. A. Jenkins, A. Valdes-Garcia, J. P. Small, D. B. Farmer, and P. Avouris, Nano Lett. 9, 422 (2009).
- ¹⁵F. Miao, S. Wijeratne, Y. Zhang, U. C. Coskun, W. Bao, and C. N. Lau, Science **317**, 1530 (2007).
- ¹⁶A. Arndt, D. Spoddig, P. Esquinazi, J. Barzola Quiquia, S. Dusari, and T. Butz, Phys. Rev. B 80, 195402 (2009).
- ¹⁷J. C. González, M. Muñoz, N. García, J. Barzola Quiquia, D. Spoddig, K. Schindler, and P. Esquinazi, Phys. Rev. Lett. 99, 216601 (2007).
- ¹⁸N. García, P. Esquinazi, J. Barzola Quiquia, B. Ming, and D. Spoddig, Phys. Rev. B 78, 035413 (2008).
- ¹⁹J. Barzola-Quiquia, J.-L. Yao, P. Rödiger, K. Schindler, and P. Esquinazi, Phys. Status Solidi A 205, 2924 (2008).
- ²⁰J. Barzola-Quiquia, S. Dusari, G. Bridoux, F. Bern, A. Molle, and P. Esquinazi, Nanotechnology **21**, 145306 (2010).
- ²¹G. Wexler, Proc. Phys. Soc. London 89, 927 (1966).
- ²²T. Stauber, N. M. R. Peres, and F. Guinea, Phys. Rev. B **76**, 205423 (2007).
- ²³N. García and L. Escapa, Appl. Phys. Lett. 54, 1418 (1989).
- ²⁴I. Snyman, J. Tworzydło, and C. W. J. Beenakker, Phys. Rev. B 78, 045118 (2008).

- ²⁵J. L. Costa-Krämer, N. García, and H. Olin, Phys. Rev. Lett. 78, 4990 (1997).
- ²⁶B. J. van Wees, H. van Houten, C. W. J. Beenakker, J. G. Williamson, L. P. Kouwenhoven, D. van der Marel, and C. T. Foxon, Phys. Rev. Lett. **60**, 848 (1988).
- ²⁷D. A. Wharam, T. J. Thornton, R. Newbury, M. Pepper, H. Ahmed, J. E. F. Frost, D. G. Hasko, D. C. Peacockt, D. A. Ritchie, and G. A. C. Jones, J. Phys. C: Solid State Phys. **21**, L209 (1988).
- ²⁸R. D. Brown, Phys. Rev. B **2**, 928 (1970).
- ²⁹F. Y. Yang, K. Liu, K. M. Hing, D. H. Reich, P. C. Searson, C. L. Chien, Y. Leprince-Wang, K. Yu-Zhang, and K. Han, Phys. Rev. B 61, 6631 (2000).

- ³⁰Z. Zhang, X. Sun, M. S. Dresselhaus, J. Y. Yin, and J. Heremans, Phys. Rev. B **61**, 4850 (2000).
- ³¹J. E. Drut and T. A. Lähde, Phys. Rev. B **79**, 241405(R) (2009).
- ³²J. M. Schneider, M. Orlita, M. Potemski, and D. K. Maude, Phys. Rev. Lett. **102**, 166403 (2009).
- ³³X. Du, S.-W. Tsai, D. L. Maslov, and A. F. Hebard, Phys. Rev. Lett. 94, 166601 (2005).
- ³⁴A. Nikolaeva, D. Gitsu, L. Konopko, M. J. Graf, and T. E. Huber, Phys. Rev. B **77**, 075332 (2008).
- ³⁵H. Peng, K. Lai, D. Kong, S. Meister, Y. Chen, X.-L. Qi, S.-C. Zhang, Z.-X. Shen, and Y. Cui, Nature Mater. 9, 225 (2010).
- ³⁶A. Schadewitz, J. Barzola-Quiquia, A. Ballestar, and P. Esquinazi (to be published).