Comparative ab initio study of half-Heusler compounds for optoelectronic applications

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For the advancement of optoelectronic applications, such as thin-film solar cells or laser diodes, there is a strong demand for new semiconductor materials with tailored structural and electronic properties. The eightelectron half-Heusler compounds include many promising materials with a big variety of lattice constants and band gaps. So far only a small number of them have been investigated. With the help of *ab initio* calculations, we have studied all possible configurations of ternary 1:1:1 compounds in the half-Heusler structure. We have investigated 648 half-Heusler materials, including compounds of the types I-I-VI, I-III-V, I-III-IV, and II-III-III. For all compounds, we have optimized the lattice constant and determined the most stable arrangement of elements on the half-Heusler lattice sites. Preferred configurations and semiconductivities are compared for the different half-Heusler types. A discussion of the lattice geometries provides a parameter-free function for estimating the lattice constants. The calculated band gaps and lattice constants are used to select potential substitute materials for CdS in the buffer layer of CuInSe₂ and Cu(In,Ga)Se₂ thin-film solar cells.

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I. INTRODUCTION

The development and optimization of optoelectronic devices depends crucially on the availability of suitable semiconductor materials. During the last years, there has been a clear trend toward multinary compounds, providing a wider range of electrical, optical, and chemical properties. Obviously, by going from silicon and binary semiconductors such as GaAs to ternary or higher multinary materials, the number of possible compounds grows strongly, providing a great variety of material properties together with a growing difficulty to choose the right one for the respective applications.

A particularly interesting class of ternary materials are half-Heusler compounds with composition XYZ. If the elements X, Y, and Z have a total number of eight valence electrons they form a particularly stable ground-state structure. The most electropositive element X donates n valence electrons to the more electronegative elements Y and Z. Therefore, a cationic X^{n+} fills the gaps of a covalently bound $(YZ)^{n-}$ sublattice with eight valence electrons. As an intermetallic compound with ionic and covalent bonds the eightelectron half-Heusler material is a ternary Zintl compound.¹ The eight valence electrons of the anionic sublattice act like a closed shell and form a particularly stable configuration. Therefore, the class of eight-electron half-Heusler compounds includes a large number of semiconductors, whose band gaps vary in a wide range.² Similar stable eightelectron states cause the band gaps in binary semiconductors of the IV-IV, III-V, II-VI, or I-VII type.

In general, eight-electron half-Heusler materials can be of the I-I-VI, I-III-V, I-III-IV, II-II-V, and II-III-III type. In this paper, we investigate a set of 648 half-Heusler compounds with the help of all-electron density-functional theory (DFT) calculations. The selection of compounds focuses on materials that are particularly relevant for industrial applications. Therefore, strongly toxic, rare, and heavy elements have been omitted. Pure main group compounds, such as LiAlSi with elements from main groups Ia, IIIa, and IVa, have been investigated as well as compounds with main group elements and transition metals. From the huge class of possible eightelectron half-Heusler compounds, only a very small number has been synthesized up to now. In the I-II-V class, the compounds LiYZ with Y=(Zn, Mg) and Z=(N, P, As) have been synthesized and analyzed^{3–7} as well as LiAlGe (Ref. 8) and LiCdP.⁹ The same compounds have also been investigated with *ab initio* calculations.^{10–13} In the I-III-IV class, structural properties of synthesized LiAlSi,¹⁴ LiGaSi,⁸ LiGaSn,¹⁵ LiInGe,¹⁶ LiInSn,¹⁶ AuScSn,¹⁷ and AuYPb (Ref. 18) have been reported. Recently, various I-II-V half-Heusler compounds have been studied with the help of density-functional theory and Hartree-Fock methods.¹⁹

Comparing the structural and electronic properties of the 648 compounds allows to derive global trends for the crystalline structure and the semiconductivity. It should be noted that testing the absolute stability of the half-Heusler phases is beyond the scope of this paper. Thus, for several compounds other phases may be more stable than the half-Heusler phase. Known examples are the compounds NaZnZ with Z = P, As, Sb, which form a tetragonal Cu₂Sb at ambient conditions while half-Heusler phases become stable only at high pressure.²⁰

The obtained data for crystal geometries and band structures can be used to preselect compounds as candidate materials for specific optoelectronic applications. The procedure is used for finding new buffer layer materials for thin film solar cells based on chalcopyrite absorber layers such as CuInSe₂ (CISe) or Cu(In,Ga)Se₂ (CIGSe). In most highefficiency thin-film solar cells, the chalcopyrite absorber layer is separated from the ZnO-based window layer by a thin buffer layer. CdS is frequently used as buffer layer material. However, the heavy metal cadmium is harmful for the environment. As more and more large-size solar cells are manufactured, the necessity to find a replacement for cadmium increases. A suitable alternative buffer material must fulfill various criteria: its crystal structure must match well with that of the absorber layer to ensure a good contact. The band gap must be suitably large to avoid absorption losses of the incoming light. At the absorber-buffer interface, the conduction band of the absorber should be close to the Fermi



FIG. 1. (Color online) Unit cell of a half-Heusler compound with fcc sublattices *A*, *B*, and *C*. Sublattice *C* occupies the sparsely filled layers between the NaCl structure formed by sublattices *A* and *B*. The closest distance d_{AB} between atoms in sublattice *A* and *B* is smaller than corresponding distances $d_{AC}=d_{BC}$ to atoms in lattice site *C*.

level (inverted interface), and a barrier reduction should be avoided in order to minimize recombination.²¹ In this paper, we use the calculated lattice constants and band gaps of half-Heusler materials to select potential substitutes of CdS.

The paper is organized as follows: in Sec. II, the half-Heusler structure is explained. Details on the calculation methods are given in Sec. III. Results for the preferred configurations, the lattice constants, and the band gaps are presented and discussed in Sec. IV. In Sec. V, results are used to select potential buffer layer materials for chalcopyrite solar cells. Some conclusions are drawn in Sec. VI.

II. CRYSTALLINE STRUCTURE

A half-Heusler compound *XYZ* has a 1:1:1 stoichiometry and a $C1_b$ structure with space group $F\overline{4}3m$. It consists of three nested face-centered-cubic (fcc) sublattices *A*, *B*, and *C* with origins at $\mathbf{r}_A = (0.5, 0.5, 0.5)$, $\mathbf{r}_B = (0, 0, 0)$, and \mathbf{r}_C = (0.25, 0.25, 0.25) in units of the cubic lattice constant *a*. In contrast to Heusler compounds, there is no sublattice originating from (0.75, 0.75, 0.75). As a consequence, there is a gap between \mathbf{r}_A and \mathbf{r}_B along the (1,1,1) diagonal axis of the cubic unit cell.

Sublattices *A* and *B* together form a NaCl structure. Layers, in which *A* and *B* are arranged in a checkerboardlike structure, alternate with sparsely filled layers of the *C* sublattice. The half-Heusler structure is shown in Fig. 1. It is important to note that the distance $d_{AB}=a/2$ between neighboring atoms of *A* and *B* is bigger than the smallest distance $d_{AC}=d_{BC}=\sqrt{3}a/4 \approx 0.433a$ between atoms of *A* and *C* or atoms of *B* and *C*, respectively. The closest distances between two atoms of the same sublattice is given by $d_{AA}=d_{BB}=d_{CC}=a/\sqrt{2}\approx 0.71a$.

In general, there are six ways to distribute the elements X, Y, and Z over the sublattices A, B, and C. For symmetry reasons, exchanging the elements on A and B results in a physically equivalent structure. Therefore, only three differ-

ent configurations have to be distinguished, depending on which component occupies sublattice C. In the following, we denote a specific configuration of a compound XYZ of elements X, Y, and Z by underlining the element on sublattice C. Thus, LiZnP has phosphor on sublattice C.

The electronic structure in the half-Heusler is strongly influenced by the Pauling electronegativity χ of the elements. In the following, we will write components *XYZ*, ordered by the Pauling negativity, such that $\chi_X \leq \chi_Y \leq \chi_Z$. The electronic structure of LiZnP has been studied by several groups theoretically^{10,22} and experimentally.^{9,23–25} In LiZnP, the cation Li⁺ coexists with a covalently bound (ZnP)⁻ that forms a zincblende structure. With the extra electron from Li, the zincblende sublattice has eight valence electrons and is particularly stable. As predicted theoretically,¹⁰ the presence of the Li⁺ cation shifts the conduction-band states at the X point of the Brillouin zone to higher-energy values. As a consequence, LiZnP has a direct band gap. The effect is characterized by the interstitial insertion rule.¹³

III. CALCULATION METHOD

Properties of eight-electron half-Heusler compounds XYZ are investigated with density-functional theory methods. We apply all-electron calculations with the augmented planewave approximation using the program WIEN2K.²⁶ Calculations for the cubic unit cells of the compounds are performed with 10 000 k points. For all compounds XYZ, the three physically different configurations XYZ, XYZ, and XYZ have been considered. For each configuration, we determined the lattice constant a that minimizes the total energy. In a first step, values of a were spread over the reasonable range of the lattice constant. In a second step, a refined grid of test points a in the range of the energy minimum was calculated. Another grid refinement is used in a third step to obtain the optimum lattice constant. The total energies of the configurations XYZ, XYZ, and XYZ were compared to determine the most stable configuration. For the geometry optimization, we used the generalized gradient approximation (GGA) of DFT introduced by Perdew, Burke, and Ernzerhof (PBE). With the optimized lattice constant, the band structure was determined with the alternative GGA method proposed by Engel and Vosko (EV-GGA).²⁷ The EV-GGA is typically less accurate for optimizing the cell parameters²⁸ but it provides more precise results for nonoccupied states. Especially, the band gap for semiconductors is more accurate. However, it is still distinctly underestimated in many cases, which is a known weakness of DFT methods. A comparison between band gaps calculated with EV-GGA and experimentally measured band gaps is made in Table I.

IV. RESULTS

We have performed a numerical study of eight-electron half-Heusler compounds. Using PBE-GGA for structure optimization and EV-GGA for calculating the band structures we have studied 648 compounds, chosen from the I-I-VI, I-II-V, I-III-IV, II-II-IV, and II-III-III classes.

TABLE I. Comparison of calculated lattice constants a_{calc} and band gaps $E_{gap,EV}$ with corresponding values from experiments a_{exp} and $E_{gap,exp}$. A hyphen in the last column indicates that no experimental value has been found. All values are rounded to the second decimal. Compounds with As have been added for a more comprehensive comparison. Note that DFT calculations typically underestimate the band gap.

Compound	a _{calc} (Å)	a _{exp} (Å)	$E_{gap, EV}$ (eV)	$E_{gap,exp}$ (eV)
LiAlGe	6.02	5.96 ⁸	0.07	
LiAlSi	5.94	5.93 ¹⁴	0.12	
LiCdP	6.13	6.10 ⁹	1.25	
LiGaSi	5.97	6.09 ⁸	0.20	
LiGaSn	6.41	6.33 ¹⁵	0	
LiInGe	6.39	6.30 ¹⁶	0	
LiInSn	6.79	6.68 ¹⁶	0	
LiMgAs	6.21	6.18 ²⁹	2.30	2.38 ²⁹
LiMgN	5.02	4.99 ⁷	2.82	3.2 ³⁰
LiMgP	6.02	6.00 ³¹	2.51	2.43 ³²
LiZnAs	5.98	5.94 ⁵	1.10	1.51 ⁵
LiZnN	4.93	4.90 ⁶	0.95	1.91 ³³
LiZnP	5.76	5.77 ³	2.14	2.04 ²³
AuScSn	6.52	6.42 ¹⁷	0.41	
AuYPb	6.83	6.73 ¹⁸	0	

A. Configurations

For each compound of elements *X*, *Y*, and *Z*, we have compared the total energies E(XYZ), E(XYZ), and E(XYZ) of the respective configurations. The calculations showed that for a ratio of $r(XYZ) \approx 78\%$ of the 648 tested compounds the most stable configuration is the XYZ. For $r(XYZ) \approx 17\%$ of all compounds XYZ is most stable, and for less than 5% the most stable configuration is XYZ.

It is interesting to distinguish between half-Heusler compounds that consist of main group elements only (main) and those that include also transition metals (trans). One example of a *main* compound is the half-Heusler prototype LiAlSi while LiZnP is an example for a *trans* compound. Table II shows the total number of calculated main and trans compounds as well as the respective numbers, separated into compound types I-I-VI, I-III-V, I-III-IV, II-II-IV, and II-III-III. For each half-Heusler type, main and trans, Table II gives the percentage of compounds that favor the XYZ, XYZ, and XYZ configuration, respectively. One finds that, altogether, the XYZ configuration is favored more often by pure main group compounds (about 86%) than by trans compounds (about 76% of the calculated materials). Remarkably, the XYZ is never the most stable configuration for any main compound. Furthermore, in the I-II-V and the II-II-IV class all tested main compounds favor the XYZ configuration. In the I-IVI and the II-III-III class, there are specially high ratios of trans compounds that favor the XYZ configuration.

The fact that XYZ is energetically favorable in most cases while XYZ is rarely favored can be understood as follows: typically, the half-Heusler compound in the XYZ configuration forms an anionic $(YZ)^{n-}$ zincblende structure with Y and Z on sublattice B and C, respectively, that is filled with X^{n+} cations on sublattice A.² The distance d_{XY} between the elements X and Y is larger than the distances $d_{XZ} = d_{YZ}$. A close distance between Y and Z favors the formation of stable covalent bonds between the two elements. A close distance between the cationic X^{n+} and the most electronegative element Z reduces the local electric dipoles and the corresponding energy contributions. In the XYZ structure, there is a larger distance between X^{n+} and the most anionic Z, leading to a larger dipole. The XYZ structure separates the partners of the covalent bonds, which turns out to be strongly disadvantageous in most cases.

If the difference $\chi_Z - \chi_Y$ is small, the dipole energy difference between the *XYZ* configuration with a larger distance d_{XY} and the *XYZ* configuration with a larger distance d_{XZ} is of less relevance. Indeed, our results show that compounds favoring the *XYZ* configuration have an average value $(\chi_Z - \chi_Y)_{av}^{XYZ} \approx 0.35$ that is distinctly smaller than $(\chi_Z - \chi_Y)_{av}^{XYZ} \approx 0.63$. If $\chi_Z - \chi_X$ is small, all electronegativities χ_X , χ_Y , and χ_Z are of comparable size. According to this, the average value of $(\chi_Z - \chi_X)_{av}^{XYZ} \approx 0.64$ for compounds favoring \underline{XYZ} is considerably below $(\chi_Z - \chi_X)_{av}^{XYZ} \approx 1.15$. This means that the \underline{XYZ} configuration is typically most stable if the cationic character of X is less pronounced and the bond between Y and Z is comparably weak in any configuration. In Fig. 2 the obtained values for $\chi_Z - \chi_X$ and $\chi_Z - \chi_Y$ are shown for compounds favoring the \underline{XYZ} configuration the \underline{XYZ} configuration, respectively.

TABLE II. Number of calculated half-Heusler materials of type I-I-VI, I-II-V, I-III- IV, II-II-IV, and II-III-III, divided into compounds that consist of main group elements only (main) and those that include transition metals (trans). For all half-Heusler types, the values of r(XYZ), r(XYZ), and r(XYZ) denote the respective percentage of compounds that favor configuration XYZ, XYZ, and XYZ, respectively. The quantity r(semi) denotes the percentage of semiconducting materials for the respective half-Heusler type.

	I-I-VI		I-II-V		I-II	I-IV	II-II	-IV	II-II	I-III	All	
Туре	main	trans	main	trans	main	trans	main	trans	main	trans	main	trans
N _{comp}	18	44	32	121	75	200	30	73	22	33	177	471
r(XYZ)	83.3%	81.8%	100.0%	77.7%	74.7%	73.0%	100.0%	69.9%	86.4%	97.0%	85.9%	76.2%
$r(X\underline{Y}Z)$	16.7%	13.6%	0.0%	17.4%	25.3%	17.5%	0.0%	26.0%	13.6%	3.0%	14.1%	17.4%
r(XYZ)	0.0%	4.5%	0.0%	5.0%	0.0%	9.5%	0.0%	4.1%	0.0%	0.0%	0.0%	6.4%
r(semi)	100.0%	40.9%	100.0%	21.5%	24.0%	34.0%	93.3%	12.3%	63.6%	39.4%	62.1%	28.5%



FIG. 2. Differences of the Pauling negativities $\chi_Z - \chi_X$ of elements *X* and *Z* and $\chi_Z - \chi_Y$ of elements *Y* and *Z* for all compounds *XYZ*. Values are shown for compounds favoring the *XYZ* (×), the *XYZ* (•), and the *XYZ* (◊) configuration, where the underlined element occupies sublattice *C*. For most of the *XYZ* and *XYZ* compounds, the difference $\chi_Z - \chi_Y$ is below 0.75 (horizontal line). For almost all *XYZ* compounds, the difference $\chi_Z - \chi_X$ is below 1 (vertical line). Note that the components *XYZ* are sorted such that $\chi_X \le \chi_Y \le \chi_Z$.

Many eight-electron half-Heusler compounds are semiconductors because of the stable configuration formed by the valence electrons in the $(YZ)^-$ sublattice. Using EV-GGA, we have calculated the band structures of all compounds.

B. Lattice constants

The lattice constant has been optimized for all compounds in all three configurations. In the following, the *lattice constant of a compound* refers to the optimized lattice constant of the most stable half-Heusler configuration of this compound. Calculated lattice constants are compared with known experimental values in Table I. Complete lists of lattice constants for calculated half-Heusler compounds of type I-I-VI, I-III-V, I-III-IV, II-III-IV, and II-III-III are given in Tables III–VII. We restrict the analysis of the lattice constants on compounds with stable XYZ configuration, which enables a reasonable comparison of the geometric properties. It is instructive to discuss the optimized lattice constants a as a function of the atomic radii r_X , r_Y , and r_Z . A widely used set of atomic radii for elements in crystals has been determined phenomenologically by Slater.³⁴ In a first step, we assume that the shortest atom distances $d_{XZ}=d_{YZ}$ have the strongest influence on the unit-cell size. From the definition of the Slater radii one expects that, in the absence of other constraints, the optimum distance d_{XZ} of atoms X and Z is approximately $r_X + r_Z$. However, in most cases, elements X and Y with $\chi_X < \chi_Y$ have different radii $r_X > r_Y$ so that d_{XZ} $=r_X+r_Z$ and $d_{YZ}=r_Y+r_Z$ cannot be satisfied at the same time. As shown in Fig. 3, the distances $d_{XZ} = d_{YZ} = \frac{\sqrt{3}}{4}c$ are typically smaller than $r_X + r_Z$ but larger than $r_Y + r_Z$. One finds that deviations in both directions are of the same order. In fact, the equilibrium lattice constant can be approximated by the arithmetic mean of $\frac{4}{\sqrt{3}}(r_X + r_Z)$ and $\frac{4}{\sqrt{3}}(r_Y + r_Z)$ as shown in Fig. 4. Note that the resulting relation

$$a \simeq f_1 \equiv \frac{2}{\sqrt{3}} (r_X + r_Y + 2r_Z)$$
 (1)

does not include any fit parameter and the average relative deviation between f_1 and the calculated lattice constant a is below 5%.

Let us consider a notional mechanical analogon of the half-Heusler crystals, in which the distances d_{XZ} and d_{YZ} are controlled by ideal linear springs with an equilibrium length of r_X+r_Z and r_Y+r_Z , respectively. The expression in Eq. (1) would provide the geometrically optimum configuration if the springs would have the same strength. We can now think of a more refined virtual model system in which centers of neighboring atom pairs XY, XZ, and YZ are connected by springs of different strengths and equilibrium lengths r_X+r_Y , r_X+r_Z , and r_Y+r_Z , respectively. With $a=2d_{XY}=\frac{4}{\sqrt{3}}d_{XZ}=\frac{4}{\sqrt{3}}d_{YZ}$, the optimum lattice constant *a* results from the combination of three phenomenological harmonic potentials for d_{XY} , d_{XZ} , and k_{YZ} , with individual potential strengths k_{XY} , k_{XZ} , and k_{YZ} .

TABLE III. Equilibrium lattice constants a for I-I-VI half-Heusler compounds. In the energetically favored configuration, the underlined element occupies sublattice C.

Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)
AgAuO	5.792	KAuO	6.206	KNaSe	7.334	LiCuS	5.594	NaLiO	5.239	RbCuSe	6.846
AgAuS	6.219	KAuS	6.740	KRbQ	6.734	LiCuSe	5.870	NaLi§	6.223	RbLiQ	6.179
AgAu <u>Se</u>	6.407	KAu <u>Se</u>	6.923	KRbS	7.712	NaAgQ	5.696	NaLiSe	6.500	Rb <u>Li</u> S	6.686
CuAgQ	5.899	KCuQ	5.864	KRb <u>Se</u>	7.960	NaAgS	6.334	RbAgQ	6.410	Rb <u>Li</u> Se	6.868
CuAg§	5.961	K <u>Cu</u> S	6.400	LiAgQ	5.409	NaA <u>gSe</u>	6.539	RbAg§	7.064	RbNaQ	6.420
<u>Cu</u> AgSe	6.081	K <u>Cu</u> Se	6.593	LiAg§	6.026	NaAuQ	5.803	RbAg <u>Se</u>	7.278	RbNa§	7.338
CuAu§	5.966	KLiQ	5.888	LiAg <u>Se</u>	6.259	NaAuS	6.299	RbAuQ	6.443	RbNa <u>Se</u>	7.608
<u>Cu</u> AuSe	6.098	KLi§	6.849	LiAuQ	5.490	NaAu <u>Se</u>	6.510	RbAuS	7.000		
KAgQ	6.165	K <u>Li</u> Se	6.656	LiAuS	6.006	NaCuQ	5.338	RbAu <u>Se</u>	7.177		
KAg§	6.801	KNaQ	6.147	Li <u>Au</u> Se	6.214	NaCuS	6.021	RbCuQ	5.984		
KAg <u>Se</u>	7.010	KNa <u>S</u>	7.089	LiCuQ	4.990	Na <u>Cu</u> Se	6.143	Rb <u>Cu</u> S	6.666		

TABLE IV. Equilibrium lattice constants *a* for I-II-V half-Heusler compounds. In the energetically favored configuration, the underlined element occupies sublattice *C*.

Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)
BaAgN	6.430	CaPAu	6.421	KSrN	6.567	MgPAu	6.107	RbBa₽	7.817	SrCuP	6.574
BaAgP	7.052	CaVAg	6.662	KSrP	7.445	MgVAg	6.165	RbBa⊻	8.378	SrLiN	5.932
BaAuN	6.470	CaVAu	6.588	KSr⊻	8.184	MgV <u>Cu</u>	5.881	RbCa№	6.536	Sr <u>Li</u> Nb	7.018
BaCuN	6.246	CaV <u>Cu</u>	6.390	KVCd	6.867	NaCaN	5.885	RbCa <u>Nb</u>	8.060	SrLiP	6.824
Ba <u>Cu</u> P	6.723	CdAgN	5.777	KV <u>Zn</u>	6.889	<u>Na</u> CaNb	7.208	RbCa <u>P</u>	7.409	Sr <u>Li</u> V	6.970
BaLiN	6.250	CdAgP	6.289	KZnŊ	5.972	NaCaP	6.790	RbCa⊻	8.062	SrNbAg	6.975
Ba <u>Li</u> Nb	7.064	CdAuN	5.822	KZnP	6.668	NaCaY	7.375	RbCdN	6.493	SrNbCu	6.720
BaLiP	7.144	CdCuN	5.502	LiCaŊ	5.572	NaCdN	5.706	RbCdP	7.130	SrPAu	6.694
BaLiY	7.055	CdCuP	6.036	LiCaP	6.506	NaCdP	6.440	RbMgŊ	6.321	SrVAg	6.934
BaNaŊ	6.468	CdPAu	6.276	<u>Li</u> CaV	6.660	NaMgŊ	5.460	RbMgNb	7.289	SrV <u>Au</u>	6.863
BaNa <u>Nb</u>	7.535	KBaŊ	6.762	LiCdN	5.383	NaMgP	6.376	RbMgP	7.097	SrV <u>Cu</u>	6.670
BaNa <u>P</u>	7.343	K <u>Ba</u> Nb	7.801	LiCdP	6.134	NaMgV	6.747	RbMg⊻	7.408	VCdAg	6.022
BaNa⊻	7.460	KBa <u>P</u>	7.658	LiMgŊ	5.018	NaNb <u>Cd</u>	6.651	Rb <u>Nb</u> Cd	7.176	VCd <u>Au</u>	6.235
Ba <u>Nb</u> Ag	6.937	KBaV	8.193	LiMgP	6.019	NaNb <u>Zn</u>	6.326	RbNb <u>Zn</u>	7.062	VCd <u>Cu</u>	5.922
BaNb <u>Cu</u>	6.866	KCaŊ	6.330	<u>Li</u> MgV	6.047	NaSrN	6.190	RbSrN	6.751	VZnAg	5.986
BaPAu	6.987	KCa <u>Nb</u>	8.137	<u>Li</u> VCd	5.947	<u>Na</u> SrNb	7.389	RbSr <u>Nb</u>	8.294	VZn <u>Au</u>	5.993
BaVAg	6.888	KCaP	7.207	LiV <u>Zn</u>	5.807	NaSrP	7.068	RbSrP	7.623	VZn <u>Cu</u>	5.648
BaYAu	6.703	KCaV	7.888	LiZnŊ	4.927	NaSr⊻	7.345	RbSr⊻	8.326	ZnAgŊ	5.496
BaV <u>Cu</u>	6.875	KCdŊ	6.200	LiZnP	5.757	NaV <u>Cd</u>	6.589	RbYCd	7.166	ZnAgP	6.021
CaAgŊ	5.849	KCdP	6.875	MgAgŊ	5.524	NaV <u>Zn</u>	6.254	Rb V Zn	6.959	ZnAuN	5.555
CaAgP	6.478	KMgŊ	6.025	MgAgP	6.141	NaZnŊ	5.360	RbZnŊ	6.302	<u>Zn</u> CuN	5.306
CaAuN	5.895	KMgNb	7.313	MgAuN	5.586	NaZnP	6.149	RbZn <u>P</u>	6.958	ZnCuP	5.700
CaCuN	5.592	KMgP	6.841	MgCuN	5.165	NbCd <u>Cu</u>	6.050	SrAgŊ	6.134	ZnPAu	6.016
CaCuP	6.260	KMg⊻	7.277	MgCuP	5.850	NbZn <u>Cu</u>	5.813	SrAgP	6.755		
CaNbAg	6.721	KNb <u>Cd</u>	7.134	MgNbAg	6.323	RbBaŊ	6.917	SrAuN	6.173		
CaNb <u>Cu</u>	6.472	KNb <u>Zn</u>	6.856	MgNb <u>Cu</u>	6.020	RbBa <u>Nb</u>	8.816	SrCuN	5.929		

$$U(a) = k_{XY} \left(r_X + r_Y - \frac{1}{2}a \right)^2 + k_{XZ} \left(r_X + r_Z - \frac{\sqrt{3}}{4}a \right)^2 + k_{YZ} \left(r_Y + r_Z - \frac{\sqrt{3}}{4}a \right)^2.$$
 (2)

Taking the minimum of U provides the relation

$$a \simeq f_2 \equiv \frac{4}{4k_{XY} + 3k_{XZ} + 3k_{YZ}} [2k_{XY}(r_X + r_Y) + \sqrt{3}k_{XZ}(r_X + r_Z) + \sqrt{3}k_{YZ}(r_Y + r_Z)].$$
(3)

Fitting the parameters with the calculated data gives $k_{XZ} \approx 1.11k_{XY}$ and $k_{YZ} \approx 1.31k_{XY}$ (see Fig. 4). With these values, the relative deviation $|f_2 - a|/a$ is on average 3.0%. The largest potential strength k_{YZ} regulates the distance between the *Y* and the *Z* component. This means that the stiffest interatomic bond is the covalent bond, followed by the ionic bond between *X* and *Z*. It is noteworthy that within this picture the

phenomenological potential for the distance between X and Y is not much weaker than that for d_{XZ} .

C. Band gap

The band structures of the optimized compounds have been calculated with EV-GGA and PBE-GGA. A comparison of the obtained band gaps $E_{gap, EV}$ and $E_{gap, PBE}$ with existing experimental results $E_{gap, exp}$ shows that band gaps obtained with EV-GGA are always more accurate than those found with PBE-GGA. Band gaps calculated with EV-GGA are compared with existing experimental band gaps in Table I. In the case of LiMgP, LiZnP, and LiMgAs, $E_{gap,EV}$ differs less than 6% from the experimental values. However, the calculated band gap for LiZnAs is 32% smaller than the experimental value and in the case of LiZnN, $E_{gap,EV}$ is only half as big as $E_{gap,exp}$. In general, the relative deviation q_{gap} $= (E_{gap,exp} - E_{gap,EV})/E_{gap,exp}$ is in the range of $-3\% \le q_{gap}$ \leq 50%. This allows us to use the calculated values as an approximate lower bound of the real band gap. Especially, all compounds with a finite $E_{gap,EV}$ can be considered as semiconductors.

TABLE V. Equilibrium lattice constants *a* for I-III-IV half-Heusler compounds. In the energetically favored configuration, the underlined element occupies sublattice *C*.

Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)
AgBC	5.085	KBÇ	5.641	LiGeB	5.163	NaGeB	5.608	RbHfB	6.507	TiAgB	5.523
AgGeB	5.632	KBPb	6.639	LiHfAl	6.087	NaHfAl	6.741	RbHfSc	7.687	TiAlAg	6.126
AlAgC	5.430	KGaÇ	6.096	LiHfB	5.520	NaHfB	5.878	RbInC	6.641	TiAlAu	6.111
AlAgGe	6.201	KGaGe	6.889	LiHfGa	6.242	NaHfGa	6.584	RbInGe	7.353	TiAlCu	5.827
AlAgSn	6.463	KGaPb	7.301	LiHfIn	6.392	NaHfIn	6.923	RbInSi	7.248	TiBAu	5.535
AlAuC	5.484	KGaSi	6.770	LiHfSc	6.497	NaHfSc	6.940	RbInSn	7.579	TiCuB	5.245
AlCuC	5.047	KGaSn	7.133	LiInGe	6.390	NaInGe	6.695	RbScC	6.380	TiGaAg	6.121
AlCuGe	5.831	KGeB	6.195	LiInPb	6.936	NaInPb	7.244	RbScGe	7.345	TiGaAu	6.104
AlCuSi	5.685	- KHfB	6.328	LiInSi	6.272	NaInSi	6.582	RbScSi	7.274	TiGaCu	5.788
AlGeAu	6.166	KHfSc	7.557	LiInSn	6.794	NaInSn	7.077	RbScTi	7.697	YAgC	5.889
AlPbAu	6.566	KInC	6.326	LiScC	5.324	NaScC	5.687	RbSiB	6.410	YAgGe	6.564
AlSiAg	6.072	KInGe	7.109	LiScGe	6.311	NaScGe	6.646	RbSnB	6.763	YAgPb	6.854
AlSiAu	6.032	KInPb	7.601	LiScPb	6.789	NaScPb	7.109	- RbTiAl	7.113	YAgSn	6.750
AlSnAu	6.432	KInSi	7.004	LiScSi	6.272	NaScSi	6.607	RbTiB	6.476	YAuC	5.910
BAuC	5.201	KInSn	7.465	LiScSn	6.333	NaScSn	7.043	RbTiGa	6.986	YCuC	5.660
CuBC	4.612	KScC	6.182	LiScTi	6.360	NaScTi	6.801	RbTiIn	7.301	YCuGe	6.244
CuGeB	5 260	KScGe	7 127	LiSiB	5.008	NaSiB	5 477	RbYC	6 5 5 5	YCuPh	6 601
CuSiB	5.089	KScPh	7 587	LiTiAl	5 895	NaSnB	5 950	RhYGe	7 526	YCuSi	6 174
GaAgC	5 541	KScSi	7.073	LiTiB	5 279	NaTiΔl	6.606	RbYHf	7.940	YCuSn	6 4 9 5
Ga∆gGe	6 287	KScSn	7.507	LiTiGa	6.055	NaTiB	5 712	RhVSi	7.240	YGeΔu	6 535
GaAgSn	6 533	KScTi	7.307	LiTiIn	6.124	NaTiGa	6.452	RbT <u>51</u> RbTi	7.402	VHfAu	6 700
GaAuC	5 501	KSiB	6.068	\underline{L}	5 602	NaTiIn	6.824	$Rb1 \underline{11}$ RbV7r	8.012	$I i 7 r S_c$	6.830
Garaç	5 150	KSnB	6.465	LIL	5.092 6.614	NaVC	5 083	$\frac{1}{21}$	7 307	VSiAg	6.400
GaCuC	5.000	KSIID VT:A1	7 120		6 752	NaVGa	5.965	Dh7rD	6 5 5 2	I <u>SI</u> Ag	6.499
Ga <u>Cu</u> Ge	5.900	KTIAI	6 259		0.752	Na I <u>Ge</u>	0.890	RUZI <u>D</u>	0.332	I SI <u>Au</u> VSn Au	6.720
Ga <u>Cu</u> SI	5.746	KTID KTC-	0.238	LITE	1.004		7.440	DhZ-La	7.200	I SII <u>Au</u>	0.729
GaGe <u>Au</u>	0.243	KII <u>Ga</u> KT:L	7.002	LI I <u>51</u> L :VC-	0.3//	Na i <u>PD</u>	1.338	K0 <u>Zr</u> In Dh7::Ca	7.428	Y TIAg	0./10
Ga <u>Si</u> Ag	0.117	K <u>II</u> IN KWO	7.152	$\underline{\Gamma}$ i Su	0.581	Na 1 <u>51</u>	0.838	KDZr <u>Sc</u>	7.940	Y TI <u>AU</u>	0.088
GaSi <u>Au</u>	6.106	KYC	6.389		6.627	Na Y <u>Sn</u>	7.280	ScAg	5.600	Y TI <u>Cu</u>	6.452
GaSn <u>Au</u>	6.533	KY <u>Ge</u>	7.333	$\underline{Li}YZr$	6.789	$\underline{Na}YT1$	7.041	ScAg <u>Ge</u>	6.300	YZr <u>Ag</u>	6.861
GeBAu	5.675	K Y <u>S1</u>	7.281	<u>Li</u> ZrAl	6.082	NaZr <u>Al</u>	6.766	Sc <u>Ag</u> Pb	6.645	YZr <u>Au</u>	6.822
HfAgB	5.732	KY <u>Sn</u>	7.693	LiZrB	5.575	NaZrB	5.916	Sc <u>Ag</u> Sn	6.506	YZr <u>Cu</u>	6.608
HfAl <u>Au</u>	6.305	KY <u>T1</u>	7.737	LiZr <u>Ga</u>	6.275	NaZr <u>Ga</u>	6.609	ScAuC	5.631	ZrAg <u>B</u>	5.768
HfAl <u>Cu</u>	6.012	KY <u>Zr</u>	7.910	<u>Li</u> ZrIn	6.286	NaZr <u>ln</u>	6.962	ScCuC	5.326	ZrAl <u>Ag</u>	6.330
Hf <u>B</u> Au	5.741	KZr <u>In</u>	7.424	<u>Li</u> ZrSc	6.521	RbAlC	6.364	Sc <u>Cu</u> Ge	5.969	ZrAl <u>Au</u>	6.311
HfCuB	5.486	KZr <u>Sc</u>	7.621	NaAlÇ	5.401	RbAl <u>Ge</u>	7.122	Sc <u>Cu</u> Si	5.888	ZrAl <u>Cu</u>	6.049
HfGa <u>Ag</u>	6.270	LiAlÇ	4.924	NaAl <u>Ge</u>	6.383	Rb <u>Al</u> Pb	7.511	Sc <u>Cu</u> Sn	6.246	Zr <u>B</u> Au	5.774
In <u>Ag</u> Ge	6.504	LiAl <u>Ge</u>	6.019	Na <u>Al</u> Pb	6.901	RbAl <u>Si</u>	7.018	ScGe <u>Au</u>	6.286	ZrCuB	5.528
In <u>Ag</u> Sn	6.728	LiAl <u>Pb</u>	6.594	NaAl <u>Si</u>	6.287	Rb <u>Al</u> Sn	7.346	ScPb <u>Au</u>	6.621	ZrGaAg	6.306
InCu <u>Ge</u>	6.294	LiAl <u>Si</u>	5.937	Na <u>Al</u> Sn	6.729	RbBC	6.047	Sc <u>Si</u> Ag	6.224	ZrGa <u>Au</u>	6.331
InGe <u>Au</u>	6.492	LiAl <u>Sn</u>	6.464	NaBÇ	4.850	RbBPb	6.915	ScSi <u>Au</u>	6.209	ZrGa <u>Cu</u>	6.007
InPb <u>Au</u>	6.930	LiBÇ	4.243	NaBPb	6.154	RbGaC	6.450	ScSn <u>Au</u>	6.526	ZrInAg	6.528
KAlÇ	6.018	LiGaÇ	4.986	NaGaÇ	5.451	RbGa <u>Ge</u>	7.164	ScTiAg	6.466	ZrIn <u>Au</u>	6.526
KAl <u>Ge</u>	6.842	LiGa <u>Ge</u>	6.032	NaGa <u>Ge</u>	6.411	Rb <u>Ga</u> Pb	7.526	ScTi <u>Au</u>	6.424	ZrScAg	6.641
K <u>Al</u> Pb	7.295	Li <u>Ga</u> Pb	6.605	Na <u>Ga</u> Pb	6.896	RbGa <u>Si</u>	7.050	ScTi <u>Cu</u>	6.188	ZrSc <u>Au</u>	6.604
KAl <u>Si</u>	6.731	LiGa <u>Si</u>	5.969	NaGa <u>Si</u>	6.284	Rb <u>Ga</u> Sn	7.375	SiAgB	5.462	ZrScCu	6.378
K <u>Al</u> Sn	7.104	Li <u>Ga</u> Sn	6.412	Na <u>Ga</u> Sn	6.716	RbGeB	6.523	SiBAu	5.501		

TABLE VI. Equilibrium lattice constants a for II-II-IV half-Heusler compounds. In the energetically favored configuration, the underlined element occupies sublattice C.

Name	a (Å)										
BaCaÇ	6.748	BaMg <u>Si</u>	7.282	Ca <u>Cd</u> Pb	7.160	HfMg <u>Cd</u>	6.628	SrCa <u>Pb</u>	7.886	SrTi <u>Cd</u>	7.255
BaCa <u>Ge</u>	7.719	BaMg <u>Sn</u>	7.691	CaCd <u>Si</u>	6.697	HfMg <u>Zn</u>	6.334	SrCa <u>Si</u>	7.415	SrTi <u>Zn</u>	6.964
BaCaHf	8.025	BaMg <u>Ti</u>	7.325	CaCd <u>Sn</u>	7.122	Hf <u>Zn</u> Cd	6.307	SrCa <u>Sn</u>	7.816	SrZnÇ	6.096
BaCaPb	8.129	BaSrC	6.930	CaHf <u>Cd</u>	7.060	MgCd <u>C</u>	5.654	SrCa <u>Ti</u>	7.943	SrZnGe	6.855
BaCa <u>Si</u>	7.714	BaSr <u>Ge</u>	7.921	CaHfMg	7.217	MgCd <u>Ge</u>	6.486	SrCdC	6.311	Sr <u>Zn</u> Pb	7.129
BaCa <u>Sn</u>	8.053	BaSrHf	8.288	CaHf <u>Zn</u>	6.793	Mg <u>Cd</u> Pb	6.952	SrCdGe	7.036	SrZn <u>Si</u>	6.778
BaCa <u>Ti</u>	7.921	BaSrPb	8.343	CaMgC	5.909	MgCd <u>Si</u>	6.386	Sr <u>Cd</u> Pb	7.389	Sr <u>Zn</u> Sn	6.994
BaCdÇ	6.643	BaSr <u>Si</u>	8.110	CaMg <u>Ge</u>	6.799	MgCd <u>Sn</u>	6.851	SrCdSi	6.964	Ti <u>Zn</u> Cd	6.159
BaCd <u>Ge</u>	7.318	BaSr <u>Sn</u>	8.268	CaMg <u>Pb</u>	7.239	MgTi <u>Cd</u>	6.491	Sr <u>Cd</u> Sn	7.261	ZnCdÇ	5.583
Ba <u>Cd</u> Pb	7.639	Ba <u>Ti</u> Cd	7.187	CaMg <u>Si</u>	6.365	MgTi <u>Zn</u>	6.178	SrHfCd	7.314	<u>Zn</u> CdGe	6.305
BaCd <u>Si</u>	7.242	BaTi <u>Zn</u>	7.173	CaMg <u>Sn</u>	7.165	MgZnÇ	5.300	SrHfMg	7.448	<u>Zn</u> CdPb	6.721
Ba <u>Cd</u> Sn	7.524	BaZnÇ	6.459	CaMgTi	7.129	MgZn <u>Ge</u>	6.215	SrHfZn	7.035	ZnCdSi	6.229
BaHf <u>Cd</u>	7.496	BaZn <u>Ge</u>	7.166	CaTi <u>Cd</u>	6.961	Mg <u>Zn</u> Pb	6.627	SrMgÇ	6.235	<u>Zn</u> CdSn	6.594
BaHfMg	7.388	Ba <u>Zn</u> Pb	7.390	CaTi <u>Zn</u>	6.690	MgZn <u>Si</u>	6.120	SrMg <u>Ge</u>	7.068		
BaHf <u>Zn</u>	7.204	BaZn <u>Si</u>	7.084	CaZnÇ	5.745	Mg <u>Zn</u> Sn	6.465	SrMg <u>Pb</u>	7.502		
BaMgÇ	6.557	Ba <u>Zn</u> Sn	7.276	Ca <u>Zn</u> Pb	6.877	SrCaÇ	6.571	SrMg <u>Si</u>	7.012		
BaMg <u>Ge</u>	7.346	CaCdC	6.008	CaZn <u>Si</u>	6.482	SrCa <u>Ge</u>	7.459	SrMg <u>Sn</u>	7.427		
BaMg <u>Pb</u>	7.778	CaCd <u>Ge</u>	6.771	CaZn <u>Sn</u>	7.331	SrCa <u>Hf</u>	8.241	Sr <u>Mg</u> Ti	7.419		

In Table II, the percentages of semiconducting materials are given for main and trans compounds of all half-Heusler types. One finds that a rate of 62.1% of main compounds are semiconducting while only 28.5% of the calculated trans compounds have a finite band gap. Remarkably, all main compounds of type I-I-VI and I-II-V and nearly all II-II-IV main compounds are semiconductors. On the other hand, only 24% of the I-III-IV main compounds have a calculated band gap $E_{gap,EV} > 0$. Particularly large rates of semiconducting trans compounds exist in the I-I-VI and the II-III-III class.

There is a strong correlation between the stability of the XYZ configuration and semiconductivity. In classes I-II-V and II-II-IV, all compounds favor the XYZ configuration and

nearly all compounds are semiconducting. For trans compounds, the classes I-I-VI and II-III-III have the highest rates of *XYZ* stability and the highest rates of semiconductivity. In Fig. 5, the calculated band gaps are shown as a function of $\Delta E = E_{XYZ} - E_{XYZ}$ and $\Delta E = E_{XYZ} - E_{XYZ}$, respectively. Consequently, compounds with negative ΔE favor the *XYZ* or the *XYZ* configuration. It turns out that only a small fraction of these compounds are semiconducting. This means, compounds that favor *XYZ* or *XYZ* states do not form a particularly stable eight-electron substructure in any configuration. For the small number of semiconductors that favor the *XYZ*, the energy difference $|E_{XYZ} - E_{XYZ}|$ is comparably low. From the compounds with a finite calculated band gap, more than 93% favor the *XYZ* configuration. The calculated band gaps

TABLE VII. Equilibrium lattice constants a for II-III-III half-Heusler compounds. In the energetically favored configuration, the underlined element occupies sublattice C.

Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)	Name	a (Å)
BaAl <u>B</u>	6.626	BaY <u>Al</u>	7.700	CaSc <u>Al</u>	7.099	MgGaB	5.497	SrInB	6.497	YMg <u>Al</u>	6.865
BaAl <u>Ga</u>	7.212	BaYB	6.884	CaScB	6.280	MgIn <u>Ga</u>	6.558	SrIn <u>Ga</u>	7.078	YMg₽	6.109
Ba <u>Al</u> In	7.377	BaY <u>Ga</u>	7.567	CaSc <u>Ga</u>	6.948	MgSc <u>Al</u>	6.629	SrSc <u>Al</u>	7.406	YMg <u>Ga</u>	6.727
BaGaB	6.631	BaY <u>In</u>	7.910	CaScIn	7.248	MgScB	5.814	SrScB	6.539	YMg <u>In</u>	7.045
BaInB	6.830	CaAlB	5.940	CaY <u>Al</u>	7.431	MgSc <u>Ga</u>	6.478	SrSc <u>Ga</u>	7.193	YMgSc	7.206
BaIn <u>Ga</u>	7.353	CaAl <u>Ga</u>	6.583	CaYB	6.520	MgSc <u>In</u>	6.814	SrSc <u>In</u>	7.364		
BaScAl	7.512	Ca <u>Al</u> In	6.880	CaY <u>Ga</u>	7.167	SrAl <u>B</u>	6.287	SrY <u>Al</u>	7.275		
BaScB	6.706	CaGaB	5.919	CaY <u>In</u>	7.478	SrAl <u>Ga</u>	6.877	SrYB	6.728		
BaSc <u>Ga</u>	7.394	CaInB	6.187	MgAl <u>B</u>	5.507	Sr <u>Al</u> In	7.159	SrY <u>Ga</u>	7.410		
BaSc <u>In</u>	7.740	CaIn <u>Ga</u>	6.810	MgAl <u>Ga</u>	6.260	SrGaB	6.265	SrY <u>In</u>	7.714		



FIG. 3. The sum of Slater radii $r_j + r_Z$ of elements j=X, Y, and Z should be comparable to the distance $d_{jZ} = \sqrt{3}a/4$. The figure shows $(r_X + r_Z) - \sqrt{3}a/4$ (+), which is larger than zero in most cases, and $(r_Y + r_Z) - \sqrt{3}a/4$ (\bigcirc), which is typically smaller than zero. Data are shown for compounds favoring the *XYZ* configuration.

cover the range from 0 to 3 eV continuously without essential interruptions. Thus, eight-electron half-Heusler compounds can be used for a wide range of applications and a suitable half-Heusler compound can be found for practically all desired band gaps.

V. NEW BUFFER MATERIALS FOR CHALCOPYRITE SOLAR CELLS

The obtained results for the half-Heusler compounds can be used to select materials for specific applications. One interesting example is the buffer layer in thin film solar cells with a chalcopyrite absorption layer. Up to now the record efficiency of 20.1% has been found for thin-film solar cells with a *p*-type Cu(In, Ga)Se₂ absorption layer, separated from the *n*-type ZnO window layer by a buffer layer made of CdS.³⁵ There must be a good geometrical matching between the absorber and the buffer layer in order to avoid interface defects. The buffer material must have a band gap of at least 2 eV so that the light absorption in the buffer layer is rea-



FIG. 4. Fit functions $f_1(\bigcirc)$ and $f_2(\spadesuit)$ of the lattice constant *a*, plotted over *a*. Functions f_1 and f_2 are defined in Eqs. (1) and (3), respectively. Data are shown for compounds favoring the *XYZ* configuration. The diagonal line corresponds to a perfect match.



FIG. 5. Calculated band gaps for the stable configuration among compounds XYZ as a function of the differences of total energies $\Delta E = E_{XYZ} - E_{XYZ}$ (\bigcirc) and $\Delta E = E_{XYZ} - E_{XYZ}$ (+). Negative ΔE correspond to compounds favoring $\underline{X}YZ$ or $\underline{X}YZ$ while E_{XYZ} is more stable for $\Delta E > 0$. Note that DFT calculations typically underestimate the band gap.

sonably small. Furthermore, carrier recombinations at the interface should be minimized.²¹ CdS satisfies these criteria but there are strong efforts to find a less toxic buffer material (see Refs. 36–38 and references therein).

The class of eight-electron half-Heusler compounds includes a huge number of compounds, many of which are semiconductors. Therefore, a proper selection of promising materials must be made before a suitable set of compounds can be synthesized and tested experimentally. Our *ab initio* results are used to select half-Heusler compounds that fulfill two relevant criteria: The band gap must be larger than 2 eV and the lattice structure must match properly with that of the absorber layer.

The most relevant chalcopyrite materials for photovoltaic applications are of the type $CuIn_{1-x}Ga_xSe_{2-y}S_y$ with $0 \le x$ ≤ 1 and $0 \leq y \leq 2$. For x=0 and y=0, one has CISe, which is chosen as a reference absorber material in the following. The tetragonal unit cell of CISe is shown in Figs. 6(a) and 6(b). The comparison with the structure of a half-Heusler-type LiZnP in Figs. 6(c) and 6(d) shows that there is a good geometrical matching if the lattice constant a of the half-Heusler is similar to the small lattice constant a of the CuInSe₂, which is approximately $a \simeq 5.8$ Å.^{39,40} The lattice structure of CISe matches well with that of CdS having lattice constants a and c with $\sqrt{2a} \approx 5.85$ Å in the wurtzite phase⁴¹ and a lattice constant $a \simeq 5.84$ Å in the zinc blende phase.⁴² CuGaSe₂ has a small lattice constant of $a \approx 5.61$ Å, for CuInS₂ a value of $a \simeq 5.52$ Å has been measured.⁴⁰ Though the lattice constants of CuInS2 and CdS differ by approximately 5%, respectable efficiencies of up to 13% have been reported for thin film solar cells with a CdS/CuInS₂ junction.⁴³ We conclude that a proper lattice matching is important but lattice constant differences of a few percent are tolerable. Therefore, we choose as a minimum criterion that the lattice constant a of a potential buffer material should deviate less than 0.4 Å from the value of 5.8 Å.

In Fig. 7, calculated band gaps and lattice constants are shown for all investigated half-Heusler compounds. Potential buffer materials are located within the framed area. Band-



FIG. 6. (Color online) Structural similarity between chalcopyrite and half-Heusler materials. (a) Top view and (b) perspective side view on the tetragonal unit cell of the absorber material CuInSe₂; (c) top view and (d) perspective side view on the half-Heusler material LiZnP.

gap values calculated with EV-GGA are typically smaller than the experimentally measured band gaps. Comparisons with measured band gaps show that calculated band gaps can be up to 50% smaller than the corresponding experimental value, see Table I. In order to make sure that all relevant



FIG. 7. Diagram of lattice constants *a* and calculated band gaps E_{gap} of half-Heusler compounds in the range of $5.3 \le a \le 7$ Å and $E_{gap} \le 3.2$ eV. Note that DFT calculations typically derestimate the band gap. The dashed vertical line denotes the small compounds located within the thin black frame are candidates for substituting CdS in the buffer layer of chalcopyrite solar cells. The dashed vertical line denotes the small lattice constant of CuInSe₂.

materials are included in our list of candidate materials, we choose a suitably small lower boundary for the band gap calculated with EV-GGA, namely, $E_{gap,EV} > 0.7$ eV. With the chosen criteria, a small set of 20 compounds out of 648 investigated eight-electron half-Heusler materials have been selected. All other calculated compounds can be excluded as CdS substitute but they may be suited for many other optoelectronic applications. The properties of the small set of potential buffer materials can be studied in detail experimentally. Suitable buffer material candidates are LiCuS, NaCuS, NaAgS, and LiCuSe from the I-I-VI group. The largest number of potential buffer materials are found in the I-II-V group, namely, NaMgN, CaAgN, LiMgP, and MgCuP as well as XCaN, XSrN, and XZnP with X=Li,Na. Furthermore, there is NaAlC and LiYC from the I-III-IV group, CaMgC from the II-II-IV group, and CaXB with X=Al,Ga,In from the II-III-III group. The optimum buffer material depends on the chosen absorber material and its lattice constant. Recently, thin films of LiCuS and LiZnP have been successfully sputtered on a CIGSe layer.⁴⁴ In both cases, a mechanically stable contact with the chalcopyrite material and a band gap of approximately 2 eV have been measured. This indicates that the criteria tested with the calculated data are indeed successfully fulfilled. Further measurements remain to be done.

VI. CONCLUSIONS

The class of eight-electron half-Heusler materials includes a large number of semiconducting materials with various lattice constants and band-gap widths. A number of 648 compounds have been calculated with density-functional theory, which allows to obtain general properties and make comparisons between the members of the I-I-VI, I-II-V, I-III-IV, II-II-IV, and II-III-III classes "in silico," which means without the need to synthesize a large number of materials. One finds that for many but not all compounds the XYZ configuration is favored. Especially for compounds that consist of main group elements only the XYZ configuration is most stable. In compounds with an XYZ configuration, a particularly stable eight-electron substructure is formed by the $(YZ)^{n-}$ anions. Consequently, most semiconducting half-Heusler compounds have a stable XYZ configuration. Two simple formulas have been derived for approximating the lattice constants of half-Heusler compounds with stable XYZ configuration. The functions depend only on the Slater atomic radii of the components. Geometric considerations provide a parameter-free expression for the equilibrium lattice constants that reasonably approximates the calculated data. A more refined model allows to compare the stiffness of bonds between neighboring sites, showing that the covalent bond between the Y and Z components is the stiffest. The results for the studied compounds can be used to preselect materials for optoelectronic applications. As a practical application, we selected a set of 20 eight-electron half-Heusler compounds that fulfill necessary conditions for replacing CdS as buffer material in CIGSe and CISe thin-film solar cells. For this small number of materials it becomes practical to test the buffer layer properties experimentally.

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