NMR and NQR study of the tetrahedral frustrated quantum spin system $Cu₂Te₂O₅Br₂$ in its **paramagnetic phase**

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The quantum antiferromagnet $Cu_2Te_2O_5Br_2$ was investigated by NMR and nuclear quadrupole resonance (NQR). The 125 Te NMR investigation showed that there is a magnetic transition around 10.5 K at 9 T, in agreement with previous studies. From the divergence of the spin-lattice relaxation rate, we ruled out the possibility that the transition could be governed by a one-dimensional divergence of the spin-spin correlation function. The observed anisotropy of the ¹²⁵Te shift was shown to be due to a spin polarization of the 5*s*² "E" doublet of the $[TeO_3E]$ tetrahedra, highlighting the importance of tellurium in the exchange paths. In the paramagnetic state, Br NQR and NMR measurements led to the determination of the Br hyperfine coupling and the electric field gradient tensor, and to the spin polarization of Br *p* orbitals. The results demonstrate the crucial role of bromine in the interaction paths between Cu spins.

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I. INTRODUCTION

In quantum antiferromagnets, triangular or tetrahedral coordination generates strong frustration. Unusual singlet ground states deriving from this frustration have been theoretically predicted and actively searched for in the recent years, mainly on Kagome or pyrochlore systems, in which the frustrated units (triangle or tetrahedra) are sharing corners. A different type of geometry, in which the tetrahedra units are isolated, and only weakly coupled has been discovered with the compounds $Cu_2Te_2O_5X_2$ $(X=Br,Cl),$ ^{[1](#page-5-2)} which contain tetrahedral clusters of Cu^{2+} $(S = \frac{1}{2})$ in a distorted square planar $CuO₃X$ coordination. These tetrahedra align to form chains along the $[001]$ direction, and are separated along the $[100]$ and $[010]$ directions by different Te-O coordinations[.2](#page-5-3) Although the ground state of individual tetrahedron is expected to be a singlet quasi-zero-dimensional system), it turns out that, below about 12 K (18 K for the Cl compound), the intertetrahedra couplings lead to an incommensurate magnetic ground state with anomalous thermody-namics properties.^{3[,4](#page-5-5)} To determine relevant dimensionality of the system several different models were considered. These include: quasi-one-dimensional (1D) ones, assuming an interaction between tetrahedra along the c axis;^{5–[7](#page-6-0)} quasi-twodimensional consisting of interacting frustrated plaquettes in the *ab* plane, in which intertetrahedra couplings are assumed to be important; $8-10$ and models of a three-dimensional (3D) tetrahedral cluster-spin system. $11,12$ $11,12$ Despite all these studies, the exact dimensionality of the system remains unclear. Nevertheless, the results of Jensen *et al.* and Jagličić *et al.* appear to favor a 3D over 1D nature of the magnetic transition.¹³⁻¹⁵ It is likely that both the intratetrahedral (and thus the frustration), leading to a creation of spin gaps, and the intertetrahedral interactions, inducing a magnetic long-range order, are present and compete together.

One of the important unsettled questions is the relative strength of the various exchange couplings within and between tetrahedra, which determine the dimensionality of the system. In this paper, we present NMR and nuclear quadrupole resonance (NQR) measurements performed on single crystals of $Cu_2Te_2O_5Br_2$. The purpose of this study was to address the question of the magnetic phase dimensionality via an investigation in the vicinity of the phase transition and to determine the spin polarization of the Cu ligands. One challenge that came along was the rather intricate assignment of the various NMR transitions possible in this system.

II. TELLURIUM NMR

A. Spectrum structure

Tellurium has two NMR-active isotopes and both have a spin- $\frac{1}{2}$ nucleus but the natural abundance of ¹²⁵Te is about eight times higher than the one of 125 Te. For this reason, all Te NMR measurements were performed on ¹²⁵Te. $Cu₂Te₂O₅Br₂$ crystalizes in the $P\overline{4}$ $(a=b=7.8 \text{ Å}, c)$ $=6.4$ Å) space group, meaning that the elementary pattern $CuTeO_{2.5}Br$ is present four times in each unit cell. As a consequence, although 125 Te has a spin- $\frac{1}{2}$ nucleus and therefore yields to a single resonance line, the crystal has four inequivalent Te sites for an arbitrary orientation with respect to the direction of the external magnetic field B_0 . Thus, the ¹²⁵Te NMR spectrum in Cu₂Te₂O₅Br₂ is generally composed of four lines. However, by applying the field in the *ab* plane, two sites become equivalent, while applying it along the *c* axis, all four sites become equivalent (see Fig. [1;](#page-1-0) for a full description of the crystal symmetry, see, e.g., the article of Johnsson *et al.*^{[1](#page-5-2)}).

FIG. 1. Schematic views of the $Cu_2Te_2O_5Br_2$ structure along the [001] axis (a) and the $[\overline{1}10]$ axis (b). Copper atoms (small spheres) are interconnected to emphasize the tetrahedral configuration. Tellurium atoms (not represented) are placed inside the sketched " O_3E " tetrahedra, E representing the $5s^2$ lone pair of the Te atom $(Ref. 1).$ $(Ref. 1).$ $(Ref. 1).$

B. Hyperfine shift

The temperature dependence of the electron spin susceptibility of $Cu_2Te_2O_5Br_2$ has been extensively studied by means of dc and ac susceptometry.^{1,[2](#page-5-3)[,13,](#page-6-5)[14](#page-6-7)[,16](#page-6-8)} NMR measurements provide a way to probe the local electron spin susceptibility through hyperfine interactions with the advantage of being essentially insensitive to paramagnetic impurities. This is of particular interest for probing magnetic systems at low temperature when the contribution from paramagnetic impurities becomes larger than the system intrinsic susceptibility. The temperature dependence of the resonance frequencies, proportional to the macroscopic spin susceptibility, of the four inequivalent 125Te nuclear spins in the crystal and their temperature dependence measured in a field of 9 T parallel to a direction nearly parallel to $[110]$ is shown in Fig. [2.](#page-1-1) The data are superimposed to the superconducting quantum interference device (SQUID) susceptibility measurements performed with a field of 0.1 T oriented along [110] on the same single crystal.

The data plotted in Fig. [2](#page-1-1) allow for the determination of the 125 Te hyperfine coupling by comparing the temperature dependence of the NMR frequencies to the temperature dependence of the magnetic susceptibility as shown in Fig. [3.](#page-1-2) In doing so, we took advantage of the multiple sites, and thus the multiple resonances, to determine the zero-shift frequency as the extrapolated frequency at which all sites have the same resonance frequency, in the present case f_0 \approx 121.5 MHz. This value corresponds to the ¹²⁵Te frequency for which the contribution of the Cu electron spins

FIG. 2. Temperature dependence of the shift of the four inequivalent ¹²⁵Te nuclear spins measured in a field of 9 T almost parallel to [110] superimposed to the SQUID susceptibility measurements (line). The existence of four NMR lines is due to a slight misorientation of the field out of the *ab* plane.

polarization is zero. Note however that it is not the resonance frequency of the "bare" 125 Te nuclear spin [121.07 MHz $(Ref. 17)$ $(Ref. 17)$ $(Ref. 17)$] since the Te electron shells also shift (essentially isotropically) the resonance. We observe here that this shift is about 0.35%, which is in the range of the observed shifts in transition-metal tellurides. 17 Conjunctively, the dependence of the NMR frequencies on the crystal orientation (see Fig. [4](#page-2-0)) yields to the full determination of the hyperfine tensor. From the data shown in Fig. [4,](#page-2-0) we deduced that the tellurium hyperfine shift (reflecting the spin susceptibility) is mainly isotropic with a small anisotropic part in the *ab* plane along a principal axis nearly parallel to the $[110]$ direction. Assuming an environment of axial symmetry (i.e., neglecting a small anisotropy in the plane perpendicular to $[110]$), we can define the hyperfine shift along the external magnetic field \mathbf{B}_0 as $K(\theta) = K_{iso} + K_{ax}(3 \cos^2 \theta - 1)/2$, where θ is the angle between B_0 and the principal anisotropy axis of the Knight shift tensor **K**, K_{iso} the isotropic part of **K** and K_{ax} its anisotropic part along the principal anisotropy axis. The data lead to $K_{iso} = 3.2$ T/ μ_B and $K_{ax} = 0.8$ T/ μ_B . A simple computa-

FIG. 3. (Color online) Linear relationship between the shift of the four inequivalent 125 Te nuclear spins measured in a field of 9 T almost parallel to $[110]$ and the SQUID susceptibility. The calculation of the slopes lead to the determination of the hyperfine field.

FIG. 4. Crystal orientation dependence of the 125 Te hyperfine field measured at 15 K and 9.4 T. The crystal was aligned to obtain only two resonance peaks in the *ab* plane (with this orientation, the filled diamonds and the filled triangles in Figs. [2](#page-1-1) and [3](#page-1-2) would be indistinguishable from the open diamonds and the open triangles, respectively). Inset: dipolar field calculated for a Te orbital pointing toward the center of the Br-Br axis.

tion of the dipolar contribution of a single Cu electron spin cannot account for either the amplitude, which is eight times weaker than the observed value, nor the angular dependence shown in Fig. [4.](#page-2-0) Considering transferred polarization on Br atoms cannot account for our observations as well. However, the measured angular dependence can be well described by considering the contribution of a Te orbital pointing toward the center of the Br-Br axis (see simulation shown in the inset of Fig. [4](#page-2-0)). Johnsson *et al.* pointed out that the Te atom is placed at the center of the O_3E tetrahedron, where E represents the $5s²$ lone pair of the Te atom.¹ As shown in Fig. $1(b)$ $1(b)$, the "E" apex of the tetrahedron stands in between two bromine atoms along the *c* axis and the E orbital should therefore point in the $[110]$ direction. Our results thus suggest that part of the spin polarization is located in this orbital. This observation is fully compatible with the description of Johnsson *et al.* who suggest that the E orbital participates in the electronic structure binding the two neighboring Br atoms along the *c* axis[.1](#page-5-2)

A quantitative estimation of this contribution is more delicate. First, it should be noted that a nearly axial symmetry around the $[110]$ direction is not compatible with a transfer of polarization from the three oxygen forming the tetrahedral environment of the tellurium atom, the E orbital being the fourth corner. In order to respect the symmetry, all three oxygen atoms should equally contribute, which is highly unlikely as their local environment differs dramatically from one another (see Fig. [5](#page-2-1)). Assuming that the E orbital can be described by a superposition of 5s and 5p orbitals (the tetrahedral symmetry of tellurium site suggests a $sp³$ hybridization) with one sp^3 orbital pointing in the [110] direction, we can write that $K_{ax} = 6/5f_p\mu B(r^{-3})$, where f_p is the fraction of unpaired electron in the corresponding orbital and $\langle r^{-3} \rangle$ is the mean value of $1/r^3$ over the 5*p* orbital. By taking $\langle r^{-3} \rangle$ $=104\times10^{24}$ cm⁻³,^{[18](#page-6-10)} one finds that $f_p=0.7\%$. Similarly, from $K_{iso} = 8\pi/3f_s\mu_B \langle |\Psi(0)|^2 \rangle$, with $\langle |\Psi(0)|^2 \rangle$ being the square of the *s*-wave function at the nucleus averaged over those elec-

FIG. 5. Schematic view of the $Cu_2Te_2O_5Br_2$ structure along the [100] axis. Oxygen atoms (smallest spheres) are displayed and dashed lines show the exchange paths proposed by Ref. [9.](#page-6-11)

trons at the Fermi surface, one can estimate the spin density in the 5*s* contribution to sp^3 orbital to give a contact term consistent with the isotropic spin part. Knowing that in an ideal $sp³$ orbital the *s* contribution is 4 times smaller than in pure *s* orbital, by taking the value given by Morton,¹⁸ i.e., $\langle |\Psi(0)|^2 \rangle = \frac{1}{4} \times 170 \times 10^{24}$ cm⁻³, one finds $f_s = 0.96\%$. This value is nearly identical to the value of f_p determined from dipolar contribution, which confirms this description in terms of sp^3 orbital.

In conclusion, this contribution from the E orbital well describes the measurements. In addition, only a small spin polarization is needed in the Te E doublet to quantitatively account for the data. One should note that this interpretation is not compatible with the model proposed by Whangbo *et al.* in which the interactions between tetrahedral clusters are presumably from two types of supersuperexchange paths:⁹ one is Cu-O-O-Cu path in the *c* direction and the other Cu-Br-Br-Cu path in the *ab* plane with a path Cu-Br-Br-Cu[.9](#page-6-11) Our results suggest that the relevant path is Cu-Br-E-Br-Cu in the *c* direction.

C. Magnetic phase transition

It has been reported in an earlier study that the system undergoes a magnetic transition at a temperature T_C of about 12 K in an external magnetic field of 9 $T²$ In the present study, we observe that the 125 Te resonance line suddenly disappears, as the temperature is lowered toward T_c . Although it was possible to observe the resonance at temperatures very close to $T_c = 12$ K, we were not able to observe the signal at temperatures below the magnetic transition temperature. This might be due to a significant broadening of the line, a strong shortening of the spin-spin relaxation time, a very large frequency shift or possibly a combination of these effects.

The temperature dependence of the 125 Te spin-lattice relaxation time measured on the lowest-frequency resonance in a field of 9 T along a direction nearly parallel to $[110]$ is shown in Fig. [6.](#page-3-0) The ¹²⁵Te spin-lattice relaxation rate decreases with decreasing temperature for temperatures below 100 K but abruptly increases around 12 K. Such a dramatic change in spin-lattice relaxation rate is an evidence for strong local field fluctuations and therefore for a magnetic transition. The occurrence of a divergence in the 125 Te spinlattice relaxation rate within a narrow region of a few kelvin

FIG. 6. Temperature dependence of the 125 Te spin-lattice relaxation rate measured at 9 T on the lowest-frequency resonance filled diamonds in Figs. 2 and 3).

above T_c unambiguously shows the three-dimensional character of the magnetic system. In a quasi-one-dimensional system, the fluctuations would extend on a temperature range comparable to T_C . The transition temperature deduced from these measurements is $T_C = 10.5$ K, which is slightly lower than the value determined by Lemmens *et al.*[2](#page-5-3)

III. BROMINE NMR AND NQR IN THE PARAMAGNETIC STATE

Halogen nuclei have a large quadrupole moment and they have been extensively studied by NQR.¹⁹ NQR frequencies strongly depend on the ionic character of the *M*-*X* bond where *M* is a metal ion and *X* is the halogen ion.²⁰ Both bromine isotopes have a spin-3/2 nucleus and ^{79}Br and ^{81}Br have almost equivalent natural abundance (Br nuclear prop-erties are summarized in Table [I](#page-3-1)). $Cu_2Te_2O_5Br_2$ contains tetrahedral arrangements of Cu atoms each one of them placed at the center of a distorted square $CuO₃Br$. As shown in Fig. [1](#page-5-2) (see also Ref. 1), copper-bromine bonds are almost perpendicular to the *c* axis of the crystal $(90^{\circ} \pm 4.42^{\circ})$. While Cu-Br and Cu_{iii}-Br_{iii} are nearly parallel to the [110] direction, $Cu_i - Cu_{ii} - Cu_{ii}$ are nearly parallel to the $[1\bar{1}0]$ one. As for tellurium, there are four inequivalent Br sites, which reduce to two inequivalent sites when the direction of B_0 is in the *ab* plane, and to one single site if B_0 is parallel to the *c* axis.

The total Hamiltonian of a Br nuclear spin in the $Cu₂Te₂O₅Br₂$ paramagnetic phase can be written as

FIG. 7. Br NQR spectrum measured at 15 K. The intensities have been divided by the square of the frequency. Note that the slight splitting observed on both lines is due to the presence of a residual nonzero B_0 field in the superconducting coil.

$$
\hat{\mathcal{H}} = -\gamma_n \hbar \mathbf{B}_0 \cdot \mathbf{I} - \gamma_n \hbar \mathbf{B}_0 \cdot \mathbf{K} \cdot \mathbf{I} + \frac{eQ}{2I(2I-1)} \mathbf{I} \cdot \mathbf{V} \cdot \mathbf{I}, \tag{1}
$$

where the first term is the nuclear Zeeman Hamiltonian, the second term is the hyperfine Hamiltonian with **K** the Knight shift tensor, and the third term is the quadrupole Hamiltonian, in which *e* is the elementary charge, *Q* is the quadrupole moment and V is the electric field gradient (EFG) tensor. In its principal axis coordinate system (X, Y, Z) , the electric field gradient is diagonal and traceless. In this particular frame, Eq. (1) (1) (1) can be rewritten as

$$
\hat{\mathcal{H}} = -\gamma_n \hbar \mathbf{B}_0 \cdot \mathbf{I} - \gamma_n \hbar \mathbf{B}_0 \cdot \mathbf{K} \cdot \mathbf{I}
$$

+
$$
\frac{1}{6} \nu_Q \left[3I_Z^2 - I(I+1) + \frac{\eta}{2} (I_+^2 + I_-^2) \right],
$$
 (2)

where $\eta = (V_{XX} - V_{YY})/V_{ZZ}$ is the asymmetry parameter of the electric field gradients, and $I_+ = I_X + iI_Y$ and $I_- = I_X - iI_Y$ are the spin raising and lowering operators. For $I=3/2$, $v_Q = v_{NQR}(1 + \eta^2/3)^{-1/2}$, where v_{NQR} is the pure quadrupole resonance frequency.

At 15 K and in the absence of applied static magnetic field B_0 , we observed two lines of identical intensity, one at 79 v_{NQR} =87.41 MHz corresponding to the 79 Br quadrupole resonance, and the other at ${}^{81}v_{NQR}$ =73.02 MHz corresponding to that of ${}^{81}Br$ (see Fig. [7](#page-3-3)). These values are in agreement with the ratio of the nuclear quadrupole moments published in the literature[.22](#page-6-14) Given the gyromagnetic ratio of the two

TABLE I. Spin, natural abundance, gyromagnetic ratio, electric quadrupole moment (Ref. [21](#page-6-15)), and measured nuclear quadrupole frequencies of the two bromine isotopes.

	Spin	Nat. abund. $(\%)$	$\gamma_n/2\pi$ (MHz/T)	(barn)	$v_{NQR,15 K}$ (MHz)
^{79}Br	3/2	50.69	10.7	0.313	87.41
81Br	3/2	49.31	11.53	0.262	73.02

FIG. 8. (a) Sketch of the energy levels of Br nuclei. The solid arrows are the $\Delta m=1$ transitions and the dotted ones the $\Delta m>1$ transitions. (b) Definition of angles Θ , Φ , Ω , and Ψ . The *X*, *Y*, and *Z* axes correspond to the principal axes of the EFG and Knight shift z axes correspond to the principal axes of the EFO and Kinght shift FIG. 9. NMR Spectra for $B_0=14$ T along [110]. The intensities tensors

bromine isotopes (cf. Table [I](#page-3-1)), it is clear that the high-field approximation, which consists in considering the quadrupole interaction as a perturbation to the Zeeman one, will not yield to the correct transition energies for standard NMR field values. Unlike in the case of a Zeeman only or a quadrupole only Hamiltonian, the eigenvectors of the total Hamiltonian are not pure and therefore the so-called forbidden transitions can have a nonzero probability of occurring. For *I*=3/2, the six possible transitions between the different available spin states are shown in Fig. $8(a)$ $8(a)$. As a consequence, analytical solutions cannot be calculated and a numerical computation is required.

For the present study, we developed a MATLAB routine to calculate the field dependence of the resonance frequencies and their associated intensities for Br sites in an arbitrary orientation of the field. The code was written such as to numerically diagonalize the Hamiltonian described in Eq. ([2](#page-3-4)), compute the resonance frequencies from its eigenvalues and determine the expected relative intensity of each transition by calculating $|\langle \varphi_i | \gamma_n \hbar B_1 \cdot I | \varphi_j \rangle|^2$, $i \neq j$, where B_1 is the radio-frequency excitation field created in the NMR coil and φ_i , φ_j are eigenstates of the Hamiltonian. In the *x*, *y*, *z* laboratory frame, $B_1 \cdot I$ can be expressed in terms of the *X*, *Y*, *Z* projections of *I* using two Euler angles, Ω and Ψ defined in Fig. [8](#page-4-0)(b), giving $B_1 \cdot I = B_1(I_X \sin \Omega \cos \Psi + I_Y \sin \Omega \sin \Psi$ $+I_Z \cos \Omega$). The magnitude of the transition probabilities will thus strongly depend on the intensity of B_0 as well as on its direction in the *X*,*Y* ,*Z* frame, i.e., on the crystal orientation. This is particularly important in the present study where the Zeeman and quadrupolar terms are of comparable magnitude.

Having determined the bromine NQR frequencies by experiment, the remaining unknown parameters in the Hamiltonian given in Eq. (2) (2) (2) are the Knight shift tensor, the orientation of the EFG tensor principal axes with respect to the crystal axes and the associated asymmetry parameter η . Several frequency and field scans were performed in the range 10–220 MHz and 5–15 T, respectively, with field applied along four different directions, namely, $[100]$, $[110]$, $[210]$, and [001]. As an example, a frequency scan performed with B_0 =14 T applied along [110] is shown in Fig. [9.](#page-4-1) The computed NMR frequencies and associated intensities calculated for various η values with $K=0$ were compared to the measurements. We concluded that the *Z* axes of the local EFG tensors are along the Cu-Br bonds, one of which being ori-

have been divided by the square of the frequency. Each line has been identified. The two sharp lines, one around 158 MHz and the other around 169 MHz indicate the position of the 63 Cu and 65 Cu resonance of the copper NMR coil and have been used to determine the exact value of B_0 . At low frequencies (150–180 MHz) we can find the eight central lines. For Br_i and Br_{ii} these lines are overlapping since shift and quadrupolar frequency are small in this orientation of the field and the misorientation is not sufficient to separate them. At high frequencies (200-210 MHz), we observe only the four high-frequency satellites of Br*ⁱ* and Br*ii*. Low frequency satellites are expected below 100 MHz and Br and Br*iii* high-frequency satellites are expected around 240 MHz. Note that since the field direction is close to the principal axis of the EFG tensor, the contribution of the quadrupolar term to the resonance frequency is nearly maximum).

ented along a direction close to $[110]$ (its exact direction is [1 0.8384 -0.0124]). In addition, a largely anisotropic Knight shift tensor with its *Z* axis also parallel to the Cu-Br bonds needed to be introduced in the Hamiltonian in order to match the computed frequencies with the measured ones. Furthermore, up to the precision of our measurements, we deduced that **K** is isotropic in the *X*-*Y* plane perpendicular to the Cu-Br bond. To simplify the Hamiltonian, we defined the *X* and *Y* axes to be parallel to the *X* and *Y* axes of the EFG tensor. It was then possible to perform experiments to fully determine the Knight shift tensor. Indeed, for B_0 applied along a Cu-Br bond, that is $[1 \ 0.8384 -0.0124]$, the temperature dependence of the Br resonance frequencies leads to the determination of K_{77} . Similarly, $K_{YY} = K_{YY}$ can be determined by applying B_0 perpendicular to a Cu-Br bond and measuring the temperature dependence of the Br resonances. By comparing these measurements to the temperature dependence of the macroscopic susceptibility, we obtained K_{ZZ} $=12$ T/ μ_B and $K_{XX} = K_{YY} = 0.97$ T/ μ_B (see Fig. [10](#page-5-7)). From $K_{ZZ} = 8/5 f_p \mu_B \langle r^{-3} \rangle$, with $\langle r^{-3} \rangle = 103 \times 10^{24}$ cm⁻³,^{[18](#page-6-10)} the experimental K_{ZZ} value leads to $f_p = 4.8\%$ along the *Z* axis. Such a rather large value of f_p indicates that the bromine ligands are involved in the exchange path between Cu spins.

To determine the only remaining unknown parameter η , we used a modified version of the MATLAB routine designed to minimize the difference between the measured resonance frequencies and fields, and the fitted frequencies and fields with η as free parameter. This led to $\eta = 0.25 \pm 0.01$. It should be noted that we had to take into account a slight misalignment of the crystal in the coil since a tilt of just one degree away from a specific direction results in dramatic

FIG. 10. (Color online) Br hyperfine shift vs magnetic susceptibility with *T* as an implicit parameter. NMR shifts were measured on ⁷⁹Br at 9 T between 12 and 50 K. Black dots correspond to K_{zz} , parallel to the Cu-Br bond, and open circles to $K_{xx} = K_{yy}$.

frequency shifts. In Fig. [11,](#page-5-8) we plot the results of simulations for B_0 aligned along a direction close to [110] (the precise direction is $\begin{bmatrix} 1 & 1 & -0.08 \end{bmatrix}$ and corresponds to an experimental crystal orientation, which was estimated from the comparison between the measurements shown in Fig. [9](#page-4-1) and the calculations). The field dependence of the 48 transitions of the two bromine isotopes located on the four inequivalent sites are plotted. The calculated intensities are shown on a color scale shown on the right of the figure. On top of the calculated transitions, horizontal and vertical bars are sketched at the frequencies, respectively, fields, of the observed resonances measured at fixed field (9 T and 14 T), respectively, fixed frequency (110 MHz). The bars reported at 14 T correspond to the measurements shown in Fig. [9.](#page-4-1)

Although it was not the purpose of the present work to detect all the transitions, many of them had to be measured in order to correctly interpret the data and to accurately determine the unknown parameters in the Hamiltonian. The observed line intensity ratios do not exactly match the calculated intensity ratios. The reason for this discrepancy is related to the large variations and short spin-spin relaxation times (typically on the order of $5-15$ μ s at 15 K). It should also be noted that the field dependence of the NMR frequencies of a spin 3/2 with large quadrupolar couplings placed in a strong external field has already been numerically calculated using the Liouvillian formalism and the results were compared to measurements performed in a 35 Cl-sodium chlorate NMR study. 23 However, the intensity ratios of the transitions were not computed in this previous study.

FIG. 11. (Color online) Computed Br transition frequencies and intensities as a function of the external magnetic field amplitude $|\mathbf{B}_0|$ for \mathbf{B}_0 oriented along [110]. The 48 possible transitions for the two Br isotopes and the four inequivalent sites are drawn. The intensities are represented on a color scale in arbitrary units: the lighter the color, the weaker the intensity. The experimental points corresponding to observed transitions are denoted by horizontal tips for spectra recorded at constant field and variable frequencies and by vertical tips for spectra recorded at fixed frequency sweeping the magnetic field.

IV. CONCLUSIONS

The temperature dependence of the Te NMR relaxation rate clearly demonstrates the three-dimensional nature of the magnetic phase transition. This implies that intertetrahedral interactions along the *c* axis as well as those in the *ab* plane are important. The transition temperature was found to be 10.5 K at 9 T. A Br NMR and NQR study in the paramagnetic phase of $Cu_2Te_2O_5Br_2$ allowed us to demonstrate the important role of bromine in the interaction paths between Cu spins. In addition, via tellurium NMR, we showed that the $[TeO_3E]$ tetrahedra participates in binding the Br atoms.

The theoretical modelization of this frustrated spin system, topic of several recent publications, will be clearly facilitated by this distinct information. A complete NMR study of this material in its magnetic phase is currently in progress and is expected to shed light on its complex magnetic phase.

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