# Thermodynamic approach to glass-forming ability of water-quenched Pd-P-based and Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> bulk metallic glasses

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Despite its importance, a thermodynamic approach to determining the glass-forming ability (GFA) of bulk metallic glass (BMG) remains a goal to be achieved. We examined the GFA of water-quenched Pd-P-based and Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> BMG's in which their molten alloys were sufficiently treated with a dehydrated B<sub>2</sub>O<sub>3</sub> flux prior to and during quenching to room temperature. This allowed us to envisage the applicability of the classical steady-state homogeneous nucleation theory because the suppression of heterogeneous nucleation worked effectively. GFA was examined by comparing the critical cooling rate  $R_c^h$  for glass formation with the maximum diameter  $d_{max}$ of glass. To calculate  $R_c^h$ , the homogeneous nucleation rate  $I_{ss}(T)$ , and the growth rate  $u_c(T)$  were estimated as functions of the undercooling temperature of molten alloys. Then, the free energy difference  $\Delta G_{L-x}(T)$  between the liquid and crystalline phases, and the viscosity  $\eta(T)$  of the liquid were experimentally determined while the surface energy  $\sigma_{sL}(T)$  at the liquid-nucleus interface was estimated by calculation. The  $d_{max}$  of rod BMG's correlated strongly to  $R_c^h$  through the relation  $R_c^h \approx d_{max}^{-3}/10 \text{ mm}^3 \text{ Ks}^{-1}$ .

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### I. INTRODUCTION

The study of the glass-forming ability (GFA) of bulk metallic glass (BMG) is one of the most interesting fields and thus has attracted great interest among many researchers. Empirical consideration about GFA has often been taken in terms of the reduced glass transition temperature  $T_{rg} [=T_g/T_l]$  and/or the  $\gamma$  parameter<sup>1</sup>  $[=T_x/(T_g + T_l)]$ , where  $T_g$ ,  $T_x$ ,  $T_m$ , and  $T_l$ are the calorimetric glass transition temperature, crystallization temperature, melting temperature, and liquidus temperature, respectively. These parameters are effective measures for explaining the GFA of a type of BMG, but they do not provide a clear physical significance of the GFA. Recently, Senkov<sup>2</sup> has proposed the use of the  $F_1$  parameter to quantify the GFA of BMG's, which is defined using  $T_{rg}$  and the fragility *m* and is given by

$$F_1 = 2\left[\frac{m}{16}\left(\frac{1}{T_{\rm rg}} - 1\right) + 2\right]^{-1},\tag{1}$$

where *m* is defined by the viscosity  $\eta$  and a scaling glass transition temperature  $T_g^*$ , which gives a viscosity of  $10^{12}$  Pa·s. The fragility is expressed as

$$m = \left. \frac{\partial \log_{10} \eta(T)}{\partial (T_g^*/T)} \right|_{T=T_s^*}.$$
 (2)

It gives the slope of the curve at  $T = T_g^*$  when  $\eta(T)$  is described as functions of  $T_g^*/T$ . This approach emphasized the strong correlation between GFA and liquid fragility. Senkov also found that the critical cooling rate  $R_c$  for glass-formation decays exponentially with the  $F_1$  parameter. Regarding the thermodynamic approach to determining the GFA of recently developed BMG's, several researchers have postulated the importance of the Gibbs free-energy difference<sup>3-5</sup>  $\Delta G_{L-x}(T)$ between a liquid and its crystalline counterpart. Jiang *et al.*<sup>4</sup> have reported that there is a close correlation between the GFA of many Zr-based BMG's and their  $\Delta G_{L-x}(T)$ .  $\Delta G_{L-x}(T)$ is a dominant factor in determining the driving force for crystallization in liquids. However, there are other factors that affect the kinetics of crystallization in liquids. Thus, it will be crucial to quantitatively discuss the reason why the  $\Delta G_{L-x}(T)$  plays a special role in suppressing the nucleation and growth of crystal nuclei during the vitrification of molten alloys. Quaternary Pd-Cu-Ni-P alloys are a system presenting a remarkable GFA, as good as that of Zr-based metallic glasses. Nishiyama and Inoue<sup>6</sup> reported that Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> BMG shows an extremely low critical cooling rate, 0.067 K/s, for glass formation and concluded that the origin of high GFA is the low nucleation ( $\approx 10^9 \text{ m}^{-3} \text{ s}^{-1}$ ) and growth ( $\approx 10^{-7} \text{ ms}^{-1}$ ) rates. Shen and Schwarz<sup>7</sup> found that the heterogeneous nucleation rate is significantly decreased after cyclic B<sub>2</sub>O<sub>3</sub> flux treatments of Pd43.2Cu28Ni8.8P20 molten alloy, and that the critical cooling rate for glass formation reaches a quite low value, 0.005 K/s. This observation suggests strongly that the Pd-Cu-Ni-P alloy system intrinsically possesses a significant GFA if the heterogeneous nucleation is effectively depressed. Several Pd-P- and Pt-P-based BMG's can be prepared easily by the water-quenching technique<sup>8–10</sup> with a  $B_2O_3$  flux. Among all such BMG's, it is not yet clarified why quaternary Pd-Cu-Ni-P BMG exhibits an extraordinarily high GFA. The B<sub>2</sub>O<sub>3</sub> flux intervenes effectively with the direct contact between the melt and the wall of the container and the vacuum environment. Drehman and Greer<sup>11</sup> examined the crystallization kinetics of a Pd40Ni40P20 BMG from a thermodynamic point of view, and they concluded that this glass system could be vitrified at a critical cooling rate as low as  $10^{-3}$  K/s if the heterogeneous nucleation sites were appropriately taken out. Later, Kui *et al.*<sup>12</sup> obtained a  $Pd_{40}Ni_{40}P_{20}$  BMG ( $d_{max} \approx$ 10 mm) with a dehydrated  $B_2O_3$  flux and predicted that the homogenous steady-state nucleation rate may be less than  $10^5 \text{ m}^{-3} \text{ s}^{-1}$ . Cheng *et al.*<sup>13</sup> have calculated the relaxation time  $\tau_{\alpha}$  of the  $\alpha$ -relaxation process in several Cu-Zr binary molten alloys over a wide temperature range from equilibrium liquid temperatures down to supercooled liquid temperatures near  $T_g$ . They reported that  $\tau_{\alpha} \approx 10^{-8}$  s near  $T_g$ . This value is much shorter than the time required for water quenching, which is roughly estimated to be a few seconds. This result ensures the thermodynamic consideration about the vitrification process of molten alloys in water quenching because the rate of atomic rearrangement at each temperature should keep up with the speed of temperature variation.

In the present study, a material's "glass-forming ability" was estimated with the maximum size  $d_{\text{max}}$  of glass sample formed. The glass samples were carefully produced under the condition that the heterogeneous nucleation and the growth mechanism did not work effectively. We estimated the homogeneous nucleation rate  $I_{ss}(T)$  and the growth rate  $u_c(T)$  for representative Pd-P- and Pt-P-based BMG's over a range from  $T_m$  to a temperature just below  $T_g.I_{ss}(T)$  and  $u_c(T)$ were estimated from the free-energy difference  $\Delta G_{L-x}(T)$ , the interfacial free energy between the nucleus and the liquid  $\sigma_{\rm sl}$  and the viscosity  $\eta(T)$ . Then both the viscosity and freeenergy difference were determined experimentally, while the interfacial free energy was obtained by calculation. Next, using  $I_{ss}(T)$  and  $u_c(T)$ , the critical cooling rate  $R_c^h$  of glass formation was calculated under the assumption that a homogeneous nucleation process worked dominantly in the vitrification of molten alloys. After that, the sequence of the order of  $R_c^h$  values was compared with the maximum diameter  $d_{\text{max}}$  of the glass sample to determine the order of the GFA among all the glasses.

### **II. EXPERIMENTAL**

Master alloys with compositions of  $Pd_{40}Ni_{40}P_{20}$ , Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub>,  $Pd_{40}Cu_{40}P_{20}$ , Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub>,  $Pd_{42.5}Cu_{30}Ni_{7.5}P_{20}$ , and  $Pd_{43}Cu_{27}Ni_{10}P_{20}$  were prepared by sintering Pd (99.95 at%), Pt (99.95 at%), Cu (99.99 at%), Ni (99.993 at%), and P (99.9999 at%) at 1473 K for 8 hr in vacuum-sealed quartz tubes. After sintering, each alloy was remelted in a quartz tube and cooled to room temperature to ensure the homogeneity of the composition. This operation was repeated two times. After being homogenized, the alloy was fluxed with a dehydrated  $B_2O_3$  by holding the melt at 1300 K for 8 hr to remove any phosphorous oxides, which are considered to become dominant heterogeneous nucleation sites.<sup>11</sup> Each BMG was prepared by the water-quenching technique to a size of 8-12 mm in diameter and 10-20 mm in length, where the melt was embedded in B<sub>2</sub>O<sub>3</sub> solution during vitrification and was prevented from direct contact with the wall of the tube and the vacuum environment. The maximum diameter  $d_{\text{max}}$  of bulk samples of the individual alloy systems was determined. In the case of  $Pd_{40}Cu_{40}P_{20}$ , bulk samples could not be prepared. Instead, we produce a  $Pd_{40}Cu_{40}P_{20}$  ribbon sample by a conventional melt-spinning technique with a B<sub>2</sub>O<sub>3</sub> flux-treated master alloy. In addition, a Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub> plate of about 1-mm thick was prepared by the copper mold casting method. Induced coupling plasma (ICP) spectroscopy proved that the compositions of glass samples were in accordance with the nominal composition within an error of  $\pm 0.4$  at %. The amorphous nature of the glass was confirmed by x-ray diffraction analysis and optical microscopy. The specific heat curves of BMG and their crystallized counterparts were measured with a differential scanning calorimeter (DSC), a Perkin Elmer Pyris 1 DSC, and Diamond DSC under a pure Ar gas flow. Then the step-scan technique was employed with a temperature step of 10 K and time durations of 180–300 s as reported elsewhere.<sup>3,14</sup> The crystalline samples used were prepared by cooling a molten alloy up to ( $T_m - 30$  K) for a week, followed by cooling it to room temperature. The weights of samples used ranged from 80 to 100 mg. The viscosities of Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub>, Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> (Ref. 15), Pt<sub>60</sub>Ni<sub>15</sub>P<sub>20</sub> (Ref. 15), and Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> (Ref. 15) BMG's were measured by isothermal creep experiments below  $T_g$ , followed by constant heating creep experiments with a rate of 0.083 K/s in a supercooled liquid region. The physical density of each sample was measured by the Archimedean method with *n*-Tridecane as a working fluid.

#### **III. RESULTS**

#### A. Thermodynamic properties of glass samples

The glass-forming range of the ternary Pd-Cu-P alloy was determined by He *et al.*<sup>16</sup> A representative  $Pd_{40}Cu_{40}P_{20}$ alloy was reported to possibly form a bulk rod with a size of at least 7-mm diameter by the water-quenching method. However, we could not prepare any bulk-form glasses with this composition by the water-quenching method. The possibility may have been inferred from the fact that a master alloy was prepared differently from the literature.<sup>16</sup> Therefore, the optimized composition near Pd40Cu40P20 was searched for and bulk-form glass with a composition of Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub> was found. The  $d_{\text{max}}$  of this glass reached approximately 12 mm. The thermodynamic properties of the glasses were examined by differential thermal analysis (DTA) conducted with a heating rate of 0.33 K/s. The DTA curves of BMG's as well as the ribbon-form Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub> prepared in the present work are shown in Fig. 1. The  $T_g, T_x, T_m$ , and  $T_l$  are summarized in Table I together with  $d_{\rm max}$ ,  $T_{\rm rg}$  and the  $\gamma$  parameter. Regarding  $Pd_{40}Cu_{40}P_{20}$  glass, we assumed  $d_{max} \approx 2 \text{ mm}$ because the range  $d_{\text{max}} > 1$  mm can be deduced from the size of the sample produced by mold casting as mentioned in Sec. II. Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glass<sup>17</sup> was obtained by further optimizing standard  $Pd_{40}Cu_{30}Ni_{10}P_{20}$  glass with a  $d_{max}$  of 72 mm<sup>9</sup>, and it is expected to show a larger  $d_{\text{max}}$  than Pd<sub>40</sub>Cu<sub>30</sub>Ni<sub>10</sub>P<sub>20</sub> glass. However, we assumed, in this work, that the  $d_{\text{max}}$  of Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glass is the same as that of  $Pd_{40}Cu_{30}Ni_{10}P_{20}$  (i.e.,  $d_{max} \approx 72$  mm). The  $d_{max}$  of  $Pd_{40}Ni_{40}P_{20}$  glass has been improved<sup>11,12,18</sup> by means of the  $B_2O_3$  flux treatment during the preparation of its master alloy and the quenching procedure. A value of  $d_{\rm max} \approx 25$  mm is reported recently in Ref. 7, and it is much larger than expected from  $T_{\rm rg}$  and the  $\gamma$  parameter. On the other hand, Pd<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> glass can be quenched in bulk form,  $d_{\rm max} \approx 8$  mm, despite it having the lowest  $T_{rg}$  and smallest  $\gamma$  parameter among all the glasses prepared in the present work. The thermodynamic data of Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub><sup>19,20</sup> and Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub><sup>21,22</sup> glasses are summarized in Table I for comparison, where Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glass with  $d_{\text{max}} \approx 0.04 \text{ mm}^{20}$  was prepared by splat cooling. In the case of Pd77.5Cu6Si16.5 glass, a variety of  $d_{\text{max}}$  values were reported and they corresponded to different types of vitrification methods. We adopted the maximum

TABLE I. Thermodynamic parameters of BMG's and ribbon-form Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub> glass. For comparison the data for Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub><sup>22</sup> and Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub><sup>20</sup> glasses are indicated.

Glass	<i>T<sub>g</sub></i> [K]	<i>T<sub>x</sub></i> [K]	<i>T<sub>m</sub></i> [K]	<i>T</i> <sub>l</sub> [K]	$T_{\rm rg}$	γ	$F_1$	d <sub>max</sub> [mm]	$\Delta H_m$ [J/mol]	$\Delta S_m$ [J/mol K]	<i>a</i> <sub>0</sub> [m]	$V_M [\mathrm{m}^3]$
Pd <sub>42.5</sub> Cu <sub>30</sub> Ni <sub>7.5</sub> P <sub>20</sub>	571	640	795	828	0.690	0.458	0.546	≈72	$6.37 \times 10^{3}$	8.01	$0.257 \times 10^{-9}$	$8.02 \times 10^{-6}$
Pd43Cu27Ni10P20	578	657	794	862	0.671	0.456	0.500	_	6.90	8.69	0.257	7.92
Pd40Ni40P20	576	650	875	979	0.588	0.418	0.486	25	10.4	11.9	0.254	7.71
Pd <sub>46</sub> Cu <sub>35.5</sub> P <sub>18.5</sub>	558	610	845	882	0.633	0.424	0.513	12	6.51	7.70	0.258	8.11
Pt <sub>60</sub> Ni <sub>15</sub> P <sub>25</sub>	481	542	755	892	0.539	0.395	0.357	8	11.6	15.4	0.259	8.7
$Pd_{40}Cu_{40}P_{20}$	536	570	883	900	0.596	0.397	$0.474^{a}$	$\approx 2^{b}$	8.10	9.17	0.257	8.01
Pd77.5Cu6Si16.5	639	672	1015	1036 <sup>c</sup>	0.617	0.401	0.378	$\approx 1^{b}$	7.25	7.15	0.268	8.67
Au <sub>76.9</sub> Ge <sub>13.65</sub> Si <sub>9.45</sub>	295	300	625	650 <sup>°</sup>	0.454	0.317	0.237	0.04 <sup>b</sup>	10.6	17.0	0.277	10.6

<sup>a</sup>The viscosity of  $Pd_{46}Cu_{35.5}P_{18.5}$  BMG is used (see the text) to calculate the  $F_1$  parameter.

<sup>b</sup>Regarding the  $Pd_{40}Cu_{40}P_{20}$  glass,  $d_{max}$  was deduced from a thickness  $\approx 1$  mm of plate-form glass. The  $Pd_{77.5}Cu_6Si_{16.5}$  glass was prepared by directional solidification<sup>21</sup> and the Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glass<sup>20</sup> was made by splat cooling.

<sup>c</sup>The  $T_l$  was measured by the master alloy prepared in the present work.

size,  $d_{\rm max} \approx 1.0 \ {\rm mm^{21}}$  among them, and it was obtained by directional solidification. Hereafter, in all the tables, the names of the glasses are arranged in the order of the magnitude of  $d_{\text{max}}$ .

### **B.** Estimation of free-energy difference $\Delta G_{L-x}(T)$

The specific heats of the supercooled liquid, appearing after the glass transition on heating the glass solid, and the melt are plotted against temperature for individual molten alloys as well as their crystalline counterparts in Fig. 2. Hereafter, the results of each glass sample



$$C_{P,L}(T) = 3R + aT + bT^{-2},$$
(3)

1000

where R is the gas constant. The specific heat data of the Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> alloy have been reported by Kui and Turnbull<sup>18</sup> and are shown together with the results of the present work. Their specific heat curves seem to behave differently from



rectangles) and their crystalline counterparts (solid rectangles)  $C_{P,x}(T)$  where each colored rectangle denotes  $Pd_{42.5}Cu_{30}Ni_{7.5}P_{20}$ (black), Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> (blue), Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> (green), Pd<sub>46</sub>Cu<sub>35,5</sub>P<sub>18,5</sub> (purple),  $Pt_{60}Ni_{15}P_{25}$  (red), and  $Pd_{40}Cu_{40}P_{20}$  (sky blue) alloy, respectively. The colored solid line corresponds to the specific heat curve of liquid against Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> (measured<sup>18</sup>), Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> (calculated<sup>5</sup>), and  $Au_{76.9}Ge_{13.65}Si_{9.45}$  (calculated<sup>20</sup>) alloys. The broken line corresponds to the specific curve of crystallized Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> (measured<sup>18</sup>) and Au<sub>76.9</sub>Ge<sub>13,65</sub>Si<sub>9,45</sub> (measured<sup>20</sup>) alloys, respectively.



FIG. 1. DTA curves of BMG's and ribbon Pd40Cu40P20 glass used in the present work. A heating rate of 0.33 K/s was employed.

Glass	$a [J/mol K^2]$	b [JK/mol]	$c  [J/mol  K^2]$	$d  [J/mol  K^3]$ 6.32 × 10 <sup>-6</sup>	
Pd <sub>42.5</sub> Cu <sub>30</sub> Ni <sub>7.5</sub> P <sub>20</sub>	$1.29 \times 10^{-2}$	$4.50 \times 10^{6}$	$1.42 \times 10^{-3}$		
Pd <sub>43</sub> Cu <sub>27</sub> Ni <sub>10</sub> P <sub>20</sub>	1.31	4.78	-3.78	14.4	
$Pd_{40}Ni_{40}P_{20}$	1.28	3.76	4.86	3.78	
$Pd_{46}Cu_{35,5}P_{18,5}$	1.33	3.85	3.43	3.37	
$Pt_{60}Ni_{15}P_{25}$	1.15	3.82	-2.28	8.92	
$Pd_{40}Cu_{40}P_{20}$	0.95	4.00	6.30	-0.204	

TABLE II. Parameters used to calculate  $C_{P,L}(T)$  and  $C_{P,x}(T)$  according to Eqs. (3) and (4).

those of other systems. Meanwhile, the specific curves in the present work do not deviate from those of other systems. However, owing to the limitation of temperatures available in an equilibrium liquid region ( $T_l = 979$  K), a single value was measured at 983 K. We deduce that the discrepancy between the literature<sup>18</sup> and our work is caused by the difference between the experimental methods used (i.e., the continuous scan mode in the literature<sup>18</sup> and the step scan mode in the present work). Regarding Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> liquid, the present result is in good accordance with that reported in Ref. 5 (solid blue line). On the other hand, the specific heat of the crystal phase was best fitted by Eq. (4) as<sup>5,23</sup>

$$C_{P,x}(T) = 3R + cT + dT^2.$$
 (4)

The coefficients *a*, *b*, *c*, and *d* are summarized in Table II for individual alloys, where in the case of Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> the specific heat difference  $\Delta C_{P,L-x}(T) = C_{P,L}(T) - C_{P,x}(T) = 1.273 + 3.027 \times 10^{-14}T + 5.021 \times 10^{6}T^{-2}$  J/mol K was cited from the literature<sup>21</sup> instead of determined by independent calculation for individual  $C_{P,L}(T)$  and  $C_{P,x}(T)$ . The free-energy difference  $\Delta G_{L-x}(T)$  between the liquid and crystalline phases was calculated using  $\Delta C_{P,L-x}(T)$  as

$$\Delta G_{L-x}(T) = (1 - T/T_m) \Delta H_m - \int_T^{T_m} \Delta C_{P,L-x} dT'$$
  
+  $T \int_T^{T_m} \Delta C_{P,L-x} / T' dT',$  (5)

where  $\Delta H_m$  is the enthalpy of fusion presented in Table I together with the entropy of fusion  $\Delta S_m = \Delta H_m/T_m$ . The  $\Delta G_{L-x}(T)$  curve was calculated as a function of the reduced temperature  $T/T_m$  and the result is shown in Fig. 3. With respect to Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub>, two curves are drawn according



FIG. 3. (Color online)  $\Delta G_{L-x}(T)$  of each BMG where, regarding Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> glass, it is cited from Ref. 21.

to the results of the present work and in the literature<sup>18</sup> for comparison. We notice that the  $\Delta G_{L-x}(T)$  curves of Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub> and quaternary Pd-Cu-Ni-P glasses show almost similar behaviors and they possess the lowest-energy difference (i.e., the smallest driving force to crystallization). On the other hand, Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> and Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> glasses exhibit fairly larger values than that of ribbon-form Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub> and Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> glasses with a lower GFA. This means that the GFA of Pd-P and Pt-P BMG's cannot be determined exclusively from the difference in  $\Delta G_{L-x}(T)$ , which is not in accordance with the prediction in the literature.<sup>3-5</sup>

#### C. Viscosity of liquid

The viscosities measured were well fitted by the Vogel-Fulcher-Tammann formula as

$$\eta = \eta_0 \exp\left(\frac{D^* T_0}{T - T_0}\right),\tag{6}$$

where the fitted parameters  $\eta_0$ ,  $D^*$ , and  $T_0$  are summarized in Table III. We used the viscosity of Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> liquid reported in the literature,<sup>24</sup> which was analyzed using a cluster model. Figure 4 shows an Angell plot<sup>25</sup> of viscosity against temperature, where  $T_g^*$ 's are summarized in Table III. Since carrying out the viscosity experiments on the ribbon-form Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub> glass with the same accuracy as the bulkform glasses was impossible, we substituted the viscosity of Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub> BMG for that of the ribbon-form Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub>



FIG. 4. (Color online) Angell plot of viscosity  $\eta(T)$  against  $T_g^*/T$ .

Glass	$\eta_0$ [Pa·s]	$D^*$	<i>T</i> <sub>0</sub> [K]	$T_g^*$ [K]	т
$Pd_{42.5}Cu_{30}Ni_{7.5}P_{20}$	$5.00 \times 10^{-6}$	16.5	379.0	536.0	59.1
$Pd_{43}Cu_{27}Ni_{10}P_{20}$ (Ref. 24)	_	_	_	569	65
$Pd_{40}Ni_{40}P_{20}$	$5.30 \times 10^{-6}$	22.1	356.0	553.8	48.4
$Pd_{46}Cu_{35} + P_{18} + S_{18} + S_$	$4.90 \times 10^{-5}$	17.0	362.6	527.0	52.3
$Pt_{60}Ni_{15}P_{25}$	$4.50 \times 10^{-6}$	13.8	345.0	464.0	67.6
$Pd_{775}Cu_6Si_{165}$ (Ref. 19)	0.0152	6.20	513.0	613.0	84.7
$Au_{76.9}Ge_{13.65}Si_{9.45}$ (Ref. 20)	0.0520	5.64	241.3	285.8	85.4

TABLE III. Parameters obtained by fitting the viscosity date to Eq. (6) and  $T_{a}^{*}$  and m.

glass. The identification of fragile and strong glass formers is generally performed using the fragility *m*, which was estimated according to Eq. (2) and summarized in Table III.  $Pd_{40}Ni_{40}P_{20}$ glass was the strongest glass former among all the glasses used in the present work. Also, we can see that the fragility is not proportional to  $d_{max}$ . The  $F_1$  parameter was calculated using Eq. (1) with *m* and  $T_{rg}$  and the result is shown in Table I.

## **IV. DISCUSSION**

From the results in the previous section, we can discuss the GFA of a glass system. Figure 5 shows plots of the logarithm of  $d_{\text{max}}$  against the  $T_{\text{rg}}$ ,  $\gamma$ , or  $F_1$  parameter. Although a moderate



FIG. 5. Plots of  $d_{\text{max}}$  against  $T_{\text{rg}}$ ,  $\gamma$  parameter and  $F_1$  parameter.

linear relation seems to be recognized from the relation of the logarithm of  $d_{\text{max}}$  versus  $\gamma$ , it seems to be poorly applicable to other parameters. Therefore, we search for another parameter that correlates to  $d_{\text{max}}$  from a fundamental aspect based on the thermodynamic consideration about the vitrification process. Following the classical nucleation theory (CNT), the steady-state homogeneous nucleation rate  $I_{\text{ss}}(T)$  and the energy barrier of nucleation  $\Delta G^*(T)$  are given by<sup>26</sup>

$$I_{\rm ss}(T) = \frac{A}{\eta(T)} \exp(-\Delta G^*/k_B T), \quad A \approx \frac{N_A}{V_M} \cdot \frac{k_B T}{3\pi a_0^2}, \quad (7)$$

$$\Delta G^*(T) = 16\pi \sigma_{\rm sL}^3 / 3[\Delta G_{L-x}(T)/V_M]^2, \qquad (8)$$

where  $k_B$  is the Boltzmann's constant,  $N_A$  is the Avogadro's constant, and  $a_0$  is the average atomic diameter calculated from the weighted sum  $r_G$  of Goldschmidt radii<sup>27</sup> for metallic elements and the atomic radius of P in tetrahedral covalent bonds. The  $a_0$  values are summarized in Table I together with the molar volume  $V_M$  for each alloy crystal.  $A \approx 10^{36}$  J/m<sup>5</sup> was obtained representatively at 600 K for all the glasses.  $\Delta G^*(T)$  is the free-energy barrier between the liquid and the crystal to be surmounted to form a nucleus with a critical size  $r^*(T)$  at a temperature T. It depends sensitively on the magnitude of the free-energy difference  $\sigma_{sL}$  at the nucleus-liquid interface as well as on  $\Delta G_{L-x}(T)$ .

# A. Interfacial free energy between nucleus and liquid

Spaepen and Meyer<sup>28</sup> calculated the surface tension (i.e., interfacial free energy) of the crystal-liquid interface at the melting point  $T_m$ . They obtained  $\sigma_g = \alpha_{\rm fcc} \Delta h_m$ , with  $\alpha_{\rm fcc} \approx 0.86$  for face-centered cubic (fcc) crystals, where  $\sigma_g$ and  $\Delta h_m$  are the tension and the heat of fusion per atom. Furthermore, on the basis of the statement by Miller and Chadwick<sup>29</sup> that the surface energy at  $T_m$  is higher than that obtained in an undercooled liquid, they proposed the temperature-dependent interfacial free energy  $\sigma_{\rm sL}(T)$  using the enthalpy of fusion  $\Delta H_m$  rather than  $\Delta h_m$  as

$$\sigma_{\rm sL}(T) = \frac{\alpha_{\rm fcc} \Delta H_m}{\left(N_A V_M^2\right)^{1/3}} \cdot \frac{T}{T_m}.$$
(9)

 $\alpha_{\rm fcc}$  was later extended to include body-centered cubic (bcc) crystals by Thompson and coworkers<sup>30,31</sup> and it gave  $\alpha_{\rm bcc} = 0.71$ . The crystallographic information on precipitates in Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> and Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glasses has been well examined. In Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> glass<sup>32</sup>, fcc-(Pd,Ni) solid solution, fcc-Pd<sub>2</sub>Ni<sub>2</sub>P, body-centered tetragonal (bct)-Ni<sub>3</sub>P,

and orthorhombic crystals appeared after crystallization, and the precipitates of Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glass<sup>33</sup> were composed of ordered Cu<sub>3</sub>Au-type Cu<sub>3</sub>Pd, Cu<sub>5</sub>Pd<sub>3</sub>P<sub>2</sub> (Pd<sub>4</sub>Se-type simple tetragonal structure<sup>34</sup>), fcc-Pd<sub>2</sub>Ni<sub>2</sub>P and orthorhombic Pd<sub>15</sub>P<sub>2</sub>. According to the results of x-ray diffraction analysis, the Bragg peaks appearing in the crystallized  $Pd_{46}Cu_{35,5}P_{18,5}$ alloy were mostly attributed to tetragonal Cu<sub>5</sub>Pd<sub>3</sub>P<sub>2</sub>. However, it is possible that the diffraction peaks of any fcc-type crystals, as observed in the Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> alloy, are hidden in the diffraction pattern of the crystallized Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub> alloy. The precipitates in the crystallized Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub><sup>35</sup> alloy are composed of an fcc-Pd solid solution and orthorhombic Pd<sub>3</sub>Si. Regarding Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glass<sup>20</sup>, fcc-gold and complex intermetallic compounds were reported as precipitates. The crystallographic data of crystal phases precipitated in Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> glass seem to be nonavailable. Thus, we worked on  $Pd_{40}Ni_{40}P_{20}$  BMG with the highest  $T_m = 875$  K among the present BMG's to examine the effect of interfacial free energy on  $I_{ss}(T)$ . Kui *et al.* predicted<sup>12</sup> that the maximum value  $I_{ss}^{max}$  of a Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> glass sufficiently treated with a B<sub>2</sub>O<sub>3</sub> flux is less than 10<sup>5</sup> m<sup>-3</sup> s<sup>-1</sup>. Using Eqs. (6)–(9),  $I_{ss}^{max} \approx 10^8 \text{ m}^{-3} \text{ s}^{-1}$  ( $\alpha_{bcc} = 0.71$ ) and  $I_{ss}^{max} \approx 10^{-2} \text{ m}^{-3} \text{ s}^{-1}$  $(\alpha_{\rm fcc} = 0.86)$  were obtained. The calculation with  $\alpha_{\rm bcc}$  is close to that predicted in the literature, but is somewhat larger. Accordingly, we regarded  $\alpha$  as an adjustable parameter to reproduce the  $I_{ss}^{max}$  predicted for  $Pd_{40}Ni_{40}P_{20}$  glass and  $\alpha \approx 0.76$  was determined. No bcc phase was reported in the Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> alloy and more complex crystal structures were visualized. Although a complex crystal structure is expected to possess a smaller  $\alpha$  than  $\alpha_{bcc}$ , the previous result suggests that any crystal structure except fcc crystals can be approximated to have the same  $\alpha$  as the bcc crystals. It is explained that the somewhat higher value  $\alpha \approx 0.76$  may be caused by the precipitation of any fcc crystals. Eventually, throughout the present study,  $\alpha \approx 0.76$  was used to evaluate the  $I_{ss}(T)$  of glass systems except  $Pt_{60}Ni_{15}P_{25}$  glass, whereas  $\alpha_{bcc} = 0.71$  was applied only to this alloy because of the lack of reports on the precipitation of fcc crystals. The  $\sigma_{\rm sL}(T)$  curves are plotted against  $T/T_m$  in Fig. 6 for all the glasses together with Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> and Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glasses. Although  $\sigma_{sL}(T)$  is very small for Pd-Cu-Ni-P<sub>20</sub> glasses, they have a large  $d_{max}$  and are the best glass former in all the glasses investigated. This is due to the fact that  $\Delta G_{L-x}(T)$  is also small for these alloy systems. We show the quantity  $\Delta G^*(T)/k_BT$  at  $T = T_{\text{max}}$  in the Table IV, where  $\Delta G^*$  is the energy barrier height for



FIG. 6. (Color online) Interfacial free-energy curves  $\sigma_{sL}(T)$  illustrated as functions of  $T/T_m$ .

the critical nucleus formation and  $T_{\text{max}}$  is the temperature that gives the maximum value of  $I_{\text{ss}}(T)$ .  $\Delta G^*(T)/k_B T_{\text{max}}$  is largest, 60.0, for two quaternary Pd-P-based glasses among all the glasses. As given in Eq. (8),  $\Delta G^*(T)$  is determined by the competition between  $\sigma_{\text{sL}}(T)$  and  $\Delta G_{L-x}(T)$ . Therefore, we conclude that the smallness of  $\sigma_{\text{sL}}(T)$  does not decisively influence the degradation of GFA as seen for these glass systems.

Although the available calculation of  $\sigma_{sL}$  is, so far, limited to fcc and bcc crystal structures, its application to the hexagonal closed packed (hcp) crystal structure may be physically acceptable because of the same atomic packing fraction as the fcc crystal structure, and it gives the result  $\alpha_{hcp} = \alpha_{fcc}$ . With respect to other crystalline systems, we approximated their  $\alpha$ 's as 0.71 (the same as  $\alpha_{bcc}$ ). This will somewhat oversimplify the actual  $\alpha$ 's of any complex crystallize phases, which are expected to be smaller than  $\alpha_{bcc}$ . Therefore, the estimation of  $\sigma_{sL}$  gave an upper limit to the actual value, in the present study, and it resulted in an under limit of  $I_{ss}(T)$  calculated.

TABLE IV. The maximum energy barrier  $\Delta G_{\text{max}}^*/k_B \cdot T_{\text{max}}$  for the formation of a critical nucleus and the maximum nucleation rate  $I_{\text{ss}}^{\text{max}}$  together with  $t_n$ ,  $T_n$ , and  $R_c^h$ .

Glass	$T_{\rm max}$ [K]	$\Delta G^*_{ m max}/k_B \cdot T_{ m max}$	$I_{\rm ss}^{\rm max} \ [{ m m}^{-3}  { m s}^{-1}]$	$T_n$ [K]	$t_n$ [s]	$R_c^h$ [Ks <sup>-1</sup> ]
Pd <sub>42.5</sub> Cu <sub>30</sub> Ni <sub>7.5</sub> P <sub>20</sub>	517	60.0	$1.27 \times 10^{-4}$	568	$9.03 \times 10^{9}$	$2.51 \times 10^{-8}$
$Pd_{43}Cu_{27}Ni_{10}P_{20}$	510	60.0	$5.26 \times 10^{-9}$	578	$2.10 \times 10^{13}$	_
$Pd_{40}Ni_{40}P_{20}$	525	38.1	$1.18 \times 10^{5}$	591	$7.41 \times 10^{7}$	$3.83 \times 10^{-6}$
Pd <sub>46</sub> Cu <sub>35.5</sub> P <sub>18.5</sub>	526	46.3	$2.70 \times 10^{4}$	584	$4.38 \times 10^{6}$	$5.95 \times 10^{-5}$
Pt <sub>60</sub> Ni <sub>15</sub> P <sub>25</sub>	459	53.3	$5.90 \times 10^{4}$	510	$2.66 \times 10^{6}$	$9.20 \times 10^{-5}$
$Pd_{40}Cu_{40}P_{20}$	531	32.8	$4.88 \times 10^{10}$	597	$3.74 \times 10^{4}$	$7.60 \times 10^{-3}$
Pd <sub>77.5</sub> Cu <sub>6</sub> Si <sub>16.5</sub>	642	32.7	$2.68 \times 10^{13}$	700	245	1.30
Au <sub>76.9</sub> Ge <sub>13.65</sub> Si <sub>9.45</sub>	317	25.7	$1.85 \times 10^{19}$	356	0.451	596



FIG. 7. (Color online) Plot of homogeneous steady-state nucleation rate  $I_{ss}(T)$  against  $T/T_m$ .

# B. $I_{SS}(T), u_c(T)$ and $R_c^h$

First, we examine the validity of CNT against the present work. According to Eqs. (5) and (9), we can calculate the critical size  $r^*(T_n) = 2\sigma_{sL}(T_n)V_M / \Delta G_{L-x}(T_n)$  of cluster nuclei and the number  $N_c(T_n) \approx (r^*/r_G)^3$  of atoms in the cluster at the temperature. The  $r^*(T_n)$  values ranged from 0.58 (Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub>) to 1.2 nm (Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub>) and they corresponded to  $N_c(T_n) \approx 70$  and  $N_c(T_n) \approx 800$  atoms, respectively. Trudu et al.<sup>36</sup> concluded from their computer simulation results that the crystallization process in a deep undercooled region could be controlled by a spinodal decomposition process due to the instability of the liquid phase instead of by a traditional nucleation and growth process because the density fluctuation in a liquid induces the spontaneous formation of the nucleus when the cluster size becomes much smaller. On the basis of this concept, Leyssale et al.<sup>37</sup> examined the validity of CNT to explain the kinematical behavior of nucleus formation and its morphology. They reported that the computer simulation result is consistent with the result obtained using CNT down to the size of a nucleus with about 40 molecules. The smallest number,  $N_c(T_n) \approx 70$ , of atoms for Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glass in the present work is larger than the critical number predicted. Thus we conclude that CNT analysis is suitable for discussing the thermodynamic stability of molten alloys prepared with B<sub>2</sub>O<sub>3</sub> flux.

The  $I_{ss}$  (*T*) curves calculated are presented as functions of  $T/T_m$  in Fig. 7. They are classified roughly into three groups: (a) Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> and Pd<sub>46</sub>Cu<sub>35.5</sub>P<sub>18.5</sub> glasses have compatible  $I_{ss}^{max}$  with Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> glass; (b) the  $I_{ss}^{max}$  of Pd<sub>40</sub>Cu<sub>40</sub>P<sub>20</sub> glass is much larger than that of Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub> glass and compatible with those of Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> and Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glasses; and (c)  $I_{ss}^{max}$  values are extremely small for quaternary Pd-P-based glasses (i.e., only on the order of magnitude of  $10^{-4}$  to  $10^{-9}$  m<sup>-3</sup> s<sup>-1</sup>. These values are much smaller than  $I_{ss}^{max} \approx 10^5$  m<sup>-3</sup> s<sup>-1</sup> calculated for Pd<sub>40</sub>Cu<sub>30</sub>Ni<sub>10</sub>P<sub>20</sub> glass<sup>38</sup> with a semiempirical expression of  $\Delta G^*(T)$ . The  $\Delta G_{max}^*/k_B \cdot T_{max}$  values are summarized in Table IV together with  $I_{ss}^{max}$ , where  $T_{max}$  denotes the temperature that gives  $I_{ss}^{max}$ .





FIG. 8. (Color online) Plot of growth rate  $u_c(T)$  against  $T/T_m$ .

We notice that both  $I_{ss}^{max}$  and  $\Delta G_{max}^*$  cannot reproduce well the sequence of the magnitude of  $d_{max}$ .

It is evident that a nucleus with a remarkable low growth rate cannot develop in size. Therefore, it is important to examine the growth rate  $u_c(T)$  as well as  $I_{ss}(T)$  during the vitrification of molten alloys. Equation (10) gives the steady-state growth rate<sup>27</sup> of the nucleus as a function of temperature

$$u_c(T) = f \frac{D}{a_0} \left[ 1 - \exp\left(-\frac{\Delta G_{L-x}}{RT}\right) \right], \quad D = \frac{k_B T}{3\pi a_0 \eta(T)},$$
(10)

where the coefficient f is approximately given<sup>28</sup> as  $f \approx$  $0.2(T_m - T)/T_m$  under the condition  $\Delta S_m < 2R$ . As seen in Table I, this constraint was satisfied for all the alloy systems. Using  $\Delta G_{L-x}(T)$  and  $\eta(T)$ ,  $u_c(T)$  was calculated and the result is illustrated in Fig. 8. The  $u_c^{\text{max}}$  values ranged from  $10^{-6}$  to  $10^{-4}$  ms<sup>-1</sup> among the present alloy systems. The smallest  $u_c^{\text{max}}$  is realized in  $Pd_{42.5}Cu_{30}Ni_{7.5}P_{20}$  glass, but it is much larger than  $u_c^{\text{max}} \approx 5 \times 10^{-9} \text{ ms}^{-1}$  obtained empirically for Pd<sub>40</sub>Cu<sub>30</sub>Ni<sub>10</sub>P<sub>20</sub> glass.<sup>38</sup> We readily notice that the  $u_c(T)$  of Pt<sub>60</sub>Ni<sub>15</sub>P<sub>25</sub> glass takes large values over a wide temperature range. This means that the introduction of a small number of crystalline embryos and/or heterogeneous nucleation sites would promote the rapid growth of the crystal phase because this system inherently possesses a smaller  $I_{ss}^{max}$ , comparable with that of  $Pd_{40}Ni_{40}P_{20}$  glass, as seen in Fig. 7. The  $u_c$  of Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> glass was relatively large in the vicinity of  $T_m$ , but it became smallest at approximately  $T_p$ and such a feature may be based on a peculiar temperature dependence of viscosity, as will be mentioned later. Drehman and Greer<sup>11</sup> measured the maximum steady-state nucleation rate  $I_{ss}^{max}$ , an order of magnitude of  $10^4 - 10^6 \text{ m}^{-3} \text{ s}^{-1}$  for  $Pd_{40}Ni_{40}P_{20}$  glass. On the basis of this value, they derived  $u_c^{\text{max}} \approx 10^{-10} \text{ ms}^{-1}$ . In the present work,  $u_c$  was calculated using only experimental values for  $\Delta G_{L-x}$  and  $\eta$  in Eq. (10), and eventually  $u_c^{\max} \approx 10^{-6} \text{ ms}^{-1}$  was obtained as shown in Fig. 8. Accordingly,  $u_c^{\max} \approx 10^{-10} \text{ ms}^{-1}$  in the literature<sup>12</sup> seems to be much smaller than that in the present work. Nishiyama and Inoue<sup>9</sup> measured  $u_c \approx 3.2 \times 10^{-7} \text{ ms}^{-1}$  from



FIG. 9. (Color online) TTT diagram calculated using  $I_{ss}(T)$  and  $u_c(T)$  together with the cooling curve of Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> melt.

the optical observation of a cross section of  $Pd_{42.5}Cu_{30}Ni_{7.5}P_{20}$ glass partially devitrified at 683 K, which is slightly higher than  $T_x$ . This value is compatible with the present result (i.e.,  $u_c \approx 1.1 \times 10^{-7} \text{ ms}^{-1}$  at 683 K). Also, it is evident that  $u_c^{\text{max}}$  is not in agreement with the sequence of the magnitude of  $d_{\text{max}}$ .

Using  $I_{ss}(T)$  and  $u_c(T)$ , we can evaluate the critical cooling rate  $R_c^h$  through the equation<sup>39</sup>  $X(t) \approx \frac{1}{3}\pi I_{ss}(T)u_c^3(T)t^4$ , where X(t) denotes the crystallized fraction at time t. The temperature-time-transformation (TTT) curve was derived with  $X = 10^{-6}$  and the result is shown in Fig. 9. To estimate  $R_c^h$ , the cooling curve of a liquid was drawn in the figure, as illustrated representatively for Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glass. The contact of the cooling curve with the nose of the TTT curve gave the time  $t_n = 0.45$  s and the temperature  $T_n = 357$  K and we could estimate  $R_c^h = (T_m - T_n)/t_n \approx 6.0 \times 10^2$  Ks<sup>-1</sup> for this case. Such an estimate was performed similarly for other glass systems, and the  $R_c^h$  values obtained are summarized in Table IV together with  $t_n$  and  $T_n$ . The relationship





FIG. 11. Comparison of the  $\eta(T)$  curve of Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glass with that of Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> glass.

between  $R_c^h$  and  $d_{max}$  is plotted in Fig. 10 and is well described by

$$\log_{10} \left( R_c^h \right) = (-3.2 \pm 0.3) \log_{10}(d_{\max}) - 1.0 \pm 0.3.$$
(11)

We can see a distinct linear relation between  $\log_{10}(R_c^h)$ and  $\log_{10}(d_{\text{max}})$  (i.e., roughly  $R_c^h \approx d_{\text{max}}^{-3}/10 \text{ mm}^3 \text{ Ks}^{-1}$ ). Kiminami and Sahm<sup>22</sup> concluded that the vitrification process of Pd<sub>77.5</sub>Cu<sub>6.0</sub>Si<sub>16.5</sub> glass is predominantly controlled by a homogeneous nucleation and growth mechanism. The present result indicates the validity of their conclusion. A similar consideration will be true for Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> glass made by the splat cooling method.<sup>19</sup>

In the present study, a  $Pd_{43}Cu_{27}Ni_{10}P_{20}$  glass showed the smallest  $R_c^h$ , and  $d_{\text{max}}$  will be the largest of all the glasses examined, although it is actually unverified. The conclusion is mostly attributed to the smallest  $I_{ss}^{max}$  of this glassy system. As shown in Table IV, the  $\Delta G^*_{max}/k_B \cdot T_{max}$  values are the same for both Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> and Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glasses at  $T_{\text{max}}$ . As a consequence, the difference in  $I_{\text{ss}}^{\text{max}}$  is ascribed to the difference in the viscosity. The viscosity curves of both glasses are shown as functions of temperature in Fig. 11. The viscosity of Pd<sub>43</sub>Cu<sub>27</sub>Ni<sub>10</sub>P<sub>20</sub> glass is larger by an order of magnitude of  $10^3$  Pa s at approximately  $T_g \approx 570$  K than Pd<sub>42.5</sub>Cu<sub>30</sub>Ni<sub>7.5</sub>P<sub>20</sub> glass. Although Kato et al.<sup>15</sup> and Fan et al.<sup>24</sup> employed different methods to measure viscosity, thermal conditions applied to both glass systems were then mostly similar. It is difficult for us to strictly control the composition of any Pd-Cu-Ni-P alloy because of the high vapor pressure and low melting temperature of P atoms and the easy formation of P oxides. It is possible that the two glass systems possess a larger fluctuation in local composition or topological disorder than expected from the difference in their nominal compositions, which affected the behavior of the viscosity at approximately  $T_g$ .

### **V. CONCLUSION**

FIG. 10. Plot of critical cooling rate  $R_c^h$  against  $d_{max}$ . Solid circles denote the data obtained from the present work and open triangle and diamond represent Au<sub>76.9</sub>Ge<sub>13.65</sub>Si<sub>9.45</sub> and Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> glass, respectively.

To elucidate the GFA of water-quenched BMG's such as ternary  $Pd_{40}Ni_{40}P_{20}$ ,  $Pd_{46}Cu_{35.5}P_{18.5}$ ,  $Pt_{60}Ni_{15}P_{25}$  and quaternary  $Pd_{43}Cu_{27}Ni_{10}P_{20}$ ,  $Pd_{42.5}Cu_{30}Ni_{7.5}P_{20}$  as well as melt-spun  $Pd_{40}Cu_{40}P_{20}$  ribbons, the validity of the thermodynamic approach in terms of the CNT was examined. The

water-quenched BMG's used in this work were sufficiently treated with a dehydrated B<sub>2</sub>O<sub>3</sub> flux prior to and while quenching the melt so that the heterogeneous nucleation and growth sites were mostly removed from the melts. Accordingly, the vitrification process was dominated by a homogenous nucleation and growth mechanism. No available parameter such as such as the  $T_{\rm rg}$ ,  $\gamma$  parameter or  $F_1$ parameter reproduced the sequence of the magnitude of  $d_{\rm max}$ experimentally obtained. Similarly, individual thermodynamic quantities such as  $I_{\rm ss}^{\rm max}$ ,  $\omega G_{\rm max}^*$ ,  $\Delta G_{L-x}^*$ , and  $\sigma_{\rm sL}$  were useless to interpret the sequence of the magnitude of  $d_{\rm max}$ . The only strong correlation appeared in the relation between  $\log_{10}(R_c^h)$  and  $\log_{10}(d_{\rm max})$ , roughly  $R_c^h \approx d_{\rm max}^{-3}/10$  mm<sup>3</sup> Ks<sup>-1</sup>, where the critical cooling rate  $R_c^h$  was estimated from the cooling curve of the melt and the TTT curve calculated by taking account of the homogeneous nucleation theory on the vitrification of molten alloys. We conclude that the GFA of a glass system should be estimated in terms of the "ideal" critical cooling rate calculated from the homogeneous steady-state nucleation and growth because it is an intrinsic property of individual alloy systems.

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