Coulomb blockade and hopping conduction in graphene quantum dots array

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We show that the low-temperature electron transport properties of chemically functionalized graphene can be explained as sequential tunneling of charges through a two-dimensional array of graphene quantum dots (GQDs). Below 15 K, a total suppression of current due to Coulomb blockade through a GQD array was observed. Temperature-dependent current-gate voltage characteristics show Coulomb oscillations with energy scales of 6.2–10 meV corresponding to GQD sizes of 5–8 nm, while resistance data exhibit an Efros-Shklovskii variable range hopping arising from structural- and size-induced disorder.

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I. INTRODUCTION

Reduced graphene oxide (RGO), a chemically functionalized atomically thin carbon sheet, provides a convenient pathway for producing large quantities of graphene via solution processing[.1–5](#page-4-0) The easy processibility of RGO and compatibility with various substrates including plastics makes it an attractive candidate for high-yield manufacturing of graphenebased electronic and optoelectronic devices. However, the electrical conductivity and field effect mobility values for RGO sheets are much inferior to that of pristine graphene. $6-10$ This has been attributed to a large amount of disorder present in the RGO sheets. The structural characterization through transmission electron microscopy (TEM), x-ray photoelectron spectroscopy (XPS), scanning tunneling microscopy (STM), and Raman spectra show that RGO consists of ordered graphitic (nanocrystalline) regions surrounded by areas of oxidized carbon atoms, point defects, and topological defects. $11-15$ The graphitic regions were estimated to be 3–10 nm from the TEM, STM, and Raman studies.¹¹⁻¹⁵ Optical studies of RGO also showed blue light emission^{[16](#page-4-0)} and infrared absorption^{17,18} determined by the size, shape, and edge configuration sp^2 graphitic domain. All these studies clearly suggest that RGO should behave as a two-dimensional (2D) array of graphene quantum dots (GQDs), which should be verified from lowtemperature electron transport measurements. However, previous electrical transport studies of RGO in a limited temperature range show 2D Mott variable range hopping (VRH), 11,19,20 11,19,20 11,19,20 which is not expected from a QD array model. Additionally, Mott VRH neglects the Coulomb interaction between localized graphitic domains, which may be significant at low temperatures as recent studies of individual 10-nm-sized GQDs show room-temperature Coulomb blockade (CB) .^{[21,22](#page-4-0)} It is therefore quite puzzling why the CB effect was not observed in lowtemperature transport of RGO sheets. A clear understanding of electron transport properties of RGO sheets is therefore still lacking, which is of great significance for the development of RGO as an important electronic and optoelectronic material.

In this paper, we present significant insights into the electron transport properties of RGO using low-temperature electron transport measurements, and we show that the properties of RGO sheets can be described as a transport through an array of GQDs with a large size distribution (polydispersed array), where graphitic domains act like QDs while oxidized domains behave like tunnel barriers between QDs. We show that below 15 K, the current is totally suppressed below a certain threshold voltage V_t due to CB of charges through a GQD array. For $V > V_t$, the current follows a scaling behavior $I \propto [(V - V_t)/V_t]^{\alpha}$ with α up to 3.4 expected from a quasi-2D QD array with topological inhomogenity. Current-gate voltage $(I-V_g)$ curves at different temperatures show reproducible Coulomb oscillation corresponding to single electron tunneling, which washes out between 70 and 120 K. These correspond to a charging energy of 6–10 meV, giving a QD size varying from 5 to 8 nm. Temperature-dependent resistance data show an Efros-Shklovskii (ES)-type VRH $(T^{-1/2}$ behavior) arising from structural- and size-induced disorder with localization length of the same order as that of the graphitic domain. Since the GQD size is tunable during the oxidation and reduction process, our study suggests that RGO will find many novel electronic and optoelectronic applications through tuning of GQD sizes.

II. EXPERIMENTAL DETAILS

A. Synthesis of RGO

RGO sheets were synthesized through a reduction of GO prepared by a modified Hummers method.²³ Oxidized graphite in water was ultrasonicated to achieve GO sheets followed by centrifugation for 30 minutes at 3000 rpm to remove any unexfoliated oxidized graphite. The pH of GO dispersion in water (0.1 mg/ml) was adjusted to 11 using a 5% ammonia aqueous solution. Hydrazine hydrate was added, and the solution was heated for 1 hour at 90 ◦C. The RGO suspension was spin coated on a mica substrate and examined using atomic force microscope (AFM). Figure $1(a)$ displays a tapping-mode AFM image of the RGO sheets along with their height (H) analysis. The lateral dimension (D) of our RGO sheets varies from 0.2 to 1 μ m. The line graph represents the thickness of the RGO sheets. Approximately 70% of the sheets displayed a height of 1.0 ± 0.2 nm.

B. Device fabrication

Devices were fabricated on heavily doped silicon (Si) substrates capped with a thermally grown 250 nm thick $SiO₂$

FIG. 1. (Color online) (a) Tapping-mode AFM images of RGO sheets with a height profile indicating the majority of the sheets are single layer. (b) Cartoon of DEP assembly setup. (c) Tappingmode AFM of a RGO device assembled via DEP along with their height profile. The height (H) varies from 2 to 10 nm in the channel, indicating that up to 10 layers of RGO sheets have been assembled in the channel. Scale $bar = 500$ nm. (d) Cartoon of electronic transport measurement setup.

layer. Source and drain electrode patterns of 500 nm \times 500 nm (channel length \times width) were defined by electron beam lithography followed by thermal deposition of 5 nm thick Cr and 20 nm thick Au and standard liftoff. The RGO sheets were then assembled between the source and drain electrodes using AC dielectrophoresis (DEP) in a probe station.^{[4](#page-4-0)} DEP has been shown to assemble 2D, 1D, and 0D nanomaterials at the selected position of the circuit for device applications.^{[4,24–](#page-4-0)[27](#page-5-0)} Figure 1(b) shows a cartoon of the DEP assembly setup. A small drop of RGO solution was placed onto the electrode pattern. An AC voltage of approximately 3 V_{P-P} at 1 MHz was applied for 20–30 seconds, after which the solution droplet was blown off by nitrogen gas. After DEP assembly, devices were thermally annealed in argon:hydrogen (1:3) gas at 200 \degree C for 1 hour, details of which can be found in our previous study.^{[4](#page-4-0)} Figure $1(c)$ shows a tapping-mode AFM image of a representative device. From the thickness measurement, we estimate that 2 to 10 layers of RGO sheets have been assembled in the channel. In our previous publication, we reported that using DEP we can assemble RGO at a selected position of the circuit with 100% device yield.^{[4](#page-4-0)} The devices were then bonded and loaded into a variable temperature cryostat for temperature-dependent electronic transport measurements. Figure 1(d) shows a schematic of the electrical measurement setup. The measurements were performed using a Keithley 2400 source meter, and a current preamplifier (DL 1211) capable of measuring pA signal interfaced with the LABVIEW program. A total of eight samples were investigated.

III. RESULTS AND DISCUSSION

Figure 2(a) shows current-voltage (*I–V*) characteristics of a representative device at 30, 25, 20, 15, 10, and 4.2 K. The backgate voltage V_{ϱ} was kept fixed at 0 V. With decreasing temperatures, the *I–V* curves become increasingly

FIG. 2. (Color online) (a) Current (*I*) – voltage (*V*) characteristics of a representative RGO device at temperatures 30, 25, 20, 15, 10, and 4.2 K. Below 15 K, the current is zero for $V < V_t$ due to Coulomb blockade of charges. Inset: AFM image of the device. Scale bar = 500 nm. (b) *I* vs. $(V - V_t)/V_t$ curves plotted in a log-log scale. Slope of the curves gives the value of exponent $\alpha = 3.1, 3.3$, and 3.4 at 4.2, 10, and 15 K, respectively. (c) V_t as a function of *T*. From the plot, $V_t(0)$ was estimated as 0.32 V.

nonlinear. However, all the curves are highly symmetric. As the temperature is lowered to less than 15 K, a complete suppression of current below a threshold voltage (V_t) was observed. Similar current suppression was observed in a previous study of individual GO devices with a highly asymmetric *I–V* curve and was explained by a Schottky barrier (SB) between metallic contact and GO[.28](#page-5-0) However, our *I–V* curves are highly symmetric giving evidence that the current suppression and symmetric nonlinear behavior is not due to a SB. Rather, such current suppression is due to CB of charges, as at low temperatures there is not enough energy for the charges to overcome Coulomb charging energies of the QD array formed by graphitic domains. In this scenario, the RGO sheet behaves as a GQD array where graphitic domains are quantum dots, and oxidized domains are tunnel barriers.

Theoretical studies of QD arrays by Middleton and Wingreen (MW) predicts that the *I–V* curves should follow the relation $I \propto [(V - V_t)/V_t)]^{\alpha}$ for $V > V_t$, where α is the scaling exponent that depends on the dimensionality of the arrays.²⁹ Although this theory was developed for nanocrystal arrays of uniform sizes (monodisperse array), experimentally it was found to be true for polydispersed array as well. $30,31$

Figure [2\(b\)](#page-1-0) shows *I* plotted versus $(V - V_t)/V_t$ in a loglog scale using $V_t = 0.18, 0.24, 0.28$ V at $T = 15, 10,$ and 4.2 K, respectively. The symbols are the experimental data points while the solid lines are fits to the above equation. From the fits, we obtain $\alpha = 3.1, 3.3,$ and 3.4 at 4.2, 10, and 15 K, respectively. For a 2D array of nanoparticles, the theoretical value of *α* was predicted as 1.6 while numerical simulations yielded as $2.0²⁹$ $2.0²⁹$ $2.0²⁹$ However, in previous experimental studies of 2D metal nanocrystal arrays, the exponent *α* was reported to vary from 2 to 2.5, which depends on size distribution, while for a quasi-2D system with multilayered nanoparticles the value was 2.6 to 3.0 .^{[30–34](#page-5-0)} Although our system is a quasi-2D system, our α values are slightly higher than these reports. Recent experimental and computer simulations involving a gold nanoparticle array with strong topological inhomogeneity show large scaling exponents $\alpha \approx 4.0^{35,36}$ $\alpha \approx 4.0^{35,36}$ $\alpha \approx 4.0^{35,36}$ Since RGO has many topological defects that came from oxidation and reduction process, the high value of α is in agreement with charge transport in an inhomogenous quasi-2D QD array network. In Figure 3, we show a schematic of RGO as a GQD array with strong topological inhomogeneity. The light gray areas represent GQDs, and the white regions represent oxidized carbon groups and topological defects. This shows that the GQDs are isolated (or localized) by oxidized carbon atom and topological defects, and there is a strong size distribution of GQDs. The lines between GQDs indicate tunnel barriers.

Figure $2(c)$ shows V_t plotted versus *T*, from which we see that V_t increases linearly with decreasing T . Extrapolation of the V_t plot to 0 K provides the global threshold voltage $V_t(0) = 0.32$ V. Similar *I–V* curves were observed for all 8 samples with α varying from 2.52 to 2.80 and $V_t(0)$ varying from 0.32 to 0.42. For an array of nanoparticles of uniform size, $V_t(0)$ can be expressed as $V_t(0) \approx E_c(\beta N)$ where E_c is charging energy of a QD, β is a prefactor whose value depends on the dimensionality and array geometry (for a 2D array $\beta = 0.3$), and *N* is the number of QDs in the conduction

FIG. 3. Schematic of RGO as GQD array. The light gray areas represent GQDs, the white regions represent oxidized carbon groups and topological defects. The lines between GQDs represent tunnel barriers.

path.^{[29,37](#page-5-0)} From here, we can estimate the number of GQDs in our array contributing to the charge transport; however, we need to estimate *Ec* first.

In order to calculate the E_c of the GQDs, we measured *I* as a function of gate voltage (V_g) at temperatures $T = 4.2$ to 120 K. This is shown in Fig. 4. For clarity, the data in Fig. 4(a) is plotted in a semi-log scale, with *I* at 50, 60, and 70 K were divided by a factor of 1.5, 2, and 3.5, respectively. The reproducible peaks in V_g correspond to single-electron tunneling (Coulomb oscillations) through GQD arrays. The bias voltage was kept fixed at $V = 0.3$ V. The peaks in V_g are not periodic, in agreement with the sequential tunneling of charges through multiple QDs. Such Coulomb oscillations have never been observed in previous studies of 2D metallic or magnetic QD array systems. This may be due to the fact that the density of states (DOS) in those systems is higher and gate voltage has a negligible effect in DOS. While in RGO, the DOS is low, allowing the gate to tune the DOS, giving

FIG. 4. (Color online) (a) Current (*I*) as a function of gate voltage (V_g) for $T = 4.2$, 10, 15, 20, 25, 30, 35, 40, 50, 60, and 70 K. The reproducible peaks correspond to Coulomb oscillations. For the unified view, *I* at 50, 60, and 70 K were divided by 1.5, 2, and 3.5. At 70 K, peaks around $V_g = 0$ were washed out. This is more clearly shown in (b). For clarity, curves from bottom to top in (b) were multiplied by a factor of 49, 41, 31, 23, 17, 12.5, 9, 6.7, 3.5, and 2.2, respectively. (c) *I* − *Vg* curves for *T* = 80–120 K with a step of 10 K. At 120 K, all the oscillations were washed out. Bias voltage was 0.3 V.

rise to Coulomb oscillations. As the temperature is increased from 4.2 to 120 K, two important features can be noticed. The peaks around $V_g = 0$ wash out around 70 K, corresponding to a thermal energy of 6.2 meV. This is more clearly shown in Fig. [4\(b\),](#page-2-0) where we plot the $-10 < V_g$ < 10 V regime up to $T = 70$ K of Fig. $4(a)$. For clear presentation, curves from bottom to top were multiplied by a factor of 49, 41, 31, 23, 17, 12.5, 9, 6.7, 3.5, and 2.2, respectively. The other peaks survive up to 120 K [Fig. $4(c)$], which corresponds to a thermal energy of 10 meV.

From the semiclassical orthodox theory of CB, the charging energy E_C required to add an electron to a QD is given by $E_c =$ $e^2/2C_{\Sigma}$, where C_{Σ} is the total capacitance, which depends on the size of each QD and their interdot separation. In order to observe the coulomb oscillations, *Ec* should be larger than thermal energy $k_B T$. Therefore our temperature-dependent data gives an estimate of E_c to vary from 6.2 to 10 meV. We suggest that this variation in charging energy is indicative of a large size distribution of GQDs in the transport pathway (polydispersed GQD array).

Using the E_c values, the total capacitance is estimated to vary from $C_{\Sigma} = 8$ to 13 aF. Neglecting the size variation for the time being, C_{Σ} can also be estimated from the geometrical consideration and can be written as $C_{\Sigma} = C_g + 9C$, where $C_g \approx 4\pi \varepsilon \varepsilon_o r$, and $C \approx 2\pi \varepsilon \varepsilon_0 r \ln[(r+d)/d]$ are self-capacitance and mutual capacitance of QDs, respectively.^{[31](#page-5-0)} Here *r* is the radius of GQD, 2*d* is spacing between QDs, ε is the dielectric constant of RGO, ε_0 is the value for permittivity of vacuum, and the factor 9 is the average number of nearest neighbors of each QD in a quasi-2D system.^{[31,38](#page-5-0)} The factor 9 was estimated as follows: For 2D and 3D hexagonal arrays, each nanocrystal has between 6 and 12 nearest neighbors. It was estimated in Refs. [31](#page-5-0) and [38](#page-5-0) that for a quasi-2D array, on average each GQD has ∼9 nearest neighbors. The value of ε_r can be calculated by using $\varepsilon_r = n^2 - k^2$, where *n* and *k* are refractive index and extinction coefficient of RGO film, respectively. Using the values of *n* and *k* in the thermally reduced GO, the calculated value of dielectric constant ε_r is estimated to be around 3.5^{39} 3.5^{39} 3.5^{39} By comparing experimental value and theoretical equation of C_{Σ} , we can calculate the value of $r = 2.5-4$ nm (domain size 5–8 nm) using $d = 0.75$ nm. These values obtained from electron transport spectroscopy are in excellent agreement with microscopic studies using TEM, which highlighted that the size of graphitic regime varies from 3 to 10 nm.^{[14,15](#page-4-0)} We used $d = 0.75$ nm, as a recent TEM study shows that the typical size of the oxidized or defective region varies from 1 to 2 nm,^{[14](#page-4-0)} giving an average value for $2d =$ 1.5 nm. The calculated domain size of GQDs is also in good agreement with the domain size obtained from our Raman study.^{[40](#page-5-0)}

We can now estimate the number of GQDs in the conduction pathway (*N*) of the array using the global threshold voltage formula $V_t(0) \approx E_C(\beta N)$. Using an average value of E_c to be 8.1 meV, we estimate $N = 131$. This is a slight overestimation considering the average size of each dot as 6.5 nm and average interdot separation of 1.5 nm; we would expect about 65 QDs in a 500 nm channel. The discrepancies may be due to the fact that we are using the MW formula, which neglects size disorder, which can have a great influence on V_t . For example, if we consider that the smallest dot size has the most influence

in the determination of V_t as pointed out be Muller *et al.*^{[41](#page-5-0)} then we obtain a more reasonable value of $N \sim 90$.

In order to further understand the electronic transport mechanism of the GQD array, we study the temperature dependence of the resistance of our devices. Temperature dependence of resistance can provide evidence about size distribution and the degree of disorder of the GQD array. Figure 5(a) shows the resistance (*R*) versus temperature (*T*) plot in the temperature range 30–250 K for one of the devices. It can be seen that *R* changes by over three orders of magnitude over this temperature range. *R* was calculated by measuring the current at a constant $V = 100$ mV as the temperature was lowered [see solid line in Fig. $5(a)$]. We have also measured *I–V* curves at a few selected temperatures and obtained the *R* values from the Ohmic part of the *I–V* curves [open circle in Fig. $5(a)$]. The *R* values of the two measurements were in agreement. Below 30 K, the *I–V* curves were non-Ohmic under 100 mV, and those data were discarded from this plot.

According to the QD array model, if QDs are monodispersed, the temperature dependence of resistance should follow thermally activated behavior *R* ∼ $R_0 \exp(E_0/k_B T)$,^{[31](#page-5-0)} while if the nanocrystals have significant size variation (polydispersed), it should follow ES VRH,

FIG. 5. (Color online) (a) Resistance (*R*) versus temperature (*T*) in a semi-log scale showing four orders of change in R for $T =$ 30–250 K. The solid line respresnts *R* measured at a fixed $V =$ 100 mV as *T* was decreased. The open symbols show *R* measured from the Ohmic part of the *I–V* curves measured at a few selected *T*. (b) Reduced activation energy $W = -\partial \ln R(T)/\partial \ln T = p(T_0/T)^p$ plotted vs. *T* on a log-log scale. From the slope of this plot we obtain $p = 0.48 \pm 0.05$ corresponding to the ES-VRH. For a comparison we also show lines with $p = 1$ (activated hopping) and $p = 1/3$ (Mott VRH). Our data do not fit with those models. (c) *R* in log scale as a function of $T^{-1/2}$. From the slope we obtain $T_0 = 4200$ K.

 $R \sim R_0 \exp(T_0/T)^{1/2},$ ^{[42,43](#page-5-0)} where T_0 is a constant related to the disorder of the material. Fitting resistance data with different behavior can be tricky, and the same data can often fit several behaviors (such as T^{-1} , $T^{-1/2}$, and $T^{-1/3}$). A better way of determining the exponent value is to consider a generalized formula $R(T) = R_0 \exp(T_0/T)^p$ and then calculate the value of *p* from $\ln W = A - p \ln T$, where $W = -\partial \ln R(T)/\partial \ln T =$ $p(T_0/T)^p$ is the reduced activation energy and *A* is a constant. $44,45$

Figure [5\(b\)](#page-3-0) shows ln*W* plotted versus ln*T*. From the slope (indicated by red line) of this curve, we obtain $p = 0.48 \pm 0.05$, which is consistent with ES VRH over the whole temperature range. For comparison, we have also plotted two lines for $p =$ $1/3$ and $p = 1$, which unequivocally show that the transport is described only by the $p = 1/2$ model. In previously reported data on single-layer RGO devices, 2D Mott VRH $(p = 1/3)$ was reported.11,19,20 This may be due to the limited temperature range of the data, where it might be possible to fit the same data with both $T^{-1/2}$ and $T^{-1/3}$ laws. Our selfconsistent analysis of the resistance data that span over three orders of magnitude clearly indicates that there is no conduction mechanism other than the *T* [−]1*/*² (ES VRH) for the entire temperature ranges. The characteristics of the ES VRH model is in strong agreement with what is expected for a polydispersed GQD array.

The ES VRH indicates strong localization of wavefunctions in GQDs. Further analysis of ES VRH data allows us to calculate the localization length *ξ* by plotting *R* against $T^{-1/2}$ in a semi-log scale. This is shown in Fig. [5\(c\),](#page-3-0) which shows a straight line as expected. From the slope of this

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curve, we obtain $T_0 = 4200$ K. T_0 is related to ξ through $T_0 = [(2.8e^2/4\pi \varepsilon \varepsilon_0 k_B \xi).^{42}$ $T_0 = [(2.8e^2/4\pi \varepsilon \varepsilon_0 k_B \xi).^{42}$ $T_0 = [(2.8e^2/4\pi \varepsilon \varepsilon_0 k_B \xi).^{42}$ The calculated value of ξ is about 3.5 nm, which is comparable to the calculated GQD sizes, indicating strong localization of the wavefunction inside each graphitic domain. Similar ES VRH was observed for all the eight samples with *ξ* varying from 2.3 to 3.8 nm.

IV. CONCLUSION

All the measurements and analysis presented here clearly demonstrate that the low-temperature charge transport properties of RGO can be modeled as due to a CB and hopping conduction through a polydispersed GQD array with topological inhomogenity. From our temperature-dependence data, we obtain the GQD sizes to vary from 5 to 8 nm, in excellent agreement with previous TEM studies. Observation of ES VRH with a localization length comparable to the size of each GQD shows that Coulomb interaction and size disorder play an important role. Our description of the RGO sheet as a 2D GQD array suggests that RGO will find many novel electronic and optoelectronic applications through tuning of GQD sizes via controlled oxidation and reduction

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