

Three energy scales characterizing the competing pseudogap state, the incoherent, and the coherent superconducting state in high- T_c cuprates

Y. Okada,¹ T. Kawaguchi,¹ M. Ohkawa,² K. Ishizaka,² T. Takeuchi,³ S. Shin,² and H. Ikuta¹

¹*Department of Crystalline Materials Science, Nagoya University, Nagoya 464-8603, Japan*

²*Institute for Solid State Physics (ISSP), The University of Tokyo, Kashiwa 277-8581, Japan*

³*EcoTopia Science Institute, Nagoya University, Nagoya 464-8603, Japan*

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We have studied the momentum dependence of the energy gap of $\text{Bi}_2(\text{Sr},R)_2\text{CuO}_y$ by angle-resolved photoemission spectroscopy (ARPES), particularly focusing on the difference between $R = \text{La}$ and Eu . By comparing the gap function and characteristic temperatures between the two sets of samples, we show that there exist three distinct energy scales, Δ_{pg} , Δ_{sc0} , and Δ_{sc0}^{eff} , which correspond to T^* (pseudogap temperature), T_{onset} (onset temperature of fluctuating superconductivity), and T_c (critical temperature of coherent superconductivity). The results not only support the existence of a pseudogap state below T^* that competes with superconductivity, but also the duality of competition and superconducting fluctuation at momenta around the antinode below T_{onset} .

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I. INTRODUCTION

One of the significant differences between high- T_c cuprates and conventional superconductors is the presence in the former of a pseudogap state above T_c . Whether the pseudogap state is a precursor to superconductivity or a state that competes with it has been a matter of long-standing debate.^{1–8} To address this problem, angle-resolved photoemission spectroscopy (ARPES) is one of the most powerful techniques, since the momentum dependence of the energy gap is directly linked to the pseudogap issue. Many ARPES experiments have investigated this problem, however, the data and their interpretations are still controversial.

If the momentum dependence of the gap function is constituted by only one component, the pseudogap state can be regarded as a precursor to the superconducting state. This picture has been supported by some of the ARPES experiments, which concluded that the energy gap has predominantly a d -wave symmetry.^{9–14} An intimate relation between pseudogap and superconductivity has been suggested also by high-frequency conductivity measurements,¹⁵ the enhanced Nernst signal,¹⁶ enhanced diamagnetism,¹⁷ and the observation of the quasiparticle interference pattern suggesting a phase incoherent pairing gap above T_c .¹⁸ On the other hand, other ARPES experiments suggested the existence of two gap components that depend differently on momentum, temperature, and carrier doping.^{19–28} If the gap function consists of two components, the presence of an additional order other than the d -wave superconductivity must be assumed. This picture was supported further by a recent experiment providing evidence for the existence of a density wave state in high- T_c cuprates.^{29,30} Here, if the co-existing state competes with superconductivity and suppresses T_c by reducing the number of paired electrons, the superconducting order would significantly fluctuate as has been suggested.⁴ In this case, both *competition* and *superconducting fluctuation* should be consistently accounted for above T_c .

It is known that T_c can be controlled both by the element R and x in $\text{Bi}_2\text{Sr}_{2-x}R_x\text{CuO}_y$ ($R = \text{rare-earth elements}$).^{27,31–33} Using $R = \text{La}$ and Eu single crystals of this system, it was

demonstrated in our earlier works that three characteristic temperatures, T^* (pseudogap temperature), T_{onset} (onset temperature of fluctuating superconductivity), and T_c , can be defined, which behave differently on the phase diagram with change of both R and x .^{34,35} To approach the pseudogap issue further in the present study, we probed the momentum dependence of the energy gap and compared the characteristic energy scales to the above three temperatures, focusing on the same system as in the previous study. All the experimental results shown in this paper consistently point to the existence of three distinct energy and temperature scales arising from the competition between the two states in high- T_c cuprates. Moreover, the duality of competition and superconducting fluctuation around the antinodal region is suggested to be important.

II. EXPERIMENT

Single crystals of $\text{Bi}_2\text{Sr}_{2-x}R_x\text{CuO}_y$ ($R = \text{La}$ and Eu) were grown by the floating zone method.^{34,36} The bulk sensitive ARPES spectra with an ultraviolet laser (6.994-eV photons) were taken by a Scienta R4000 hemispherical analyzer at the Institute of Solid State Physics (ISSP).³⁷ In this study, the total-energy resolution of a photoemission spectrometer (ΔE) is defined by fitting the Au spectrum with the Fermi Dirac function; its intensity at each energy is broadened by the Gaussian (full width at half maximum ΔE). The energy resolutions of all the ARPES experiments with the 6.994-eV photons shown in this paper were better than 2.2 meV, and all the measurements were performed at pressures below 5×10^{-11} Torr. Prior to the ARPES measurements, we carefully evaluated the doping levels of the crystals with c -axis lattice constant, thermopower, and/or inductive coupling plasma (ICP) spectroscopy.³⁴

III. RESULTS AND DISCUSSIONS

A. Δ_{sc0} : Energy scale of pairing at the antinode

Figure 1 shows the ARPES results obtained at 5 K with 6.994-eV photons on the optimally doped $\text{Bi}_2\text{Sr}_{2-x}R_x\text{CuO}_y$

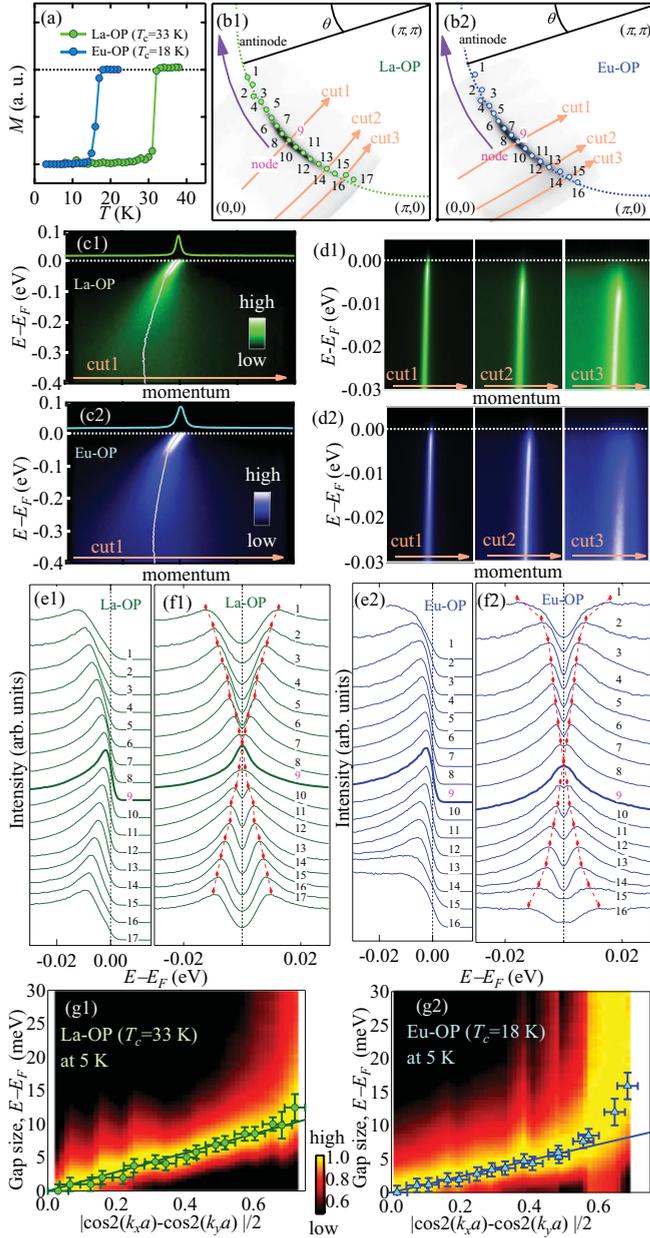


FIG. 1. (Color online) ARPES data obtained with 6.994-eV photons at 5 K for optimally doped $\text{Bi}_2\text{Sr}_{2-x}\text{R}_x\text{CuO}_y$ with $R = \text{La}$ (La-OP, $T_c = 33$ K) and $R = \text{Eu}$ (Eu-OP, $T_c = 18$ K) are shown. (a) Temperature dependence of magnetization of the crystals. (b1) and (b2) Mapping of the Fermi momenta k_F for La-OP and Eu-OP, respectively. Here, the Fermi surface that was determined with 21.214-eV photons in our previous study (Ref. 38) is shown with dotted lines. (c1) and (d1) [(c2) and (d2)] show the dispersion images along the momentum shown in (b1) [(b2)] for La-OP (Eu-OP). We show also momentum distribution curves at E_F in the upper part of (c1) and (c2). (e1) and (f1) [(e2) and (f2)] show the energy distribution curves and their symmetrized spectra at k_F for La-OP (Eu-OP), respectively. (g1) [(g2)] shows the intensity map of (f1) [(f2)] together with the gap size as a function of $|\cos(k_x a) - \cos(k_y a)|/2$ for La-OP (Eu-OP). The intensity is normalized to unity at the gap energy, and the color scales are the same for both figures.

with $R = \text{La}$ (La-OP) and $R = \text{Eu}$ (Eu-OP). As shown in Fig. 1(a), the T_c of the La-OP and Eu-OP samples was 33

and 18 K, respectively. Figures 1(b1) and 1(b2) show the Fermi momenta k_F where the ARPES spectra were taken. The Fermi surfaces determined with 21.214-eV photons in our previous work using samples with similar doping³⁸ are also shown in Figs. 1(b1) and 1(b2). Figures 1(c1) and 1(d1) [Figs. 1(c2) and 1(d2)] show the momentum dependence of the spectral intensity of La-OP (Eu-OP) along the cuts shown in Fig. 1(b1) [Fig. 1(b2)]. The energy distribution curves at k_F and the spectra that were symmetrized about E_F are shown in Figs. 1(e1) and 1(e2), and 1(f1) and 1(f2), respectively. We determined the energy gap by fitting the symmetrized spectra with the phenomenological spectral function,^{39,40} which has been used in many other reports.^{9,11–13,22}

The gap size with La-OP and Eu-OP is plotted as a function of $|\cos(k_x a) - \cos(k_y a)|/2$ in Figs. 1(g1) and 1(g2), respectively. Since a d -wave gap is expressed as $\Delta = \Delta_{sc0} |\cos(k_x a) - \cos(k_y a)|/2$, Figs. 1(g1) and 1(g2) show that the gap has a pure d -wave form around the node for both La-OP and Eu-OP. On the other hand, the data points deviated from the d -wave form near the antinode. This deviation is accompanied by a huge broadening of the spectral linewidth as is evident from the image plot of the ARPES spectra shown in the same figure. We determined Δ_{sc0} by fitting the linear part of the data, which gave 14.1 and 12.0 meV for La-OP ($T_c = 33$ K) and Eu-OP ($T_c = 18$ K), respectively. Hence the value of Δ_{sc0} changed together with T_c . However, the difference in Δ_{sc0} is not as large as the change of T_c since the ratio of Δ_{sc0} ($14.1/12.0 \approx 1.23$) is much smaller than the T_c ratio $33/18 \approx 1.8$. This is in strong contrast to conventional superconductors, for which T_c scales with the binding energy of the paired electrons Δ_{sc0} , and suggests the possible existence of an energy scale other than Δ_{sc0} corresponding to T_c .

B. Δ_{sc0}^{eff} : Energy scale related to T_c

The temperature evolution of the symmetrized spectrum of La-OP and Eu-OP across T_c is shown in Figs. 2(a1)–2(a4) and 2(b1)–2(b4) for various momenta. Figures 2(c) and 2(d) show the temperature dependence of the gap size (left axis) together with the gap depth (right axis; see the caption for the definition) for the momentum that is closest to the antinode among the data shown in Fig. 2. From this figure, a sudden change in the gap depth was observed across T_c , although the gap size for this momentum did not show obvious change. On the contrary, a more dramatic change happened across T_c at momenta around the node: The energy gaps all collapsed simultaneously at T_c . Based on this experimental observation, we can define a characteristic energy scale Δ_{sc0}^{eff} , which is indicated by the arrows in Figs. 2(c) and 2(d) on the left axes. When the energy gap at $T = 0$ was smaller than this characteristic energy Δ_{sc0}^{eff} , it decreased abruptly to zero at T_c , while the energy gap remained finite above T_c if it was larger than Δ_{sc0}^{eff} at $T = 0$. The existence of such a characteristic energy is consistent with other recent reports.^{13,22,41–43} Here, Δ_{sc0}^{eff} of La-OP ($T_c = 33$ K) and Eu-OP ($T_c = 18$ K) are 5.6 ± 1.1 meV and 3.5 ± 1.1 meV, respectively. The ratio of Δ_{sc0}^{eff} between the two samples is about 1.6 ± 0.5 , which is close to the ratio of T_c (≈ 1.8) within experimental error. Moreover, the values of $2\Delta_{sc0}^{eff}/k_B T_c$ for La-OP (3.9 ± 0.8)

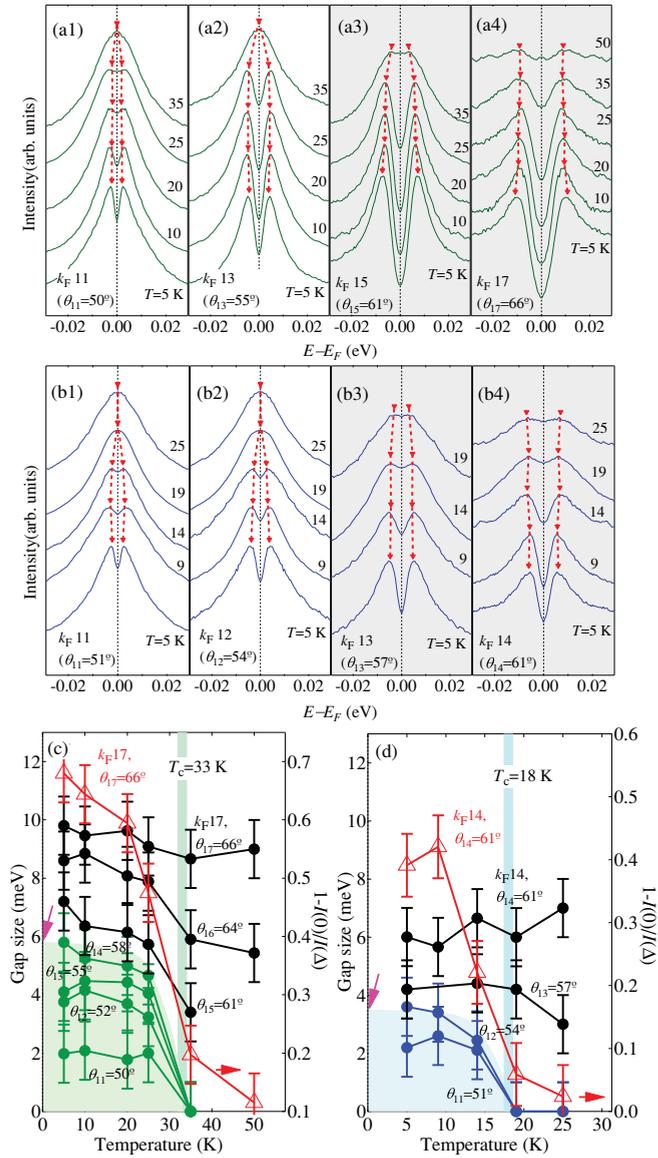


FIG. 2. (Color online) Evolution of the energy gap across T_c of La-OP ($T_c = 33$ K) and Eu-OP ($T_c = 18$ K) measured with laser ARPES (6.994-eV photons). (a1)–(a4) and (b1)–(b4) show the temperature dependence of the symmetrized ARPES spectra for La-OP and Eu-OP, respectively. Here, the index of k_F corresponds to the numbers in Figs. 1(b1) and 1(b2), where θ is also defined. (c) and (d) show the temperature evolution of the gap size (left axis) at various momenta across T_c for La-OP and Eu-OP, respectively. The hatched area shows roughly the range where the energy gap was strongly temperature dependent and collapsed at T_c . The characteristic energy Δ_{sc0}^{eff} is indicated by the arrows on the left axes of (c) and (d). The temperature dependence of $1 - I(0)/I(\Delta)$ (right axis) calculated from the spectra measured at point 17 (14) for the $R = \text{La}$ (Eu) sample is also plotted, where $I(0)$ and $I(\Delta)$ are the intensity at E_F and at the gap edge, respectively.

and Eu-OP (4.5 ± 1.4) were close to the value observed by Andreev reflection experiments on a wide range of cuprates with various T_c 's.⁴⁵ These quantitative comparisons indicate that Δ_{sc0}^{eff} can be attributed to the energy scale corresponding to T_c .

C. Δ_{pg} : Energy scale related to a competing pseudogap state

The question to be addressed next is why Δ_{sc0}^{eff} is much lower than Δ_{sc0} . Figure 3 shows the momentum dependence of the energy gap of the La-OP and Eu-OP samples at $T = 5$ K and $T \gtrsim T_c$. The energy gap in the antinodal region obtained with 21.214-eV photons (at 5 K with less than 20 meV resolution) in our previous studies^{38,45} are also included. In contrast to the gap around the node, the antinodal gap Δ_{pg} is clearly larger for Eu-OP ($T_c = 18$ K) than La-OP ($T_c = 33$ K) showing that the nodal and antinodal gaps depend differently on T_c , which is qualitatively consistent with scanning tunnel microscopy (STM)/scanning tunnel spectroscopy (STS) results.⁴⁶ Previously, we observed that the coherent part of the remnant Fermi surface, where clear peaks were observed in the ARPES spectra at the superconducting state, narrowed with increasing Δ_{pg} .³⁸ This observation suggested that Δ_{pg} shrinks the coherent part of the remnant Fermi surface, which naturally decreases the superfluid density. All our experimental observations suggest that the antinodal pseudogap state characterized by Δ_{pg} competes with superconductivity and suppresses T_c , resulting in the deviation of Δ_{sc0}^{eff} from Δ_{sc0} . The $T = 5$ K data of Fig. 3 is the indication of the co-existence of the competing state with superconductivity. This supports the existence of two different momentum dependent gap components^{19–24,26–28}; that is, the antinodal gap Δ_{pg} has its origin in a competing state with no direct relation to the d -wave superconductivity.⁴⁷

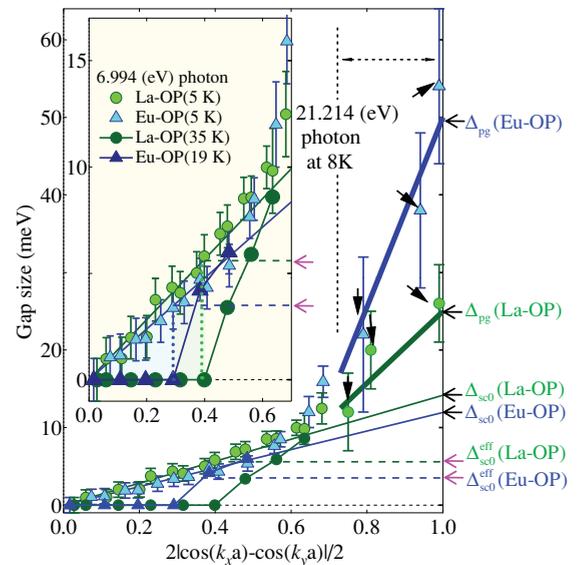


FIG. 3. (Color online) Comparison of the momentum dependence of the energy gaps of La-OP ($T_c = 33$ K) and Eu-OP ($T_c = 18$ K) at $T = 5$ K, which is well below T_c , and at $T \gtrsim T_c$. The three data points closest to the antinode (indicated by arrows) are obtained using 21.214-eV photons both for La-OP and Eu-OP (at 5 K with less than 20 meV resolution) (Refs. 38 and 45). The three characteristic energy scales for both La-OP and Eu-OP are shown on the right axis. The inset is an enlarged plot around the node to show more clearly the neighborhood of the node and Δ_{sc0}^{eff} .

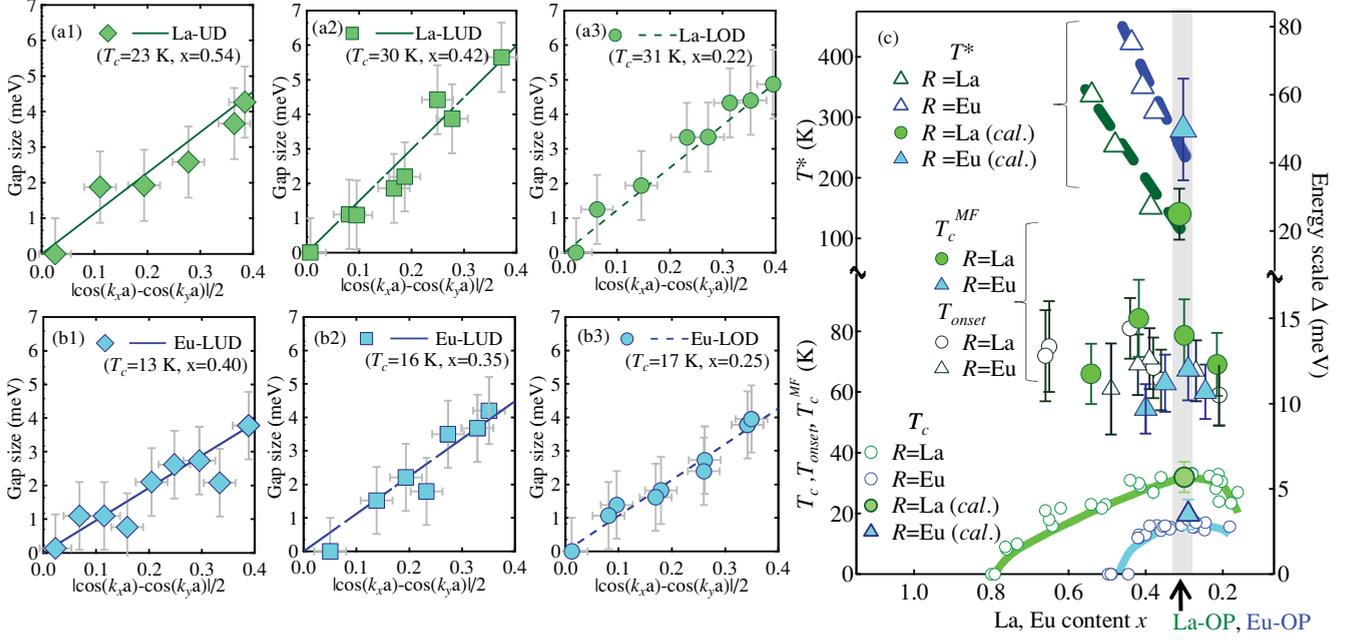


FIG. 4. (Color online) Energy gaps around the node of $\text{Bi}_2\text{Sr}_{2-x}\text{R}_x\text{CuO}_y$ with $R = \text{La}$ and Eu samples determined by the laser-ARPES measurements (6.994-eV photons) are shown in (a1)–(a3) and (b1)–(b3), respectively. All data shown here were measured at $T \leq 5$ K, which is well below T_c . (c) Phase diagram of the three characteristic temperatures. The data of T^* , T_c^{MF} , and T_c plotted with solid symbols were calculated from Δ_{pg} , Δ_{sc0} , and Δ_{sc0}^{eff} assuming $2\Delta/k_B T = 4.3$. The right axis of (c) gives the energy scale Δ that is connected to the temperature scale (left axis) by the above relation. The T_c , T_{onset} , and T^* data shown with empty symbols are from our previous studies (Refs. 32–34).

D. Intimate relation between Δ_{sc0} and T_{onset}

Figures 4(a1)–4(a3) and 4(b1)–4(b3) show the momentum dependence of the energy gap around the node of various $\text{Bi}_2\text{Sr}_{2-x}\text{R}_x\text{CuO}_y$ crystals with different x for $R = \text{La}$ and Eu , respectively. The results indicate that the slope of the energy gap as a function of $|\cos(k_x a) - \cos(k_y a)|/2$ did not change much with R or x despite the large variation of T_c . This relatively insensitive behavior of Δ_{sc0} mimics that of T_{onset} , the temperature below which the Nernst signal starts to be enhanced with decreasing temperature.³⁴ To address this similarity more quantitatively, we calculated the mean-field transition temperature (T_c^{MF}) based on the weak-coupling theory of d -wave superconductivity ($2\Delta_{sc0}/k_B T_c^{MF} = 4.3$). Figure 4(c) shows T_c^{MF} calculated from the data shown in Figs. 4(a1)–4(a3) and 4(b1)–4(b3) together with T_c , T_{onset} , and T^* reported in our previous studies.^{34–36} Interestingly, we found that T_c^{MF} agrees quite well with T_{onset} . We think that this agreement implies that the energy scale Δ_{sc0} is related to the onset pairing temperature T_{onset} . The large difference between T_{onset} and T_c (Δ_{sc0} and Δ_{sc0}^{eff}) indicates that there exists a large superconducting fluctuation. The phenomenological explanation of the existence of a large superconducting fluctuation is due to weak perturbation of the pairing energy Δ_{sc0} by stabilization of the competing state (increasing Δ_{pg}). We think that this is consistent with the existence of a relatively homogeneous gap despite the large variation of the pseudogap in real space as was revealed by recent STM experiments.^{47,48}

Note that while Δ_{sc0} is the pairing energy scale at the antinode, the energy gap observed at this momentum is not

Δ_{sc0} but Δ_{pg} . As shown in Fig. 4(c), the characteristic temperature scale Δ_{sc0} is related to T_{onset} . Therefore the observed relation between T_{onset} and Δ_{sc0} suggests the existence of both competition and superconducting fluctuation at momenta around the antinode below T_{onset} .

E. Three energy and temperature scales in high- T_c cuprates

In Fig. 4(c), we plot all the experimentally obtained energy and temperature scales changing both x and R in $\text{Bi}_2\text{Sr}_{2-x}\text{R}_x\text{CuO}_y$. This phase diagram clearly shows the existence of three energy (Δ_{sc0}^{eff} , Δ_{sc0} , and Δ_{pg}) and temperature (T_c , T_{onset} , and T^*) scales connected by the relation $2\Delta/k_B T = 4.3$. The natural consistent picture led by the phase diagram of Fig. 4(c) is that the pseudogap state (characterized by Δ_{pg} and T^*) suppresses coherent superconductivity (Δ_{sc0}^{eff} and T_c) while keeping the pairing strength (Δ_{sc0} and T_{onset}) similar.⁴⁹ Therefore the competing state kills superconductivity mainly by enhancing fluctuation of superconducting order through reducing superfluid density (phase stiffness). In other words, one may say that the *competition* enhances the *superconducting fluctuation*. We think the conclusion in this paper can be extended more or less to all the high- T_c cuprates, including systems that have a comparable Δ_{sc0} and Δ_{pg} , such as $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_y$.

IV. SUMMARY

In summary, we compared the momentum dependence of the gap function and the characteristic temperature scales of $\text{Bi}_2\text{Sr}_{2-x}\text{R}_x\text{CuO}_y$ ($R = \text{La}$ and Eu). All the experimental

results point toward the existence of three distinct energy and temperature scales corresponding to the competing pseudogap state and the incoherent and coherent superconducting states. Accounting for all these three phenomena consistently would be crucial for understanding the pseudogap issue in high- T_c cuprates.

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